

# Task Transfer with Stability Guarantees via Elastic Dynamical System Motion Policies

Anonymous Author(s)

Affiliation

Address

email

## 1 Appendix

### 2 A LPV-DS Parameter Optimization

3 **GMM-based LPV-DS formulation** It is described in Section 3 Preliminaries:  $\mathcal{PC}$ -GMM and LPV-  
4 DS Motion Policy.

$$\dot{\xi} = f(\xi) = \sum_{k=1}^K \gamma_k(\xi) (A^k \xi + b^k) \quad \text{s.t.} \quad \begin{cases} (A^k)^T P + P A^k = Q^k, Q^k = (Q^k)^T \prec 0 \\ b^k = -A^k \xi^* \end{cases} \quad (1)$$

5 **DS Estimation** The set of DS parameters  $\theta_{DS} = \{A^k, b^k\}$  for  $f(\xi)$  is estimated with LPV-DS  
6 by minimizing the Mean Square Error (MSE) against the demonstrations [1] subject to stability  
7 constraints in Equation 1.

$$\min_{\theta_{DS}} J(\theta_{DS}) = \sum_{n=1}^{N_{\text{ref}}} \sum_{t=1}^{T_N} \left\| \dot{\xi}_{t,n}^{\text{ref}} - f(\xi_{t,n}^{\text{ref}}) \right\|^2 \quad (2)$$
$$\text{s. t.} \quad \begin{cases} (A^k)^T P + P A^k = Q^k, Q^k = (Q^k)^T \prec 0 \\ b^k = -A^k \xi^* \quad \forall k = 1, \dots, K \end{cases}$$

8 which is a constrained non-convex semi-definite program (SDP). Further, when  $P$  is known (or esti-  
9 mated beforehand as in [1]) the problem becomes a convex SDP that can be solved highly efficiently  
10 with off-the-shelf QP solvers [1, 2].

## 11 B 2D Experiments

### 12 B.1 Via Point

13 By specifying an interesting point in the demonstration (usually by human specification or upstream  
14 computer vision method), the trajectory will be split into separate components. Each individual  
15 segment will be processed with Elastic-GMM to meet the new interesting via-point geometric con-  
16 straints as depicted in green polygons. By performing such steps, we can pose constraints not just  
17 on the endpoints of the demonstration but also on the intermediate points of the demonstration. This  
18 via-point experiment shows that with changes in the via-point constraints, Elastic-DS can adapt to  
them.

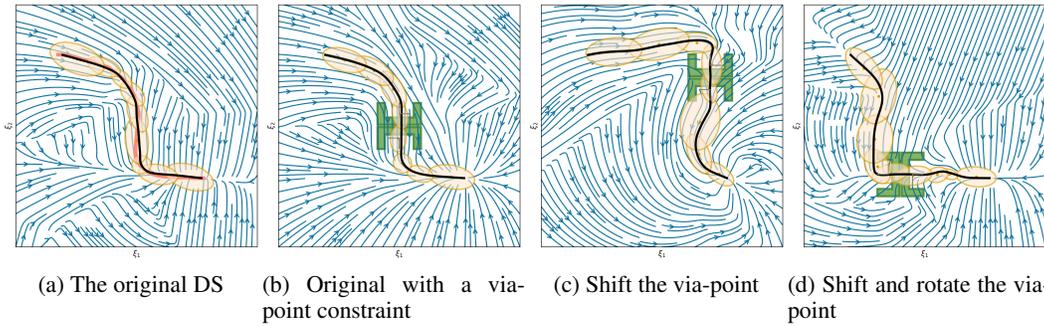


Figure 1: Modified DS based on the via point as a single DS without new demonstration

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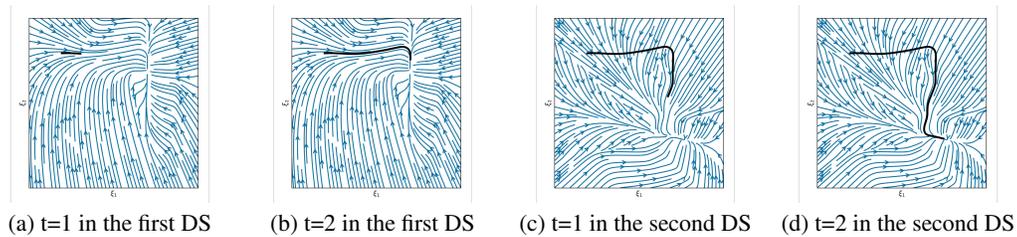


Figure 2: Modified DS based on the via point as multi-segment DS without new demonstration. The plots here show the rollout trajectory of the switch DS. It uses the same GMM as in 1c.

