

AMA-Bench: Evaluating Long-Horizon Memory for Agentic Applications

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Abstract

Large Language Models (LLMs) are deployed as autonomous agents in increasingly complex applications, where enabling long-horizon memory is critical for achieving strong performance. However, a significant gap exists between practical applications and current evaluation standards for agent memory: existing benchmarks primarily focus on dialogue-centric, human-agent interactions. In reality, agent memory consists of a continuous stream of agent-environment interactions that are primarily composed of machine-generated representations. To bridge this gap, we introduce **AMA-Bench (Agent Memory with Any length)**, to evaluate long-horizon memory for LLMs in real agentic applications. It features two key components: (1) a set of real-world agentic trajectories across representative agentic applications, paired with expert-curated QA, and (2) a set of synthetic agentic trajectories that scale to arbitrary horizons paired with rule-based QA. Our comprehensive study shows that existing memory systems underperform on AMA-Bench primarily because they lack causality and objective information, and are constrained by the lossy nature similarity-based retrieval employed by many memory systems. To address these limitations, we propose **AMA-Agent**, an effective memory system featuring a causality graph and tool-augmented retrieval. Our results demonstrate that AMA-Agent achieves 57.22% average accuracy on AMA-Bench, surpassing the strongest memory system baselines by 11.16%.

1. Introduction

Large Language Models (LLMs) have rapidly evolved from solving closed-form reasoning tasks (Fig. 1 (a)) and serving as chatbots (Fig. 1 (b)), to serving as autonomous agents (Fig.

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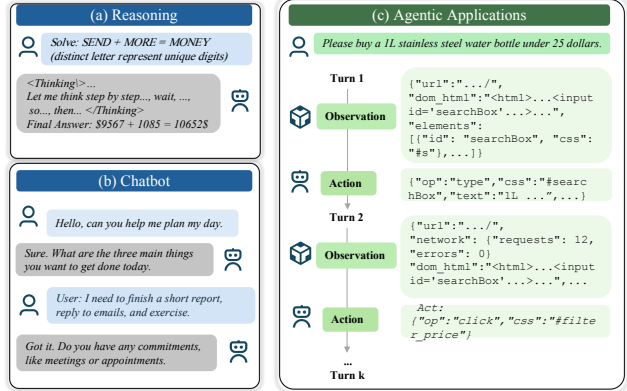


Figure 1. Comparison of memory across reasoning, chatbots, and agent applications. Agent trajectories exhibit unique properties, including being causally grounded, diverse symbolic artifacts, and dense objective information.

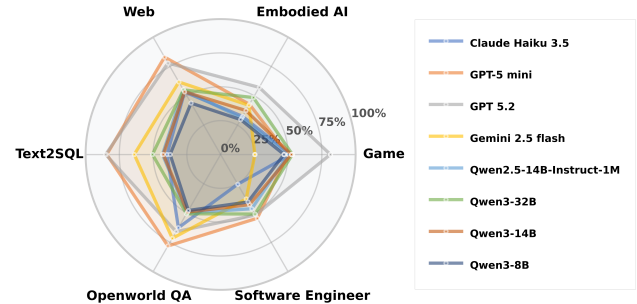


Figure 2. Model performance across agent task families in AMA-Bench.

1(c)). Autonomous agents require long-horizon reasoning and experience reuse to complete tasks like open-space navigation, code editing, and web search. To empower LLMs with these capabilities, agent memory has become an important component of agent design to manage LLM context (Wang et al., 2025b; Agashe et al., 2024). Strong memory modules are expected to satisfy two core capabilities: (1) effective memory processing, where complete agentic trajectories are transformed into structured factual representations, such as summaries, fact tables, or embeddings (Edge et al., 2025; Packer et al., 2023; Liu et al., 2026); and (2) effective memory retrieval, reliably selecting and leveraging the most relevant memory to guide decision-making. Existing benchmarks typically evaluate these capabilities in dialogue-centric or synthetic retrieval tasks (Hsieh et al., 2024; Maharana et al., 2024), focusing on specific subcomponents,

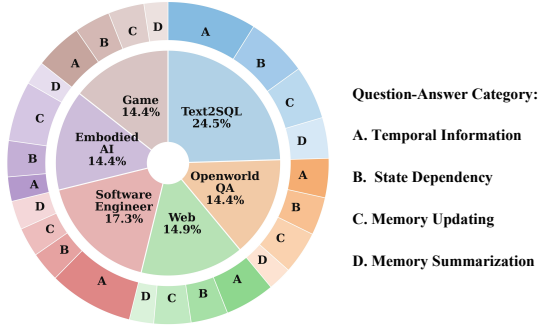


Figure 3. Domain and question type distribution in AMA-Bench.

such as single- or multi-hop questions for memory retrieval or state updating and memory condensation questions for memory processing. There is a lack of benchmarks and evaluations of memory modules in long-horizon agentic tasks.

Real-world agents mainly operate in machine generated environments such as databases, code executors, and web interfaces, where they must process large volumes of *machine generated representations*. Yet, most existing memory benchmarks are still natural language centric and have three key limitations: (1) **A lack of representation types**: Agent trajectories encompass diverse machine generated symbolics (e.g., ASCII tables, JSON data, Unicode snippets, Python or HTML code blocks), whereas current benchmarks predominantly center on free-form natural languages; (2) **A lack of causality**: agent trajectories are causally grounded, where each action induces a latent environment state transition that constrains subsequent observations; but existing benchmarks follow unconstrained linguistic flow; (3) **Sparse objective information**: agent trajectories are machine-generated and objective, whereas dialog-centric benchmarks contain abundant redundant information such as phatic chit-chat.

To bridge this gap, we introduce AMA-Bench (Benchmarking Agent Memory with Any length), which comprises two complementary subsets: a real-world subset and a synthetic subset. The real-world component consists of expert-annotated and sanity-checked Question-Answer (QA) pairs sourced from six representative agent domains: Web, open-world QA, Text2SQL, Software Engineering, Gaming, and Embodied AI (see Fig. 3). Furthermore, we construct a synthetic subset in programmatic agent environments with automatically generated QA pairs. This design enables controlled synthesis of tasks at arbitrary horizons while keeping the agent-environment interaction pattern.

As shown in Fig. 2, our systematic evaluation indicates that agent memory remains challenging even for frontier commercial models, with GPT 5.2 achieving only 72.26% accuracy. Evaluating memory systems on AMA-Bench yields **three key insights**: (1) While existing agent memory techniques often outperform long-context LLM baselines on dialogue-centric benchmarks, they fall short to the baselines

in many long-horizon agentic tasks, highlighting the unique diagnostic value of our benchmark (Sec. 4); (2) Our analysis reveals that suboptimal memory system design, rather than base model capability, serves as the primary bottleneck for their poor performance (Sec. 4); (3) Existing lossy compression and similarity-based retrieval techniques are insufficient for the nuanced demands of agent memory, necessitating a paradigm shift toward agent-centric memory management strategies (Sec. 4).

Motivated by these insights, we present AMA-Agent, a framework designed to address the memory demands of agentic applications. Moving beyond lossy compression or similarity-based graphs, AMA-Agent implements a Causality Graph to preserve the objective information and explicit causal dependencies within interaction histories. To transcend the limitations of similarity-based retrieval, we introduce a Hybrid Tool-Augmented Retrieval mechanism. This approach enables more efficient information extraction and synthesis in machine-generated representations.

This paper makes the following main contributions:

AMA-Bench. We introduce the first benchmark suite built for evaluating memory in agent applications, AMA-Bench, with two complementary subsets: *Real world* preserves authentic machine-generated interaction patterns, and a *Synthetic* suite that enables controlled scaling of any horizon length and complexity.

Comprehensive Evaluations. Through comprehensive evaluation using AMA-Bench, we show that many existing agent memory designs underperform the long-context baseline, as errors introduced by lossy memory compression and similarity-based retrieval accumulate and compound over long-horizon agentic tasks; this highlights the critical need for agent-centric memory designs.

AMA-Agent. We propose AMA-gent that addresses the identified bottlenecks with two mechanisms: (i) Causality Graph that preserves the integrity of objective information and causal dependencies, and (ii) Tool-Augmented Retrieval, which utilizes both graph node search and keyword-based search. Experimental results show that AMA-Agent outperforms the strongest existing memory baselines by 11.16% on average.

2. Related Work

2.1. Agent Memory Evaluation

We categorize existing memory benchmarks into two primary classes (as shown in Tab. 1): Dialogue-Centric and Long-Context. Dialogue-centric benchmarks evaluate memory retention over multi-turn human-agent interactions. LoCoMo (Maharana et al., 2024) and LongMemEval (Wu et al., 2025) evaluate long-term interactive memory in

Table 1. Comparison of memory benchmarks. NL: Natural Language.

Category	Benchmark	Interaction Paradigm	Content Source	Average Length (tokens)	Representation Types	Memory Organization
Dialogue-Centric	LoCoMo (Maharana et al., 2024)	Dialogue	Real + Synthetic	9K	NL + Vision	Episodic
	LongMemEval (Wu et al., 2025)	Dialogue	Synthetic	115K	NL	Multi-session
	MemoryAgentBench (Hu et al., 2025b)	Dialogue	Real + Synthetic	100K–500K	NL	Multi-domain
	MemoryBench (Ai et al., 2025)	Dialogue	Real + Synthetic	~30–380K	NL	Multi-session + Feedback
	RealTalk (Lee et al., 2025)	Dialogue	Real	17K	NL	Multi-day
Long-Context	QuALITY (Pang et al., 2022)	Long-Context	Real	5K	NL	Multi-hop
	RULER (Hsieh et al., 2024)	Long-Context	Synthetic	4K–128K	NL	Single-turn
	LongBench v2 (Bai et al., 2025)	Long-Context	Real	8K–2M	NL	Document-level
Agent-Centric	AMA-Bench	Agent-Env	Real + Synthetic	57K	NL + Machine	Trajectory-based

assistant-style chats; MemoryAgentBench (Hu et al., 2025b) tests multiple long-term memory competencies across diverse memory capabilities; MemoryBench (Ai et al., 2025) unifies diverse memory tasks into a continual learning suite; and RealTalk (Lee et al., 2025) grounds long-term memory evaluation in multi-day human dialogues. Long-context benchmarks such as QuALITY (Pang et al., 2022), RULER (Hsieh et al., 2024), and LongBench v2 (Bai et al., 2025) evaluate static document-level reasoning, focusing on multi-hop comprehension over long inputs rather than interactive or incremental memory. In contrast, AMA-Bench evaluates memory for agent applications, where the interaction trajectory is characterized by machine-generated representations, causal dependencies, and dense, objective information.

