#### <span id="page-0-0"></span>**000 001 002 003** DENOISING TASK DIFFICULTY-BASED CURRICULUM FOR TRAINING DIFFUSION MODELS

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## A EXTENDED RELATED WORK

#### A.1 ANALYZING DIFFUSION MODEL BEHAVIORS IN EACH TIMESTEP

**014 015 016 017 018 019 020 021 022 023 024 025 026 027 028 029** In this section, we review works related to analyzing diffusion model behaviors in each timestep but not covered in detail in Section 2.1. Deja *et al.* [\(Deja et al.,](#page-11-0) [2022\)](#page-11-0) explore denoising during the backward diffusion process and observe that transition from denoising to generation exists in the backward process. Go *et al.* [\(Go et al.,](#page-11-1) [2023\)](#page-11-1) investigate the affinity between denoising tasks, showing that temporal proximal denoising tasks exhibit higher task affinity. Then, they also observe that simultaneously learning all denoising tasks by one model suffers from negative transfer. They can achieve better performance than standard diffusion training by alleviating negative transfer. Lee *et al.* [\(Lee et al.,](#page-12-0) [2023\)](#page-12-0) analyze frequency characteristics according to timesteps and observe that high-frequency components are lost as timesteps increase. From this observation, they propose a multi-architecture multi-experts diffusion model, which utilizes multiple denoiser models specialized in each timestep interval but utilizes a transformer-like model as the timestep increases. From observations that smaller and larger models produce similar latent noise, Pan *et al.* [\(Pan et al.,](#page-12-1) [2023\)](#page-12-1) propose T-Stitch, which leverages a pre-trained smaller model at the beginning of the backward process to accelerate the sampling speed. Xu *et al.* [\(Xu et al.,](#page-12-2) [2023\)](#page-12-2) investigate the average traceof-covariance of training targets according to timesteps, showing that it peaks in the intermediate timesteps, causing unstable training targets. For more stable training targets, they utilize weighted conditional scores with a reference batch.

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## A.2 EASY-TO-HARD TRAINING STRATEGY

Progressive distillation [\(Salimans & Ho,](#page-12-3) [2022\)](#page-12-3) focuses on reducing the number of sampling steps by training the model to progressively skip more steps, while cascaded diffusion [\(Ho et al.,](#page-12-4) [2022\)](#page-12-4) aims to improve sample quality by progressively increasing the image resolution during training. Both methods concentrate on altering the model's behavior or structure to tackle specific challenges, such as efficiency or resolution enhancement. In contrast, our work identifies trends in task difficulty across timestep-wise denoising tasks and leverages these findings to propose an easy-to-hard training scheme. This training strategy directly addresses the order and structure of the learning process, optimizing task sequencing to enhance performance. This distinction emphasizes that our approach is fundamentally different from these methods, as it addresses a unique aspect of diffusion model training.

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#### B DETAILED EXPERIMENTAL SETUPS FOR OBSERVATION

**046 047 048 049 050 051 052 053** In Section 4, we examined the difficulty of denoising tasks in terms of convergence with various models  $\{M\}_{i=1}^{20}$ , which are trained within specific timesteps  $\left[\frac{i-1}{20}T, \frac{i}{20}T\right]$  for DiT and SiT, and  $[\Phi^{-1}(\frac{i-1}{N}), \Phi^{-1}(\frac{i}{N})]$  for EDM where  $\Phi^{-1}$  is the inverse cumulative distribution function of the Gaussian distribution. For the DiT architecture, we employed the DiT-B/2, whereas for EDM, we used the DDPM++ architecture. Both DiT and EDM models were trained on the FFHQ dataset, with a batch size of 256, for approximately 20,000 iterations and 4,000 kimg iterations (equivalent to processing 1 million images), respectively. This training was conducted until both loss and performance converged. As illustrated in Fig. A, we additionally plotted the iterations of each timestep interval when their loss values start to oscillate. We measured this by counting the number of times the loss value increased

<span id="page-1-0"></span> after the step reached 100. As shown in the results, losses of all timestep intervals are stabilized within 20K iterations, while the lower timesteps reach this point more slowly. This also suggests that the convergence speed of lower timesteps tends to exhibit a slower regime. To examine specifically at the observation of convergence, we also analyzed the convergence speed on the ImageNet dataset. As shown in Fig. B, we obtained similar results as on the FFHQ dataset. Configuration of training optimizers and learning rates are the same as setups in Section 6.