20 **C Reconstruct from Multiple Segments**

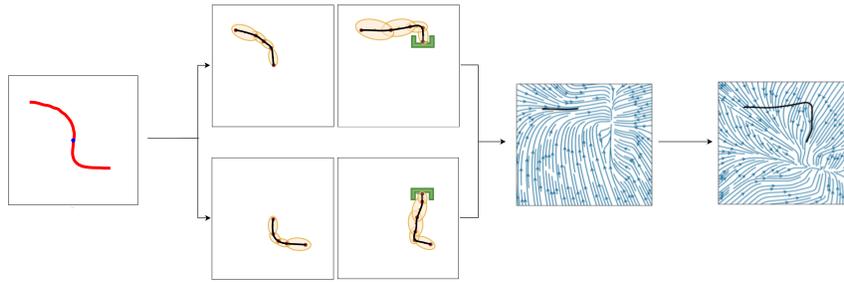


Figure 3: An example of the pipeline for sequential DS. In this case, the single demonstration (in red) is separated at the blue spot. Both segments perform Elastic GMM to meet the geometric descriptor constraints and learn DS individually. The end results are two DS which will run sequentially. After the first DS reaches its attractor, the robot will start to follow the second DS.

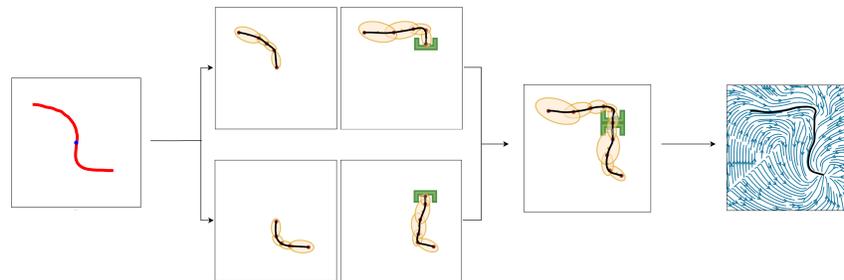


Figure 4: An example of the pipeline for building a single DS. In this case, the single demonstration (in red) is separated at the blue spot. After obtaining the GMM for each segment, they are stitched together and generate a single DS; such an approach will generate smooth velocity but could result in trajectories missing the geometric constraints.

## 21 **D Robot Experiments Snapshots**

### 22 **D.1 Bookshelf**

23 The goal of this experiment is to teach the robot how to insert a book into a desktop bookshelf. A  
24 motion capture marker object is attached to the side of the bookshelf. The geometric descriptor is at  
25 an offset from the marker object so that it is inside the bookshelf. We start with the book held by the  
gripper. It is predefined that the gripper will open once it reaches the attractor.



Figure 5: Demonstration for inserting book into a desktop bookshelf



Figure 6: The execution for the learned DS in the original configuration

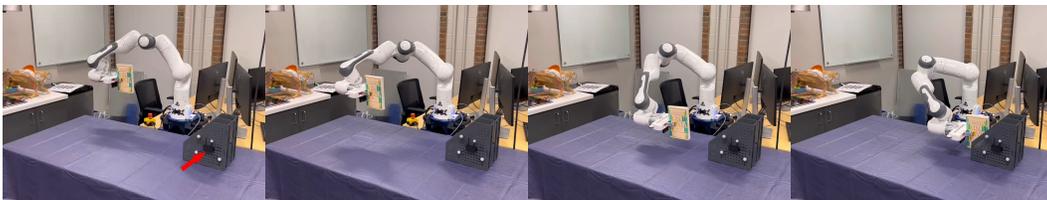


Figure 7: The bookshelf was shifted closer to the robot (The shifting direction is indicated by the red arrow). Without any new demonstration, the learned DS was able to adapt to the new configuration.

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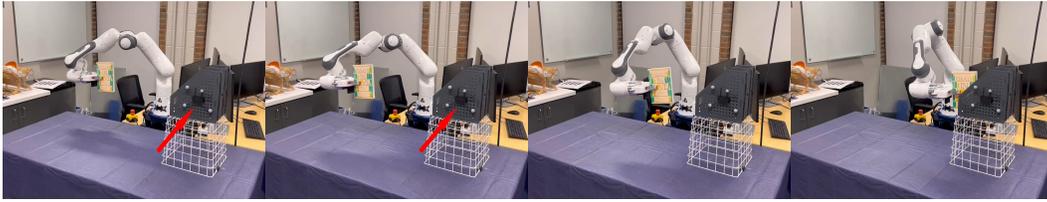


Figure 8: The bookshelf was shifted up (The shifting direction is indicated by the red arrow). Without any new demonstration, the Elastic-DS was able to adapt to the new configuration.



