7 Appendix

8 The Relationship Between Software Portability and Innovation

While some innovation happens de-novo, building something new from scratch, much happens from local adaptation, where an existing innovation is adapted [Eisenhardt and Tabrizi] [1995]. This practice is ubiquitous in machine learning where there is extensive reuse of code and models. Lack of software portability constrains innovation because it means that someone who has previously developed their work in a framework is tied to a particular piece of hardware and may be unable to switch to another advantageous framework if that other framework lacks the functionality/performance needed. While it is hard to count instances of non-invention attributable to hardware because "didn't invent" also means "didn't publish," we can nevertheless see particular examples where the lack of software portability has stifled innovation such as:

- 1. Efficiency gains from early exiting [Teerapittayanon et al.] [2017] (Abadi et al. 2016) is a very popular efficiency strategy for avoiding unnecessary computation. However, early exiting has no impact on memory requirements or efficiency when using software stacks that fully instantiate the computation graph prior to running the program (i.e., TensorFlow). Thus this is an optimization that works well in other frameworks but gains us nothing in the case of TensorFlow.
- 2. Naive multi-device training distribution strategies are sensitive to the choice of software stack used. It can have a pronounced impact on differences in dispatch overhead and communication patterns with PyTorch not being able to engage in some distributed workloads [Barham et al.] 2022].
- 3. Capsule networks [Sabour et al., 2017] have unique operations like squashing and routing that stray from the matrix multiplies. Capsule networks are far less efficient in TensorFlow, given the requirement for adaptive routing [Barham and Isard, 2019].
- 4. Adaptive learning or data pruning. Both require removing examples from a batch that are estimated not to be important (adaptive pruning does it over the course of training, and data pruning can be a single shot before training). Both techniques have no impact on efficiency when using software stacks that require fixed shapes (i.e., TensorFlow), as instead of changing the batch size on the fly, you need to pad the batch with zeros.
- 5. **Proximal gradient optimization and variants** [Parikh and Boyd, 2014]. Implementing these techniques in PyTorch is straightforward due to PyTorch's flexible design granting granular control over the training loop. Conversely, Keras abstracts much of the underlying intricacies, which can limit the direct control users have over specific training loop customizations.

We will continue to curate a list of examples where lack of software portability has impacted innovation in research. If you have other examples we should add to this list, please reach out to the authors of this paper.

9 Discussion of Differences in Latency

While an in-depth analysis of differences between GPU and TPU kernels of functions is beyond the scope of our paper, we wanted to categorize some high-level reasons for differences as a starting point for discussion. We note these are anecdotal observation, but may be of interest to the reader as a starting point for discussion.

Broadly, we expect slowdowns to be attributed to one of the following categories:

- 1. **Misalignment between workload and implementation:** frameworks and hardware may assume certain usage patterns (e.g., uniform input sizes) that are mismatched with actual workloads.
- 2. **Memory architectures:** The substantially different memory architecture choices made by TPU and GPU architects advantage particular data structures and operations, making framework optimizations uneven in their effectiveness [Zhu et al., [2020].

3. **Bottlenecks:** Unimplemented features in some frameworks can lead to data transfer bottlenecks that lead to the full performance not being able to be taken advantage of.

PyTorch Latency Differences For TPUs, we observe **long data transfer times** between the TPUs memory and CPUs can be a bottleneck. This is a problem that is much worse in PyTorch than TensorFlow due to a lack of an infeed processing implementation. TensorFlow specifically runs input processing on the CPU while TPU operations take place. PyTorch has chosen not to implement this, which makes TPUs slower than GPUs for PyTorch. Another contributing bottleneck for TPUs is **kernel recompilation on dynamic shapes** which can lead to slower results in tests that use dynamic shapes when running on TPUs.

TensorFlow Latency Differences kernel recompilation on dynamic shapes is also a contributing factor for TensorFlow. This leads to our greatest latency difference in TensorFlow on the SVD function. **Data transfer pauses:** While input processing is implemented in TensorFlow, data transfer remains a bottleneck. In some cases, this data preparation and transfer can take longer than the XLA process itself. **Unequal Speedups Due to Specialization:** The largest benefits of TPUs will be on operations involving matrix multiplication. For other operations, large speed-ups are not ensured.

Performance Comparison Across Hardware Versions: Referring to Figure 7, 9.09% of TensorFlow functions exhibit a 1.5X performance enhancement when transitioning from a T4 GPU to a A100 GPU. Additionally, 28.07% and 9.09% of PyTorch functions achieve a 1.5X speed improvement when operating newer GPU and TPU versions, respectively. In contrast, JAX functions display minimal gains of just 0.05% on the GPU and 0.02% on the TPU.