Figure A: Converged points are plotted during training for each diffusion model  $M_i$  in SiT.



Figure B: Loss convergence plotted during training for each diffusion model  $M_i$  in DiT on ImageNet dataset.

To evaluate the performance of diffusion models through the FID score of the generated images, performing a recursive denoising task from  $T$  to zero is necessary, complicating the assessment using only  $M_i$ . Following [\(Go et al.,](#page-11-1) [2023\)](#page-11-1), we generated samples where  $M_i$  was specifically utilized for denoising within its trained intervals. At the same time, the diffusion model is responsible for the denoising tasks across the entire range of timesteps. For this evaluation, we sampled 10K images using a DDPM sampler over 250 steps for DiT and SiT, and an Euler solver over 40 steps for the other models.

C APPROXIMATION OF KL DIVERGENCE OF  $p_{t-1}$  and  $p_t$ .

 

 Here, we supplement the approximation of KL Divergence of  $p_{t-1}$  and  $p_t$  omitted in Section 4.2.To explore the difficulties of denoising tasks from the distributional viewpoint, we analyze the KL divergence of  $p_{t-1}$  and  $p_t$ ,  $D_{KL}(p_{t-1}||p_t)$ . However, due to the unknown explicit density form of <span id="page-2-1"></span>**108 109**  $p_0$ , it is approximated through unbiased estimators as follows:

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\hat{D}_{KL}\left(p_{t-1}||p_t\right) = \frac{1}{M} \sum_{\substack{i \in \{1, 2, \cdots, M\} \\ \mathbf{x}_i \sim p_{t-1}}} \log\left(\frac{p_{t-1}(\mathbf{x}_i)}{p_t(\mathbf{x}_i)}\right),\tag{1}
$$

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$$
\hat{p}_t(\boldsymbol{x}_t) = \frac{1}{L} \sum_{\substack{j \in \{1, 2, \cdots, L\} \\ \boldsymbol{y}_j \sim p_0}} p_{0t}(\boldsymbol{x}_t | \boldsymbol{x}_0 = \boldsymbol{y}_j), \tag{2}
$$

**117 118** where  $D_{KL}$  and  $\hat{p}_t$  are unbiased estimators of  $D_{KL}$  and  $p_t$ , respectively, and we choose Monte-Carlo estimators for them [\(Glasserman,](#page-11-2) [2004;](#page-11-2) [McLeish,](#page-12-5) [2011\)](#page-12-5).

**119 120 121 122 123 124 125** We sampled 5,000 images to approximate the KL divergence, which is enough for Monte-Carlo sampling and might be no changes for larger samples. Despite the large amount of samples, the exploding appearance observed in Fig. 2 when  $t$  is close to zero is due to the characteristics of the data distribution. The image data distribution has narrow support (roughly speaking, it is non-zero only within a narrow range) [\(Ruderman & Bialek,](#page-12-6) [1993;](#page-12-6) [Karras et al.,](#page-12-7) [2024\)](#page-12-7). As t increases, information about the original data distribution gradually diminishes with the modes in the distribution of  $x_t$ vanishing towards zero.