Figure 9: The bookshelf was shifted up (The shifting direction is indicated by the red arrow). Without any new demonstration, the Elastic-DS was able to adapt to the new configuration. The robot was still able to reach the new bookshelf position with human disturbances



Figure 10: The bookshelf is rotated and shifted to the left side of the robot. Without any new demonstration, the Elastic-DS was able to adapt to the new configuration. The robot was still able to reach the new bookshelf configuration. We rotate the end-effector to be parallel with the bookshelf beforehand.

27 **D.1.1 Pick and Place**

28 In this task, we will show the robot how to pick a cube and place it in a bin. The cube position could  
29 be changed (labeled by the motion capture marker as the geometric descriptor while the bin position  
30 is fixed. During the demonstration, the gripper open/close is done through voice commands (with  
31 the microphone at the bottom right of the snapshots). The gripper state is memorized and associated  
32 with each segment. At the end of each segment (reaching the attractor), the robot will open/close  
the gripper depending on the demonstration.

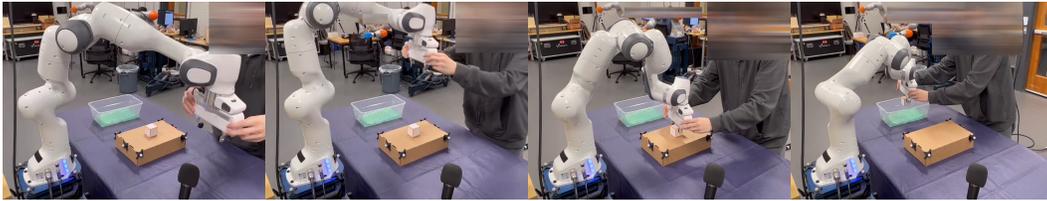


Figure 11: Demonstration for a pick and place task

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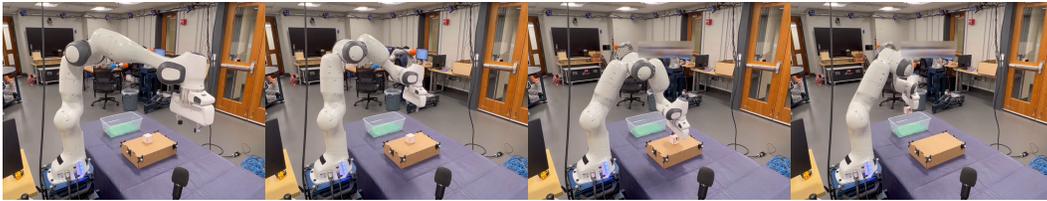


Figure 12: The execution for the learned DS in the original configuration

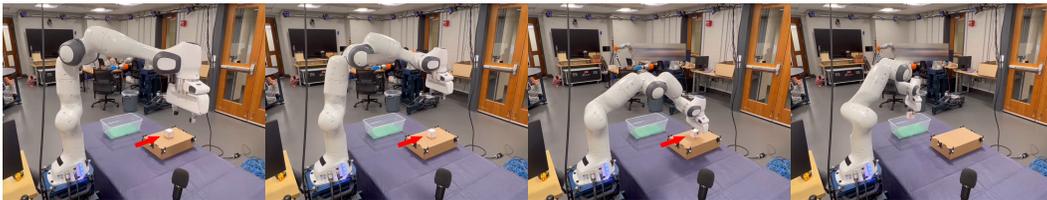


Figure 13: The cube was shifted further away from the robot (The shifting direction is indicated by the red arrow).

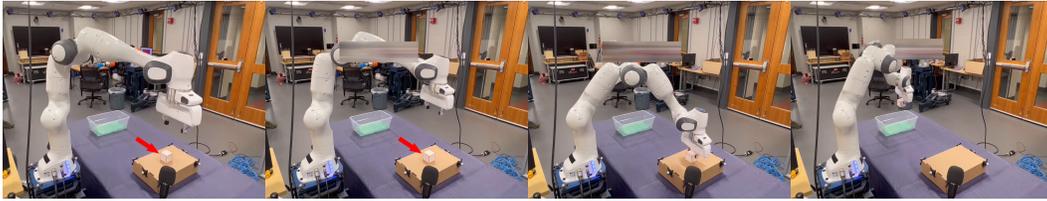


Figure 14: The cube was shifted to the right side of the robot (The shifting direction is indicated by the red arrow).