10 Why Functions

To avoid overfitting to specific machine learning workloads that may not capture future machine learning research directions, we **evaluate the portability of functions and not scripts**. A major concern when overly focusing on popular architectures or tasks is the sidelining the diverse range of code and ideas that researchers are exploring, some of which might not have reached popularity or high optimization levels. In addition, choosing to analyze workloads instead of functions would have posed several challenges for fairly comparing frameworks:

- 1. Analysis can be difficult: For example, if we have input x, go through three functions F, G, and H in the order F(G(H(x))). If the middle function, which is G in this case, fails because it is not portable, we will not be able to test the function F.
- 2. **Different workloads use different framework versions:** If we use a deprecated function, we might face (1).
- 3. **Privileging common workloads introduces bias:** The function X might work on a common task, but it might not work in a more niche case. Therefore, the function sampling is much more thorough and thus more suitable for extrapolation.
- 4. **Operations are the building blocks of ML workloads:** The performance and portability of the operations directly impact the workloads that use them.

11 Hardware Evaluation and Device Running Procedures

Types of Hardware Evaluated: We primarily ran test suites on a T4 GPU and a v3-8 TPU [Jouppi et al., 2017]. For certain analyses, we utilized an A100 GPU and v2-8 TPU, and we specifically indicate such instances in the charts and tables. Unless otherwise indicated, readers should assume the use of a T4 GPU and a v3-8 TPU.

Ensuring operations executed on correct device: To ensure that PyTorch, TensorFlow, and JAX tests ran on the right hardware, we provided a device environment variable, which we then referred to in test helpers and startup code to force tests to be on the correct device.

This ensures that operations are not split between multiple devices but instead run on a single device. This was necessary because many tests specifically test transferring values between the CPU and another device, whereas our goal is to establish the viability of running a function on a single device. We include more details in the appendix Section 13 about the technical implementation of ensuring functions are only run on the device of interest.

Latency measuring procedure: For every script and each framework we wrap the relevant operation with time.perf_counter(). Before recording the ending time, we include a synchronization point. This will synchronize asynchronous XLA and Cuda operations, allowing the operations to finish before we take the time. We include more details in the appendix in Section 14 about how we implement the synchronization points. We record 3 runs for every test, framework, and device combination. Unless indicated otherwise, results are reported as the average of the 3 runs.

12 Data Filtering

We filter the files obtained from the CodeParrot-clean dataset to only include files that import the respective framework using the regexes '(from.*tensorflow|import.*tensorflow)', '(from.*jax|import.*jax)', and '(from.*torch|import.*torch)' respectively. These files were subsequently parsed and tokenized [Richter and Wehrheim, 2022] to obtain frequency count for functions. Our goal was to approximate the frequency of functions in everyday engineering usage. While this process was imperfect due to name collisions with identifiers with the same names as framework functions, we managed to get a broad overview of framework function use.

To ensure we capture function calls and variables without including irrelevant pieces of the code, we tokenize each individual Python file. We use code_tokenize [Richter and Wehrheim, 2022] to parse the files and determine if something is an identifier. We run the tokenization on each file and then count the frequencies of relevant identifiers. This ensured we were not looking at import statements, control statements, and other parts of Python code. Instead, we include just function calls, variables, and class usages. Next, we count the frequency of identifiers that were also functions in the respective framework.

While framework functions are our primary interest, classes were necessary to include as well. A frequent pattern is to see classes that act in a very function-like way. A good example of this would be ReLU in PyTorch. It is a common pattern in PyTorch to initialize a class and use the resulting instance as a function you can pass input to. With ReLU, this would look like this example from the documentation⁶. This brought a certain level of ambiguity because we need to include classes but not all classes are directly relevant. In the interest of ensuring we included everything relevant, we included all class names in the list of all relevant identifiers in a framework.

13 Ensuring Functions are Run on Device of Interest

PyTorch Device Running Procedure: For PyTorch we leverage the existing instantiate_ device_type_tests functionality found in the PyTorch test suite. This function allows you to pass a device parameter into each test and use that to set the device of any tensors. We customized this to include XLA TPU support. This involved us overriding the onlyNativeDeviceTypes decorator to include the TPU while running. We also created a new decorator to go along with this functionality called onlyAcceleratedDeviceTypes for tests that previously had the onlyCuda decorator. The onlyAcceleratedDeviceTypes decorator ensures that only accelerated devices, such as GPUs and TPUs, are used to run the test. This was necessary because many tests specifically test transferring values between the CPU and another device. So just using onlyNativeDevices would not work on those tests.

