## The detailed description of Proposition 1 Α 1

In the Proposition 1 in the main body, we talk about the condition that the intervention gets the perfect 2

mean compared to the real mean. Given Equation 3 in the main body, we have  $\mu_{true} = \mu_{obser} - \mu_z$ . Assuming  $p^*$  is the optimal probability for flipping and interventional data and observational data, 3

4

5 then we have:

$$p^* \mu_{ven} + (1 - p^*) \mu_{obser} = \mu_{true} \tag{1}$$

$$p^*\mu_{ven} + (1-p^*)\mu_{obser} = \mu_{obser} - \mu_{\mathcal{Z}}$$
<sup>(2)</sup>

$$p^*(\mu_{ven} - \mu_{obser} = -\mu_{\mathcal{Z}} \tag{3}$$

$$p^* = -\frac{\mu_{\mathcal{Z}}}{\mu_{ven} - \mu_{obser}} \tag{4}$$

$$p^* = \frac{\mu_{\mathcal{Z}}}{\mu_{obser} - \mu_{ven}} \tag{5}$$

- The obvious condition that satisfies this Equation 5 is that  $\mu_{ven}$  is getting closer and closer to the real 6
- mean  $\mu_{true}$  as well as p is closer to 1. The reason is obvious. Assuming the interventional data is 7
- perfect:  $\mu_{ven} = \mu_{obser} \mu_{\mathcal{Z}}$ . Then we have  $p^* = 1$  according to Equation 5. 8