
Factorized Tensor Networks for Multi-Task and Multi-Domain Learning (Supplementary Material)

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1 In this section, we present additional material and details to supplement the main paper.

2 **A Dataset and training details**

3 **A.1 Imagenet-to-sketch dataset**

4 The dataset contains five different domains: Flowers [1], Cars [2], Sketch [3], Caltech-UCSD Birds
5 (CUBs) [4], and WikiArt [5] with 102, 195, 250, 196, and 200 classes, respectively. We randomly
6 crop images from each domain to 224×224 pixels, along with normalization and random horizontal
7 flipping. We report the baseline experiments, Fine-Tuning, Feature-Extractor, and 'FC and BN only'
8 with 0.005 learning rate (lr) and SGD optimizer with no weight decay. We train for 30 epochs with a
9 batch size 32 and a cosine annealing learning rate scheduler.

10 The experiments with our proposed FTN approach are learned through the Adam optimizer with
11 lr 0.005 for low-rank layers and through the SGD optimizer with lr 0.008 for remaining trainable
12 layers (task-specific batchnorm and classification layers). Again, we train them for 30 epochs with
13 batch size 32 and cosine annealing scheduler. We showed the experiments for different low-ranks,
14 $R \in \{1, 5, 10, 15, 20, 25, 50\}$.

15 **A.2 DomainNet dataset**

16 This dataset contains six domains: Clipart, Sketch, Painting (Paint), Quickdraw (Quick), Infograph
17 (Info), and Real, with an equal number of 345 classes/categories. We train the baseline experiments,
18 Fine-Tuning, Feature-Extractor, and 'FC and BN only' with 0.005 lr with 0.0001 weight decay and
19 SGD optimizer. Similar to the Imagenet-to-sketch dataset, we apply the same data augmentation
20 techniques and train for 30 epochs with 32 batch size and a cosine annealing learning rate scheduler.

21 For our experiments with the FTN method, we train the low-rank tensor layers with Adam optimizer
22 and 0.005 lr. The remaining layers were optimized using the SDG optimizer with the same 0.005
23 learning rate and no weight decay. We train the FTN networks for 30 epochs with the same learning
24 rate scheduler. We showed our experiments for different low-ranks, $R \in \{1, 5, 10, 20, 30, 40\}$.

25 **A.3 NYUD dataset**

26 In multi-task learning, we use NYUD dataset, which consists of 795 training and 654 testing
27 images of indoor scenes, for dense prediction experiments. It has four tasks: edge detection (Edge),
28 semantic segmentation (SemSeg), surface normals estimation (Normals), and depth estimation
29 (Depth). We evaluated the performance using optimal dataset F-measure (odsF) for edge detection,
30 mean intersection over union (mIoU) for semantic segmentation, and mean error (mErr) for surface
31 normals. At the same time, we report root mean squared error (RMSE) for depth. We perform random

32 scaling in the range of $[0.5, 2.0]$ and random horizontal flipping for data augmentation and resize
 33 each image to 425×560 . We train our baseline experiments, Fine-tuning, Feature Extractor, and 'FC
 34 and BN only' for 60 epochs with batch size 8 and polynomial learning rate scheduler. We learn the
 35 network using SGD optimizer and 0.005 learning rate with 0.9 momentum and 0.0001 weight decay.

36 In FTN we train for the same 60 epochs, batch size 8, and polynomial learning rate scheduler. We
 37 learn over low-rank layers using the Adam optimizer with a 0.01 learning rate and no weight decay.
 38 The remaining decoder and batchnorm layers are optimized using the same hyperparameters used for
 39 baseline experiments. This dataset shows experiments with different low-ranks, $R \in \{1, 10, 20, 30\}$.

40 B Effect on performance with different number of low-rank factors.

41 We performed an experiment by removing the low-rank factors from our trained FTN backbone
 42 network at different thresholds. We perform this experiment on five domains of the Imagenet-to-
 43 sketch dataset and compute the ℓ_2 -norm of ΔW at every layer. We selected equally spaced threshold
 44 values from the minimum and maximum ℓ_2 -norm and removed the low-rank factors below the
 45 threshold. The performance vs. the number of parameters of low-rank layers for different thresholds
 46 is shown in Figure S1. We observe a drop in performance on every domain as we increase the
 47 threshold and reduce the number of layers from the backbone. Interestingly, when we reduce
 48 the number of layers from 52 to 28 on the Flowers and CUBS dataset, we did not see a significant drop
 49 in accuracy.

