UNSUPervised UNIVERSal SELF-ATTENTION NETWORK FOR GRAPH CLASSIFICATION

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ABSTRACT

Existing graph embedding models often have weaknesses in exploiting graph structure similarities, potential dependencies among nodes and global network properties. To this end, we present U2GAN, a novel unsupervised model leveraging on the strength of the recently introduced universal self-attention network (Dehghani et al., 2019), to learn low-dimensional embeddings of graphs which can be used for graph classification. In particular, given an input graph, U2GAN first applies a self-attention computation, which is then followed by a recurrent transition to iteratively memorize its attention on vector representations of each node and its neighbors across each iteration. Thus, U2GAN can address the weaknesses in the existing models in order to produce plausible node embeddings whose sum is the final embedding of the whole graph. Experimental results show that our unsupervised U2GAN produces new state-of-the-art performances on a range of well-known benchmark datasets for the graph classification task. It even outperforms supervised methods in most of benchmark cases.

1 INTRODUCTION

Many real-world and scientific data are represented in forms of graphs, e.g. data from knowledge graphs, recommender systems, social and citation networks as well as telecommunication and biological networks (Battaglia et al., 2018; Zhang et al., 2018c). In general, a graph can be viewed as a network of nodes and edges, where nodes correspond to individual objects and edges encode relationships among those objects. For example, in online forum, each discussion thread can be constructed as a graph where nodes represent users and edges represent commenting activities between users (Yanardag & Vishwanathan, 2015).

Early approaches focus on computing the similarities among graphs to build a graph kernel for graph classification (Gärtner et al., 2003; Kashima et al., 2003; Borgwardt & Kriege, 2005; Shervashidze et al., 2009; Vishwanathan et al., 2010; Shervashidze et al., 2011; Yanardag & Vishwanathan, 2015; Narayanan et al., 2017; Ivanov & Burnaev, 2018). These graph kernel-based approaches treat each atomic substructure (e.g., graphlet, subtree structure, random walk or shortest path) as an individual feature, and count their frequencies to construct a numerical vector to represent the entire graph, hence they ignore substructure similarities and global network properties.

One recent notable strand is to learn low-dimensional continuous embeddings of the whole graphs (Hamilton et al., 2017b; Zhang et al., 2018a; Zhou et al., 2018), and then use these learned embeddings to train a classifier to predict graph labels (Wu et al., 2019). Advanced approaches in this direction have attempted to exploit graph neural network (Scarselli et al., 2009), capsule network (Sabour et al., 2017) or graph convolutional neural network (Kipf & Welling, 2017; Hamilton et al., 2017a) for supervised learning objectives (Li et al., 2016; Niepert et al., 2016; Zhang et al., 2018b; Ying et al., 2018; Verma & Zhang, 2018; Xu et al., 2019; Xinyi & Chen, 2019; Maron et al., 2019b; Chen et al., 2019). These graph neural network (GNN)-based approaches usually consist of two common phases: the propagating phase and the readout phase. The former phase aims to iteratively update vector representation of each node by recursively aggregating representations of its neighbors, and then the latter phase applies a pooling function (e.g., mean, max or sum pooling) on output node representations to produce an embedding of each entire graph; and this graph embedding is used to predict the graph label. We find that these approaches are currently showing very promis-
ing performances, nonetheless the dependency aspect among nodes, which often exhibit strongly in many kinds of real-world networks, has not been exploited effectively.

