Limitations of this work are larger scale models, more vision tasks, further optimization of accuracy, power and parameter amount, optimization of training consumption caused by multiple timesteps, etc., and we will work on them in future work. The experimental results in this paper are reproducible. We explain the details of model training and configuration in the main text and supplement it in the appendix. Our codes and models of Meta-SpikeFormer will be available on GitHub after review. Moreover, in this work, the designed meta SNN architecture is tested on vision tasks. For language tasks, the challenges faced will be different, such as parallel spiking neuron design, long-term dependency modeling in the temporal dimension, pre-training, architecture design, etc. need to be considered. This work can at least provide positive inspiration for SNN processing language tasks in long-term dependency modeling and architecture design, and we are working in this direction.

### A SPIKE-DRIVEN SELF-ATTENTION (SDSA) OPERATORS

In this Section, we understand vanilla and spike-driven self-attention from the perspective of computational complexity.

### A.1 VANILLA SELF-ATTENTION (VSA)

Given a float-point input sequence  $X \in \mathbb{R}^{N \times D}$ , float-point Query (Q), Key (K), and Value (V) in  $\mathbb{R}^{N \times D}$  are calculated by three learnable linear matrices, where N is the token number, D is the channel dimension. The vanilla scaled dot-product self-attention is computed as (Dosovitskiy et al., 2021):

$$VSA(Q, K, V) = \operatorname{softmax}\left(\frac{QK^{\mathrm{T}}}{\sqrt{d}}\right)V,$$
(16)

where d = D/H is the feature dimension of one head and H is the head number,  $\sqrt{d}$  is the scale factor. Generally, VSA performs multi-head self-attention, i.e., divide Q, K, V into H heads in the channel dimension. In the *i*-th head,  $Q^i, K^i, V^i$  in  $\mathbb{R}^{N \times D/H}$ . After the self-attention operation is performed on the H heads respectively, the outputs are concatenated together.

In VSA, Q and K are matrix multiplied first, and then their output is matrix multiplied with V. The computational complexity of VSA(·) is  $O(N^2D)$ , which has a *quadratic* relationship with the toke number N.

### A.2 SPIKE-DRIVEN SELF-ATTENTION (SDSA)

In our Transformer-based SNN blocks, as shown in Fig. 2, given a spike input sequence  $S \in \mathbb{R}^{T \times N \times D}$ , spike-form (binary)  $Q_S$ ,  $K_S$ , and  $V_S$  in  $\mathbb{R}^{T \times N \times D}$  are calculated by three learnable re-parameterization convolutions Ding et al. (2021) with  $3 \times 3$  kernel size:

$$Q_S = \mathcal{SN}(\operatorname{RepConv}_1(U)), K_S = \mathcal{SN}(\operatorname{RepConv}_2(U)), V_S = \mathcal{SN}(\operatorname{RepConv}_3(U)), \quad (17)$$

where  $\operatorname{RepConv}(\cdot)$  denotes the re-parameterization convolution,  $\mathcal{SN}(\cdot)$  is the spiking neuron layer. For the convenience of mathematical expression, we assume T = 1 in the subsequent formulas.

**SDSA-1.** The leftmost SDSA-1 in Fig. 3 is the operator proposed in Spike-driven Transformer (Yao et al., 2023b). The highlight of SDSA-1 is that the matrix multiplication between  $Q_S$ ,  $K_S$ ,  $V_S$  in SDSA is replaced by Hadamard product:

$$SDSA_1(Q_S, K_S, V_S) = Q_S \otimes S\mathcal{N} \left( SUM_c \left( K_S \otimes V_S \right) \right), \tag{18}$$

where  $\otimes$  is the Hadamard product,  $SUM_c(\cdot)$  represents the sum of each column, and its output is a D-dimensional row vector. The Hadamard product between spike tensors is equivalent to the mask operation. Compared to the VSA in Eq. 16,  $SUM_c(\cdot)$  and  $SN(\cdot)$  take the role of softmax and scale.

