

546 **Test-Time Adaptation to Distribution Shifts**  
 547 **by Confidence Maximization and Model Augmentation**

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550 **A Appendix**

551 **A.1 Input transformation module**

552 Note that we define our adaptable model as  $g = f \circ d$ , where  $d$  is a trainable network prepended to a  
 553 pretrained neural network  $f$  (e.g., pretrained ResNet50). We choose  $d(x) = \gamma \cdot [\tau x + (1 - \tau)r_\psi(x)] +$   
 554  $\beta$ , where  $\tau \in \mathbb{R}$ ,  $(\beta, \gamma) \in \mathbb{R}^{n_{in}}$  with  $n_{in}$  being the number of input channels,  $r_\psi$  being a network with  
 555 identical input and output shape, and  $\cdot$  denoting elementwise multiplication. Here,  $\beta$  and  $\gamma$  implement  
 556 a channel-wise affine transformation and  $\tau$  implements a convex combination of unchanged input  
 557 and the transformed input  $r_\psi(x)$ . We set  $\tau = 1$ ,  $\gamma = \mathbf{1}$ , and  $\beta = \mathbf{0}$ , to ensure that  $d(x) = x$  and thus  
 558  $g = f$  at initialization. In principle,  $r_\psi$  can be chosen arbitrarily. In this work, we choose  $r_\psi$  as a  
 559 simple stack of  $3 \times 3$  convolutions with stride 1 and padding 1, group normalization, and ReLUs  
 560 without any upsampling/downsampling layers. Specifically, the structure of  $g$  is illustrated in Figure  
 561 A1.

562 **A.2 Frozen layers in different networks**

563 As discussed in Section 3.2.2, we freeze all trainable parameters in the top layers of the networks to  
 564 prohibit “logit explosion”. That implies, we do not optimize the channel-wise affine transformations  
 565 of the top layers but normalization statistics are still estimated. Similar to the hyperparameters of  
 566 test time adaptation settings, the choice of these layers are made using ImageNet-C validation data.  
 567 We mention the frozen layers of each architecture below. Note that the naming convention of these  
 568 layers are based on the model definition in torchvision:

- 569 • DenseNet121 - *features.denseblock4, features.norm5*.
- 570 • MobileNetV2 - *features.16, features.17, features.18*.
- 571 • ResNeXt50, ResNet50 and ResNet50 (DeepAugment+Augmix) - *layer4*.

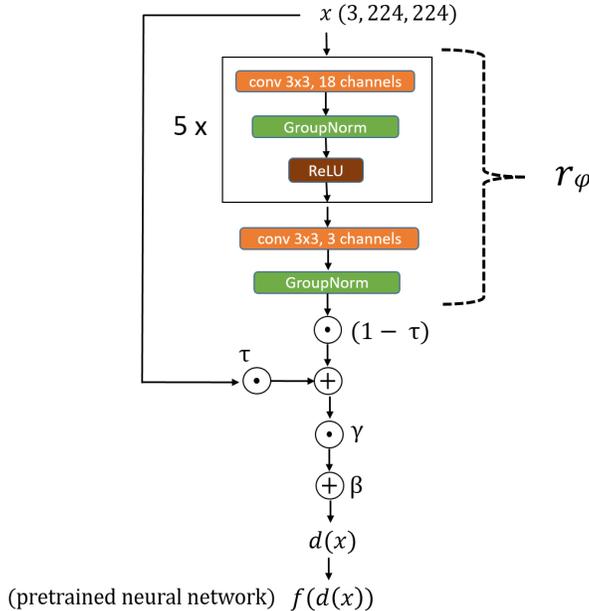


Figure A1: Structure of our adaptable model  $g$ , that comprises of  $r_\psi$ .