2.2. Agent Memory Mechanisms

Three main approaches have been explored to equip agents with long-horizon memory.

Long-Context Models. The first direction adapts LLMs to process memory directly as the context. For instance, GPT 5.2 (OpenAI, 2025) exposes an effective context window of approximately 400,000 tokens. On the open-source side, the Qwen2.5 1M (Yang et al., 2025b) series extends models to 100,000 tokens. Although simple and often strong in practice, this strategy remains bounded by physical context limits.

Retrieval-Augmented Generation (RAG). Another prominent research direction is RAG, which externalizes information into external storage during the memory construction stage and fetches relevant items based on similarity to augment the model’s context during retrieval. Traditional methods, such as BM25 (Robertson & Zaragoza, 2009) and the Qwen3 Embedding series (Zhang et al., 2025b), store memory by partitioning data into discrete chunks. Structured RAG approaches have emerged to capture more complex relationships. For instance, GraphRAG (Edge et al., 2025) utilizes graph-based retrieval by constructing and aggregating entity-document graphs to capture these structural dependencies. Furthermore, HippoRAG2 (Gutiérrez et al., 2025) formalizes retrieval as a nonparametric form of. Despite these advances, existing methods primarily rely on similarity-based or entity-centric retrieval, often neglecting

the underlying causality within stored information.

Memory Agent Systems. Recent research has shifted from rule-based RAG pipelines to agent-centric memory management, where LLM agents autonomously decide how to perform memory construction and retrieval. MemoryBank (Zhong et al., 2023) enables models to autonomously summon and update the stored memories. MemGPT (Packer et al., 2023) formulates memory access as a decision problem, where the LLM learns when to retrieve and how to manage the long-term context. MemoRAG (Qian et al., 2025) proposes a dual system RAG architecture that maintains a global memory store and retrieves semantically similar clues to assemble a high-level draft for answering. MEM1 (Zhou et al., 2025), Mem- α (Wang et al., 2025a), Mem0 (Chhikara et al., 2025), MemAgent (Yu et al., 2025), and A MEM (Xu et al., 2025) construct memory by iterative compression or edit-style operations such as insertion, deletion, and modification, and then directly condition generation on the compressed memory. SimpleMem (Liu et al., 2026) introduced a structured compression pipeline that filters redundancy, organizes memories into hierarchies, and adaptively retrieves relevant contexts. However, memory compression and similarity-based retrieval perform poorly on agent memory tasks for two main reasons. First, most compression methods are designed for natural language, where redundancy and subjective fillers are common. However, agent trajectories contain dense, causally structured state transitions. Second, agent memories are often machine-generated representations, and similarity retrieval frequently fails to extract the required evidence.

3. AMA-Bench

In this section, we introduce AMA-Bench (Benchmarking Agent Memory with Any length), a benchmark suite designed to evaluate memory systems in agent-centric memory. We first present a general problem formulation that abstracts agent-environment interaction and provides a unified definition of memory systems for agent applications in Sec. 3.1. Building on this formulation, Sec. 3.2 identifies which memory capabilities are essential for long-horizon decision-making and operationalizes them as evaluation dimensions. Finally, Sec. 3.3 describes how we construct AMA-Bench, including both real-world and synthetic subsets.

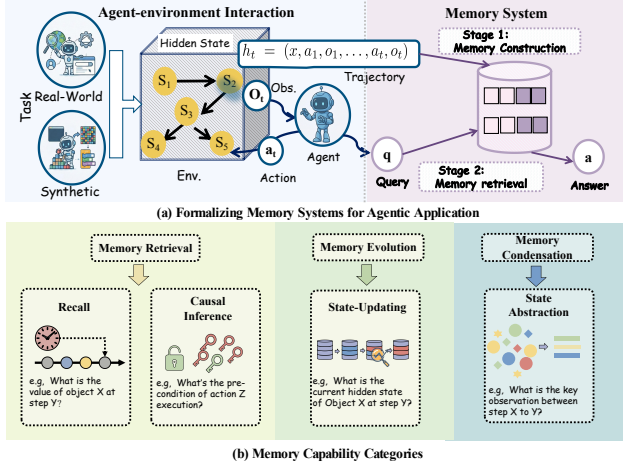


Figure 4. Formalizing memory system and capability for agentic applications.

3.1. Problem formulation

Agent Environment Interactions. We consider LLM agents operating within the reason and act paradigm (Yao et al., 2022; Shinn et al., 2023; Wang et al., 2023), where sequential decision-making is formulated as a Partially Observable Markov Decision Process (POMDP) defined by the tuple $\mathcal{M} = (\mathcal{S}, \mathcal{A}, \mathcal{O}, P, r)$ (See Fig. 4 (a)). At each time step t , the environment resides in a latent state $s_t \in \mathcal{S}$. Upon executing an action $a_t \in \mathcal{A}$, the agent receives an observation $o_t \in \mathcal{O}$ sampled from the observation function $O(s_t)$, and the environment transitions to s_{t+1} according to the dynamics $P(s_t | s_t, a_{t+1})$. Given a task instruction x , the interaction generates a trajectory history $h_t = (x, a_1, o_1, \dots, o_t)$. The partial observability motivates an explicit memory mechanism to persist the agent memory.

The Memory System. We formalized a memory system through two stages (see Fig. 4 (a)), memory construction (Build) and memory retrieval (Retrieve). The construction stage, $\text{Build}: \mathcal{H} \rightarrow \mathcal{M}_{\text{mem}}$, maps the interaction history h_t to an external memory state $m_t \in \mathcal{M}_{\text{mem}}$. The memory space \mathcal{M}_{mem} accommodates diverse structured representations, such as recursive summaries, knowledge graphs, and vector embeddings (Edge et al., 2025; Packer et al., 2023; Liu et al., 2026). Upon receiving a query q_t , the retrieval module extracts a query-relevant context $c_t = \text{Retrieve}(m_t, q_t)$. The agent policy π then determines the subsequent response based on the retrieved context and query: $a_t \sim \pi(\cdot | q_t, c_t)$.

3.2. Memory Capability Categories

The proposed formulation, supported by recent literature (Du et al., 2025; Zhang et al., 2024), underscores that an effective memory system must facilitate three core capabilities: 1. Memory Retrieval: targeted access to the correct evidence. 2. Memory Evolution: continually updates memory as new observations arrive. 3. Memory Condensation: precisely

Table 2. Memory capability described in Sec 3.2. We group evaluation dimensions into three mechanisms and four capabilities.

Mechanism	Capability	Description
Memory Retrieval	A. Recall	Identification of Temporal and sequential information.
	B. Causal Inference	Verification of action preconditions and dependency relations between states.
Memory Evolution	C. State Updating	Tracking updates to states, including explicit observations and hidden states.
Memory Condensation	D. State Abstraction	Filtering redundant content while extracting precise and condensed key information.

extracting and condensing memory without information loss. Aligning these essential mechanisms with the specific requirements of agent-based tasks, we categorize memory capabilities into three functional modules. The formal definitions are detailed in Tab. 2, while illustrative examples are provided in Fig. 4 (b). These modules encompass: Recall and Causal Inference (Retrieval), State Updating (Evolution), and State Abstraction (Condensation).

3.3. Benchmark Construction

With the above formulation and capability taxonomy, we now describe how we build AMA-Bench to jointly capture real-world complexity and provide controllable scaling complexity. AMA-Bench comprises two complementary components: (i) a real-world subset and (ii) a synthetic subset.

3.3.1. REAL-WORLD SUBSET

We curate high-quality, long-horizon trajectories from six representative real-world agent tasks, including web navigation, software engineering, text-to-SQL, embodied AI, gaming, and open-world tool with 2496 QA pairs (see Fig. 3 and Tab. 8 in Appendix A for the detailed category). For each task family, we gathered action-observation interaction traces from representative benchmarks using either state-of-the-art agent frameworks or expert-level trajectories provided directly by the environment. From this pool, we curated a subset for annotation, prioritizing longer trajectories while maintaining the original task distribution within each family. Specific details regarding the benchmarks and frameworks used are provided in Appendix A.