**126 127 128 129 130 131 132** Given this, when t is close to zero (i.e. when the distribution of  $x_t$  is still analogous to the original data distribution), the narrow support and the tendency to move towards zero give rise to a region where  $p_{t-1}$  does not overlap with  $p_t$ . Consequently, when calculating the KL divergence  $D_{KL}(p_{t-1}||p_t)$  =  $E_{x \sim p_{t-1}}[\log(\frac{p_{t-1}(x)}{p_t(x)})], x_{t-1}$  potentially falls outside the support of  $p_t$ , which leads to  $p_t(x_{t-1}) = 0$ and numerical unstability. On the other hand, as  $t$  increases, the accumulated noise broadens the support of x's distribution, reducing the occurrence of zero values and stabilizing the numerical estimation.

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#### D ALGORITHM

**136 137 138 139 140** Due to the limited space of the main manuscript, we hereby present the step-by-step process of our method to supplement the details of our approach. The pacing function, which determines the moments to transit between curriculum stages is described in Algorithm [1.](#page-2-0) By incorporating this pacing function, the detailed procedure of our proposed curriculum learning method for training diffusion is illustrated in Algorithm [2.](#page-2-0)

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#### E DETAILS ON EXPERIMENTAL SETUPS

**<sup>160</sup> 161** Evaluation metrics. To evaluate the performance of models, we utilized three metrics: FID [\(Heusel](#page-11-3) [et al.,](#page-11-3) [2017\)](#page-11-3), IS [\(Salimans et al.,](#page-12-8) [2016\)](#page-12-8), and Precision/Recall [\(Kynkäänniemi et al.,](#page-12-9) [2019\)](#page-12-9). Specifically, we applied FID and IS to measure sample quality, while Precision is used to assess quality further

<span id="page-3-0"></span> and Recall was utilized to evaluate the diversity of the generated samples in ImageNet setup. In other datasets, we employed FID to evaluate sample quality. Unless otherwise mentioned, we sampled 50K samples for evaluation. In tasks involving conditional generation, including class-conditional image generation (e.g. CIFAR-10, ImageNet) and text-to-image conversion (e.g. MS-COCO), we adapted the classifier-free guidance (Ho  $&$  Salimans, [2022\)](#page-12-10) with a guidance scale of 1.5.

**Training details.** For training diffusion models, we utilized the AdamW optimizer [\(Loshchilov](#page-12-11)  $\&$  Hutter, [2017\)](#page-12-11) with a constant learning rate of 0.0001, and weight decay was not applied. The exponential moving average (EMA) to the model's weights was used to stabilize the training and the decay ratio was set to 0.9999. The batch size was set to 256, and we augmented the training data by a horizontal flip. While the diffusion timestep  $T$  was configured as 1,000 for all experiments, we trained for 100K iterations for the FFHQ dataset [\(Karras et al.,](#page-12-12) [2019\)](#page-12-12), and 400K iterations for the ImageNet dataset [\(Deng et al.,](#page-11-4) [2009\)](#page-11-4) and MS-COCO dataset [\(Lin et al.,](#page-12-13) [2014\)](#page-12-13). The number of clusters N was 20 unless otherwise specified. The maximum patience  $\tau$  was varied across model sizes: it was set at 200 for DiT-S/2, DiT-B/2, and EDM, and 400 for DiT-L/2. EDM was trained using fp16, while the other models were trained using fp32. We used 8 A100 GPUs for all experiments.



Figure C: Qualitative comparison between vanilla, naive curriculum, and ours on the FFHQ dataset.





## F QUALITATIVE RESULTS

 

> In this section, we present qualitative comparisons between three methods: 1) *Vanilla*, 2) *NaiveCL*, and 3) *Ours*, across the FFHQ, ImageNet, and MS-COCO datasets. All methods are evaluated using



"A man is on a path riding a horse." "Tower of a brick "A dog leaps through "A person in white and "A group of young "A young boy is smil-"a small boy with a hat building with a clock the air as it catches a red snow suit skiing on the front." frisbee." on a slope." playing game of soccer." ing and he has food is standing on a surf around him on a ta-board." ble."