Very recently, the universal self-attention network \citep{dehghani2019universal} has been shown to be very powerful in NLP tasks such as question answering, machine translation and language modeling. Inspired by this new attention network, we propose U2GAN – a novel unsupervised universal graph attention network embedding model for the graph classification task. Our intuition comes from an observation that the recurrent attention process in the universal self-attention network can memorize implicit dependencies between each node and its neighbors from previous iterations, which can be then aggregated to further capture the dependencies among substructures into latent representations in subsequent iterations; this process, hence, can capture both local and global graph structures. Algorithmically, at each timestep, our proposed U2GAN iteratively exchanges a node representation with its neighborhood representations using a self-attention mechanism \citep{vaswani2017attention} followed by a recurrent transition to infer node embeddings. After the training process, we take the sum of all learned node embeddings to obtain the embedding of the whole graph. Our main contributions are as follows:

- In our proposed U2GAN, the novelty of memorizing the dependencies among nodes implies that U2GAN can explore the graph structure similarities locally and globally – an important feature that most of existing approaches are unable to do.
- The experimental results on 5 social network datasets and 6 bioinformatics datasets show that U2GAN produces new state-of-the-art (SOTA) accuracies on 8 datasets by a large margin and comparable accuracies on 3 remaining datasets. Noticeably, despite being unsupervised, it even outperforms most of up-to-date supervised approaches.
- To qualitatively demonstrate an advantage of U2GAN in capturing local and global graph properties, we utilize t-SNE \citep{maaten2008visualizing} to visualize the learned node and graph embeddings to show well-separated clusters of embeddings according to their labels.

\section{Related Work}

Early popular approaches are based on “graph kernel” which aims to recursively decompose each graph into “atomic substructures” \textit{e.g.}, graphlets, subtree structures, random walks or shortest paths) in order to measure the similarity between two graphs \citep{gartner2003graph}. For this reason, we can view each atomic substructure as a word token and each graph as a text document, hence we represent a collection of graphs as a document-term matrix which describes the normalized frequency of terms in documents. Then, we can use a dot product to compute the similarities among graphs to derive a kernel matrix used to measure the classification performance using a kernel-based learning algorithm such as Support Vector Machines (SVM) \citep{hofmann2008kernel}. We refer to an overview of the graph kernel-based approaches in \citep{nikolentzos2019survey, kriege2019survey}.

Since the introduction of word embedding models i.e., Word2Vec \citep{mikolov2013efficient} and Doc2Vec \citep{le2014distributed}, there have been several efforts attempted to apply them for the graph classification task. Deep Graph Kernel (DGK) \citep{yanardag2015deep} applies Word2Vec to learn embeddings of atomic substructures to create the kernel matrix. Graph2Vec \citep{narayanan2017graph2vec} employs Doc2Vec to obtain embeddings of entire graphs in order to train a SVM classifier to perform classification. Anonymous Walk Embedding (AWE) \citep{ivanov2018anonymous} maps random walks into “anonymous walks” which are considered as word tokens, and then utilizes Doc2Vec to achieve the graph embeddings to produce the kernel matrix.

In parallel, another recent line of work has focused on using deep neural networks to perform the graph classification in a supervised manner. PATCHY-SAN \citep{niepert2016learning} adapts a graph labeling procedure to generate a fixed-length sequence of nodes from an input graph, and orders k-hop neighbors for each node in the generated sequence according to their graph labelings; PATCHY-SAN then selects a fixed number of ordered neighbors for each node and applies a convolutional neural network to classify the input graph. MPNN \citep{gilmer2017neural}, DGCNN \citep{zhang2018end} and DiffPool \citep{ying2018hierarchical} are end-to-end supervised models which share similar two-phase process by (i) using stacked multiple graph convolutional layers \textit{e.g.}, GCN layer \citep{kipf2016semi} or GraphSAGE layer \citep{hamilton2017inductive} to aggregate node feature vectors, and (ii) applying a graph-level pooling layer \textit{e.g.}, mean, max or sum pooling, sort pooling or differentiable
pooling) to obtain the graph embeddings which are then fed to a fully-connected layer followed by a softmax layer to predict the graph labels.