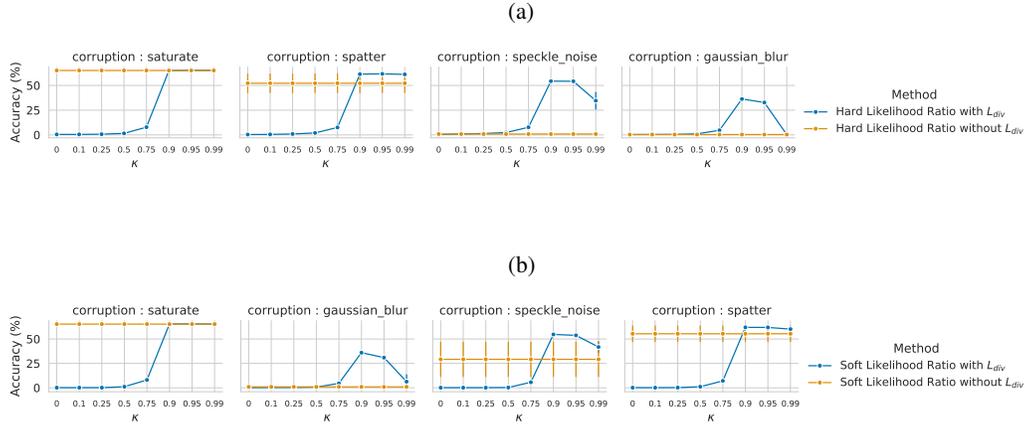


Figure A2: Effect of different  $\kappa$  on both (a) HLR and (b) SLR

### 572 A.3 Effect of $\kappa$

573 Note that the running estimate of  $L_{div}$  prevents model collapsed to trivial solutions i.e., model predicts  
 574 only a single or a set of classes as outputs regardless of the input samples.  $L_{div}$  encourages model to  
 575 match it's empirical distribution of predictions to class distribution of target data (uniform distribution  
 576 in our experiments). Such diversity regularization is crucial as there is no direct supervision attributing  
 577 to different classes and thus aids to avoid collapsed trivial solutions. In Figure A2, we investigate  
 578 different values of  $\kappa$  on validation corruptions of ImageNet-C to study its effectiveness on our  
 579 approach. It can be observed that both the HLR and SLR without  $L_{div}$  leads to collapsed solutions  
 580 (e.g., accuracy drops to 0%) on some of the corruptions and the performance gains are not consistent  
 581 across all the corruptions. On the other hand,  $L_{div}$  with  $\kappa = 0.9$  remain consistent and improve the  
 582 performance across all the corruptions.

### 583 A.4 Test-time adaptation of pretrained models with SHOT

584 Following SHOT [11], we use their pseudo labeling strategy on the ImageNet pretrained ResNet50 in  
 585 combination with TENT+, HLR and SLR. Note that TENT+ and pseudo labeling strategy jointly  
 586 forms the method SHOT. The pseudo labeling strategy starts after the 1st epoch and thereafter  
 587 computed at every epoch. The weight for the loss computed on the pseudo labels is set to 0.3, similar  
 588 to [11]. Different values for this weight is explored and found 0.3 to perform best. Table A2 compares  
 589 the results of the methods with and without pseudo labeling strategy. It can be observed that the  
 590 results with pseudo labeling strategy perform worse than without taking this strategy into account.

591 We further modified the pretrained ResNet50 by following the network modifications suggested  
 592 in [11], that includes adding a bottleneck layer with BatchNorm and applying weight norm on the  
 593 linear classifier along with smooth label training to facilitate the pseudo labeling strategy. Table  
 594 A3 shows that the pseudo labeling strategy on such network improve the results of TENT+ from  
 595 epoch 1 to epoch 5. However, there are no improvements noticed in SLR. Moreover, Table A4 shows  
 596 that NO pseudo labeling strategy on the same network performs better than applying the pseudo  
 597 labeling strategy. Finally, the no pseudo labeling results from Table A2 and A4 shows that additional  
 598 modifications to ResNet50 do not improve the performance when compared to the standard ResNet50.