Figure E: Qualitative comparison between vanilla, naive curriculum, and ours on MS-COCO dataset.

DiT-B models, and the final trained models generate all samples shown in the results. As shown in the results in the following subsections, our approach can synthesize more accurate and realistic images compared to *Vanilla* and *NaiveCL*.

## F.1 QUALITATIVE EVALUATION ON THE FFHQ DATASET.

Figure C presents a qualitative analysis of the performance in unconditional facial image synthesis among the vanilla, the naive curriculum approach, and our method. Our approach demonstrates superior ability in generating realistic images.

**244** F.2 QUALITATIVE ANALYSIS ON THE IMAGENET DATASET.

**246 247 248** In the conditional image synthesis, we exhibit the outcomes generated by the vanilla, the naive curriculum strategy, and our proposed method. Figure D clearly shows that our methodology surpasses the competing approaches in terms of quality.

F.3 QUALITATIVE ASSESSMENT ON THE MS-COCO DATASET.

To further substantiate the effectiveness of our proposed technique, we conduct a qualitative comparison of the results in the text-to-image generation task among the vanilla, the naive curriculum method, and our own approach, as depicted in Fig. E.

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## G FURTHER EXPERIMENTAL RESULTS

G.1 CONVERGENCE SPEED ACROSS MODEL SIZE

**262** By leveraging the advantages of curriculum learning in diffusion training, our method offers faster convergence than vanilla training. To further investigate this aspect, we measured FID-10K through training iterations for DiT-S and DiT-L. Figure F describes the results, showing that our curriculum approach achieves faster convergence in both models. These results also support the effectiveness of our method.

G.2 ROBUSTNESS ON NOISE SCHEDULE

**267 268 269** For a more comprehensive ablation study, we also trained the diffusion model with different noise schedules. In contrast to cosine scheduling, the  $\beta_t$  is set by uniformly dividing the interval  $[0.0001, 0.02]$ , and the  $C_i$  are obtained corresponding to SNR on a linear schedule. As shown in Table. A, our approach improves the performance with cosine and linear noise schedulers.

  $-$  DiT-S/2 DiT-S/2 + Ours  $-$  - DiT-B/2 DiT-B/2 + Ours  $\overline{\phantom{a}}$  $\rightarrow$  DiT-L/2 DiT-L/2 + Ours FID-10k 150 200 250 300 350 400 Training Steps(K)

Figure F: We observed an increase in convergence speed across various model sizes when the proposed curriculum learning approach was applied.

Table A: Ablation study on noise scheduler. Note that our approach improves performance consistently across each scheduler.

Class-Conditional ImageNet $256\times256$ .					
Schedule	Method	FIDJ	IS↑	Prec <sup><math>\uparrow</math></sup>	$Rec+$
cosine	Vanilla	30.27	60.06	0.55	0.52
	Ours	22.22	75.98	0.62	0.52
linear	Vanilla	16.99	83.62	0.68	0.53
	Ours	16.03	87.66	0.69	0.53

 

#### G.3 QUALITATIVE RESULTS FROM DIT-L/2 WITH 2M ITERATIONS

In Figures G-K, we present images generated by DiT-L using our curriculum training method for 2M iterations. The results demonstrate that our method produces highly realistic images.





- Figure G: Uncurated 256×256 DiT-L/2 samples. Classifier-free guidanzce scale = 2.0. Class label = "golden retriever" (207)
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- Figure H: Uncurated 256×256 DiT-L/2 samples. Classifier-free guidance scale = 2.0. Class label = "panda"  $(388)$
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- Figure I: Uncurated 256×256 DiT-L/2 samples. Classifier-free guidance scale = 2.0. Class label = "cliff drop-off" (972)
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- Figure J: Uncurated 256×256 DiT-L/2 samples. Classifier-free guidance scale = 2.0. Class label = "lake shore" (975)
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- Figure K: Uncurated 256×256 DiT-L/2 samples. Classifier-free guidance scale = 2.0. Class label = "lion"  $(291)$
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# H DISCUSSION ON SIMILARITY WITH THE PREVIOUS WORK