Now, we analyze the computational complexity of SDSA-1. Before that, we would like to introduce the concept of *linear attention*. If the softmax in VSA is removed, K and V can be multiplied first, and then their output is matrix multiplied with Q. The computational complexity becomes  $O(ND^2/H)$ , which has a linear relationship with the toke number N. This variant of attention is called linear attention (Katharopoulos et al., 2020). Further, consider an extreme case in linear attention, set

H = D. That is, in each head,  $Q^i, K^i, V^i$  in  $\mathbb{R}^{N \times 1}$ . Then, the computational complexity is O(ND), which has a linear relationship with both the toke number N and the channel dimension D. This variant of linear attention is called *hydra attention* (Bolya et al., 2023).

SDSA-1 has the same computational complexity as hydra attention, i.e., O(ND). Firstly,  $K_S$  and  $V_S$  in Eq. 18 participate in the operation first, thus it is a kind of linear attention. Further, we consider the special operation of Hadamard product. Assume that the *i*-th column vectors in  $K_S$  and  $V_S$  are *a* and *b* respectively. Taking the Hadamard product of *a* and *b* and summing them is equivalent to multiplying *b* times the transpose of *a*, i.e.,  $SUM_c(a \otimes b) = a^T b$ . In total, there are *D* times of dot multiplication between vectors, and *N* additions are performed each time. Thus, the computational complexity of SDSA-1 is O(ND), which is consistent with hydra attention (Bolya et al., 2023).

**SDSA-2.** SDSA-1 in Eq. 18 actually first uses  $Q_S$  and  $K_S$  to calculate the binary self-attention scores, and then performs feature masking on  $V_S$  in the channel dimension. We can also get the binary attention scores using only  $Q_S$ , i.e., SDSA-2 is presented as:

$$SDSA_2(Q_S, V_S) = SN(SUM_c(Q_S)) \otimes V_S.$$
 (19)

We evaluate SDSA-1 and SDSA-2 in Table 5. Specifically, SDSA-1-based Meta-SpikeFormer vs. SDSA-2-based Meta-SpikeFormer: Param, 31.3M vs. 28.6M; Power, 7.2mJ vs. 6.3mJ; Acc, 74.6% vs. 74.2%. It can be seen that with the support of the Meta-SpikeFormer architecture, even if the Key matrix  $K_S$  is removed, the accuracy is only lost by 0.4%. The number of parameters and energy consumption are reduced by 8.7% and 12.5% respectively. Since the Hadamard product between spiking tensors  $Q_S$  and  $K_S$  in SDSA-1 can be regarded as a mask operation without energy cost, SDSA-1 and SDSA-2 have the same computational complexity, i.e., O(ND). SDSA-2-based Meta-SpikeFormer has fewer parameters and power because there is no need to generate  $K_S$ .

**SDSA-3** is the spike-driven self-attention operator used by default in this work, which is presented as:

$$SDSA_3(Q_S, K_S, V_S) = \mathcal{SN}_s\left(Q_S\left(K_S^{\mathrm{T}}V_S\right)\right) = \mathcal{SN}_s((Q_SK_S^{\mathrm{T}})V_S).$$
(20)

In theory, the time complexity of  $Q_S(K_S^T V_S)$  and  $(Q_S K_S^T) V_S$  are  $O(N^2 D)$  and  $O(ND^2)$ , respectively. The latter has a linear relationship with N, thus SDSA-3 is also a linear attention. Since  $Q_S K_S^T V_S$  yields large integers, a scale multiplication s for normalization is needed to avoid gradient vanishing. In our SDSA-3, we incorporate the s into the threshold of the spiking neuron to circumvent the multiplication by s. That is, the threshold in Eq. 20 is  $s \cdot u_{th}$ . We write such a spiking neuron layer with threshold  $s \cdot u_{th}$  as  $S \mathcal{N}_s(\cdot)$ .

**SDSA-4.** On the basis of SDSA-3, we directly set the threshold of  $SN(\cdot)$  in Eq. 15 as a learnable parameter, and its initialization value is  $s \cdot u_{th}$ . We have experimentally found that the performance of SDSA-3 and SDSA-4 is almost the same (see Table 5). SDSA-4 consumes 0.1mJ less energy than SDSA-3 because the network spiking firing rate in SDSA-4 is slightly smaller than that in SDSA-3.