Graph neural networks (GNNs) (Scarselli et al., 2009) aim to iteratively update the vector representation of each node by recursively propagating the representations of its neighbors using a recurrent function until convergence. The recurrent function can be a neural network e.g., gated recurrent unit (GRU) (Li et al., 2016), or multi-layer perceptron (MLP) (Xu et al., 2019). Note that both stacked GCN and GraphSAGE multiple layers can be seen as variants of the recurrent function in GNNs. Other graph embedding models are briefly summarized in (Zhou et al., 2018; Zhang et al., 2018c; Wu et al., 2019).

3 THE PROPOSED U2GAN

In this section, we detail how to construct our U2GAN and then present how U2GAN learns model parameters to produce node and graph embeddings.

Graph classification. Given a set of graphs \( \{G_1, G_2, ..., G_N\} \subseteq G \) and their corresponding class labels \( \{y_1, y_2, ..., y_N\} \subseteq \mathcal{Y} \), our U2GAN aims to learn a plausible embedding \( \mathbf{o}_G \) of each entire graph \( G \) in order to predict its label \( y \).

![Figure 1: Illustration of our U2GAN learning process.](image)

Each graph \( G \) is defined as \( G = (\mathcal{V}, \mathcal{E}, \mathbf{X}) \), where \( \mathcal{V} \) is a set of nodes, \( \mathcal{E} \) is a set of edges, and \( \mathbf{X} \in \mathbb{R}^{|\mathcal{V}| \times d} \) represents feature vectors of nodes. In U2GAN, as illustrated in Figures 1 and 2, we use a universal self-attention network (Dehghani et al., 2019) to learn a node embedding \( \mathbf{o}_v \) of each node \( v \in \mathcal{V} \), and then \( \mathbf{o}_G \) is simply returned by summing all learned node embeddings as follows:

\[
\mathbf{o}_G = \text{SUM}(\{\mathbf{o}_v, \forall v \in \mathcal{V}\})
\]  

(1)

Constructing U2GAN. Formally, given an input graph \( G \), we uniformly sample a set of \( N \) neighbors for each \( v \in \mathcal{V} \), and then use node \( v \) and its neighbors for the U2GAN learning process. For example, as illustrated in Figure 2, we generate a set of \( N = 3 \) neighbors \( \{1, 2, 4\} \) for node 3, and then consider \( \{3, 1, 2, 4\} \) as an input to U2GAN where we leverage on the universal self-attention network (Dehghani et al., 2019) to learn an effective embedding of node 3.

Intuitively, the universal self-attention network can help to better aggregate feature vectors from neighbors of a given node to produce its plausible embedding. In particular, each node and its neighbors is transformed into a sequence of feature vectors which are then iteratively refined at each timestep – using a self-attention mechanism (Vaswani et al., 2017) followed by a recurrent transition along with adding residual connection (He et al., 2016) and layer normalization (LAYERNORM) (Ba et al., 2016).

Given a sampled sequence of \((N + 1)\) nodes \( \{v_i\}_{i=1}^{N+1} \) where \( \{v_2, v_3, ..., v_N+1\} \) are neighbors of \( v_1 \), we obtain an input sequence of feature vectors \( \{\mathbf{h}_{v_i}\}_{i=1}^{N+1} \) for which \( \mathbf{h}_{v_i} = \mathbf{X}_{v_i} \in \mathbb{R}^d \). In U2GAN, at

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1. The experimental results in Xu et al. (2019) show that the sum pooling performs better than the mean and max poolings.
2. We sample a different set of neighbors at each training step.
each step $t$, we consider $\{h_{v_i}^{t-1}\}_{i=1}^{N+1}$ as an input sequence and produce an output sequence $\{h_{v_i}^t\}_{i=1}^{N+1}$ for which $h_{v_i}^t \in \mathbb{R}^d$ as follows:

$$h_{v_i}^t = \text{LAYERNORM} \left( x_{v_i}^t + \text{TRANSITION} \left( h_{v_i}^{t-1} \right) \right)$$

(2)

with

$$x_{v_i}^t = \text{LAYERNORM} \left( h_{v_i}^{t-1} + \text{ATT} \left( h_{v_i}^{t-1} \right) \right)$$