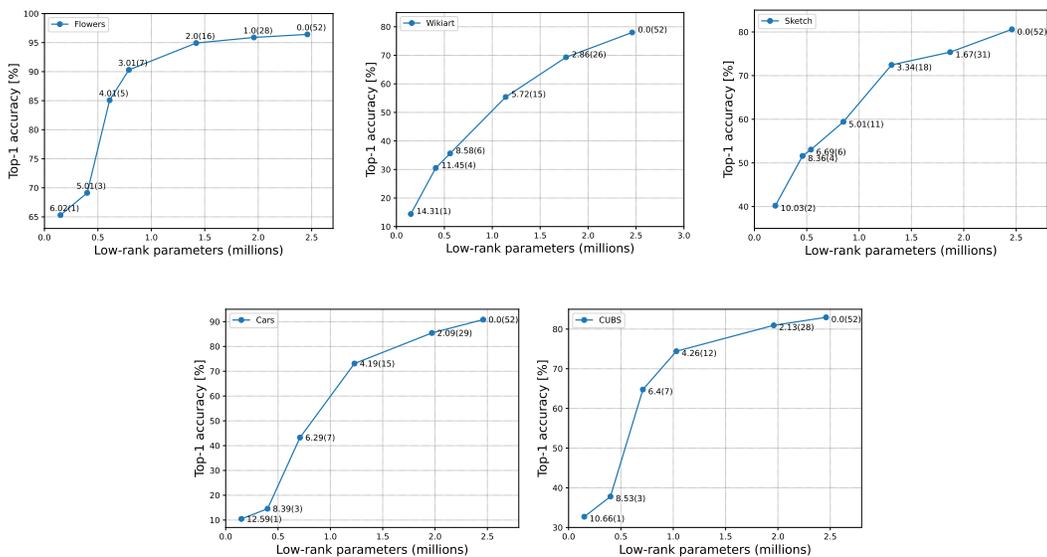


Figure S1: Performance on five domains of the Imagenet-to-sketch dataset as we remove the low-rank parameters. We selected the number of layers in the backbone based on a moving threshold. We annotate the specified threshold at each marker point and the number of affected layers (in parentheses).

50 C Visualization of changes in FTN with low-rank factors

51 We present the norm of low-rank factors at every adapted layer in the backbone of our FTN as a
 52 heatmap in Figures S2–S3. The colors indicate relative norms because we normalized them for every
 53 network in the range 0 to 1 to highlight the relative differences. Figure S2 presents results on five
 54 domains of the Imagenet-to-sketch dataset (resnet-50 backbone), adapting every layer with rank-50
 55 FTN. We observe the maximum changes in the last layer of the backbone network instead of the
 56 initial layers. We also show a similar trend on the DomainNet dataset with resnet-34 backbone where
 57 maximum changes occur in the network's later layer (see Figure S4). We observe from Figure S3 that
 58 on the wikiart domain of the Imagenet-to-sketch dataset, the layers in the backbone network become
 59 more adaptive upon increasing the rank of FTN. The rank-50 FTN has more task adaptive layers than
 60 the rank-1 FTN on the wikiart domain.

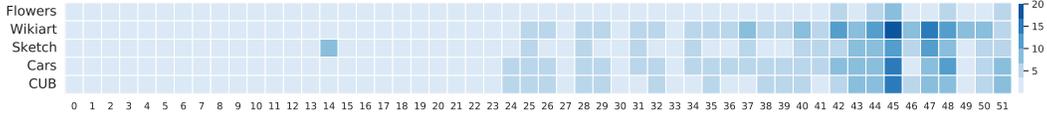


Figure S2: Norm of low-rank factors in the adapted backbone layers for different domains of the Imagenet-to-sketch dataset with $R = 50$.

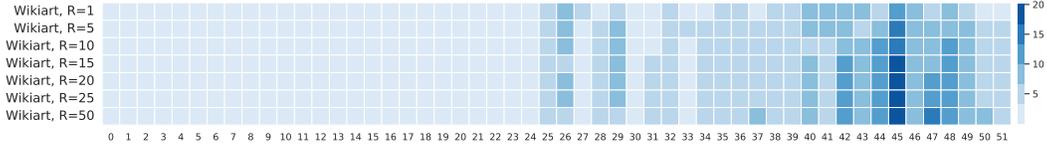


Figure S3: Norm of low-rank factors in the adapted backbone layers for different values of $R \in \{1, 5, 10, 15, 20, 25, 50\}$ with the wikiart domain of the Imagenet-to-sketch dataset.