#### A.3 DISCUSSION ABOUT SDSA OPERATORS

Compared with vanilla self-attention, the  $Q_S$ ,  $K_S$ ,  $V_S$  matrices of spike-driven self-attention are in the form of binary spikes, and the operations between  $Q_S$ ,  $K_S$ ,  $V_S$  do not include softmax and scale. Since there is no softmax and  $K_S$  and  $V_S$  can be computed first, spike-driven self-attention must be linear attention. This is the natural advantage of a spiking Transformer. On the other hand, in the current SDSA design, the operation between  $Q_S$ ,  $K_S$ ,  $V_S$  is Hadamard product or matrix multiplication, both of which can be converted into sparse addition operations. Therefore, SDSA not only has low computational complexity, but also only has sparse addition. Its energy consumption is much lower than that of vanilla self-attention (see Appendix B).

In Yu et al. (2022a;b), the authors summarized various ViT variants and argued that there is general architecture abstracted from ViTs by not specifying the token mixer (self-attention). This paper experimentally verifies that this view also holds true in Transformer-based SNNs. In Table 5, we tested four SDSA operators and found that the performance changes between SDSA-1/2/3/4 were not large (less than 1.2%). We expect the SNN domain to design more powerful SDSA operators in the future, e.g., borrowing from Swin (Liu et al., 2021), hierarchical attention (Hatamizadeh et al., 2023), and so on.

Table 6: FLOPs of self-attention modules. The FLOPs in VSA and SDSA are multiplied by  $E_{MAC} = 4.6pJ$  and  $E_{AC} = 0.9pJ$  respectively to obtain the final energy cost.  $R_C$ ,  $\hat{R}$  denote the sum of spike firing rates of various spike matrices.

	VSA	SDSA-1	SDSA-2	SDSA-3	SDSA-4
Q, K, V	$3ND^2$	$T \cdot R_C \cdot 3 \cdot FL_{Conv}$	$T \cdot R_C \cdot 2 \cdot FL_{Conv}$	$T \cdot R_C \cdot 3 \cdot FL_{Conv}$	$T \cdot R_C \cdot 3 \cdot FL_{Conv}$
f(Q, K, V)	$2N^2D$	$T\cdot \widehat{R}\cdot ND$	$T\cdot \widehat{R}\cdot ND$	$T\cdot \widehat{R}\cdot ND^2$	$T\cdot \widehat{R}\cdot ND^2$
Scale	$N^2$	-	-	-	-
Softmax	$2N^2$	-	-	-	-
Linear	$FL_{MLP}$	$T \cdot R_C \cdot FL_{Conv}$			

### **B** THEORETICAL ENERGY EVALUATION

#### **B.1** SPIKE-DRIVEN OPERATORS IN SNNs

Spike-driven operators for SNNs are fundamental to low-power neuromorphic computing. In CNNbased SNNs, spike-driven Conv and MLP constitute the entire network. Specifically, the matrix multiplication between the weight and spike matrix in spike-driven Conv and MLP is transformed into sparse addition, which is implemented as addressable addition in neuromorphic chips (Frenkel et al., 2023).

By contrast,  $Q_S$ ,  $K_S$ ,  $V_S$  in spike-driven self-attention involve two matrix multiplications. One way is to execute element-wise multiplication between  $Q_S$ ,  $K_S$ ,  $V_S$ , like SDSA-1 in (Yao et al., 2023b) and SDSA-2 in this work (Eq. 19). And, element multiplication in SNNs is equivalent to mask operation with no energy cost. Another method is to perform multiplication directly between  $Q_S$ ,  $K_S$ ,  $V_S$ , which is then converted to sparse addition, like spike-driven Conv and MLP (SDSA-3/4 in this work).