**598 599 600 601 602 603 604 605 606 607 608 609** While both our work and [\(Go et al.,](#page-11-1) [2023\)](#page-11-1) explore the characteristics of denoising tasks in diffusion models, the aspects of exploration in each work are substantially different. The notion of task affinity introduced in [\(Fifty et al.,](#page-11-5) [2021;](#page-11-5) [Go et al.,](#page-11-1) [2023\)](#page-11-1) refers to how harmoniously the model can learn multiple tasks together. Specifically, their work focuses on identifying and mitigating conflicts between tasks, emphasizing task interactions and transferability by analyzing task similarities (e.g., gradient similarity or alignment). In contrast, our work explicitly quantifies the relative difficulty of individual denoising tasks across timesteps as a standalone property, independent of task interdependencies. The analysis of task difficulty in our work involves evaluating metrics such as loss behavior or convergence rates, directly reflecting the complexity of solving each task at different timesteps. Therefore, while [\(Go et al.,](#page-11-1) [2023\)](#page-11-1) addresses how tasks relate and interact during multi-task learning, our focus lies in systematically characterizing the intrinsic difficulty of tasks across timesteps in diffusion models.

**610 611** I BROADER IMPACTS

> Generative models, such as diffusion models, have the potential to significantly impact society, particularly through DeepFake applications and the use of biased datasets. One primary concern is the possibility for these models to amplify misinformation, which can erode trust in visual media. Additionally, if these models are trained on biased or deliberately altered content, they may unintentionally perpetuate and intensify existing social biases. This situation may result in the dissemination of incorrect information and the manipulation of public opinion.

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## J LIMITATIONS

**624 625 626** In this work, we demonstrated the varying difficulties of denoising tasks through empirical results on various diffusion frameworks and proposed a curriculum learning approach that effectively enhances diffusion model training. While we have shown the robustness of our method's hyperparameters in improving vanilla diffusion training, there is potential for further improvement. Specifically, curriculum learning methods that utilize smaller hyperparameters and adjust dynamically based on the model itself could yield better results. We acknowledge the validity of this direction and consider it a promising avenue for future work.