(3)

where $\text{TRANSITION}(.)$ and $\text{ATT}(.)$ denote a feed-forward network and a self-attention network respectively as follows:

$$\text{TRANSITION} \left( x_{v_i}^t \right) = W_2 \text{ReLU} \left( W_1 x_{v_i}^t + b_1 \right) + b_2$$

(4)

where $W_1$ and $W_2$ are weight matrices, and $b_1$ and $b_2$ are bias parameters, and:

$$\text{ATT} \left( h_{v_i}^{t-1} \right) = \sum_{j=1}^{N+1} \alpha_{i,j} \left( V h_{v_j}^{t-1} \right)$$

(5)

where $V \in \mathbb{R}^{d \times d}$ is a value-projection weight matrix; $\alpha_{i,j}$ is an attention weight which is computed using the softmax function over scaled dot products between the $i$-th and $j$-th input nodes:

$$\alpha_{i,j} = \text{softmax} \left( \frac{(Q h_{v_i}^{t-1}) \cdot (K h_{v_j}^{t-1})}{\sqrt{d}} \right)$$

(6)

where $Q \in \mathbb{R}^{d \times d}$ and $K \in \mathbb{R}^{d \times d}$ are query-projection and key-projection matrices, respectively.

After $T$ steps, we use the vector representation $h_{v_i}^T$ to infer node embeddings $o_{v_i}$. For example, as shown in Figure 2 we have $v_1 = 3$, $v_2 = 1$, $v_3 = 2$ and $v_4 = 4$, and then consider $h_{v_3}^T$ to infer $o_3$.

![Learning node embeddings](image)

**Algorithm 1: The U2GAN learning process.**

1. **Input:** A graph $G = (V, E, X)$.
2. **for** $t = 1, 2, ..., T$ **do**
3.     **for** $v \in V$ **do**
4.         **SAMPLE** a set $C_v$ of $N$ neighbors of $v$
5.         $\forall u \in \{v\} \cup C_v$
6.         $x_{v_i}^t \leftarrow \text{LAYERNORM} \left( h_{v_i}^{t-1} + \text{ATT} \left( h_{v_i}^{t-1} \right) \right)$
7.         $h_{v_i}^t \leftarrow \text{LAYERNORM} \left( x_{v_i}^t + \text{TRANSITION} \left( x_{v_i}^t \right) \right)$
8.     $o_v \leftarrow h_{v_i}^T, \forall v \in V$
9. **end**
10. $o_G = \text{SUM} \left( \{o_v, \forall v \in V\} \right)$

**Learning parameters of U2GAN:** We learn our model parameters (including the weight matrices and biases as well as node embeddings $o_v$) by minimizing the sampled softmax loss function (Jean et al. 2015) applied to node $v \in V$ as follows:

$$\mathcal{L}_{U2GAN} (v) = - \log \frac{\exp(o_v \cdot h_v^T)}{\sum_{v' \in V'} \exp(o_{v'} \cdot h_{v'}^T)}$$

(7)

where $V'$ is a subset sampled from $V$.

We briefly describe the general learning process of our proposed U2GAN model in Algorithm 1.

Here, the learned node embeddings $o_v$ are used as the final representations of nodes $v \in V$. After that, we obtain the plausible embedding $o_G$ of the graph $G$ by summing all learned node embeddings as mentioned in Equation 1.

**Intuition:** In general, on the node level, each node and its neighbors are iteratively attended in the recurrent process with weight matrices shared across timesteps and iterations, thus U2GAN
can memorize the potential dependencies among nodes within substructures. On the graph level, U2GAN views the shared weight matrices as memories to access the updated node-level information from previous iterations to further aggregate broader dependencies among substructures into implicit graph representations in subsequent iterations. Therefore, U2GAN is advantageous to capture both global and local graph structures to learn effective node and graph embeddings, leading to state-of-the-art performances for the graph classification task.