TensorFlow Device Running Procedure: To ensure that all TensorFlow tests were using the correct device we needed to handle the following cases:

- 1. Tensors running eagerly in the default way.
- 2. Tensors utilizing graph mode through self.session and self.cached_session which are built into the TensorFlow test suite.
- 3. Tensors utilizing tf.Graph.as_default to set the graph. This undoes any device setting we do with our contexts and thus needs device setting within tf.Graph.as_default call.

⁶https://pytorch.org/docs/stable/generated/torch.nn.ReLU.html

To handle these cases, we did the following:

- 1. Utilize a device context that sets the device to the one specified in our environment variable.
- 2. Handle tests utilizing self.session and self.cached_session by monkeypatching the TensorFlow TestCase class to use our environment specified device. This was done by overriding the private method _constrain_devices_and_set_default.
- 3. Handle tests utilizing tf.Graph.as_default by using a monkeypatched tf.Graph.as_default to include the device based upon our environment variable within the call tf.Graph.as_default. For most tests this was sufficient. But for several, this broke something else inside these tests. For these specific tests, we created a blacklist upon which we do not apply the monkey patch, and instead, we set the device manually inside the tf.Graph.as_default call.

14 Measuring Latency on Devices

The synchronization points are as follows:

- TensorFlow on GPU and TPU: We call .numpy on the result of the operation which forces all asynchronous operations to finish before times are recorded.
- PyTorch on GPU: We use torch.cuda.synchronize() in order to sync the operation.
- PyTorch on TPU: We use xm.mark_step() as a synchronization point.
- JAX on GPU and TPU: We use block_until_ready() on the output of the operation as a synchronization point.

Table 5: Latency in milliseconds for PyTorch on GPU and TPU. The table is ordered by the ratio GPU/TPU in descending order. Note that values are rounded to 3 decimal places.

	Function	GPU	TPU	TPU/GPU	
1	torch.argsort	0.157	948.210	6039.554	
2	torch.optim.Adamax	0.069	392.712	5691.478	
3	torch.fliplr	0.201	725.480	3609.353	
4	torch.broadcast_tensors	0.044	39.030	887.045	
5	torch.nn.AdaptiveAvgPool3d	0.074	65.219	881.338	
6	torch.addr	0.106	83.030	783.302	
7	torch.cat	0.100	64.652	646.520	
8	torch.optim.LBFGS	0.097	50.358	519.155	
9	torch.triangular_solve	0.091	33.536	368.527	
10	torch.nn.Module.state_dict	0.053	19.508	368.075	
11	torch.nn.Module.zero_grad	0.057	17.572	308.281	
12	torch.sum	0.084	23.921	284.774	
13	torch.Tensor.is_same_size	0.025	6.973	278.920	
14	torch.nn.KLDivLoss	0.187	48.865	261.310	
15	torch.nn.LSTMCell	0.372	93.617	251.659	
16	torch.moveaxis	0.034	7.878	231.706	
17	torch.nn.functional.dropout	0.041	8.847	215.780	
18	torch.lt	0.055	8.857	161.036	
19	torch.autograd.Variable	0.051	7.519	147.431	
20	torch.utils.data.Subset	0.069	8.722	126.406	
21	torch.nn.Sequential	0.115	11.639	101.209	
22	torch.multinomial	1.193	115.240	96.597	
23	torch.nn.Linear	0.459	37.842	82.444	
24	torch.nn.BCEWithLogitsLoss	0.855	55.768	65.226	
25	torch.diag	0.494	27.232	55.126	
26	torch.von_mises.VonMises	0.680	31.054	45.668	
	Continued on next page				

