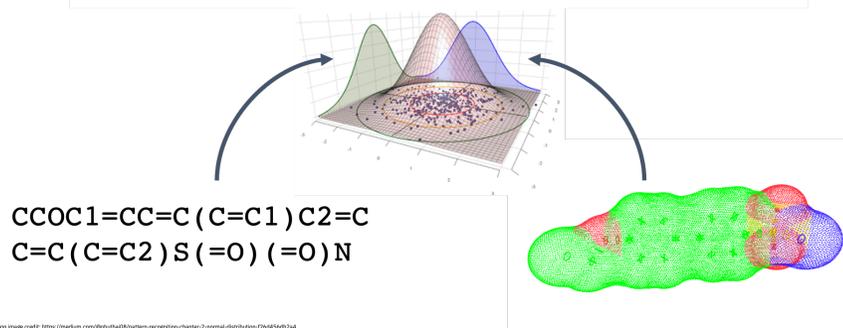


Characterizing the Latent Space of Molecular Deep Generative Models with Persistent Homology Metrics

Motivation

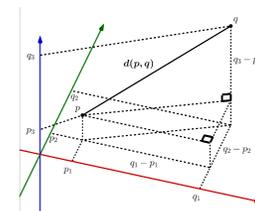
How much relevant semantic information is captured in the latent space of molecular generative models?



Distribution image credit: <https://medium.com/@math408/pattern-recognition-chapter-2-normal-distribution-f26656d2d4>

Approach

Euclidean distance of latent vectors



L2 distance of Restricted Hilbert function of 2-parameter persistence diagrams

$$| \text{Hil}_F^i(a) := \beta_i(F_a) |$$

$$\text{RH}_F^i(a) := \begin{cases} \text{Hil}_F^i(a) & \text{for } a \in R_i(F), \\ 0 & \text{otherwise.} \end{cases}$$

$$\ell_2(f, g) = \sqrt{\int (f - g)^2 dA}$$

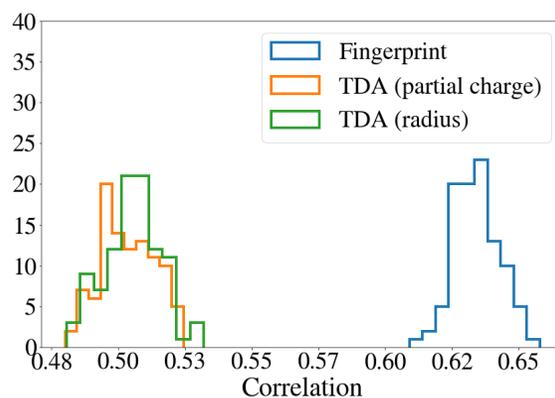
vs.

Tanimoto distance on Fingerprint representations

$$\text{Tanimoto}(A, B) = \frac{A \cap B}{A \cup B}$$

Euclidean distance image credit: https://commons.wikimedia.org/wiki/File:Euclidean_distance_3d_1_cropped.png

Results



Metric correlation analysis on a recent molecular VAE reveals that topological features are consistently preserved across that model's latent space

	Training data			Random latent sample		
	Fingerprint	TDA (partial charge)	TDA (radius)	Fingerprint	TDA (partial charge)	TDA (radius)
Median	0.635	0.503	0.507	0.377	0.464	0.449
Mean	0.636	0.504	0.506	0.377	0.465	0.449
Std. dev.	0.008	0.010	0.010	0.014	0.010	0.011