The real-world environments are treated as black boxes: we only observe agent-environment interaction logs (action and observation trajectories) and do not have access to the environment backend state. Building on the capability taxonomy in Sec. 3.2, we manually annotate each selected trajectory with 12 memory-intensive QA pairs that collectively cover all categories in Tab. 2. Each question is formulated such that its answer is supported by explicit and unambiguous evidence within the trajectory, ensuring that the correctness

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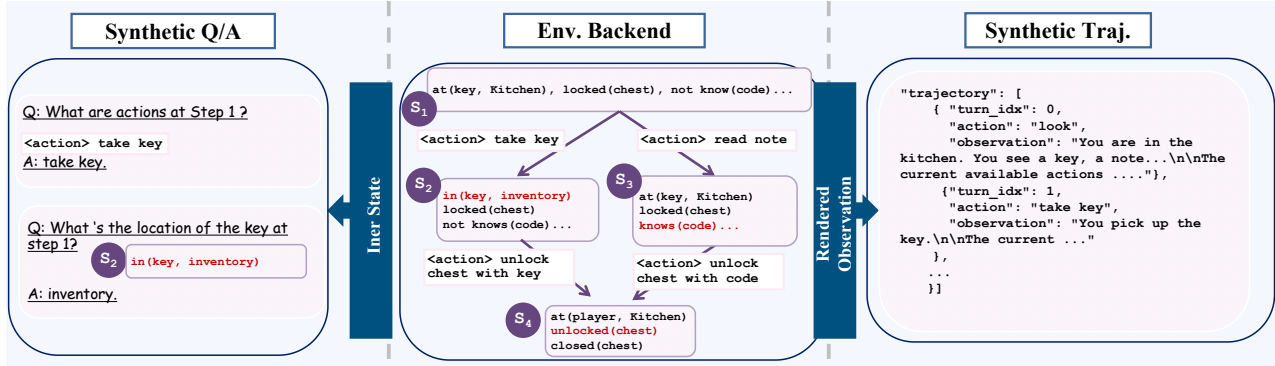


Figure 5. Synthetic subset construction pipeline. We synthesize an executable environment backend with explicit latent states and transitions, render machine-generated observations to form trajectories, and programmatically generate trajectory-grounded QA pairs.

of the question can be verified from the log itself.

QA pairs are then authored by graduate-level annotators with research experience in LLM agents, following shared guidelines that standardize evidence grounding and category coverage across six domains. To improve annotation reliability, each annotated trajectory undergoes a cross-review sanity check by a second annotator. This protocol yields expert-level QA annotations that are trajectory-grounded, category-aligned, and consistent across the task families. Examples of trajectories and QA are listed in Appendix E.1.

3.3.2. SYNTHETIC SUBSET

To systematically evaluate agent memory scaling, we construct a synthetic subset via programmatic environment synthesis. Each instance comprises an executable backend with controllable state transitions and a tunable perception interface, enabling the generation of verifiable trajectories with arbitrary horizons. Fig. 5 shows the pipeline of the synthetic subset construction. We synthesize tasks from two distinct environments characterized by long-range dependencies and partial observability: TextWorld (Côté et al., 2018), BabyAI (Chevalier-Boisvert et al., 2019). The description of the two tasks is listed in Appendix A.2.

Environment Synthesis. We parameterize each instance using a difficulty vector ϕ and a random seed to synthesize the environment backend. The latent state s_t and transition kernel $s_{t+1} = P_\phi(s_t, a_{t+1})$ are programmatically defined and machine-verifiable. This allows us to systematically scale the interaction context length L by increasing the environmental difficulty as dictated by ϕ . For instance, in BabyAI, ϕ encompasses parameters such as the grid dimensions, the number of rooms, and the length of the instruction chain. By increasing the map size or adding nested dependencies, we can provably extend the trajectory length L .

Trajectory Synthesis. The synthetic nature of our environments grants full access to the environment MDP, enabling

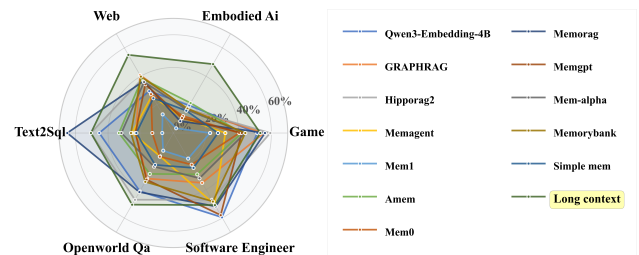


Figure 6. LLM-as-a-judge accuracy across different memory systems using Qwen3-32B as the base model.

the derivation of an optimal policy π^* despite the agent’s partial observability. We generate stepwise sequences $\{(a_t, o_t)\}_{t=1}^T$ grounded in these gold-standard transitions to resolve the issue of low-structural density. To further address representational diversity and robustness, we introduce two auxiliary perturbations beyond ϕ : (1) Action Stochasticity (ϵ): we inject random noise into π^* to simulate sub-optimal action ratios, testing memory robustness under varying agent policies; and (2) Observation Verbosity (γ): we employ various symbolic representations with controllable descriptive granularity γ for o_t .

QA Synthesis. Since we have access to the full MDP, we can programmatically generate golden QA pairs anchored to backend state variables such as state s_t or transition kernel $s_{t+1} = P_\phi(s_t, a_t)$.

Needle Synthesis. Following the widely used needle-in-a-haystack (NIAH) paradigm (Nelson et al., 2024; Hsieh et al., 2024; Kamradt) for evaluating memory capabilities, we also instantiate a needle protocol in AMA-Bench. The *needle* here is the minimal set of trajectory turn IDs that contains all the evidence necessary to answer a query. Crucially, because AMA-Bench is backed by a programmatic environment, we can automatically synthesize and verify the needles. More details about the needle generation pipeline are listed in Appendix F.

4. Empirical Motivation

We benchmarked a broad set of representative memory systems on the AMA-Bench (see Fig. 6). The results reveal three key empirical insights that highlight the current limitations and directly motivate the design of our proposed method in Sec. 2.2.

Motivation1:

Memory systems fall short of the long-context baseline.

Fig. 6 compares representative memory systems against a long context baseline across six agent task families. A clear pattern emerges: the long context baseline is consistently strong and often achieves the best performance, whereas existing memory systems exhibit large variance across families and frequently underperform, even when they introduce structured memory construction or retrieval augmentation.

Motivation2:

Memory Design bottlenecks the model performance.

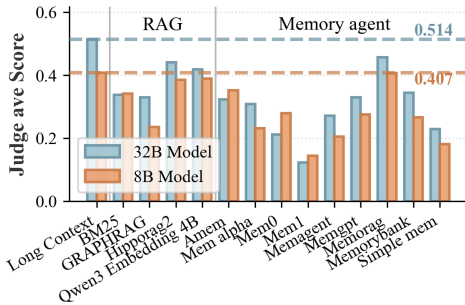


Figure 7. Impact of Model Scale vs. Memory Architecture. While scaling the backbone yields marginal gains, the choice of memory system accounts for the majority of performance variance.

A central question in building memory-augmented agents is whether performance bottlenecks reside in the backbone capacity or memory system design. Fig. 7 illustrates that scaling from 8B to 32B provides only marginal improvements (avg. improvement is 0.038), whereas varying the memory architecture induces significantly higher variance, with score ranges reaching 0.45.

Motivation3:

Limitations of Existing Memory System Designs.

To further pinpoint bottlenecks, we performed needle protocol ablation in BabyAI with three settings. *Full Observation (Needle)* provides the raw needle turns and serves as an upper bound. *Constructed Memory (Needle)* replaces them with method specific constructed memory to isolate construction loss. *End to End System* evaluates the full pipeline with retrieval.

Tab. 3 demonstrates two limitations. First, many methods degrade sharply after construction, e.g., MemoryBank drops

Method	Full Observation w/ Needle ACC	Constructed Memory w/ Needle ACC	End to End System ACC
HippoRAG2	0.46	0.37 (-19.6%)	0.21 (-43.2%)
Mem1		0.29 (-37.0%)	0.20 (-31.0%)
AMem		0.29 (-37.0%)	0.24 (-17.2%)
MemoryBank		0.27 (-41.3%)	0.26 (-3.7%)

Table 3. Ablation study on performance bottlenecks under the needle retrieval protocol in BabyAI, evaluated by accuracy (ACC). Dark red values denote relative decrease vs. the previous column.

by 41.3%, suggesting that compression tuned for redundant natural language fails to preserve dense state and causal information in agent memory. Second, similarity-based retrieval is unreliable: HippoRAG2 remains strong under constructed memory with needle turn but drops by 43.2% performance end-to-end.

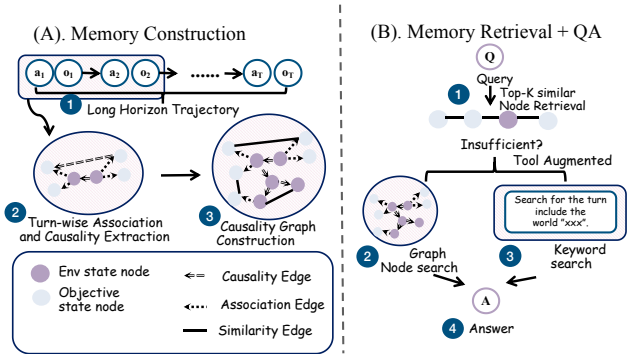


Figure 8. Overview of the AMA-agent. (A) Illustrates the transition from trajectories to a structured causality graph. (B) depicts the retrieval mechanism, utilizing tool-augment search.

5. The AMA-Agent

Motivated by the observations in Sec. 4, we develop the AMA-Agent with two core mechanisms: (A) a Causality Graph for memory construction to minimize information loss; and (B) a tool augmented retrieval module that complements standard retrieval with graph node traversal and keyword search to improve retrieval effectiveness.

5.1. Memory Construction: Causality Graph

AMA-Agent constructs a **Causality Graph** from the agent’s trajectory. The construction proceeds in three stages: For each timestep t , the agent parses the adjacent turn pairs (o_{t-1}, a_t, o_t) to extract environment and object states, identifying latent inter-state causal dependencies and state-object associations (Fig. 8 (A) 1). These signals are instantiated as directed causality edges and undirected association edges connecting the respective state nodes (Fig. 8 (A) 2). Finally, these local interactions are integrated into a global Causality Graph, where nodes are mapped into a latent embedding space to facilitate similarity-based retrieval and relational reasoning (Fig. 8 (A) 3).

5.2. Memory Retrieval: Tool-Augmented Search

Beyond similarity-based retrieval, AMA-Agent adopts a tool-augmented search mechanism. It first retrieves the top K nodes based on embedding similarity (Fig. 8 (B) ①) and performs self-evaluation to assess whether the retrieved evidence is sufficient to answer the query. If the evidence is insufficient, the agent categorizes the missing context and invokes either the *graph node search tool* or the *keyword search tool*.

