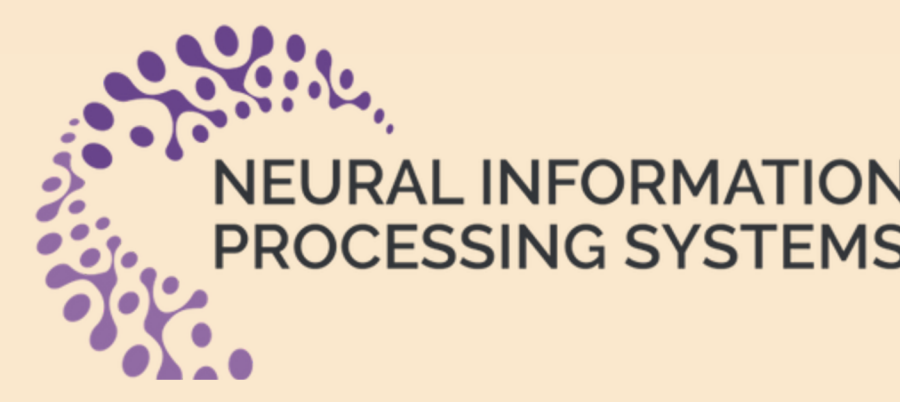


Towards the Identification of Latent Structures in Language Embeddings

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Introduction

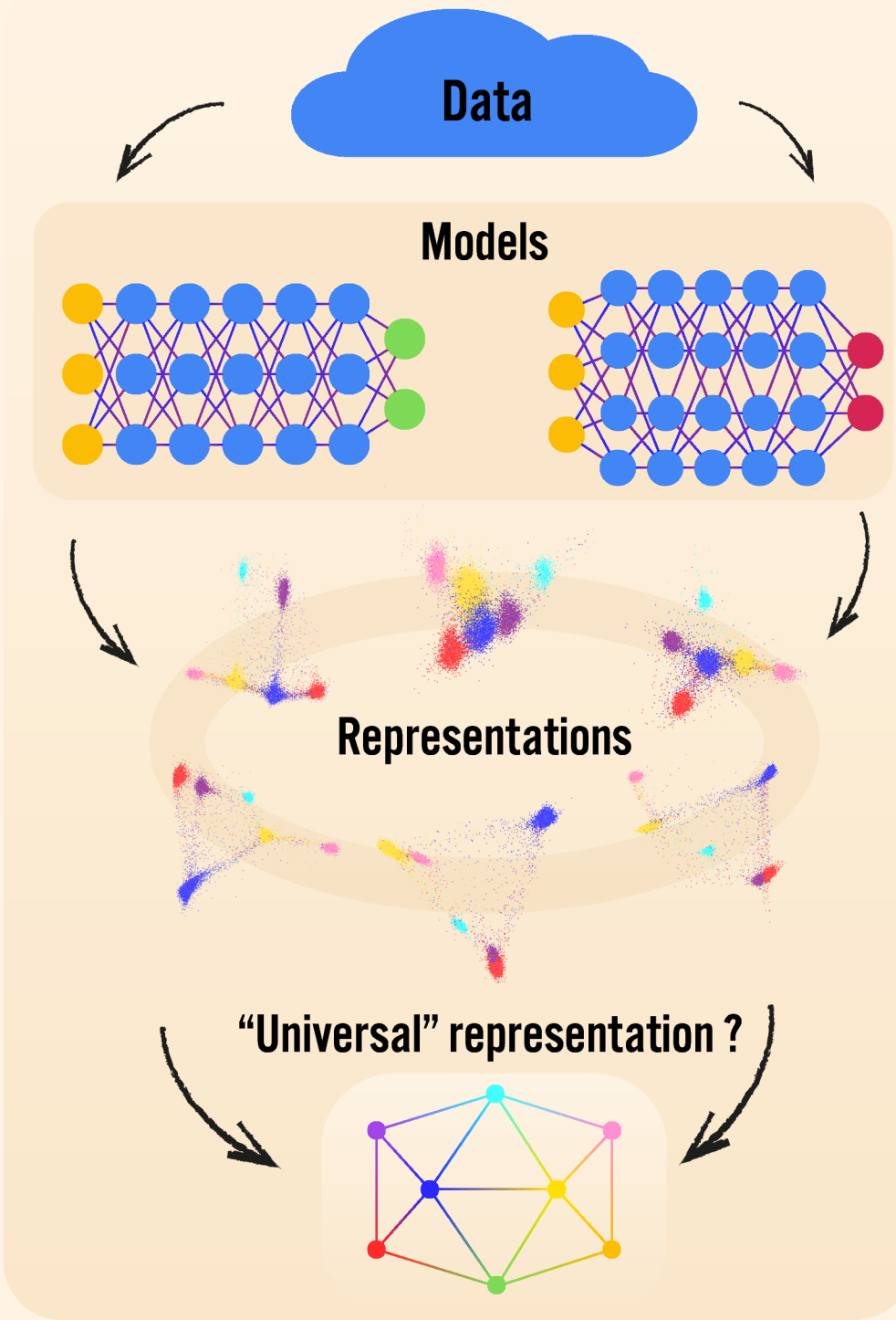
Background: Intrinsic universality in latent representations