#### **B.2** ENERGY CONSUMPTION OF META-SPIKEFORMER

When evaluating algorithms, the SNN field often ignores specific hardware implementation details and estimates theoretical energy consumption for a model (Panda et al., 2020; Yin et al., 2021; Yang et al., 2022; Yao et al., 2023d; Wang et al., 2023a). This theoretical estimation is just to facilitate the qualitative energy analysis of various SNN and ANN algorithms.

Theoretical energy consumption estimation can be performed in a simple way. For example, the energy cost of ANNs is FLOPs times  $E_{MAC}$ , and the energy cost of SNNs is FLOPs times  $E_{AC}$  times network spiking firing rate.  $E_{MAC} = 4.6pJ$  and  $E_{AC} = 0.9pJ$  are the energy of a MAC and an AC, respectively, in 45nm technology (Horowitz, 2014).

There is also a more refined method of evaluating energy consumption for SNNs. We can count the spiking firing rate of each layer, and then the energy consumption of each layer is FLOPs times  $E_{AC}$  times the layer spiking firing rate. The nuance is that the network structure affects the number of additions triggered by a single spike. For example, the energy consumption of the same spike tensor differs when doing matrix multiplication with various convolution kernel sizes.

In this paper, we count the spiking firing rate of each layer, then estimate the energy cost. Specifically, the FLOPs of the n-th Conv layer in ANNs Molchanov et al. (2017) are:

$$FL_{Conv} = (k_n)^2 \cdot h_n \cdot w_n \cdot c_{n-1} \cdot c_n, \tag{21}$$

where  $k_n$  is the kernel size,  $(h_n, w_n)$  is the output feature map size,  $c_{n-1}$  and  $c_n$  are the input and output channel numbers, respectively. The FLOPs of the *m*-th MLP layer in ANNs are:

$$FL_{MLP} = i_m \cdot o_m,\tag{22}$$

where  $i_m$  and  $o_m$  are the input and output dimensions of the MLP layer, respectively.

For spike-driven Conv or MLP, we only need to consider additional timestep T and layer spiking firing rates. The power of spike-driven Conv and MLP are  $E_{AC} \cdot T \cdot R_C \cdot FL_{Conv}$  and  $E_{AC} \cdot T \cdot R_M \cdot FL_{MLP}$  respectively.  $R_C$  and  $R_M$  represent the layer spiking firing rate, defined as the proportion of non-zero

elements in the spike tensor. For the SDSA modules in Fig. 3, the energy cost of the Rep-Conv part is consistent with spike-driven Conv. The energy cost of the SDSA operator part is given in Table 6. Combining Table 5, we observe that the  $SDSA(\cdot)$  function itself does not consume much energy because the Q, K, and V matrices themselves are sparse. The evidence is that SDSA-1 saves about 0.6mJ of energy consumption compared to SDSA-3 (see Table 5). In order to give readers an intuitive feeling about the spiking firing rate, we give the detailed spiking firing rates of a Meta-SpikeFormer model in Table 11.

# C DETAILED CONFIGURATIONS AND HYPER-PARAMETER OF META-SPIKEFORMER MODELS

## C.1 IMAGENET-1K EXPERIMENTS

On ImageNet-1K classification benchmark, we employ three scales of Meta-SpikeFormer in Table 7 and utilize the hyper-parameters in Table 8 to train models in our paper.