Under the *graph node search tool* route, the agent performs depth-controlled neighborhood traversal to aggregate multi-hop context and causal relations (Fig. 8 (B) ②). Under the *keyword search tool* route, the AMA-Agent uses a tool interface that allows it to write and execute scripts for programmatic analysis, enabling precise keyword matching and statistical aggregation (Fig. 8 (B) ③). Finally, the AMA-Agent synthesizes the retrieved evidence to produce a response (Fig. 8 (B) ④).

6. Evaluation

6.1. Experimental Setup

Benchmarks. We evaluate our baselines on two complementary subsets: 1. Real-world Subset: This subset comprising a total of 2,496 QA pairs. 2. Synthetic Subset: we utilize two tasks with a total of 1,200 QA pairs. These tasks are stratified across five trajectory lengths (8K, 16K, 32K, 64K, and 128K tokens), with 240 samples per interval.

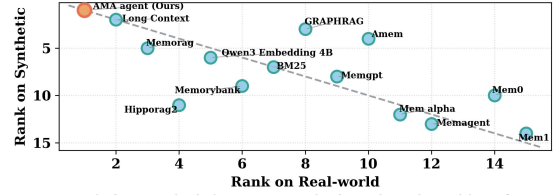
Baselines. We consider three categories of baselines: long context models, RAG, and memory agents.

Implementation Details. To ensure a fair comparison, we evaluate all RAG baselines, memory-based agents, and our proposed AMA-Agent using the same backbone architectures: **Qwen3-32B** and **Qwen3-8B**. For each baseline, we adhere to the original authors’ default embedding models and indexing configurations (refer to Appendix B for reproduction details). For AMA-Agent, we employ Qwen3-4B-embedding to map the causality graph into the latent space and set $K = 5$ for similarity-based node retrieval.

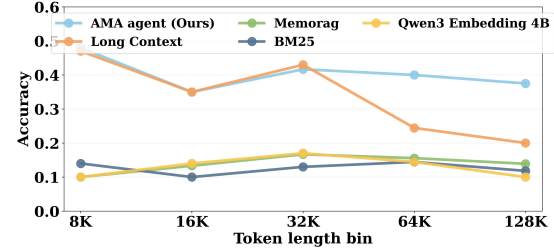
Metrics. We report both Accuracy and F1-score. Accuracy measures the instances judged as correct by an LLM-as-judge based on Qwen3-32B. Additional details and validation of the LLM-as-judge protocol are provided in Appendix C.

6.2. Key Results

Real-world Subset. We report the main results on the real-world subset in Tab. 4 (evaluating models with long contexts) and Tab. 5 (comparing different memory systems). While GPT 5.2 achieves the highest average accuracy (0.73) as Tab. 4 shows, its performance suggests that even strong commercial models have not fully mastered trajectory-based



A. Correlation Analysis between Synthetic and Real-world Performance.



B. Scalability Analysis Across Trajectory Lengths

Figure 9. Performance Benchmarking. We evaluate 15 memory methods across Qwen 8B and 32B backbones.

agent memory capabilities. Crucially, when controlled under the Qwen3 32B backbone (Tab. 5), **AMA-Agent** establishes a new state-of-the-art across all dimensions—Recall (0.6238), Causal Inference (0.6145), State Updating (0.5305), and State Abstraction (0.4719)—reaching an average of 0.5722. This significantly outperforms the strongest RAG baseline HippoRAG2 (0.4480) and the leading memory method MemoRAG (0.4606). These results demonstrate that explicit modeling of long-horizon state dynamics and causal memory organization provides a more robust framework for agent reasoning than standalone retrieval-based approaches.

Synthetic Subset. We also evaluate all memory methods on the Synthetic subset and compare their scores against the real-world subset. Fig. 9 A illustrates the strong ranking correlation between real-world scenarios and our synthetic subset. The close alignment of most methods with the diagonal line demonstrates that the synthetic environment serves as a high-fidelity proxy for real-world performance, which is crucial given the high costs of real-world data acquisition and manual annotation.

Fig. 9 evaluates the performance stability of our method compared to other baselines as the sequence length increases from 8K to 128K. While the Long Context approach maintains competitive accuracy at shorter scales, its performance degrades significantly beyond 32K, revealing the inherent limitations of fixed context window. In contrast, AMA-agent exhibits superior scalability, maintaining robust and consistently high accuracy even at 128K.

6.3. Ablation Study

To validate the contributions of our key components, we perform ablation studies on the Causality Graph and tool augmented retrieval. The variant *w/o Causality Graph* replaces our structured Graph-based memory with a vanilla

Table 4. Performance of different models on real-world subset.

Method	Recall	Causal Inference	State Updating	State Abstraction	Average
Claude Haiku 3.5 (Anthropic, 2025)	0.4943 (0.3510)	0.4507 (0.2792)	0.4287 (0.3015)	0.3090 (0.2648)	0.4361 (0.3067)
GPT-5-mini (OpenAI, 2025)	<u>0.6951</u> (0.4010)	<u>0.7157</u> (0.3027)	0.6575 (0.3288)	0.6235 (0.3262)	<u>0.6784</u> (0.3464)
GPT 5.2 (Wailgum, 2025)	0.7741 (0.4758)	0.8047 (0.3512)	<u>0.6563</u> (0.3686)	<u>0.6037</u> (0.3582)	0.7226 (0.3988)
Gemini 2.5 flash (Gemini Team, 2025)	0.5834 (0.3682)	0.5087 (0.2628)	0.5000 (0.2395)	0.4196 (0.2361)	0.5168 (0.2878)
Qwen2.5-14B-1M (Yang et al., 2025b)	0.5570 (0.4157)	0.4111 (0.3209)	0.4728 (0.3348)	0.3368 (0.3560)	0.4638 (0.3622)
Qwen3-32B (Yang et al., 2025a)	0.6149 (0.4074)	0.5178 (0.3289)	0.4903 (0.3334)	0.3657 (0.3172)	0.5181 (0.3545)
Qwen3-14B (Yang et al., 2025a)	0.5675 (0.3636)	0.4430 (0.2931)	0.4502 (0.3204)	0.3176 (0.2716)	0.4659 (0.3203)
Qwen3-8B (Yang et al., 2025a)	0.5024 (0.3801)	0.3776 (0.2830)	0.3987 (0.3177)	0.2923 (0.2792)	0.4109 (0.3240)

Note: Results are reported as Accuracy (F1). The **best** and second best Accuracy values are highlighted.

Table 5. Performance comparison of Agent Memory and RAG methods using base model Qwen-32B on real-world subset.

Method	Recall	Causal Inference	State Updating	State Abstraction	Average
RAG					
BM25	0.3301 (0.1465)	0.4264 (0.1549)	0.3450 (0.1325)	0.2498 (0.1623)	0.3436 (0.1475)
Qwen3-Emb-4B (Zhang et al., 2025b)	<u>0.4843</u> (0.1590)	0.4974 (0.1549)	0.3520 (0.1353)	0.3011 (0.1610)	0.4227 (0.1522)
GraphRAG (Edge et al., 2025)	0.3077 (0.2769)	0.3905 (0.2634)	0.3140 (0.2551)	0.2879 (0.2588)	0.3258 (0.2650)
HippoRAG2 (Gutiérrez et al., 2025)	0.4579 (0.2356)	0.5080 (0.1966)	<u>0.4403</u> (0.1892)	0.3538 (0.1785)	0.4480 (0.2048)
Agent Memory Methods					
MemAgent (Yu et al., 2025)	0.2550 (0.1489)	0.3380 (0.1606)	0.2849 (0.1432)	0.2202 (0.1655)	0.2768 (0.1530)
Mem1 (Zhou et al., 2025)	0.1180 (0.1857)	0.1427 (0.1732)	0.1205 (0.1659)	0.1080 (0.2042)	0.1229 (0.1807)
Amem (Xu et al., 2025)	0.3084 (0.2707)	0.3653 (0.2731)	0.3088 (0.2480)	0.2873 (0.2953)	0.3186 (0.2695)
Mem0 (Chhikara et al., 2025)	0.2011 (0.2413)	0.2645 (0.2443)	0.2101 (0.2225)	0.1516 (0.2241)	0.2104 (0.2343)
MemoRAG (Qian et al., 2025)	0.4708 (0.1789)	<u>0.5497</u> (0.1811)	0.4257 (0.1713)	<u>0.3659</u> (0.2073)	<u>0.4606</u> (0.1822)
MemGPT (Packer et al., 2023)	0.3289 (0.1318)	0.4404 (0.1475)	0.2809 (0.1259)	0.2526 (0.1431)	0.3304 (0.1359)
Mem-alpha (Wang et al., 2025a)	0.2876 (0.2325)	0.4172 (0.1993)	0.3064 (0.2000)	0.2171 (0.2135)	0.3117 (0.2130)
MemoryBank (Zhong et al., 2023)	0.3231 (0.3128)	0.4100 (0.2861)	0.3006 (0.2678)	0.3332 (0.3011)	0.3397 (0.2928)
Simple mem (Liu et al., 2026)	0.2012 (0.2039)	0.1884 (0.1612)	0.1764 (0.1594)	0.1373 (0.1689)	0.1811 (0.1764)
AMA-Agent (AMA)	0.6238 (0.3280)	0.6145 (0.3103)	0.5305 (0.2625)	0.4719 (0.2825)	0.5722 (0.2992)

Note: Results are reported as Accuracy (F1). The **best** and second best Accuracy values are highlighted.