### 599 A.5 Experiments on other domain adaptation datasets

600 We extended our experiments to VisDA-C. We followed similar network architecture from SHOT  
 601 [11] and evaluated TENT+, our SLR loss function with diversity regularizer. Similar to ImageNet-C,  
 602 we adapted only the channel wise affine parameters of batchnorm layers for 5 epochs with Adam  
 603 optimizer with cosine decay scheduler of the learning rate with initial value  $2e-5$ . Here, the batchsize  
 604 is set to 64, the weight of  $L_{conf}$  in our loss function to  $\delta = 0.25$  and  $\kappa = 0$  in the running estimate  
 605  $p_t(y)$  of  $L_{div}$ , since the number of classes in this dataset (12 classes) is smaller than the batchsize.  
 606 Setting  $\kappa = 0$  enables the batch wise diversity regularizer. Table A5 shows average results from three

Table A1: Test-time adaptation of ResNet50 on ImageNet-C at highest severity level 5. Same as Table 1 with error bars.

| name<br>corruption | No adaptation |       |            | Epoch 1           |            |                   |            | Epoch 5           |                   |                   |  |
|--------------------|---------------|-------|------------|-------------------|------------|-------------------|------------|-------------------|-------------------|-------------------|--|
|                    | No adaptation | PL    | TENT       | TENT+             | HLR        | SLR               | TENT       | TENT+             | HLR               | SLR               |  |
| Gauss              | 2.44          | 2.44  | 32.70±0.10 | 33.96±0.09        | 38.39±0.25 | <b>39.51±0.23</b> | 16.04±0.51 | 33.97±0.17        | 41.37±0.09        | <b>41.52±0.08</b> |  |
| Shot               | 2.99          | 2.99  | 35.34±0.17 | 36.66±0.19        | 41.11±0.13 | <b>42.09±0.26</b> | 23.22±0.74 | 37.95±0.10        | <b>44.04±0.09</b> | 42.90±0.08        |  |
| Impulse            | 1.96          | 1.96  | 35.11±0.09 | 35.75±0.15        | 40.28±0.20 | <b>41.58±0.04</b> | 25.85±1.01 | 36.93±0.09        | 43.68±0.06        | <b>44.07±0.06</b> |  |
| Defocus            | 17.92         | 17.92 | 32.79±0.10 | 33.70±0.14        | 38.25±0.32 | <b>39.35±0.13</b> | 19.05±0.61 | 32.69±0.25        | <b>41.74±0.12</b> | 41.69±0.07        |  |
| Glass              | 9.82          | 9.82  | 31.80±0.15 | 33.33±0.01        | 38.18±0.08 | <b>39.02±0.09</b> | 17.40±0.21 | 33.36±0.13        | <b>41.09±0.17</b> | 40.78±0.08        |  |
| Motion             | 14.78         | 14.78 | 47.22±0.11 | 47.73±0.12        | 51.63±0.08 | <b>52.67±0.25</b> | 49.02±0.08 | 51.42±0.07        | 54.26±0.02        | <b>54.76±0.04</b> |  |
| Zoom               | 22.50         | 22.50 | 53.02±0.06 | 53.22±0.07        | 55.55±0.06 | <b>55.80±0.07</b> | 52.78±0.16 | 54.33±0.06        | 56.43±0.07        | <b>56.59±0.05</b> |  |
| Snow               | 16.89         | 16.89 | 51.82±0.05 | 52.16±0.09        | 55.45±0.11 | <b>55.92±0.06</b> | 52.72±0.13 | 54.55±0.07        | 57.03±0.12        | <b>57.35±0.03</b> |  |
| Frost              | 23.31         | 23.31 | 43.42±0.30 | 44.79±0.20        | 48.96±0.07 | <b>49.64±0.14</b> | 34.31±0.50 | 45.80±0.27        | 50.81±0.08        | <b>51.01±0.02</b> |  |
| Fog                | 24.43         | 24.43 | 60.44±0.08 | 60.62±0.05        | 62.19±0.03 | <b>62.62±0.04</b> | 61.19±0.08 | 62.09±0.05        | 63.05±0.04        | <b>63.53±0.08</b> |  |
| Bright             | 58.93         | 58.93 | 68.82±0.02 | <b>68.91±0.03</b> | 68.17±0.01 | 68.47±0.05        | 68.54±0.06 | <b>69.03±0.06</b> | 68.29±0.09        | 68.72±0.10        |  |
| Contrast           | 5.43          | 5.43  | 27.53±0.98 | 35.60±0.77        | 49.47±0.20 | <b>50.27±0.08</b> | 1.26±0.32  | 24.08±1.36        | <b>50.98±2.54</b> | 50.65±0.55        |  |
| Elastic            | 16.95         | 16.95 | 58.47±0.05 | 58.81±0.05        | 60.34±0.18 | <b>60.80±0.08</b> | 59.26±0.06 | 60.36±0.02        | 61.15±0.04        | <b>61.49±0.07</b> |  |
| Pixel              | 20.61         | 20.61 | 61.63±0.06 | 61.82±0.07        | 62.51±0.10 | <b>63.01±0.08</b> | 62.15±0.04 | 63.10±0.08        | 63.08±0.06        | <b>63.46±0.08</b> |  |
| JPEG               | 31.65         | 31.65 | 55.98±0.09 | 56.23±0.05        | 57.42±0.13 | <b>57.80±0.04</b> | 56.17±0.07 | 57.21±0.02        | 58.13±0.09        | <b>58.32±0.05</b> |  |