stage	# Tokens	Laye	r Specification		15M 31M 55M
		Downson	mlina	Conv	7x7 stride 2
		Downsam	iping	Dim	32 48 64
	H = W		SanConv	DWConv	7x7 stride 1
	$\frac{1}{2} \times \frac{1}{2}$	Conv-based	SepConv	MLP ratio	2
		SNN block	Channal Conv	Conv	3x3 stride 1
1			Channel Conv	Conv ratio	4
1		Downsam	nling	Conv	3x3 stride 2
		Downsam	ipning	Dim	64 96 128
	$H \downarrow W$		SenConv	DWConv	7x7 stride 1
	$\frac{1}{4} \times \frac{1}{4}$	Conv-based	Sepconv	MLP ratio	2
		SNN block	Channel Conv	Conv	3x3 stride 1
			Channel Conv	Conv ratio	4
$2 \qquad \frac{H}{2} \times \frac{W}{2}$	Downsam	nling	Conv	3x3 stride 2	
		Downsam	ipning	Dim	128 192 256
		$\frac{W}{2}$ Conv based	SepConv	DWConv	7x7 stride 1
	$\frac{\pi}{2} \times \frac{w}{2}$			MLP ratio	2
	8 8	SNN block	Channel Conv	Conv	3x3 stride 1
$2 \qquad \frac{H}{8} \times$		SININ DIOCK	Channel Conv	Conv ratio	4
			# Bloc	ks	2
		Downsam	nling	Conv	3x3 stride 2
		Downsam	ipning	Dim	256 384 512
3	$\frac{11}{10} \times \frac{11}{10}$	Transformer based	SDSA	RepConv	3x3 stride 1
	16 16	SNN block	Channel MLP	MLP ratio	4
		SININ DIOCK	# Bloc	:ks	6
		Downsam	nling	Conv	3x3 stride 1
	H W	Downsam	ping	Dim	360 480 640
4	$\frac{11}{1c} \times \frac{1}{1c}$	Transformer-based	SDSA	RepConv	3x3 stride 1
	10 10	SNN block	Channel MLP	MLP ratio	4
		STATA DIOOK	# Bloc	cks	2

Table 7.	Configurations	of different	Meta-Sni	keFormer	models
rable 7.	Configurations	of unforcint	Micia-Spi	Ker onner	moucis.

### C.2 COCO EXPERIMENTS

In this paper, we have used two methods to utilize Meta-SpikeFormer for object detection. We first exploit Meta-SpikeFormer as backbones for object detection, fine-tuning for 24 epochs after inserting the Mask R-CNN detector (He et al., 2017). The batch size is 12. The AdamW is employed with an initial learning rate of  $1 \times 10^{-4}$  that will decay in the polynomial decay schedule with a power of 0.9. Images are resized and cropped into  $1333 \times 800$  for training and testing and maintain the ratio. Random horizontal flipping and resize with a ratio of 0.5 was applied for augmentation during

Hyper-parameter	Directly Training	Finetune	
Model size	15M/31M/55M	15M/31M/55M	
Timestemp	1	4	
Epochs	200	20	
Resolution	224*:	224	
Batch size	1568	336	
Optimizer	LAN	/IB	
Base Learning rate	6e-4	2e-5	
Learning rate decay	Cosi	ne	
Warmup eopchs	10	2	
Weight decay	0.0	5	
Rand Augment	9/0	.5	
Mixup	Noi	ne	
Cutmix	Noi	ne	
Label smoothing	0.1	1	

Table 8:	Hyper-parameters	for image c	classification	on ImageNet-1K
	~1 1	0		0

training. This pre-training fine-tuning method is a commonly used strategy in ANNs. We use this method and get SOTA results (see Table 3), but with many parameters. To address this problem, we then train Meta-SpikeFormer in a direct training manner in conjunction with the lightweight Yolov5<sup>1</sup> detector, which Yolov5 is re-implemented by us in a spike-driven manner. Results are reported in Table 9. The current SOTA result in SNNs on COCO is EMS-Res-SNN (Su et al., 2023), which improves the structure. We get better performance using parameters that are close to EMS-Res-SNN.

Table 9:	Performance o	f obiect	detection	on COCO	val2017 (	Lin et al	2014)
14010 / .	1 0110111101100 0		accection	0		,	

Methods	Architecture	Spike -driven	Param (M)	Power (mJ)	Time Step	mAP@0.5 (%)
Conv-based SNN	EMS-Res-SNN (Su et al., 2023)	1	26.9	-	4	50.1
Transformer based SNN	Meta-SpikeFormer + Yolo	1	16.8	34.8	1	45.0
Transformer-based Sinn	(This Work)	1	16.8	70.7	4	50.3

# C.3 ADE20K EXPERIMENTS

Meta-SpikeFormer is employed as the backbone equipped with Sementic FPN Lin et al. (2017), which is re-implemented in a spike-driven manner. In T = 1, ImageNet-1K trained checkpoints are used to initialize the backbones while Xavier is utilized to initialize other newly added SNN layers. We train the model for 160K iterations with a batch size of 20. The AdamW is employed with an initial learning rate of  $1 \times 10^{-3}$  that will decay in the polynomial decay schedule with a power of 0.9. Then we finetuned the model to T = 4 and decreased the learning rate to  $1 \times 10^{-4}$ . To speed up training, we warm up the model for 1.5k iterations with a linear decay schedule.