Table 6. Ablation results for AMA-Agent

Method	Recall	Causal Inference	State Updating	State Abstraction	Avg.
AMA-agent	0.62	0.61	0.53	0.47	0.57
w/o Causality Graph	0.48 (-22.6%)	0.48 (-21.3%)	0.36 (-32.1%)	0.35 (-25.5%)	0.43 (-24.6%)
w/o Tool-Augmented Retrieval	0.47 (-24.2%)	0.51 (-16.4%)	0.42 (-20.8%)	0.31 (-34.0%)	0.44 (-22.8%)

Note: Values in **dark red** indicate the relative performance decrease compared to the full AMA agent.

Qwen3 Embedding 4B indexes the context directly, while *w/o Tool Augmented Retrieval* disables tool calls and relies solely on embedding similarity retrieval. The results in Tab. 6 show that both modules are necessary for strong performance. Removing the Causality Graph causes a substantial degradation, with the average score dropping from 0.57 to 0.43, indicating that causality-aware representations are critical for agent memory. Likewise, removing tool augmented retrieval reduces performance to 0.44, suggesting that similarity search alone is insufficient and that tools provide complementary evidence access for robust reasoning.

7. Conclusion

In this paper, we introduced AMA-Bench to bridge the disparity between natural language-centric evaluations and the machine-generated, causally grounded nature of real-world agent trajectories. Our systematic analysis revealed that memory architecture is the primary determinant of performance, highlighting the limitation of lossy compression and similarity-based retrieval for dense, objective information. To address these challenges, we proposed AMA-Agent, which leverages a Causality Graph and Hybrid Tool-Augmented Retrieval to significantly outperform state-of-the-art baselines. A limitation of this study is its focus on in-episode memory; future work should extend these rigorous standards to cross-task scenarios involving lifelong learning.

Impact Statement

This paper presents work whose goal is to advance the field of Machine Learning. There are many potential societal consequences of our work, none of which we feel must be specifically highlighted. Regarding the introduced benchmark, we confirmed that it was constructed entirely from open-source data sources. All data entries underwent human verification to ensure that no personally identifiable information (PII) or private data were included.

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Appendix

A. Details of Dataset

Here, we provide a detailed introduction to the datasets used for evaluating the four core competencies, including the dataset curation, corresponding metrics, average context length, and a brief description.

A.1. Real-world Subset

This section details the composition of the real-world subset, which comprises multi-turn trajectories curated from **six diverse domains** of agent-environment interactions (Table 7).

Table 7. Implementation details of collected agent trajectories across task families.

Field	Benchmark	Trace Source	Total	Selected
Embodied AI	ALFWorld-verified (seen)	ALFRED (Li et al., 2025)	140	33
Gaming	BALROG / Imgame bench	BALROG / GamingAgent	367	30
Web Task Execution	WebArena (Zhou et al., 2023)	WebArena (Zhou et al., 2023)	162	31
Software Engineering	SWE-bench (Jimenez et al., 2023)	OpenHands (Wang et al., 2024)	162	34
Open World Tool QA	GAIA (Mialon et al., 2023)	CoSight (Zhang et al., 2025a)	100	30
Text 2 SQL	Spider 2.0 (Lei et al., 2024)	Spider2 agent (Lei et al., 2024)	120	51

Embodied AI. We collect trajectories from both the **seen** and **unseen test splits** of ALFWorld (Shridhar et al., 2020b), a text-based embodied environment aligned with the ALFRED benchmark. These trajectories are generated using the expert-level demonstrations from ALFRED (Shridhar et al., 2020a) to ensure high-quality task completion in both familiar and novel environments.

Gaming. We curate gaming trajectories from two sources: BALROG (Paglieri et al., 2024), which includes Crafter (resource management), Baba is AI (long-horizon puzzle solving), and MiniHack (navigation); and LMGame-Bench (Hu et al., 2025a), which includes 2048 and Candy Crush. Trajectories are collected using GPT-5.1 with the BALROG agent framework and GamingAgent (lmgame-org, 2025) with memory and perception modules. For 2048, we use rule-based methods due to the extensive action sequences required. We select 30 trajectories totaling 360 QA pairs, with an average of 150 turns per episode.

Web Task Execution. We use WebArena (Zhou et al., 2023), a realistic web environment featuring fully functional websites across e-commerce, social forums, software development, and content management domains. Trajectories are collected using GPT-4.1 with the WebArena agent framework. We select 31 trajectories comprising 372 QA pairs, with an average of 25 turns and 34K tokens per trajectory, reaching up to 166K tokens for complex tasks.

Software Engineering. We collect trajectories from SWEBench Verified (Jimenez et al., 2023; OpenAI, 2024), which consists of real GitHub issues and pull requests from popular Python repositories. Trajectories are generated using Claude Sonnet 4 with the OpenHands framework (Wang et al., 2024), an open platform for AI software developers. We select 36 trajectories totaling 432 QA pairs, with an average of 103 turns and 19K tokens per trajectory.

Open World Tool QA. We use the GAIA benchmark (Mialon et al., 2023), which tests general AI assistants on real-world questions requiring reasoning, multi-modality handling, web browsing, and tool-use proficiency. Trajectories are collected using GPT-5 with the Co-Sight framework (Zhang et al., 2025a), which achieves state-of-the-art performance on open-sourced agent benchmarks. We select 30 trajectories across all three difficulty levels from the validation set, comprising 360 QA pairs with an average of 41 turns and 289K tokens – the longest among all domains, reaching up to 997K tokens.

Text-to-SQL. We collect trajectories from the Spider 2.0 benchmark (Lei et al., 2024), specifically sampling from the Spider2-Snow subset which focuses on enterprise-level text-to-SQL tasks with Snowflake databases. Spider 2.0 comprises three subsets (Snow, DBT, and Lite), with the Snow subset containing 547 examples. Among these, gold answers are provided for 120 examples to enable verification of generated SQL queries. We sample 51 trajectories from these verified examples to ensure answer correctness can be validated. Trajectories are generated using Claude Sonnet 4.5 with the Spider2-Agent framework, totaling 612 QA pairs with an average of 22 turns and 6K tokens per trajectory.

A comprehensive breakdown of the Real-world Subset is provided in Table 8. To provide a clearer illustration of our defined problem types, we present a representative example from the Web Task Execution domain (Figure E.1). This example shows how an agent must use different memory operations, such as tracking incremental UI changes, recognizing high level strategic failures, and handling long horizon interactions. Aligned with the three memory capabilities (Table 2), we define four QA categories that probe whether an agent has acquired the corresponding competencies required to answer them reliably, and we instantiate all four categories in this example. For additional qualitative visualizations of data samples, please refer to Appendix E.

Table 8. Statistics of QA pairs, evaluation type distribution, and interaction complexity.

Field	#Samples	#QA	Evaluation Type				Avg. Turns	Avg. Tokens	Max Tokens
			Type A	Type B	Type C	Type D			
Text 2 SQL	51	612	223	153	134	102	21.80	6,049	10,718
Open World Tool QA	30	360	98	95	107	60	41.40	288,651	996,826
Web Task Execution	31	372	125	93	93	61	24.77	34,265	166,260
Gaming	30	360	120	90	90	60	149.87	14,909	33,360
Embodied AI	30	360	61	90	150	59	130.33	26,306	60,717
Software Engineering	36	432	212	75	73	72	103.22	19,296	28,615
TOTAL	208	2,496	839	596	647	414	73.29	57,506	996,826

A.2. Synthetic Subset

BabyAI are generated from the BabyAI environment (Chevalier-Boisvert et al., 2019), which supports six difficulty levels: `easy`, `medium`, `medium_hard`, `hard`, `very_hard`, and `hard_large`. Each trajectory is paired with 12 questions by default, and we collect a total of 50 trajectories, with an average length of 563 turns and 30,042 tokens per trajectory.

TextWorld are generated from the TextWorld (Côté et al., 2018) environment. We consider three game types: `coin_collector`, `cooking`, and `treasure_hunter`. The environment supports eight difficulty levels: `easy`, `medium`, `medium_hard`, `hard`, `very_hard`, `extreme`, `ultra`, and `mega`. On average, each trajectory contains 57 turns and 31,662 tokens.

To provide a concrete realization of the Synthetic subset described in Section 3.3, we present qualitative case studies from BabyAI and TextWorld. These examples are designed to illustrate how our programmatic framework evaluates specific agent capabilities by modulating synthesis parameters. For additional qualitative visualizations of data samples, please refer to Appendix E.

- **Probing Memory Robustness under Action Stochasticity (ϵ):** Figure E.2 presents a diagnostic episode from the **BabyAI** environment under high action stochasticity (ϵ). This setup evaluates the agent’s ability to maintain the task goal within its interaction context when π^* is perturbed by suboptimal exploratory noise. The observed failure—a task truncation—indicates that the agent’s memory mechanism fails to distinguish gold-standard goal alignment from the increased “interaction noise,” even when target objects are clearly rendered via the perception interface $O_\phi(s_t)$.
- **Evaluating State Tracking across Subgoal Chains (ϕ):** Figure E.2 captures a failure in **TextWorld** that probes the agent’s internal state-tracking of the backend transition kernel P_ϕ . By scaling the difficulty vector ϕ to increase subgoal chain length, we test whether the agent can correctly update its “memory slots” based on transition events Δs . The repetitive invalid actions (e.g., attempting a `put` before a verified `take` event) reveal a breakdown in causal reasoning, where the agent loses track of the latent state s_t despite having navigated the correct spatial transitions.

B. Baseline Implementation Details

Long-Context Model Baseline. For long-context baselines, we directly *pack* the trajectory into the model input without retrieval or compression until reaching the maximum context length permitted by each API or checkpoint in Tab. 9. We reserve a fixed 4K-token budget for the model to generate the final answer, and use the remaining tokens as the effective input budget. When a trajectory exceeds this budget, we apply a simple truncation strategy that preserves both early and late interactions: we keep the first 50% and the last 50% budget length of the trajectory (by token count) and discard the middle portion to fit the context window.