	Function	GPU	TPU	TPU/GPU
27	torch.zeros	0.252	10.577	41.972
28	torch.round	0.301	12.178	40.458
29	torch.range	0.193	5.627	29.155
30	torch.autograd.functional.jvp	0.788	22.298	28.297
31	torch.linalg.matrix_rank	2.568	68.511	26.679
32	torch.nn.GELU	0.787	19.317	24.545
33	torch.Tensor.to	0.105	1.728	16.457
34	torch.nn.Transformer	216.593	3066.136	14.156
35	torch.bitwise_not	1.925	23.535	12.226
36	torch.nn.Conv3d	0.240	1.202	5.008
37	torch.slogdet	30.606	151.092	4.937
38	torch.optim.lr_scheduler.ExponentialLR	0.037	0.157	4.243
39	torch.utils.data.Dataset	0.035	0.117	3.343
40	torch.utils.data.ConcatDataset	0.031	0.092	2.968
41	torch.nn.Parameter.register_parameter	0.039	0.091	2.333
42	torch.cuda	0.041	0.061	1.488
43	torch.nn.Conv2d	46.053	67.081	1.457

Table 6: Latency in milliseconds for TensorFlow on GPU and TPU. The table is ordered by the ratio GPU/TPU in descending order. Note that values are rounded to 3 decimal places.

	Function	GPU	TPU	TPU/GPU		
1	tf.linalg.svd	0.931	112.843	121.206		
2	tf.math.reduce_logsumexp	13.028	474.586	36.428		
3	tf.nn.conv3d	3.596	49.867	13.867		
4	tf.tensor_scatter_nd_update	1.625	21.626	13.308		
5	tf.signal.idct	6.965	87.764	12.601		
6	tf.python.ops.numpy_ops.clip	1.223	15.409	12.599		
7	tf.image.adjust_brightness	10.264	129.021	12.570		
8	tf.train.list_variables	0.358	4.032	11.263		
9	tf.reshape	1.161	10.185	8.773		
10	tf.cast	1.214	10.546	8.687		
11	tf.lookup.KeyValueTensorInitializer	2.534	17.919	7.071		
12	tf.Tensor.eval	3.332	22.366	6.712		
13	tf.range	2.108	13.782	6.538		
14	tf.convert_to_tensor	2.027	9.683	4.777		
15	tf.sequence_mask	10.962	46.188	4.213		
16	<pre>tf.compat.v1.distributions.Normal</pre>	1.871	5.340	2.854		
17	tf.debugging.assert_less	5.541	14.911	2.691		
18	tf.math.reduce_mean	7.629	19.746	2.588		
19	${\tt tf.python.framework.smart_cond}$	3.067	7.838	2.556		
20	tf.compat.v1.test.compute_gradient_error	164.855	377.978	2.293		
21	tf.nn.conv2d_transpose	72.639	152.463	2.099		
22	tf.dtypes.as_dtype	0.009	0.018	2.000		
23	tf.compat.v1.distributions.Normal.survival_function	9.521	18.128	1.904		
24	tf.compat.v1.distributions.Normal.param_shapes	0.542	1.022	1.886		
25	tf.contrib.framework.nest.map_structure_up_to	0.404	0.760	1.881		
26	tf.numpy_function	1.572	2.954	1.879		
27	tf.sets.intersection	1.926	3.606	1.872		
28	tf.compat.v1.saved_model.simple_save	27.784	50.100	1.803		
29	tf.compat.v1.placeholder	0.721	1.293	1.793		
30	tf.keras.optimizers.experimental.Adadelta	7.951	13.918	1.750		
31	tf.linalg.set_diag	1.409	2.344	1.664		
32	tf.compat.v1.variable_scope	3.017	4.834	1.602		
	Continued on next page					

	Function	GPU	TPU	TPU/GPU
33	tf.constant	1.094	1.717	1.569
34	tf.nn.space_to_batch	1.597	2.492	1.560
35	tf.summary.flush	0.823	1.274	1.548
36	tf.Variable	12.660	18.490	1.461
37	<pre>tf.compat.v1.metrics.accuracy</pre>	26.136	38.095	1.458
38	$tf.compat.v1.get_collection$	0.015	0.021	1.400
39	tf.math.igammac	0.918	1.274	1.388
40	tf.test.TestCase.assert_equal	0.040	0.052	1.300
41	tf.compat.v1.global_variables_initializer	0.585	0.760	1.299
42	tf.Graph.as_default	0.117	0.152	1.299
43	tf.train.ExponentialMovingAverage	0.021	0.025	1.190
44	<pre>tf.compat.v1.TextLineReader.restore_state</pre>	1.201	1.416	1.179
45	tf.distribute.Strategy.get_per_replica_batch_size	0.016	0.018	1.125
46	tf.estimator.CheckpointSaverHook	0.051	0.055	1.078
47	tf.Tensor.get_shape	0.040	0.042	1.050
48	tf.nest.map_structure	0.084	0.087	1.036
49	tf.compat.v1.train.get_global_step	0.069	0.071	1.029
50	tf.estimator.LoggingTensorHook	0.042	0.038	0.905
51	tf.compat.v1.Session.run	5.722	3.804	0.665