## C.4 Additional results on VOC2012 segmentation

VOC2012 (Everingham et al., 2010) is a benchmark for segmentation which has 1460 and 1456 images in the training and validation set respectively, and covering 21 categories. Previous work using SNN for segmentation has used this dataset. Thus we also test our method on this dataset. We train the Meta-SpikeFormer for 80k iterations in T = 1 with ImageNet-1k trained checkpoints to initialize the backbones while Xavier is utilized to initialize other newly added SNN layers. Then we finetune the model to T = 4 with lower learning rate  $1 \times 10^{-4}$ . Other experiment settings are the same as the ADE20k benchmark. Results are given in Table 10, and we achieve SOTA results.

<sup>&</sup>lt;sup>1</sup>https://github.com/ultralytics/yolov5

-based SNN

Spike Param Power Time Methods Architecture MIoU(%) -driven (M) Step (mJ) X 49.5 FCN-R50 (Long et al., 2015) 909.6 1 62.2 ANN DeepLab-V3 (Chen et al., 2017) Х 68.1 1240.6 1 66.7 1 64 ANN2SNN Spike Calibration (Li et al., 2022) --55.0 9.9 Spiking FCN (Kim et al., 2022) 1 49.5 CNN-based 383.5 20 SNN Spiking DeepLab (Kim et al., 2022) 1 68.1 523.2 20 22.3 Transformer Meta-SpikeFormer 1 16.5 81.4 4 58.1

58.9

1

179.8

4

61.1

(This Work)

Table 10: Performance of semantic segmentation on VOC2012 (Everingham et al., 2010)