Figure 15: The cube was shifted slightly to the right side of the robot (The shifting direction is indicated by the red arrow). During the execution, the human held the robot and switched to another cube. After that, the robot finished the task

#### 34 D.1.2 Tunnel

35 In this experiment, we will show the robot how to pass through a tunnel, mimicking an inspection  
 36 task. The entrance and the exit are labeled by two different marker objects. There are a total of three  
 segments in this task.

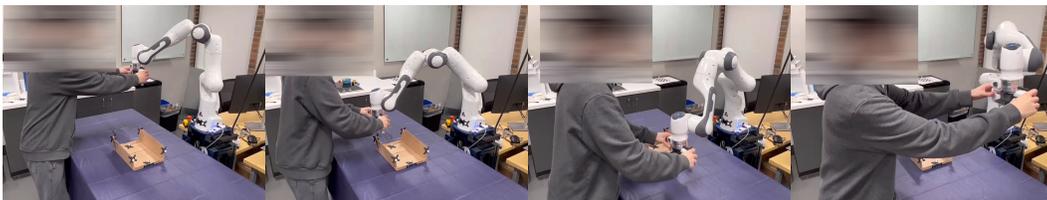


Figure 16: The human guides the end-effector for an inspection task, starting from the left side, passing through a tunnel, and stopping on the right side

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Figure 17: The execution for the learned DS in the original configuration from the demonstration

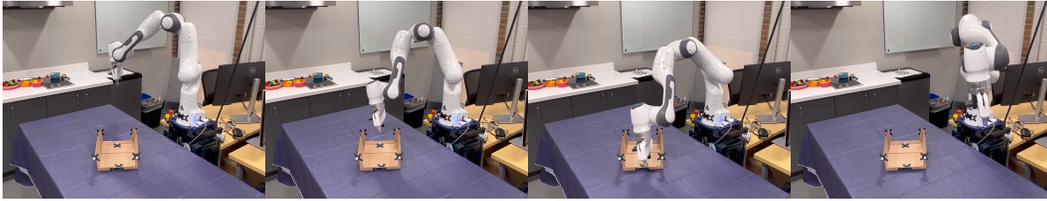


Figure 18: The tunnel is rotated. We rotate the end-effector to be parallel with the tunnel before the execution.

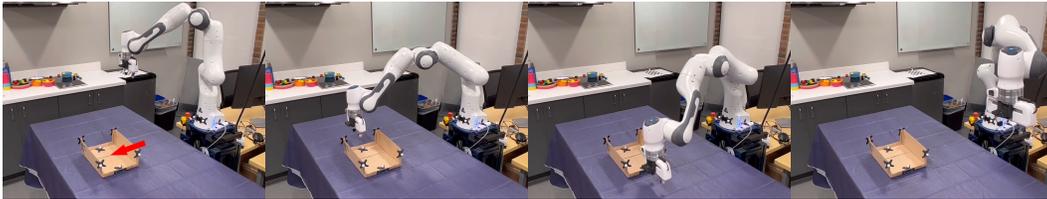


Figure 19: The tunnel is shifted further away from the robot, indicated by the red arrow.



Figure 20: The tunnel is flipped, indicated by the arrow in the tunnel (as opposed to the direction from the demonstration). The robot needs to move to the right side to enter the tunnel and exit to the left side before reaching the end pose.

### 38 D.1.3 Combine

39 There is no demonstration in this task. In the previous experiments, we generate different motion  
 40 policies for different tasks. We can reuse them (the segments being separated by geometric descrip-  
 tors) to compose new sequences which perform new tasks.



Figure 21: Composing the learned DSs with task transfer parameters from the "pick and place" and "tunnel" tasks. The robot is able to pick up a block, pass through the tunnel for scanning, and place the block in the bin. The entire motion does not require extra demonstration. Note the positions of the objects are not the same as in the original demonstrations.



Figure 22: We shift the cube starting platform, the tunnel, and the bin. By reusing and composing the previously learned DS with task transfer, the robot is able to finish the tasks of picking, scanning, and placing without new demonstration in this new environment configuration. Also, there is human disturbance involved during the task execution.

## 41 **References**

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43 for dynamical system learning. In A. Billard, A. Dragan, J. Peters, and J. Morimoto, editors,  
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