Table 9. Maximum context lengths used for long context baselines.

Model	Max context tokens	Notes
Claude 3.5 Haiku	200,000	API context window
OpenAI GPT 5 mini	400,000	API context window
OpenAI GPT 5.2	400,000	API context window
Gemini 2.5 Flash	1,048,576	Max input tokens
Qwen2.5 14B Instruct 1M	1,010,000	Long context checkpoint
Qwen3 32B	32,768	Native
Qwen3 14B	32,768	Native

B.1. RAG Baseline

GraphRAG. constructs memory by using an LLM (Qwen3-8B/32B) to extract entities (object, location, action) and their relationships from trajectory text, storing them as a knowledge graph in parquet format. The trajectory is first chunked into semantic units of 15 turns per chunk with a maximum of 24,000 tokens. This construction process is inherently lossy, as it discards substantial raw trajectory details, particularly the detailed observation states and fine-grained action sequences present in the original data. During retrieval, GraphRAG selects the top- k most relevant entities and relationships from the knowledge graph based on their descriptions, concatenating these structured elements into the prompt as context rather than including the full trajectory. We follow the default GraphRAG configuration with $k = 50$ entities and relationships, `max_gleanings=0`, and a description summarization disabled to preserve extraction fidelity.

HippoRAG. constructs memory by applying OpenIE-style extraction to trajectory text, yielding entities and relation triples that form a heterogeneous graph of passage (trajectory chunk), entity, and fact nodes; synonymy edges are added via nearest-neighbor search over entity embeddings. This construction is lossy because raw trajectories are distilled into triples and edges, potentially omitting fine-grained state transitions or action details. At retrieval time, HippoRAG computes query-fact similarity with dense embeddings, reranks top facts, maps them to linked entities, and runs personalized PageRank over the graph; the graph scores are combined with dense passage retrieval to select top- k passages for QA. We use the default HippoRAG configuration with top- k fact/entity linking = 5, passage retrieval top- $k = 200$, and QA context limited to the top 5 passages. All passage, entity, and fact embeddings use the same model BAAI/bge-m3.

B.2. Memory Agents Baseline

MemoryBank. constructs a hierarchical memory by first chunking the trajectory into segments of 5,000 tokens with 500-token overlap, then using the LLM to summarize each chunk into a compact memory piece that preserves key subgoals, actions, observations, and failures. Each memory piece is embedded using a local sentence-transformer model (all-MiniLM-L6-v2), and a global summary is generated from all memory pieces to capture the overall strategy and critical facts. This summarization process is lossy, as fine-grained trajectory details are compressed into concise text. During retrieval, MemoryBank computes cosine similarity between the question embedding and memory piece embeddings, combined with an Ebbinghaus-inspired retention score that accounts for memory strength and recency of recall. The top- k memory pieces are retrieved and concatenated with the global summary as context for answering. We use the default configuration with $k = 6$, forget decay $\tau = 5.0$, and strength increment of 1 upon each recall.

MemAgent. processes the trajectory as a stream of fixed-length sections, iteratively updating a recurrent memory state. For each chunk of 5,000 tokens, the LLM reads the current trajectory section along with the previous memory, then generates an updated memory that summarizes the agent’s progress while retaining relevant details from earlier sections. This recurrent summarization is inherently lossy, as information from earlier chunks may be progressively compressed or forgotten as new sections are processed. During retrieval, MemAgent directly reads from its final accumulated memory without additional retrieval mechanisms, the memory itself serves as the complete context for answering questions. We follow the default configuration with a 4,096-token context window partitioned into: the current trajectory chunk (5,000 tokens, truncated if needed), the accumulated memory (dynamically sized), and generation budget (1,024 tokens), with memory truncated from the beginning when context limits are exceeded to preserve more recent information.

Mem-alpha. employs a three-tier hierarchical memory architecture with an agentic approach to memory management. The system maintains: (1) Core Memory for high-level task understanding and rules, (2) Semantic Memory for storing factual

770 knowledge as embedded vectors, and (3) Episodic Memory for recording specific events with temporal context. Trajectories
771 are chunked using sentence-aware tokenization into segments of 4,096 tokens, preserving sentence boundaries. For each chunk,
772 an agent equipped with memory tools (insert, update, delete, retrieve) autonomously decides which information to store and
773 in which memory tier. Both semantic and episodic memories are embedded using text-embedding-3-small (1,536 dimensions)
774 and retrieved via Top-K similarity search. During question answering, MemAlpha retrieves relevant memories using BM25
775 sparse retrieval, fetching the top-20 most relevant items per memory type. We follow the default configuration with a thinking
776 budget of 1,024 tokens, maximum generation of 2,048 tokens, and memory consolidation occurring every 5 items.
777

778 **Mem1.** processes the trajectory through recurrent memory consolidation, iteratively updating a compact memory state with
779 each new chunk of observations. For each chunk of 5,000 tokens, the LLM reads the current trajectory section along with the
780 previous accumulated memory, then generates an updated memory that integrates new information while maintaining context
781 and discarding redundant details. After processing all chunks, a final comprehensive summary is generated that consolidates
782 key actions, important observations, overall progress, and patterns encountered. MEM1 directly uses this global consolidated
783 memory as the complete context for answering all questions. We follow the default configuration with a 120,000-token
784 maximum context window, trajectory chunks of 5,000 tokens, memory update budget of 1,024 tokens per chunk.
785

786 **Mem0.** constructs its memory layer through an LLM-driven fact extraction process, distilling raw trajectory data into a series
787 of "atomic facts." These facts are subsequently embedded and stored in a vector database. To ensure memory consistency,
788 Mem0 incorporates a conflict resolution mechanism that updates or replaces outdated information (e.g., evolving user
789 locations). However, this extraction-based approach is inherently lossy for structured trajectory data, as it often omits critical
790 low-level details. Empirical observations during our experiments indicate that bypassing the extraction layer and utilizing
791 raw data directly can significantly enhance performance on trajectory-based benchmarks. During retrieval, Mem0 employs
792 vector-based cosine similarity to identify the top- k most relevant facts, which are then injected into the LLM prompt as context
793
794

795 **A-Mem.** implements a recurrent memory processing strategy to handle long-term trajectories. The input is segmented
796 into chunks, and new memory states are built recursively by integrating the current chunk with preceding memory. Each
797 memory entry consists of a concatenated representation of content, context, keywords, and tags, which is then embedded
798 and stored in a vector database. This recursive construction, while thorough, introduces significant computational latency
799 for long-context sequences. Furthermore, A-Mem supports memory evolution: it retrieves top- k neighboring entries via
800 vector search, and an LLM determines whether to establish new relational connections or update existing metadata. We set
801 the RECURRENT_CHUNK_SIZE to 8,000 tokens.
802

803 **MemGPT.** implements a hierarchical memory architecture that separates memory into core memory (in-context) and
804 archival memory (external storage with retrieval). The trajectory is inserted directly into archival memory as a complete
805 text block, which is then indexed for retrieval. MemGPT uses an agentic approach where the LLM autonomously manages
806 memory through function calls. It can search, insert, and retrieve from archival memory as needed during question answering.
807 The archival memory is embedded using a local embedding model (BAAI/bge-small-en-v1.5) for vector-based retrieval.
808 Unlike other memory agents that pre-process trajectories into summaries, MemGPT stores the raw trajectory text and relies
809 on the agent's retrieval capabilities to fetch relevant portions at query time. During question answering, the agent receives
810 the question and uses its memory tools to search archival storage, with retrieved content brought into the limited core memory
811 context window. We use the default MemGPT configuration with auto-save disabled, maximum chaining steps set to 5 to
812 prevent infinite tool-calling loops, and observations truncated to 8,000 characters when exceeding length limits.
813

814 **MemoRAG.** constructs memory by first building a global memory representation of the entire trajectory using a dedicated
815 memory model, then enabling retrieval-augmented generation for question answering. The trajectory is converted to text
816 format and processed by a memory encoder (Qwen2-7B-Instruct with beacon compression at ratio 4) that compresses the
817 long context into a compact memory representation. This memory is then used to guide retrieval from the original text chunks.
818 During retrieval, MemoRAG uses a dual-model architecture: the memory model generates retrieval cues based on the query
819 and global memory, while a separate retriever (BAAI/bge-m3) fetches the top- k most relevant chunks from the original
820 trajectory. The retrieved chunks are then passed to a generation model to produce the final answer. This approach is lossy
821 during memory encoding, as the beacon compression mechanism reduces the original context to a fraction of its size. We
822 use the default configuration with retrieval chunk size of 512 tokens, top- k = 3 retrieved hits, beacon ratio of 4, and maximum
823 generation length of 256 tokens, retrieval via bge-m3.
824

SimpleMem. constructs memory through an LLM-driven extraction process that converts raw trajectory data into atomic memory entries. The trajectory is processed in sliding windows, where each window is passed to an LLM that extracts structured fields including lossless restatements with forced coreference resolution (eliminating pronouns and converting relative time to absolute timestamps), keywords, locations, persons, entities, and topics. These atomic entries are embedded and stored in a vector database. This extraction process is lossy, as trajectory details are abstracted into discrete semantic units. During retrieval, SimpleMem employs a hybrid strategy combining semantic vector similarity, lexical keyword matching, and symbolic metadata filtering. The system supports multi-query planning that decomposes complex questions into targeted sub-queries, and reflection-based refinement that iteratively checks information completeness and generates additional queries to fill gaps. We use the default configuration with parallel memory building (2 workers), parallel retrieval (3 workers), reflection enabled with maximum 2 rounds, and planning enabled for query decomposition.

C. LLM-as-Judge Calibration Protocol

We include the following materials to ensure reproducibility and transparency of our LLM-as-judge evaluation.