Table 7: Latency in milliseconds for JAX on GPU and TPU. The table is ordered by the ratio GPU/TPU in descending order. Note that values are rounded to 3 decimal places.

ax.named_call ax.numpy.array ax.numpy.zeros ax.lax.select axsrc.interpreters.partial_eval ax.core.eval_context() ax.lax.all_gather ax.lax.integer_pow ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	$\begin{array}{c} 0.007\\ 0.435\\ 0.673\\ 197.595\\ 0.012\\ 0.005\\ 0.348\\ 0.197\\ 0.015\\ 0.013\\ 2.608\end{array}$	0.012 0.638 0.890 225.906 0.013 0.005 0.342 0.190 0.014 0.012	1.714 1.467 1.322 1.143 1.083 1.000 0.983 0.964 0.933
ax.nunpy.zeros ax.lax.select axsrc.interpreters.partial_eval ax.core.eval_context() ax.lax.all_gather ax.lax.integer_pow ax.nunpy.size ax.tree_util.Partial ax.make_jaxpr	$\begin{array}{c} 0.673 \\ 197.595 \\ 0.012 \\ 0.005 \\ 0.348 \\ 0.197 \\ 0.015 \\ 0.013 \end{array}$	$\begin{array}{c} 0.890 \\ 225.906 \\ 0.013 \\ 0.005 \\ 0.342 \\ 0.190 \\ 0.014 \end{array}$	1.322 1.143 1.083 1.000 0.983 0.964 0.933
ax.lax.select axsrc.interpreters.partial_eval ax.core.eval_context() ax.lax.all_gather ax.lax.integer_pow ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	197.595 0.012 0.005 0.348 0.197 0.015 0.013	225.906 0.013 0.005 0.342 0.190 0.014	$1.143 \\ 1.083 \\ 1.000 \\ 0.983 \\ 0.964 \\ 0.933$
axsrc.interpreters.partial_eval ax.core.eval_context() ax.lax.all_gather ax.lax.integer_pow ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	0.012 0.005 0.348 0.197 0.015 0.013	$\begin{array}{c} 0.013 \\ 0.005 \\ 0.342 \\ 0.190 \\ 0.014 \end{array}$	1.083 1.000 0.983 0.964 0.933
ax.core.eval_context() ax.lax.all_gather ax.lax.integer_pow ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	0.005 0.348 0.197 0.015 0.013	0.005 0.342 0.190 0.014	1.000 0.983 0.964 0.933
ax.lax.all_gather ax.lax.integer_pow ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	0.348 0.197 0.015 0.013	0.342 0.190 0.014	0.983 0.964 0.933
ax.lax.integer_pow ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	0.197 0.015 0.013	0.190 0.014	0.964 0.933
ax.numpy.size ax.tree_util.Partial ax.make_jaxpr	0.015 0.013	0.014	0.933
ax.tree_util.Partial ax.make_jaxpr	0.013		
ax.make_jaxpr		0.012	
	2 608		0.923
	2.000	2.395	0.918
ax.numpy.log	0.309	0.283	0.916
ax.numpy.isscalar	0.010	0.009	0.900
ax.tree_util.tree_unflatten	0.008	0.007	0.875
ax.vjp	9.834	8.565	0.871
ax.numpy.einsum_path	0.282	0.243	0.862
ax.numpy.delete	0.013	0.011	0.846
axsrc.interpreters.partial_eval.trace_to_jax_pr_dynamic	0.380	0.308	0.811
ax.scipy.stats.norm.cdf	0.005	0.004	0.800
ax.lax.stop_gradient	0.166	0.132	0.795
ax.numpy.reshape	3.714	2.845	0.766
ax.numpy.average	0.004	0.003	0.750
ax.disable_jit	0.027	0.020	0.741
ax.tree_util.tree_map	0.051	0.033	0.647
axsrc.core.get_aval	0.073	0.047	0.644
ax.scipy.signal.convolve2d	401.254	206.587	0.515
ax.lax.erf	14.456	7.296	0.505
ax.scipy.special.ndtr	77.206	33.315	0.432
ax.numpy.convolve	211.884	86.244	0.407
ax.numpy.linalg.svd	794.990	301.459	0.379
	<pre>ax.numpy.log ax.numpy.isscalar ax.tree_util.tree_unflatten ax.vjp ax.numpy.einsum_path ax.numpy.delete ax.src.interpreters.partial_eval.trace_to_jax_pr_dynamic ax.scipy.stats.norm.cdf ax.lax.stop_gradient ax.numpy.reshape ax.numpy.average ax.disable_jit ax.tree_util.tree_map ax.src.core.get_aval ax.scipy.signal.convolve2d ax.lax.erf ax.scipy.special.ndtr ax.numpy.convolve</pre>	ax.numpy.log 0.309 ax.numpy.isscalar 0.010 ax.tree_util.tree_unflatten 0.008 ax.vjp 9.834 ax.numpy.einsum_path 0.282 ax.numpy.delete 0.013 ax.scipy.stats.norm.cdf 0.005 ax.numpy.reshape 0.166 ax.numpy.average 0.004 ax.scipy.signal.convolve2d 401.254 ax.scipy.signal.convolve2d 401.254 ax.scipy.special.ndtr 77.206 ax.numpy.convolve 211.884 ax.numpy.linalg.svd 794.990	ax.numpy.log 0.309 0.283 ax.numpy.isscalar 0.010 0.009 ax.tree_util.tree_unflatten 0.008 0.007 ax.vjp 9.834 8.565 ax.numpy.einsum_path 0.282 0.243 ax.numpy.delete 0.013 0.011 ax.scipy.stats.norm.cdf 0.005 0.004 ax.scipy.stats.norm.cdf 0.166 0.132 ax.numpy.reshape 3.714 2.845 ax.numpy.average 0.004 0.003 ax.tree_util.tree_map 0.051 0.033 ax.scipy.signal.convolve2d 401.254 206.587 ax.scipy.special.ndtr 77.206 33.315 ax.numpy.convolve 211.884 86.244