4 EXPERIMENTAL SETUP

We prove the effectiveness of our unsupervised U2GAN on the graph classification task using a range of well-known benchmark datasets as follows: (i) We unsupervisedly train U2GAN to obtain graph embeddings. (ii) We use the obtained graph embeddings as feature vectors to train a classifier to predict graph labels. (iii) We evaluate the classification performance, and then analyze effects of main hyper-parameters.

4.1 DATASETS

We use 11 well-known datasets consisting of 5 social network datasets (COLLAB, IMDB-B, IMDB-M, REDDIT-B and REDDIT-M5K) (Yanardag & Vishwanathan, 2015) and 6 bioinformatics datasets (DD, MUTAG, NCI1, NCI109, PROTEINS and PTC). We follow (Niepert et al., 2016; Zhang et al., 2018b) to use node degrees as features on all social network datasets as these datasets do not have available node features. Table 1 reports the statistics of these experimental datasets.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>#G</th>
<th>#Cls</th>
<th>A.NG</th>
<th>A.NN</th>
<th>d</th>
</tr>
</thead>
<tbody>
<tr>
<td>COLLAB</td>
<td>5,000</td>
<td>3</td>
<td>74.5</td>
<td>65.9</td>
<td>–</td>
</tr>
<tr>
<td>IMDB-B</td>
<td>1,000</td>
<td>2</td>
<td>19.8</td>
<td>9.8</td>
<td>–</td>
</tr>
<tr>
<td>IMDB-M</td>
<td>1,500</td>
<td>3</td>
<td>13.0</td>
<td>10.1</td>
<td>–</td>
</tr>
<tr>
<td>REDDIT-B</td>
<td>2,000</td>
<td>2</td>
<td>429.6</td>
<td>2.3</td>
<td>–</td>
</tr>
<tr>
<td>REDDIT-M5K</td>
<td>5,000</td>
<td>5</td>
<td>508.5</td>
<td>2.3</td>
<td>–</td>
</tr>
<tr>
<td>DD</td>
<td>1,178</td>
<td>2</td>
<td>284.3</td>
<td>5.0</td>
<td>82</td>
</tr>
<tr>
<td>MUTAG</td>
<td>188</td>
<td>2</td>
<td>17.9</td>
<td>2.2</td>
<td>7</td>
</tr>
<tr>
<td>NCI1</td>
<td>4,110</td>
<td>2</td>
<td>29.8</td>
<td>2.2</td>
<td>37</td>
</tr>
<tr>
<td>NCI109</td>
<td>4,127</td>
<td>2</td>
<td>29.6</td>
<td>2.2</td>
<td>38</td>
</tr>
<tr>
<td>PROTEINS</td>
<td>1,113</td>
<td>2</td>
<td>39.1</td>
<td>3.7</td>
<td>3</td>
</tr>
<tr>
<td>PTC</td>
<td>344</td>
<td>2</td>
<td>25.6</td>
<td>2.0</td>
<td>19</td>
</tr>
</tbody>
</table>

Table 1: Statistics of the experimental benchmark datasets. #G denotes the numbers of graphs. #Cls denotes the number of graph classes. A.NG denotes the average number of nodes per graph. A.NN denotes the average number of neighbors per node. d is the dimension of node feature vectors (i.e. the number of node labels).

Social networks datasets. COLLAB is a scientific dataset where each graph represents a collaboration network of a corresponding researcher with other researchers from each of 3 physics fields; and each graph is labeled to a physics field the researcher belongs to. IMDB-B and IMDB-M are movie collaboration datasets where each graph is derived from actor/actress and genre information of different movies on IMDB, in which nodes correspond to actors/actresses, and each edge represents a co-appearance of two actors/actresses in the same movie; and each graph is assigned to a genre. REDDIT-B and REDDIT-M5K are datasets derived from Reddit community, in which each online discussion thread is viewed as a graph where nodes correspond to users, two users are linked if at least one of them replied to another’s comment; and each graph is labeled to a sub-community the corresponding thread belongs to.

