

## Supplementary Material for “Diffusion Model Based Posterior Sampling for Noisy Linear Inverse Problems”

In this supplementary material, we provide results on the effect of scaling parameter  $\lambda$ , as well as results on more datasets.

### Effect of Scaling Parameter $\lambda$

As shown in both Algorithm 1 and Algorithm 2, a hyper-parameter  $\lambda$  is introduced as a scaling value for the likelihood score. Empirically it is found that DMPS is robust to different choices of  $\lambda$  around 1 though most of the time  $\lambda > 1$  yields slightly better results. As one specific example, we show the results of DMPS for super-resolution for different values of  $\lambda$ , as shown in Figure 5 (DDPM version) and Figure 6 (flow-based version). It can be seen that DMPS is robust to different choices of  $\lambda$ , i.e., it works well in a wide range of values.



Figure 5: Results of DMPS (DDPM version) with different  $\lambda$  for the task of noisy super-resolution ( $\times 4$ ) with  $\sigma = 0.05$ .

### Results on More Datasets

We provide more experimental results on AFHQ-cat and LSUN-bedroom for flow-based models are shown as follows:

Method	super-resolution			deblur			colorization			denoising		
	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$
DMPS (DDPM, ours)	<b>26.79</b>	<b>0.7653</b>	<b>0.2632</b>	<b>27.22</b>	<b>0.7571</b>	<b>0.2909</b>	<b>25.07</b>	<b>0.9190</b>	<b>0.3124</b>	28.59	<b>0.7994</b>	<b>0.2882</b>
DPS (DDPM)	23.08	0.6127	0.3860	24.64	0.6625	0.3033	15.92	0.5976	0.6381	<b>28.86</b>	0.7828	0.2941
PGDM	25.44	0.7185	0.2837	26.69	0.7316	0.2896	16.74	0.6348	0.5335	27.06	0.7453	0.3236

Table 3: Results on FFHQ-Cat validation dataset using the same pre-trained DDPM model.



Figure 6: Results of DMPS (flow-based version) with different  $\lambda$  for the task of noisy super-resolution ( $\times 4$ ) with  $\sigma = 0.05$ .

Method	super-resolution			deblur			colorization			denoising		
	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$
DMPS (DDPM, ours)	<b>25.63</b>	<b>0.7362</b>	<b>0.2281</b>	<b>28.21</b>	<b>0.8162</b>	<b>0.2113</b>	<b>23.19</b>	<b>0.9344</b>	<b>0.2117</b>	29.81	0.8599	0.1884
DPS (DDPM)	22.83	0.6190	0.3275	24.97	0.6988	0.2593	11.38	0.5375	0.6606	<b>30.75</b>	<b>0.8674</b>	<b>0.1841</b>
PGDM	24.60	0.6854	0.2590	26.90	0.7721	0.2482	17.69	0.7335	0.3350	27.90	0.8153	0.2304

Table 4: Results on LSUN-Bedroom validation dataset using the same pre-trained DDPM model.

Method	super-resolution			deblur			colorization			denoising		
	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$
DMPS (Flow-based, ours)	<b>29.06</b>	<b>0.7905</b>	<b>0.2627</b>	<b>26.74</b>	<b>0.6942</b>	<b>0.3192</b>	24.65	<b>0.9140</b>	<b>0.2531</b>	<b>26.53</b>	<b>0.7870</b>	<b>0.3353</b>
DPS (Flow-based)	27.61	0.7089	0.3190	23.26	0.5534	0.4122	21.64	0.8259	0.3833	26.10	0.6418	0.4049
OT-ODE	27.61	0.7081	0.3205	26.32	0.6592	0.3333	<b>25.21</b>	0.8692	0.3180	23.12	0.3647	0.5289

Table 5: Results on AFHQ-Cat validation dataset using the same pre-trained flow-based model.

Method	super-resolution			deblur			colorization			denoising		
	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$	PSNR $\uparrow$	SSIM $\uparrow$	LPIPS $\downarrow$
DMPS (Flow-based, ours)	<b>24.36</b>	<b>0.6795</b>	0.3837	<b>23.19</b>	<b>0.5869</b>	<b>0.4384</b>	<b>23.37</b>	<b>0.8756</b>	<b>0.2838</b>	22.68	<b>0.6477</b>	<b>0.4458</b>
DPS (Flow-based)	24.39	0.6430	<b>0.3781</b>	20.13	0.4318	0.4931	11.03	0.5283	0.7843	23.18	0.5457	0.4598
OT-ODE	23.88	0.6193	0.4001	22.69	0.5590	0.4264	<b>23.62</b>	0.7592	0.3923	18.17	0.2039	0.6405

Table 6: Results on LSUN-Bedroom validation dataset using the same pre-trained flow-based model.