	Function	GPU	TPU	TPU/GPU
31	jax.numpy.compress	133.591	45.108	0.338
32	jax.numpy.stack	145.019	44.748	0.309
33	jax.scipy.special.i0	389.510	118.412	0.304
34	jax.numpy.var	309.684	93.786	0.303
35	jax.numpy.tril	192.110	57.478	0.299
36	jax.numpy.sum	63.060	18.442	0.292
37	jax.numpy.triu_indices	357.124	103.997	0.291
38	jax.numpy.power	114.465	33.004	0.288
39	jax.numpy.ones	42.366	12.144	0.287
40	jax.lax.pmax	69.271	19.671	0.284
41	jax.numpy.max	147.327	39.700	0.269
42	jax.scipy.linalg.lu	654.291	164.111	0.251
43	jax.numpy.prod	180.961	45.276	0.250
44	jax.lax.slice_in_dim	30.590	7.504	0.245
45	jax.lax.bitwise_and	109.078	25.885	0.237
46	jax.numpy.tril_indices_from	923.872	217.183	0.235
47	jax.numpy.arange	466.126	107.242	0.230
48	jax.numpy.add	130.517	29.742	0.228
49	jax.numpy.all	206.400	46.815	0.227
50	jax.scipy.special.gammaln	161.529	34.914	0.216
51	jax.numpy.mean	222.164	47.596	0.214
52	jax.numpy.flip	75.649	14.542	0.192
53	jax.numpy.split	252.392	46.583	0.185
54	jax.numpy.fliplr	64.010	11.766	0.184
55	jax.lax.top_k	122.615	22.130	0.180
56	jax.numpy.exp	45.239	7.792	0.172
57	jax.lax.ge	90.087	15.302	0.170
58	jax.nn.one_hot	138.935	23.335	0.168
59	jax.random.PRNGKey	1485.077	227.995	0.154
60	jax.numpy.cos	172.002	26.102	0.152
61	jax.numpy.sqrt	98.118	13.860	0.141

Table 8: Comparison of TPUs and GPUs in terms of failure and success counts.

Comparison of TPU and GPU in terms of failure and success counts						
	GPUs			TPUs		
	Partial Failure	Complete Failure	Success	Partial Failure	Complete Failure	Success
TensorFlow	5/65	9/65	51/65	10/65	9/65	46/65
PyTorch	2/63	3/63	58/63	17/63	11/63	36/63
JÁX	0/63	1/63	62/63	0/63	2/63	61/63



Figure 8: Distribution of times for operations in TensorFlow on GPUs and TPUs.



Figure 9: Distribution of times for operations in PyTorch on GPUs and TPUs.



Figure 10: Distribution of times for operations in JAX on GPUs and TPUs.