Bioinformatics datasets. DD (Dobson & Doig, 2003) is a collection of 1,178 protein network structures with 82 discrete node labels, where each graph is classified into enzyme or non-enzyme class. PROTEINS comprises 1,113 graphs obtained from Borgwardt et al. (2005) to present secondary structure elements (SSEs). NCI1 and NCI109 are two balanced datasets of 4,110 and 4,127 chemical compound graphs with 37 and 38 discrete node labels, respectively. MUTAG (Debnath et al., 1991) is a collection of 188 nitro compound networks with 7 discrete node labels, where classes indicate a mutagenic effect on a bacterium. PTC (Toivonen et al., 2003) consists of 344 chemical compound networks with 19 discrete node labels where classes show carcinogenicity for male and female rats.
4.2 Training Protocol to Learn Graph Embeddings

**Coordinate embedding.** The relative coordination among nodes might provide meaningful information about graph structure. We follow [Dehghani et al. (2019)] to associate each position \(i\) at step \(t\) a pre-defined coordinate embedding \(p^t_i\) using the sinusoidal functions [Vaswani et al. (2017)], thus we can change Equation 3 in Section 3 to:

\[
x^t_{vi} = \text{LAYERNORM} \left( h^{-1}_{vi} + \text{ATT} \left( h^{-1}_{vi} + p^t_i \right) \right)
\]

with

\[
p^t_{i,2j} = \sin(i/10000^{2j/d}) + \sin(t/10000^{2j/d})
\]

\[
p^t_{i,2j+1} = \cos(i/10000^{2j/d}) + \cos(t/10000^{2j/d})
\]

From the preliminary experiments, adding coordinate embeddings enhances classification results on MUTAG and PROTEINS, hence we use the coordinate embeddings only for these two datasets.

**Hyper-parameter setting.** To learn our model parameters for all experimental datasets, we fix the hidden size of the feed-forward network in Equation 4 to 1024, and the number of samples in the sampled loss function \(L_{U2GAN}\) to 512 (\(|V'| = 512\)) in Equation 7. We set the batch size to 512 for COLLAB, DD, REDDIT-B and REDDIT-M5K, and 128 for remaining datasets. We use the number \(N\) of neighbors sampled for each node from \(\{4, 8, 16\}\) and the number \(T\) of steps from \(\{1, 2, 3, 4, 5, 6\}\). We apply the Adam optimizer [Kingma & Ba (2014)] to train our U2GAN model and apply a grid search to select the Adam initial learning rate \(lr\) from \(\{5e^{-5}, 1e^{-4}, 5e^{-4}\}\). We run up to 50 epochs and evaluate the model as in what follows.

4.3 Evaluation Protocol

For each dataset, after obtaining the graph embeddings, we perform the same evaluation process from [Yanardag & Vishwanathan (2015); Niepert et al. (2016); Zhang et al. (2018b); Xu et al. (2019); Xinyi & Chen (2019)], which is using 10-fold cross-validation scheme to calculate the classification performance for a fair comparison. We use LIBLINEAR [Fan et al. (2008)] and report the mean and standard deviation of the accuracies over 10 folds within the cross-validation procedure.

**Baseline models:** We compare our U2GAN with up-to-date strong baselines as follows:

- **Unsupervised approaches:** Graphlet Kernel (GK) [Shervashidze et al. (2009)], Weisfeiler-Lehman kernel (WL) [Shervashidze et al. (2011)], Deep Graph Kernel (DGK) [Yanardag & Vishwanathan (2015)] and Anonymous Walk Embedding (AWE) [Ivanov & Burnaev (2018)].