Table A2: Test-time adaptation of ResNet50 on ImageNet-C at highest severity level 5 with and without the pseudo labeling strategy [11].

| name<br>corruption | No pseudo labeling: Epoch 5 |            |            |            | Pseudo labeling: Epoch 5 |            |            |
|--------------------|-----------------------------|------------|------------|------------|--------------------------|------------|------------|
|                    | No adaptation               | TENT+      | HLR        | SLR        | TENT+                    | HLR        | SLR        |
| Gauss              | 2.44                        | 33.97±0.17 | 41.37±0.09 | 41.52±0.08 | 34.08±0.11               | 34.88±0.35 | 35.58±0.06 |
| Shot               | 2.99                        | 37.95±0.10 | 44.04±0.09 | 42.90±0.08 | 36.74±0.26               | 37.61±0.49 | 37.98±0.19 |
| Impulse            | 1.96                        | 36.93±0.09 | 43.68±0.06 | 44.07±0.06 | 36.69±0.04               | 37.24±0.22 | 37.77±0.05 |
| Defocus            | 17.92                       | 32.69±0.25 | 41.74±0.12 | 41.69±0.07 | 33.99±0.28               | 34.76±0.11 | 35.11±0.10 |
| Glass              | 9.82                        | 33.36±0.13 | 41.09±0.17 | 40.78±0.08 | 34.06±0.12               | 34.51±0.30 | 34.81±0.27 |
| Motion             | 14.78                       | 51.42±0.07 | 54.26±0.02 | 54.76±0.04 | 50.91±0.09               | 48.96±0.39 | 49.46±0.20 |
| Zoom               | 22.50                       | 54.33±0.06 | 56.43±0.07 | 56.59±0.05 | 54.10±0.10               | 52.49±0.02 | 52.50±0.23 |
| Snow               | 16.89                       | 54.55±0.07 | 57.03±0.12 | 57.35±0.03 | 54.06±0.08               | 52.49±0.19 | 52.95±0.07 |
| Frost              | 23.31                       | 45.80±0.27 | 50.81±0.08 | 51.01±0.02 | 44.44±0.07               | 45.47±0.26 | 46.06±0.20 |
| Fog                | 24.43                       | 62.09±0.05 | 63.05±0.04 | 63.53±0.08 | 61.91±0.08               | 59.66±0.14 | 59.98±0.12 |
| Bright             | 58.93                       | 69.03±0.06 | 68.29±0.09 | 68.72±0.10 | 68.98±0.02               | 65.59±0.06 | 66.00±0.03 |
| Contrast           | 5.43                        | 24.08±1.36 | 50.98±2.54 | 50.65±0.55 | 29.37±0.95               | 44.58±0.38 | 45.64±0.47 |
| Elastic            | 16.95                       | 60.36±0.02 | 61.15±0.04 | 61.49±0.07 | 60.23±0.05               | 57.48±0.14 | 57.87±0.04 |
| Pixel              | 20.61                       | 63.10±0.08 | 63.08±0.06 | 63.46±0.08 | 62.98±0.04               | 59.72±0.02 | 60.05±0.14 |
| JPEG               | 31.65                       | 57.21±0.02 | 58.13±0.09 | 58.32±0.05 | 57.09±0.04               | 54.72±0.09 | 54.88±0.07 |