				T = 1	T=2	T=3	T = 4	Average
	Down	sampling	Conv	1	1	1	1	1
		SanConv	PWConv1	0.2662	0.4505	0.3231	0.4742	0.3785
	Sepconv		DWConv&PWConv2	0.3517	0.4134	0.3906	0.4057	0.3903
	COINDIOCK	Channal Cam	Conv1	0.3660	0.5830	0.4392	0.5529	0.4852
Ctara 1		Channel Conv	Conv2	0.1601	0.1493	0.1662	0.1454	0.1552
Stage 1	Down	sampling	Conv	0.4408	0.4898	0.4929	0.4808	0.4761
		G. C.	PWConv1	0.2237	0.3658	0.3272	0.3544	0.3178
		SepConv	DWConv&PWConv2	0.2276	0.2672	0.2590	0.2567	0.2526
	ConvBlock	<u>a</u> 1.a	Conv1	0.3324	0.4640	0.4275	0.4433	0.4168
		Channel Conv	Conv2	0.0866	0.0838	0.0811	0.0775	0.0823
	Down	sampling	Conv	0.3456	0.3916	0.3997	0.3916	0.3821
		<u> </u>	PWConv1	0.2031	0.3845	0.3306	0.3648	0.3207
		SepConv	DWConv&PWConv2	0.1860	0.2101	0.2020	0.1988	0.1992
	ConvBlock		Conv1	0.2871	0.4499	0.4013	0.4233	0.3904
Stage 2		Channel Conv	Conv2	0.0548	0.0541	0.0501	0.0464	0.0513
			PWConv1	0.3226	0.4245	0.4132	0.4158	0.3940
		SepConv	DWConv&PWConv2	0.1051	0.1051	0.1025	0.0995	0.1030
	ConvBlock		Conv1	0 2863	0 3787	0.3732	0 3728	0 3528
		Channel Conv	Conv2	0.0453	0.0418	0.0408	0.0382	0.0415
	Down	sampling	Conv	0.3817	0.4379	0.4436	0.4401	0.4259
	Down	sumpring	RepConv-1/2/3	0.1193	0.1975	0.2396	0.2722	0.2309
		SDSA	$O_{\alpha}$	0.2165	0.2220	0.2377	0.2722	0.2289
			$\mathcal{Q}S$ $K_{G}$	0.0853	0.0031	0.0035	0.0818	0.0884
	Dlook1		$V_{\alpha}$	0.0853	0.0751	0.0755	0.1234	0.0004
			$K^{VS}$	0.0000	0.1414	0.1227	0.1234	0.1102
	DIOCKI		$O_{\alpha}(K^T V_{\alpha})$	0.3083	0.4550	0.4250	0.4023	0.3971
			$Q_S(\Lambda_S v_S)$ <b>PenConv</b> 4	0.7571	0.66032	0.6074	0.6420	0.8370
			Lincor 1	0.4115	0.0402	0.0054	0.3398	0.3407
		Channel MLP	Linear 1	0.2147	0.3049	0.5205	0.3037	0.3224
stage3			DanCany 1/2/2	0.0555	0.0298	0.0202	0.0252	0.0200
			C C C C C C C C C C C C C C C C C C C	0.2045	0.4095	0.5700	0.3910	0.5590
			$Q_S$	0.1394	0.1639	0.1915	0.1071	0.1809
		SDSV	$\Lambda_S$	0.0774	0.1029	0.1001	0.1034	0.0973
	Dlash2	SDSA	$V_S$	0.0852	0.12/1	0.1228	0.1252	0.1140
	DIOCK2		$K_{\bar{S}}V_{S}$	0.4125	0.5852	0.5805	0.3833	0.5404
			$Q_S(K_S V_S)$	0.8240	0.9210	0.9231	0.9190	0.8970
			RepConv-4	0.4148	0.6622	0.6/3/	0.0545	0.6013
		Channel MLP	Linear I	0.2899	0.4026	0.3756	0.3884	0.3641
			Linear 2	0.0302	0.0269	0.0239	0.0219	0.0258
			RepConv-1/2/3	0.2894	0.3877	0.3706	0.3773	0.3562
			$Q_S$	0.1419	0.1397	0.1437	0.1405	0.1415
		and t	$K_S$	0.0590	0.0609	0.0639	0.0616	0.0614
	SDSA		$V_S$	0.0904	0.1232	0.1279	0.1261	0.1169
	Block3		$K_S^{\perp}V_S$	0.3674	0.4703	0.4825	0.4863	0.4516
			$Q_S(K_S^I V_S)$	0.8423	0.8912	0.9010	0.8961	0.8827
			RepConv-4	0.3613	0.4850	0.5281	0.5072	0.4704
		Channel MLP	Linear 1	0.3047	0.3795	0.3676	0.3727	0.3561
			Linear 2	0.0274	0.0248	0.0227	0.0211	0.0240

Table 11: Layer spiking firing rates of model Meta-SpikeFormer (T = 4, 31.3M, SDSA-3) on ImageNet-1K.