- **Supervised approaches:** PATCHY-SAN (PSCN) [Niepert et al. (2016)], Graph Convolutional Network (GCN) [Kipf & Welling (2017)], Deep Graph CNN (DGCNN) [Zhang et al. (2018b)], Graph Capsule Convolution Neural Network (GCAPS) [Verma & Zhang (2018)], Capsule Graph Neural Network (CapsGNN) [Xinyi & Chen (2019)], Graph Isomorphism Network (GIN) [Xu et al. (2019)], Graph Feature Network (GFN) [Chen et al. (2019)], Invariant-Equivariant Graph Network (IEGN) [Maron et al. (2019b)], Provably Powerful Graph Network (PPGN) [Maron et al. (2019a)] and Discriminative Structural Graph Classification (DSGC) [Seo et al. (2019)].

We report the baseline results taken from the original papers or published in [Ivanov & Burnaev (2018); Verma & Zhang (2018); Xinyi & Chen (2019); Chen et al. (2019)].

5 Experimental Results

Table 2 presents the experimental results on the 11 benchmark datasets. Regarding the social network datasets, our unsupervised U2GAN produces new state-of-the-art performances on COLLAB, IMDB-B, IMDB-M and REDDIT-M5K, especially U2GAN significantly achieves 14+% absolute higher accuracies than all baselines on these 4 datasets. In addition, U2GAN obtains comparable scores in comparison with other unsupervised models on REDDIT-B. These demonstrate a high impact of U2GAN in inferring plausible node and graph embeddings on the social networks.

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3We use the logistic regression classifier from LIBLINEAR with setting termination criterion to 0.001.

4As applied in [Ying et al. (2018)], GraphSAGE [Hamilton et al. (2017a)] obtained low accuracies for the graph classification task, thus we do not include GraphSAGE as a strong supervised baseline.
of general, our U2GAN could consistently obtain better results than those of baselines with any value
average number of neighbors per node is below 5 as shown in Table 1, hence we need to use more
data. A possible reason is that the bioinformatics datasets comprise sparse networks where the
tabular data. It is to note that the social network datasets are much denser than the bioinformatics

Next we investigate the effects of hyper-parameters on the experimental datasets in Figure 3. 
models for the graph classification task.

Regarding the bioinformatics datasets, U2GAN obtains new highest scores on DD, PROTEINS, 
MUTAG, and PTC. Note that there are only 188 graphs in this dataset, which
outperforms all baseline models on DD and PTC by large margins of 15+. It is also to note
that there are no significant differences between our unsupervised U2GAN and some supervised
outliers on MUTAG. Note that there are only 188 graphs in this dataset, which
explains the high variance in the results. Overall, our proposed U2GAN achieves state-of-the-art 
performances on a range of benchmarks against up-to-date supervised and unsupervised 
baseline models for the graph classification task.

Next we investigate the effects of hyper-parameters on the experimental datasets in Figure 3. In

Table 2: Graph classification results (% accuracy) on the experimental benchmarks. “Un-sup.” denotes unsupervised graph embedding models. “Sup.” denotes supervised graph embedding models that use graph class labels when training the models. The best scores are in bold.