Language models often share structural patterns, suggesting the presence of universal regularities in the data.

“Platonic representation hypothesis” (M. Huh et al.)

Aims: Identify the latent structure
Low-dimensional structure inherent in high-dimensional language embeddings.

Approach: CEBRA
A contrastive learning framework, grounded in the theory of nonlinear ICA.



CEBRA

CEBRA: a contrastive learning framework, originally developed for neural data. Ensures Identifiability up to linear transformation, by leveraging auxiliary variables. (e.g., time, labels).

Objective function
generalized InfoNCE loss:

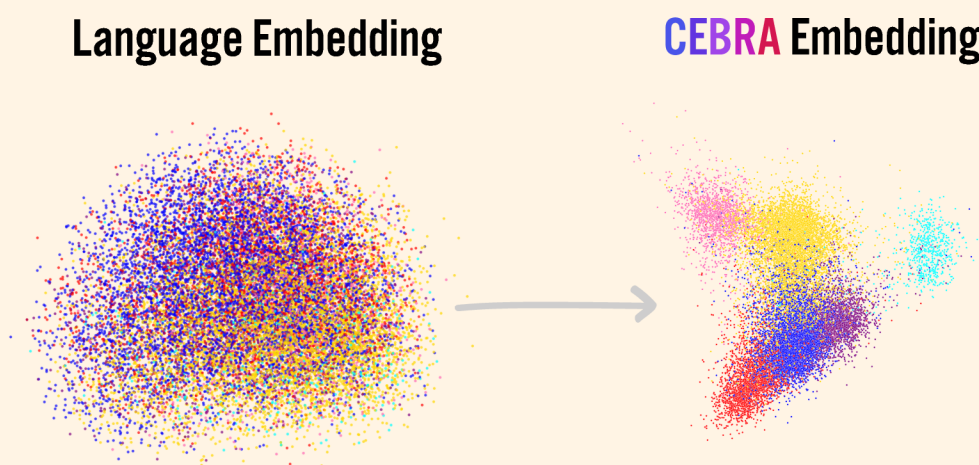
$$\mathcal{L}[\psi]_n = \mathbb{E}_{\substack{\mathbf{x} \sim p_D(\mathbf{x}), \mathbf{y}_+ \sim p(\mathbf{y}|\mathbf{x}) \\ \mathbf{y}_1, \dots, \mathbf{y}_n \sim q(\mathbf{y}|\mathbf{x})}} \left[-\psi(\mathbf{x}, \mathbf{y}_+) + \log \sum_{i=1}^n e^{\psi(\mathbf{x}, \mathbf{y}_i)} \right]$$