## **REFERENCES**

- <span id="page-11-0"></span>**631 632 633** Kamil Deja, Anna Kuzina, Tomasz Trzcinski, and Jakub Tomczak. On analyzing generative and denoising capabilities of diffusion-based deep generative models. *Advances in Neural Information Processing Systems*, 35:26218–26229, 2022. [1](#page-0-0)
	- Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pp. 248–255. Ieee, 2009. [4](#page-3-0)
- <span id="page-11-5"></span><span id="page-11-2"></span>**637 638 639 640** Chris Fifty, Ehsan Amid, Zhe Zhao, Tianhe Yu, Rohan Anil, and Chelsea Finn. Efficiently identifying task groupings for multi-task learning. *Advances in Neural Information Processing Systems*, 34: 27503–27516, 2021. [12](#page-11-6)
	- Paul Glasserman. *Monte Carlo methods in financial engineering*, volume 53. Springer, 2004. [3](#page-2-1)
	- Hyojun Go, JinYoung Kim, Yunsung Lee, Seunghyun Lee, Shinhyeok Oh, Hyeongdon Moon, and Seungtaek Choi. Addressing negative transfer in diffusion models. *arXiv preprint arXiv:2306.00354*, 2023. [1,](#page-0-0) [2,](#page-1-0) [12](#page-11-6)
- <span id="page-11-3"></span><span id="page-11-1"></span>**646 647** Martin Heusel, Hubert Ramsauer, Thomas Unterthiner, Bernhard Nessler, and Sepp Hochreiter. Gans trained by a two time-scale update rule converge to a local nash equilibrium. *Advances in neural information processing systems*, 30, 2017. [3](#page-2-1)
- <span id="page-12-10"></span> Jonathan Ho and Tim Salimans. Classifier-free diffusion guidance. *arXiv preprint arXiv:2207.12598*, 2022. [4](#page-3-0)
- <span id="page-12-4"></span> Jonathan Ho, Chitwan Saharia, William Chan, David J Fleet, Mohammad Norouzi, and Tim Salimans. Cascaded diffusion models for high fidelity image generation. *Journal of Machine Learning Research*, 23(47):1–33, 2022. [1](#page-0-0)
- <span id="page-12-12"></span> Tero Karras, Samuli Laine, and Timo Aila. A style-based generator architecture for generative adversarial networks. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 4401–4410, 2019. [4](#page-3-0)
	- Tero Karras, Miika Aittala, Tuomas Kynkäänniemi, Jaakko Lehtinen, Timo Aila, and Samuli Laine. Guiding a diffusion model with a bad version of itself. *arXiv preprint arXiv:2406.02507*, 2024. [3](#page-2-1)
- <span id="page-12-9"></span><span id="page-12-7"></span> Tuomas Kynkäänniemi, Tero Karras, Samuli Laine, Jaakko Lehtinen, and Timo Aila. Improved precision and recall metric for assessing generative models. *Advances in Neural Information Processing Systems*, 32, 2019. [3](#page-2-1)
- <span id="page-12-0"></span> Yunsung Lee, Jin-Young Kim, Hyojun Go, Myeongho Jeong, Shinhyeok Oh, and Seungtaek Choi. Multi-architecture multi-expert diffusion models. *arXiv preprint arXiv:2306.04990*, 2023. [1](#page-0-0)
- <span id="page-12-13"></span> Tsung-Yi Lin, Michael Maire, Serge Belongie, James Hays, Pietro Perona, Deva Ramanan, Piotr Dollár, and C Lawrence Zitnick. Microsoft coco: Common objects in context. In *Computer Vision– ECCV 2014: 13th European Conference, Zurich, Switzerland, September 6-12, 2014, Proceedings, Part V 13*, pp. 740–755. Springer, 2014. [4](#page-3-0)
- <span id="page-12-11"></span> Ilya Loshchilov and Frank Hutter. Decoupled weight decay regularization. *arXiv preprint arXiv:1711.05101*, 2017. [4](#page-3-0)
- <span id="page-12-5"></span> Don McLeish. A general method for debiasing a monte carlo estimator. *Monte Carlo methods and applications*, 17(4):301–315, 2011. [3](#page-2-1)
- <span id="page-12-1"></span> Zizheng Pan, Bohan Zhuang, De-An Huang, Weili Nie, Zhiding Yu, Chaowei Xiao, Jianfei Cai, and Anima Anandkumar. T-stitch: Accelerating sampling in pre-trained diffusion models with trajectory stitching. 2023. [1](#page-0-0)
- <span id="page-12-6"></span> Daniel Ruderman and William Bialek. Statistics of natural images: Scaling in the woods. *Advances in neural information processing systems*, 6, 1993. [3](#page-2-1)
- <span id="page-12-3"></span> Tim Salimans and Jonathan Ho. Progressive distillation for fast sampling of diffusion models. *arXiv preprint arXiv:2202.00512*, 2022. [1](#page-0-0)
- <span id="page-12-8"></span> Tim Salimans, Ian Goodfellow, Wojciech Zaremba, Vicki Cheung, Alec Radford, and Xi Chen. Improved techniques for training gans. *Advances in neural information processing systems*, 29, 2016. [3](#page-2-1)
	- Yilun Xu, Shangyuan Tong, and Tommi Jaakkola. Stable target field for reduced variance score estimation in diffusion models. *arXiv preprint arXiv:2302.00670*, 2023. [1](#page-0-0)

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