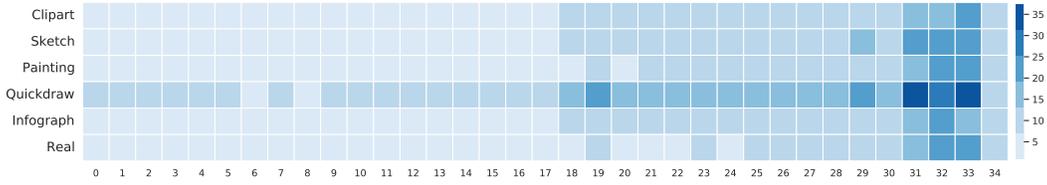


Figure S4: Norm of low-rank factors in the adapted backbone layers for different domains of the DomainNet dataset with $R = 40$.

61 D Results on DomainNet dataset under joint setting

62 We performed additional experiments under a joint learning setup on the DomainNet dataset. A single
 63 model is trained jointly on all the domains of the dataset with Fine-Tuning setup. Table S1 summarizes
 64 the results for the performance of the DomainNet dataset under a joint setup. The domains under this
 65 setting share information among each other for all parameters. The Fine-Tuning experiment achieves
 66 the overall best performance, but at the expense of a large number of parameters. We observe poor
 67 performance for the shared Feature Extractor, since that does not learn any additional task-specific
 68 parameters. The results in the third row show that by changing just the task-specific batchnorm layers
 69 in the jointly trained backbone, we can achieve better results than TAPS and Adashare. Our FTN
 70 with just $R = 1$ also outperforms Adashare and TAPS.

Table S1: Performance on DomainNet dataset under joint setting using resnet34 backbone (initialized with jointly trained weights) with our FTN approach along with comparison methods.

Methods	Params (Abs)	Clipart	Sketch	Paint	Quick	Info	Real	mean
Fine-tuning	$6 \times (127.68\text{M})$	77.43	69.25	69.21	71.61	41.50	80.74	68.29
Feature extractor	$1 \times (21.28\text{M})$	76.67	65.2	65.26	52.97	35.05	76.08	61.87
FC and BN only	$1.004 \times (21.35\text{M})$	77.07	68.34	68.76	69.06	40.63	79.07	67.15
Adashare	$1 \times (21.28\text{M})$	75.88	63.96	67.90	61.17	31.52	76.90	62.88
TAPS	$1.46 \times (31.06\text{M})$	76.98	67.81	67.91	70.18	39.30	78.91	66.84
FTN, R=1	$1.008 \times (21.45\text{M})$	77.13	68.10	68.50	69.41	40.04	79.49	67.11

71 E Image generation training details and results

72 E.1 Transient attributes dataset

73 The Transient attributes dataset [6] contains a total of 8571 images with 40 annotated attribute labels.
 74 Each label is associated with a score in the $[-1, 1]$ range. We utilize the associated confidence score
 75 for each season to build our collection of images for each season. Additionally, we only selected

Table S2: FTN PSNR for image generation under $R = \{20, 50\}$

Season	Rank 20	Rank 50
Winter	18.11	22.23
Spring	18.89	20.50
Autumn	17.95	20.08

76 images that were captured during daytime. Our training set consisted of 1875 summer, 1405 spring,
77 1353 autumn, and 2566 winter images. We normalized each image to the range of $[-1, 1]$ and resized
78 them to a resolution of 128×128 .

79 E.2 Training details

80 Our base network follows the BigGAN architecture [7] that was pre-trained for 100k iterations on
81 ImageNet using 128×128 images. We trained all the networks in this experiment using Adam
82 optimizer. We used a learning rate of 0.05 for the low-rank tensors and a learning rate of 0.001 for the
83 linear layers. We did not use any weight decay. We trained for 2000 epochs with a cosine annealing
84 learning rate scheduler and an early stopping criterion ranging from 200 to 600 iterations.

85 E.3 Additional results

86 Figure S5, we show additional generated images by our FTN network. In addition, table S2 shows the
87 average performance of our FTN network under different rank settings. We observe a performance
88 increase by increasing the rank R of our low-rank factors.



Figure S5: Generated images for different seasons using FTN.

89 **References**

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91 classes,” in *2008 Sixth Indian Conference on Computer Vision, Graphics & Image Processing*.
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