607 different random seeds and also shows that SLR outperforms TENT+ on this dataset. Similarly, we  
608 show the results on Office-Home dataset in Table A6.

Table A3: Test-time adaptation of modified ResNet50 (following [11]) on ImageNet-C at highest severity level 5 with pseudo labeling strategy at epoch 1 and epoch 5.

| name<br>corruption | Pseudo labeling: Epoch 1 |            |            | Pseudo labeling: Epoch 5 |            |            |            |
|--------------------|--------------------------|------------|------------|--------------------------|------------|------------|------------|
|                    | No adaptation            | TENT+      | HLR        | SLR                      | TENT+      | HLR        | SLR        |
| Gauss              | 2.95                     | 31.03±0.18 | 34.65±0.28 | 37.21±0.23               | 35.26±0.16 | 35.93±0.23 | 37.61±0.30 |
| Shot               | 3.65                     | 33.55±0.07 | 38.09±0.30 | 40.30±0.09               | 37.39±0.05 | 38.95±0.16 | 40.42±0.06 |
| Impulse            | 2.54                     | 32.70±0.07 | 36.95±0.05 | 39.73±0.07               | 38.16±0.08 | 38.13±0.04 | 40.12±0.11 |
| Defocus            | 19.36                    | 31.66±0.15 | 35.08±0.05 | 37.18±0.15               | 35.95±0.17 | 36.72±0.13 | 37.96±0.25 |
| Glass              | 9.72                     | 31.06±0.06 | 35.46±0.12 | 37.62±0.10               | 35.98±0.04 | 36.84±0.11 | 37.90±0.02 |
| Motion             | 15.66                    | 46.96±0.12 | 49.95±0.12 | 51.87±0.14               | 52.24±0.02 | 51.90±0.12 | 52.76±0.09 |
| Zoom               | 22.20                    | 52.45±0.02 | 54.15±0.22 | 54.84±0.18               | 54.80±0.07 | 54.84±0.09 | 54.95±0.14 |
| Snow               | 17.56                    | 51.79±0.05 | 53.98±0.06 | 55.44±0.04               | 55.15±0.02 | 55.27±0.20 | 55.75±0.02 |
| Frost              | 24.11                    | 45.59±0.06 | 47.87±0.03 | 48.96±0.11               | 48.10±0.20 | 48.52±0.11 | 49.13±0.20 |
| Fog                | 25.59                    | 60.33±0.03 | 61.55±0.10 | 62.21±0.16               | 62.39±0.03 | 62.38±0.12 | 62.38±0.11 |
| Bright             | 58.30                    | 68.84±0.04 | 68.44±0.04 | 68.60±0.10               | 69.13±0.04 | 68.50±0.02 | 68.47±0.09 |
| Contrast           | 6.49                     | 42.34±0.19 | 47.98±0.13 | 50.32±0.28               | 42.11±0.15 | 49.22±0.42 | 50.80±0.19 |
| Elastic            | 17.72                    | 58.47±0.02 | 59.70±0.06 | 60.30±0.09               | 60.40±0.04 | 60.27±0.22 | 60.45±0.21 |
| Pixel              | 21.29                    | 61.39±0.06 | 62.10±0.07 | 62.71±0.10               | 63.04±0.02 | 62.71±0.07 | 62.81±0.07 |
| JPEG               | 32.13                    | 55.22±0.03 | 56.49±0.07 | 57.04±0.07               | 57.21±0.06 | 57.25±0.07 | 57.37±0.05 |