C.1. Judge Prompt and Output Format

We use QWEN3 32B as the primary evaluator. The judge receives the input triplet (question, reference answer, predicted answer) and returns a binary decision. The judge is required to output only one token in `{yes, no}`.

Binary Correctness Judgement Prompt

System or Instruction Prompt

You are an expert evaluator. You will be given a question, a reference answer, and a predicted answer.

Your task is to determine if the predicted answer is correct based on:

1. Factual correctness compared to the reference
2. Completeness of the answer
3. Relevance to the question

`{context_str}`

Question: `{question}`

Reference Answer: `{golden_answer}`

Predicted Answer: `{predicted_answer}`

Is the predicted answer correct? Respond with ONLY `yes` or `no`. Do not include any thinking process, explanation, or additional text.

Answer

C.2. Human-Judge Agreement

To validate the reliability of our LLM-as-judge evaluation, we conducted human annotation on a sample of 300 instances (50 per subset) from the GPT-5.2 results. We obtain gold labels via independent human annotation. Each instance is labeled by at least two annotators with access to the question, reference answer, and predicted answer. Labels are binary: `yes` if the predicted answer is correct, otherwise `no`. Disagreements are resolved by majority vote, with a third annotator used for adjudication when needed.

Table 10 presents the confusion matrix and performance metrics aggregated across all subsets. The judge achieves 92.67% accuracy, indicating reliable alignment with human judgment.

Table 10. Confusion matrix (left) and performance metrics (right) for LLM-as-judge vs. human annotations.

Judge Label	Human Label			Metric	Value
	Correct	Incorrect	Total		
Correct	190 (TP)	7 (FP)	197	Accuracy	92.67%
Incorrect	15 (FN)	88 (TN)	103	Precision	96.45%
Total	205	95	300	Recall	92.68%
				F1 Score	94.53%

880 D. Prompt Templates for AMA-Agents

881 This appendix provides the prompt templates used by AMA-agent in both phases. The first phase constructs the Causality
882 Graph by extracting objective inventories, detecting environment and objective state changes, and emitting structured,
883 machine parsable records in Markdown. The second phase performs retrieval time routing, including chunk sufficiency
884 judgement and trajectory based code generation.
885

886 D.1. Memory Construction Prompt

887 Memory Construction Prompt Template

```
888 MEMORY_CONSTRUCTION_PROMPT_TEMPLATE = ""  
889 You are given an agent trajectory consisting of action and observation pairs.  
890 Your task is to analyze the trajectory turn by turn and produce a Markdown report  
891 that is strictly machine parsable.  
892  
893 Input will provide:  
894 (1) current turn: {turn_t}  
895 (2) previous turn: {turn_t_minus_1}  
896 (3) optional task description: {task}  
897  
898 You must do the following in order.  
899  
900 Section 1: OBJECTIVE INVENTORY  
901 List all objectives that the agent is tracking or manipulating.  
902  
903 Section 2: ENV STATE CHANGE DETECTION  
904 Decide whether the environment state changed at this turn.  
905  
906 Section 3: OBJECT STATE CHANGE DETECTION  
907 Decide whether the object state changed at this turn.  
908  
909 OUTPUT FORMAT  
910 Return a Markdown block with the following exact structure.  
911  
912 # OBJECTIVES  
913 1. <objective_name>: <description>  
914 2. ...  
915  
916 # STATE_CHANGES  
917 env_changed: <true or false>  
918 objective_changed: <true or false>  
919 evidence:  
920 - "<quote 1>"  
921 - "<quote 2>"  
922  
923 # STATES  
924 env_state:  
925 - <key>: <value>  
926 - ...  
927 object_states:  
928 - name: <objective_name>  
929   state:  
930   - <key>: <value>  
931   - ...  
932 - ...  
933 Constraints:  
934 (1) Do not invent facts not supported by the provided turns.  
(2) Keep rationales short and grounded.  
(3) Use consistent objective names across turns.  
""
```

D.2. Chunk Sufficiency Judgement Prompt

Chunk Sufficiency Judgement Prompt Template

```
CHUNK_SUFFICIENCY_JUDGMENT_PROMPT_TEMPLATE = """
You have retrieved the top ranked most relevant turns from an agent trajectory.
Each turn has a UNIQUE TURN INDEX that you can reference.

Query: {query}

Retrieved Turns:
{retrieved_chunks}

Your Task
Carefully analyze the retrieved turns and determine ONE of the following.

1. SUFFICIENT
The retrieved turns contain enough information to answer the query completely.
If you choose this, you MUST provide the answer immediately in the same response.
Format:
SUFFICIENT
ANSWER: <your complete and accurate answer>

2. NEED_GRAPH
The query can likely be answered by looking at adjacent turns or specific ranges.
Use this when you found relevant information but need surrounding context.

You can specify retrieval in multiple ways.

A. Request adjacent turns
NEED_GRAPH: turn_5 before=2 after=1
NEED_GRAPH: turn_8 before=3 after=0, turn_15 before=0 after=2

B. Request turn ranges
NEED_GRAPH: turns 5 to 10
NEED_GRAPH: turns 3 to 8, turns 15 to 20

C. Request individual turns
NEED_GRAPH: turns 3, 7, 12, 18
NEED_GRAPH: turns 5, 8, 15

3. NEED_CODE
The query requires computational analysis, pattern finding, counting, or aggregation
across the full trajectory and cannot be answered from the retrieved turns alone.
Format:
NEED_CODE: <explain what computation or analysis is needed>

Guidelines
Choose SUFFICIENT only if you can answer completely right now.
Choose NEED_GRAPH when you need immediate context around retrieved turns.
Choose NEED_CODE for trajectory wide computation or when turns do not contain the answer.

Response:
"""
```

D.3. Trajectory Based Code Generation Prompt

Trajectory Based Code Generation Prompt Template

```
CODE_GENERATION_PROMPT_TEMPLATE = """
Write Python code to extract information from a trajectory to answer the question.
Keep your thinking brief.

Question: {query}

Task: {task}

Trajectory Sample:
{trajectory_sample}

Trajectory JSON Structure
Variable trajectory_json contains:
{
  "trajectory": [
    {
      "turn_idx": 0,
      "action": "...",
      "observation": "..."
    },
    ...
  ],
  "task": "...",
  "episode_id": "..."
}

Requirements
(1) Only use Python standard library unless explicitly allowed otherwise.
(2) The code must be directly executable.
(3) Print intermediate results that justify the final answer.
(4) Reference turn indices in outputs whenever possible.
"""
```

E. Dataset Examples

We provide representative examples from subset below.

E.1. Real-world subset example

WebArena Case Study (ID: `task_webarena_17`)

Task: Star the eight most-starred repositories on GitLab.

Total Tokens: 38,289 **Turns:** 31

Turn	Action	Environment Observation (Structural State Snippet)
00	click [426]	Tab 0: Projects · Dashboard · GitLab (link Explore)
01	click [2040]	Tab 0: Projects · Explore · GitLab (link Most stars)
04	click [6170]	Tab 0: Projects · Explore · GitLab (link 267)
05	click [7798]	Tab 0: Issues · Umano: News Read To You / AndroidSlidingUpPanel
...
15	type [13642]	Tab 0: most starred repositories stars · Search · GitLab
...
23	type [19543]	Tab 0: The AllY Project / allyproject.com (textbox Search)
26	click [21429]	Tab 0: Projects · Dashboard (link Byte Blaze / ally...)
...
30	action: stop	[Early stop: Reach max steps 30]

QA Examples:

- **Type A (Temporal Inference):** *The search query string begins concatenating across Steps 14–16. At which step does the title first show ‘most starred repositories stars’, and what action caused that?*
Ans: Step 15 shows the title, caused by the Step 14 `type` action appending text to the query without clearing it.
- **Type B (State Dependency):** *Why did keyword searching fail to replicate the ‘Most stars’ ordering, and what prerequisite state was required instead?*
Ans: ‘Most stars’ is a view-specific ordering on Explore; Search matches text and returned zero results. The prerequisite was staying on Explore with ‘Most stars’ selected.
- **Type C (State Update):** *Compare the ‘Users’ result count between Step 14 and Step 21. What is the change?*
Ans: It increases from ‘Users 0’ to ‘Users 1’, a +1 change.
- **Type D (State Abstraction):** *Identify the redundant loop near the end and explain why it is unproductive.*
Ans: Steps 26 and 29 both click link [21429] from the Dashboard list without a state change in between. This loop fails to advance toward the goal.

E.2. Synthetic subset example

BabyAI Example (ID: task_babyai_22)

Task: put the purple key next to the green key

Total Tokens: 19,310 **Turns:** 392 **Result:** fail (truncated)

Turn	Action	Environment Observation (Structural State Snippet)
00	done	Mission: put the purple key next to the green key. You are facing south.
03	toggle	In your view: . Walls border the area. You are facing south.
10	forward	In your view: a purple key, a red ball, a grey box. You are facing east.
12	toggle	In your view: a green key, a grey ball, a red ball, a grey box, a purple box, a purple key. You are facing north.
...
24	pickup	In your view: a red ball, a grey box, a purple box, a purple key, a green box. You are facing north.
43	drop	In your view: . Walls border the area. You are facing south.
...
391	toggle	Mission: put the purple key next to the green key. [Reach max steps 392]

QA Examples:

- **Type A (Temporal Inference):** Which object is no longer visible after the agent moves at step 10?
Ans: After the agent executes the 'forward' action at step 10, '. Walls border the area' is no longer visible. It was visible at step 9, but the agent's movement changed its field of view, causing '. Walls border the area' to move out of sight.
- **Type B (State Dependency):** Background: At step 6, the agent's inventory is empty. Question: At step 7, can the agent execute the 'drop' action? Why or why not?
Ans: At step 7, the agent cannot execute the 'drop' action because the inventory is empty at step 6. The agent needs to have an item in inventory to drop it.
- **Type C (State Update):** What are the inventory changes from step 1 to step 4? At which steps did the inventory change respectively?
Ans: The inventory changes from step 1 to step 4 are: step 4: agent picks up item (inventory changes).
- **Type D (State Abstraction):** Summarize the agent's trajectory from step 0 to step 3 for the task 'put the purple key next to the green key'. What are the key actions and milestones?
Ans: From step 0 to step 3, the agent's trajectory includes: Key actions: step 0: done; step 1: done; step 2: done; step 3: toggle.

