# Learning to Sample MRI via Variational Information Maximization

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## Summary

We present a framework for **learning the sampling** pattern in MRI jointly with reconstruction using variational information maximization. Experiments with knee MRI shows improved reconstruction quality of our data-driven sampling over the prevailing variable-density sampling.

#### Background

- MRI measures tissue properties by collecting spatial Fourier domain representations (k-space).
- One of the **main challenges** in MRI is the **long** scan times.
- In order to accelerate MR imaging, one can obtain a reduced number of k-space samples below the Nyquist rate and use compressed sensing or deep learning methods to solve the inverse problem.

## Problem Statement

- Accelerating MRI scans requires **optimal sampling** of k-space data. However the sampling trajectories are usually selected heuristically.
- Can we optimize for the sampling locations in kspace in a data-driven manner?
- Given an acceleration factor, is it possible to optimize sampling pattern and image reconstruction jointly?

**Our solution:** We put forth a novel deep learning framework that leverages uncertainty autoencoders to enable joint optimization of sampling pattern and reconstruction of MRI scans.

#### Methods

We consider the multi-coil MR signal model under the additive white complex Gaussian noise as

#### Variational Information Maximization

We make use of the InfoMax principle that maximizes the mutual information between the measurements and noisy latent representations

#### Network Architecture

We use the nuFFT operator for multi-coil encoding and unrolled network architecture for decoding. Sampling locations  $\phi$  are shared between encoder and decoder.



$$z = f_{\phi}(x) + \epsilon = \left[ (F_{nu}(\phi)S_1)^H \cdots (F_{nu}(\phi)S_C)^H \right]^H x + \epsilon$$

where x is the image, z is k-space measurements. Encoding model  $f_{\phi}(x)$ contains coil sensitivity information  $S_i$ , and enables continuous parameterization of sampling coordinates  $\phi$  via nuFFT operator  $F_{nu}(\phi)$ .

$$\max_{\phi} I_{\phi}(X, Z) = \max_{\phi} \mathbb{E}_{q_{\phi}(X, Z)}[\log q_{\phi}(X|Z)]$$

$$\geq \max_{\phi, \theta} \mathbb{E}_{q_{\phi}(X, Z)}[\log p_{\theta}(X|Z)]$$
spread

where  $p_{\theta}(X|Z)$  is a variational approximation to the model posterior  $q_{\phi}(X|Z)$ . We represent the loss function as

$$\mathcal{L}(\phi, \theta; \mathcal{D}) = \max_{\phi, \theta} \sum_{x \in \mathcal{D}} \mathbb{E}_{q_{\phi}(Z|x)}[\log p_{\theta}(x|z)]$$

Figure 1: Network architecture consisting of nuFFT based encoder (a) and unrolled reconstruction network (b, c).

### Experiments







#### Conclusion



We considered four acceleration factors in our experiments: R = 5, 10, 15, 20. For each acceleration factor, we initialized the k-space sampling pattern ( $\phi$ ) by Variable Density Sampling and picked  $\sigma = 0.001$  for the measurement noise  $\epsilon$ .

Figure 2: pSNR (a) and SSIM (b) evaluated on test set for different acceleration factors. Point ead function (c) of sampling trajectories before and after optimization for R = 5.

Figure 3: Variable density (a) and optimized (b) trajectories along with the reconstruction result on a slice in the test set (c). Zero-filled reconstruction corresponds to applying  $A_{\phi}^{H}$  on z directly.

• We use variational information maximization for learning the sampling pattern in MRI jointly with image reconstruction.

• Optimizing sampling pattern improves reconstruction quality highlighting benefits that can be obtained by learning undersampling patterns.