Table A4: Test-time adaptation of modified ResNet50 (following [11]) on ImageNet-C at highest severity level 5 with and without pseudo labeling strategy.

| name     | No adaptation | No Pseudo labeling: Epoch 5 |            |            | Pseudo labeling: Epoch 5 |            |            |
|----------|---------------|-----------------------------|------------|------------|--------------------------|------------|------------|
|          |               | TENT+                       | HLR        | SLR        | TENT+                    | HLR        | SLR        |
| Gauss    | 2.95          | 34.96±0.08                  | 38.58±0.12 | 39.72±0.13 | 35.26±0.16               | 35.93±0.23 | 37.61±0.30 |
| Shot     | 3.65          | 37.22±0.17                  | 41.59±0.09 | 42.45±0.05 | 37.39±0.05               | 38.95±0.16 | 40.42±0.06 |
| Impulse  | 2.54          | 37.82±0.04                  | 40.88±0.07 | 42.39±0.03 | 38.16±0.08               | 38.13±0.04 | 40.12±0.11 |
| Defocus  | 19.36         | 34.46±0.12                  | 39.22±0.15 | 39.78±0.09 | 35.95±0.17               | 36.72±0.13 | 37.96±0.25 |
| Glass    | 9.72          | 35.12±0.05                  | 38.83±0.13 | 39.37±0.07 | 35.98±0.04               | 36.84±0.11 | 37.90±0.02 |
| Motion   | 15.66         | 51.91±0.09                  | 53.23±0.05 | 54.00      | 52.24±0.02               | 51.90±0.12 | 52.76±0.09 |
| Zoom     | 22.20         | 54.57±0.05                  | 55.76±0.04 | 55.79±0.02 | 54.80±0.07               | 54.84±0.09 | 54.95±0.14 |
| Snow     | 17.56         | 55.02±0.05                  | 56.35±0.12 | 56.80±0.04 | 55.15±0.02               | 55.27±0.20 | 55.75±0.02 |
| Frost    | 24.11         | 48.18±0.09                  | 49.86±0.22 | 50.43±0.08 | 48.10±0.20               | 48.52±0.11 | 49.13±0.20 |
| Fog      | 25.59         | 62.24±0.04                  | 62.90±0.06 | 63.29±0.06 | 62.39±0.03               | 62.38±0.12 | 62.38±0.11 |
| Bright   | 58.30         | 69.12±0.01                  | 68.72±0.06 | 68.83±0.05 | 69.13±0.04               | 68.50±0.02 | 68.47±0.09 |
| Contrast | 6.49          | 33.91±0.92                  | 52.13±0.16 | 53.04±0.14 | 42.11±0.15               | 49.22±0.42 | 50.80±0.19 |
| Elastic  | 17.72         | 60.37±0.11                  | 60.89±0.08 | 61.12±0.01 | 60.40±0.04               | 60.27±0.22 | 60.45±0.21 |
| Pixel    | 21.29         | 62.97±0.02                  | 62.95±0.05 | 63.21±0.05 | 63.04±0.02               | 62.71±0.07 | 62.81±0.07 |
| JPEG     | 32.13         | 57.10±0.06                  | 57.91±0.06 | 57.99±0.11 | 57.21±0.06               | 57.25±0.07 | 57.37±0.05 |

Table A5: Performance on VisDA-C dataset

| Method        | Accuracy(%) |
|---------------|-------------|
| No Adaptation | 46.1        |
| TENT+         | 81.83±0.16  |
| SLR           | 82.32±0.16  |

Table A6: Accuracy (%) on Office Home

| Method (Source → Target) | Art → Clipart | Art → Product | Art → RealWorld |
|--------------------------|---------------|---------------|-----------------|
| TENT+                    | 54.75         | 74.5          | 77.74           |
| SLR                      | 54.59         | 73.9          | 77.5            |