TextWorld Example (ID: `cooking_medium_103008`)

Task: Get ready to pick stuff up and put it in places... First thing I need you to do is to doublecheck that the walnut gate in the serious workshop is wide open. And then, go to the east... retrieve the old lampshade from the rusty rack... sit the old lampshade on the shoddy table inside the cramped vault.

Total Tokens: 8,384 **Turns:** 80 **Result:** *fail (reached_max_steps)*

Turn	Action	Environment Observation (Structural State Snippet)
00	put old lampshade on...	You can't see any such thing. (Inventory: tiny loaf of bread, teal keycard, mouse, synthesizer)
14	look	-= Serious Workshop =- Desk contains outmoded mouse and tiny loaf of bread. Closed walnut gate to the east.
29	open walnut gate	You open walnut gate. (Available actions: go east, close walnut gate, examine walnut gate, etc.)
59	go east	-= Cramped Vault =- You see a shoddy table (empty) and a rusty rack with an old lampshade on it.
60	put old lampshade on...	You need to take the old lampshade first.
64	put old lampshade on...	You need to take the old lampshade first.
74	go north	-= Silent Cubicle =- The agent moves away from the goal room.
78	go south	-= Serious Workshop =- Agent returns to the starting room.
79	look	<i>[Early stop: Reach max steps 80]</i>

QA Examples (Direct Extraction):

- Type A (Temporal Inference):** *What actions were performed between step 37 and step 41?*
Ans: Between step 37 and step 41, the agent performed the following actions: at step 37, eat tiny loaf of bread; at step 38, put old lampshade on shoddy table; at step 39, put old lampshade on shoddy table; at step 40, put old lampshade on shoddy table; at step 41, look.
- Type B (State Dependency):** *At step 27 with state: Inventory: empty... Object states: shoddy table [cramped vault], old lampshade [rusty rack], teal keycard [I]... can the agent perform "drop teal keycard"?*
Ans: No, the agent cannot perform this action because the inventory is empty, so there is no object to put.
- Type C (State Update):** *How did the state of I change throughout the trajectory, including what objects were placed in or removed from it?*
Ans: I evolution: step 1: tiny loaf of bread was removed; step 2: outmoded mouse was removed; step 15: tiny loaf of bread was added; step 23: tiny loaf of bread was removed; step 31: small synthesizer was removed; step 32: tiny loaf of bread was added; step 37: tiny loaf of bread was removed. At step 41, it contains: teal keycard.
- Type D (State Abstraction):** *Until step 79, what actions has the agent performed and how frequently?*
Ans: Actions performed: 'put old lampshade on shoddy table' (18 times), 'inventory' (13 times), 'look' (8 times), 'take old lampshade from rusty rack' (6 times), 'open walnut gate' (5 times), 'put tiny loaf of bread on solid desk' (4 times), 'take tiny loaf of bread from solid desk' (3 times), 'go east' (3 times), 'examine small synthesizer' (3 times), 'put outmoded mouse on solid desk' (2 times), 'examine teal keycard' (2 times), 'examine solid desk' (2 times), 'close walnut gate' (2 times), 'examine walnut gate' (1 times), 'drop small synthesizer' (1 times).

1210 F. Needle-in-a-Haystack QA Generation Pipeline

1211 To evaluate the long-context retrieval capabilities of memory-augmented agents, we developed a structured pipeline to
1212 generate QA pairs where the answer is anchored to specific "needle" turns within a trajectory "haystack." The generation
1213 logic is formalized in Algorithm 1.
1214

1215 Algorithm 1 QA Needle Generation for Trajectory Evaluation

1217 **Require:** Source trajectory data \mathcal{T} , Bin sizes $\mathcal{B} \in \{8K, 16K, \dots, 128K\}$, QA Types $\mathcal{Q} \in \{A, B, C, D\}$

1218 **Ensure:** Final balanced dataset \mathcal{D}_{final}

1219 1: $\mathcal{C} \leftarrow \emptyset$ {Initialize candidate pool}

1220 2: $H \leftarrow \text{split_by_turns}(\mathcal{T})$ {Chunk haystack with unique turn identifiers}

1221 3: **for all** $bin_size \in \mathcal{B}$ **do**

1222 4: **for all** $qa_type \in \mathcal{Q}$ **do**

1223 5: $\tau_{needle} \leftarrow \text{sample}(H, \text{strategy}=\text{"diversity_first"})$ {Ensure depth diversity}

1224 6: $qa_{needle} \leftarrow \text{generate_qa}(H, qa_type, \tau_{needle}, bin_size)$

1225 7: $qa_{needle}.source.ids \leftarrow \{t.id \mid t \in \tau_{needle}\}$ {Map for traceability}

1226 8: **if** $\text{verify_qa_quality}(qa_{needle})$ **then**

1227 9: $\mathcal{C} \leftarrow \mathcal{C} \cup \{qa_{needle}\}$

1228 10: **end if**

1229 11: **end for**

1230 12: **end for**

1231 13: $\mathcal{D}_{final} \leftarrow \text{select_balanced}(\mathcal{C}, \text{quota} = \{A:4, B:3, C:3, D:2\})$

1233 Key Strategies in Pipeline:

- 1234 • **Diversity-First Sampling:** Instead of random sampling, we pick "needle" turns from various depths of the trajectory (early,
1235 middle, and late stages) to prevent the LLM from exploiting positional biases.
- 1236 • **Ground Truth Traceability:** By binding each QA pair to specific `turn_ids`, we can verify whether the agent's retrieval
1237 mechanism successfully identified the correct "needle" from the "haystack" during inference.
- 1238 • **Balanced Distribution:** The final selection ensures that different reasoning types (e.g., spatial reasoning vs. object state
1239 tracking) are represented proportionally to avoid data skew.

1245 G. Example of needle turn for ablation study

1246 To further illustrate the distinction between the three evaluation branches discussed in Section 5.3, we provide a concrete
1247 example from a Type A3 task (Object Visibility Change).
1248

1249 Sample Query (Type A3)

1250 **Question:** Which object is no longer visible after the agent moves at step 1?

1251 **Ground Truth:** After the agent executes the 'forward' action at step 1, 'a purple box' is no longer visible. It was
1252 visible at step 0, but the agent's movement changed its field of view.

1253 • Raw Observation Branch:

1254 [Turn 0] Action: forward; Obs: "In your view: a yellow box, a purple box, a green
1255 ball..."

1256 [Turn 1] Action: forward; Obs: "In your view: a yellow box, a green ball..."

1257 *Note: The LLM must compare the two raw observation strings to infer the disappearance of the purple box.*

1258 • Oracle Memory Branch (and System Branch upon success):

```
1265 <memory>
1266 - **Initial Position (Turn 0)**: Visible objects: Yellow box, purple box, green ball.
1267 - **Progress (Turn 1)**: Action: Moved forward. Updated view: Yellow box and
1268   green ball visible; purple box no longer in sight.
1269 - **Inference**: The disappearance of the purple box suggests movement progress.
1270 </memory>
```

1271 *Note: The state change is explicitly summarized. In the Oracle branch, this shard is force-fed to the LLM; in the System*
1272 *branch, the agent must retrieve this specific shard from the database.*

1274 H. Case-study

1275 To further illustrate the distinction between our raw data storage approach and the default Mem0 extraction process discussed
1276 in Section 3, we provide a comparative analysis using a *Qwen3-32B* model. This example demonstrates why LLM-driven
1277 "fact distillation" is inherently lossy for structured agent experiences.

1280 Case Study 1: Narrative Data (Successful Extraction)

1281 **Input:** My name is John. I like pizza and I work as a software engineer. I have a dog named Max.

1282 **Status:** Success (4 Facts Extracted)

- 1283 • Fact 1: Name is John
- 1284 • Fact 2: Likes pizza
- 1285 • Fact 3: Works as a software engineer
- 1286 • Fact 4: Has a dog named Max

1289 Case Study 2: Trajectory Data (Extraction Failure)

1290 **Input (Abridged Trajectory):**

1291 [Turn 0] Action: look; Obs: "You are in the middle of a room. Looking
1292 quickly around you, you see nothing. Available actions: go to cabinet 1, go
1293 to cabinet 2..."

1294 [Turn 1] Action: go to toilet 1; Obs: "You arrive at toilet 1. On the toilet
1295 1, you see a soapbottle 2..."

1296 **Status:** Failure (0 Facts Extracted)

1300 • **Narrative Extraction Logic:** Mem0's extraction prompt is optimized for high-level entities and static properties. In Case
1301 1, the LLM successfully maps the input into an atomic "subject-predicate-object" structure, which is ideal for standard
1302 user profiling.

1303 • **The Bottleneck in Trajectory Data:**

```
1304 <internal_log>
1305 - Input length: 5022 characters (15 turns)
1306 - Model: Qwen3-32B
1307 - Observation: The extractor fails to identify "facts" within the
1308   dynamic action-state-observation loops. Critical spatial
1309   identifiers (e.g., "toilet 1") are ignored as low-level noise.
1310 </internal_log>
```

1311 *Note: As evidenced by Case 2, the extraction-based approach is inherently lossy for agent-based tasks. By bypassing*
1312 *the infer=True extraction layer and utilizing raw trajectory segments directly in our **System Branch**, we preserve the*
1313 *environmental context that is otherwise discarded by the LLM-driven fact extractor.*