Continued on next page

				T = 1 T = 9 T = 9 T	Average
			RenConv 1/2/2	$\begin{array}{c} 1 = 1  1 = 2  1 = 3  1 = 4 \\ 0.2833  0.3460  0.3400  0.2420 \\ \end{array}$	Average
			$O_{\pi}$	0.1010 0.1884 0.1037 0.1803	0.3265
			$QS K_{\alpha}$	0.1510 0.1884 0.1557 0.1855	0.1900
		SDSA	$V_{G}$	0.0834 0.0986 0.1065 0.1043	0.0022
	Block4	5057	$K^T V_{\alpha}$	0.3421 0.4375 0.4566 0.4670	0.0702
	DIOCK+		$O_{\alpha}(K^T V_{\alpha})$	0.8279 0.8925 0.9067 0.9097	0.4250
			$QS(\Pi_S VS)$ RenConv-A	0.3632 0.4932 0.5457 0.5365	0.0042
			Linear 1	0.3040 0.3562 0.3487 0.3512	0.4047
		Channel MLP	Linear 2	0.3040 $0.3502$ $0.3407$ $0.35120.0282$ $0.0267$ $0.0244$ $0.0230$	0.0256
			RepConv-1/2/3	$0.2882 \ 0.3334 \ 0.3280 \ 0.3298$	0.0250
			$O_{\alpha}$	0.1577 0.1487 0.1501 0.1482	0.5170
			$\sqrt[4]{K_{C}}$	0.0440 0.0496 0.0528 0.0534	0.0499
	Block5	SDSA	$V_{c}$	0.0853 0.1276 0.1363 0.1377	0.01217
		52511	$K_{\alpha}^{T}V_{\alpha}$	0 3633 0 4934 0 5187 0 5365	0.4780
D	Diotilo		$Q_{\mathbf{g}}(K_{\mathbf{g}}^{T}V_{\mathbf{g}})$	0.8424 0.9031 0.9178 0.9213	0.8961
			RepConv-4	0.3550 0.5158 0.5620 0.5678	0.5001
			Linear 1	0.3211 0.3551 0.3477 0.3503	0.3436
		Channel MLP	Linear 2	0.0247 0.0223 0.0205 0.0194	0.0217
			RepConv-1/2/3	0.3072 0.3335 0.3286 0.3310	0.3251
	Block6	SDSA Channel MLP	Qs	0.1468 0.1392 0.1392 0.1376	0.1407
			$\widetilde{K}_{S}$	0.0373 0.0437 0.0442 0.0449	0.0426
			$V_S$	0.0935 0.1255 0.1331 0.1333	0.1213
			$K_{S}^{T}V_{S}$	0.3380 0.4449 0.4569 0.4667	0.4266
			$Q_S(K_S^T V_S)$	0.8073 0.8623 0.8706 0.8725	0.8532
			RepConv-4	0.2862 0.4085 0.4315 0.4352	0.3903
			Linear 1	0.3084 0.3267 0.3192 0.3230	0.3193
			Linear 2	0.0241 0.0218 0.0202 0.0194	0.0214
	Dow	nsampling	Conv	0.2456 0.2487 0.2414 0.2438	0.2449
		1 0	RepConv-1/2/3	0.1662 0.3402 0.3052 0.3280	0.2849
			$Q_S$	0.2044 0.1330 0.1202 0.1096	0.1418
		SDSA	$K_S$	0.0221 0.0259 0.0214 0.0205	0.0225
			$V_S$	0.0870 0.1556 0.1438 0.1443	0.1327
	Block1		$K_S^T V_S$	0.1782 0.2832 0.2455 0.2412	0.2370
			$Q_S(\tilde{K}_S^T V_S)$	0.6046 0.6607 0.5710 0.5285	0.5912
			RepConv-4	0.2379 0.2635 0.1852 0.1592	0.2115
		Channal MI D	Linear 1	0.2332 0.3966 0.3615 0.3859	0.3443
stage4			Linear 2	0.0262 0.0252 0.0192 0.0171	0.0219
			RepConv-1/2/3	0.3053 0.4001 0.3907 0.4018	0.3745
			$Q_S$	0.1389 0.1245 0.1176 0.1108	0.1230
			$K_S$	0.0227 0.0231 0.0224 0.0218	0.0225
		SDSA	$V_S$	0.0764 0.1038 0.1051 0.1048	0.0975
	Block2		$K_S^T V_S$	0.1600 0.1968 0.1985 0.1979	0.1883
			$Q_S(\tilde{K}_S^T V_S)$	0.5439 0.5558 0.5348 0.5079	0.5356
			RepConv-4	0.1718 0.1697 0.1578 0.1384	0.1594
		Channal MI D	Linear 1	0.3000 0.3811 0.3768 0.3913	0.3623
			Linear 2	0.0030 0.0035 0.0032 0.0029	0.0032
	Head	d	Linear	0.4061 0.4205 0.4323 0.4545	0.4283

Table 11 –	continued f	from previ	ous page