<table>
<thead>
<tr>
<th>Model</th>
<th>COLLAB</th>
<th>IMDB-B</th>
<th>IMDB-M</th>
<th>REDDIT-B</th>
<th>REDDIT-M5K</th>
</tr>
</thead>
<tbody>
<tr>
<td>GK 2009</td>
<td>72.84 ± 0.28</td>
<td>65.87 ± 0.98</td>
<td>43.89 ± 0.38</td>
<td>77.34 ± 0.18</td>
<td>41.01 ± 0.17</td>
</tr>
<tr>
<td>WL 2011</td>
<td>79.02 ± 1.77</td>
<td>73.40 ± 4.63</td>
<td>49.33 ± 4.75</td>
<td>81.10 ± 1.90</td>
<td>49.44 ± 2.36</td>
</tr>
<tr>
<td>DGK 2015</td>
<td>73.09 ± 0.25</td>
<td>66.96 ± 0.56</td>
<td>44.55 ± 0.52</td>
<td>78.04 ± 0.39</td>
<td>41.27 ± 0.18</td>
</tr>
<tr>
<td>AWE 2018</td>
<td>73.93 ± 1.94</td>
<td>74.45 ± 5.83</td>
<td>51.54 ± 3.61</td>
<td>87.89 ± 2.53</td>
<td>50.46 ± 1.91</td>
</tr>
<tr>
<td>U2GAN</td>
<td>95.62 ± 0.92</td>
<td>93.50 ± 2.27</td>
<td>74.80 ± 4.11</td>
<td>84.80 ± 1.53</td>
<td>77.25 ± 1.46</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Model</th>
<th>DD</th>
<th>PROTEINS</th>
<th>NCI1</th>
<th>NCI109</th>
<th>MUTAG</th>
<th>PTC</th>
</tr>
</thead>
<tbody>
<tr>
<td>GK 2009</td>
<td>78.45 ± 0.26</td>
<td>71.67 ± 0.55</td>
<td>62.49 ± 0.27</td>
<td>80.32 ± 0.33</td>
<td>81.58 ± 2.11</td>
<td>57.26 ± 1.41</td>
</tr>
<tr>
<td>WL 2011</td>
<td>79.78 ± 0.36</td>
<td>74.68 ± 0.49</td>
<td>82.19 ± 0.18</td>
<td>82.46 ± 0.24</td>
<td>82.05 ± 0.36</td>
<td>57.97 ± 0.49</td>
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<td>DGK 2015</td>
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<td>75.68 ± 0.54</td>
<td>80.31 ± 0.46</td>
<td>62.69 ± 0.23</td>
<td>87.44 ± 2.72</td>
<td>60.08 ± 2.55</td>
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<tr>
<td>AWE 2018</td>
<td>71.51 ± 4.02</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>87.89 ± 7.96</td>
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<tr>
<td>U2GAN</td>
<td>95.67 ± 1.89</td>
<td>78.07 ± 3.36</td>
<td>82.55 ± 2.11</td>
<td>83.33 ± 1.78</td>
<td>81.34 ± 6.56</td>
<td>84.59 ± 5.12</td>
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<td>REDDIT-B</td>
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<td>87.61 ± 2.51</td>
<td>76.02 ± 1.73</td>
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5 More figures can be found in Appendix A.
To qualitatively demonstrate the effectiveness of capturing the local and global graph properties, we use t-SNE [Maaten & Hinton, 2008] to visualize the learned node and graph embeddings on the DD dataset where the node labels are available. It can be seen from Figure 4 that our U2GAN can effectively capture the local structure wherein the nodes are clustered according to the node labels, and the global structure wherein the graph embeddings are well-separated from each other; verifying the plausibility of the learned node and graph embeddings.

6 Conclusion

In this paper, we introduce a novel unsupervised embedding model U2GAN for the graph classification task. Inspired by the universal self-attention network, given an input graph, U2GAN applies a self-attention mechanism followed by a recurrent transition to learn node embeddings and then sums all learned node embeddings to obtain an embedding of the entire graph. We evaluate the performance of U2GAN on 11 well-known benchmark datasets, using the same 10-fold cross-validation scheme to compute the classification accuracies for a fair comparison, against up-to-date unsupervised and supervised baseline models. The experiments show that our U2GAN achieves new highest results on 8 out of 11 datasets and comparable results on the rest. In addition, U2GAN can be seen as a general framework where we can derive effective node and graph embeddings, as we plan to investigate the effectiveness of U2GAN on other important tasks such as node classification and link prediction in the future work. Our code is available at: https://anonymous-url/.
REFERENCES


### Appendix

**Figure 5:** Effects of the number of steps \((T)\). For each dataset, for all 10 folds, we vary the value of either \(T\) or \(N\) while using the same fixed values of other hyper-parameters.
Figure 6: Effects of the number of neighbors (N) sampled for each node. For each dataset, for all 10 folds, we vary the value of either T or N while using the same fixed values of other hyperparameters.