Minimizer of generalized InfoNCE loss:

$$\psi^*(\mathbf{x}, \mathbf{y}) = \log \frac{p(\mathbf{y} | \mathbf{x})}{q(\mathbf{y} | \mathbf{x})} + C(\mathbf{x}),$$

The representations match:

$$\mathbf{f}(\mathbf{x}) = \mathbf{L}\tilde{\mathbf{f}}(\mathbf{x})$$

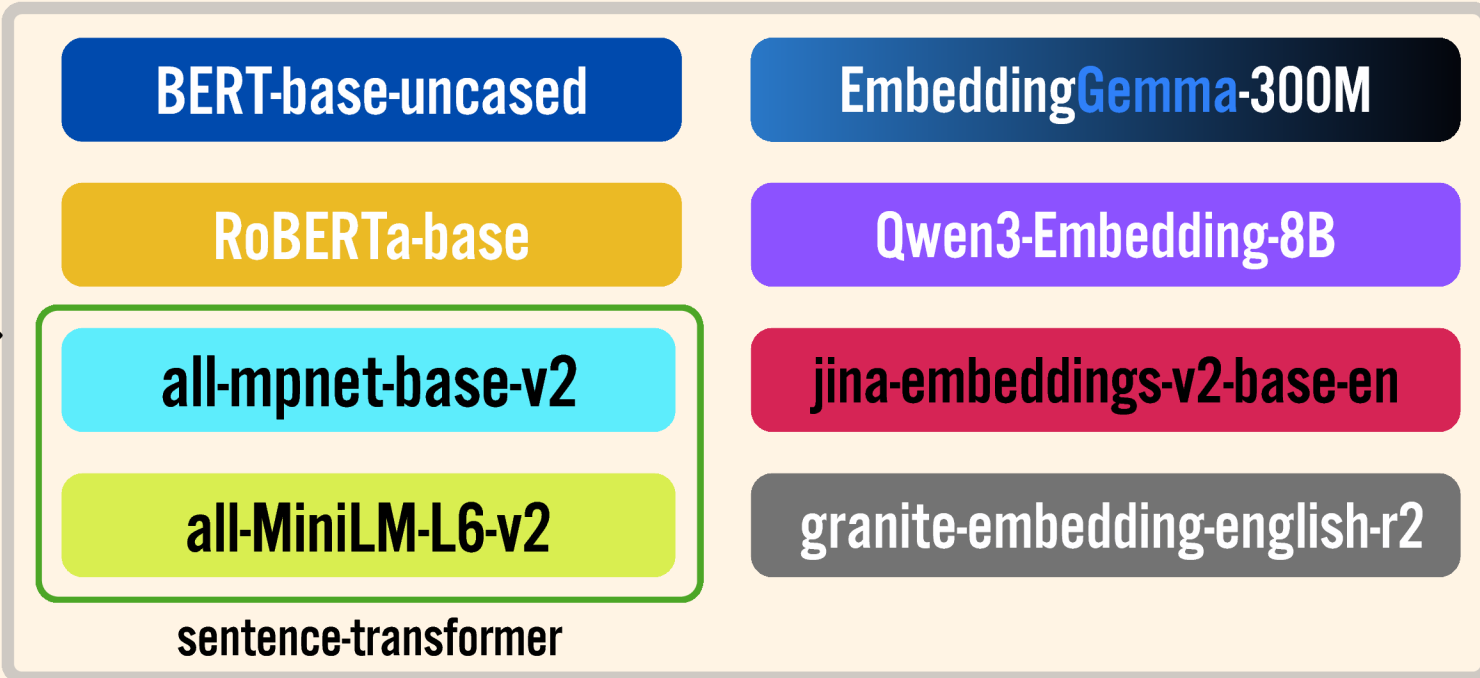


Materials & Methods

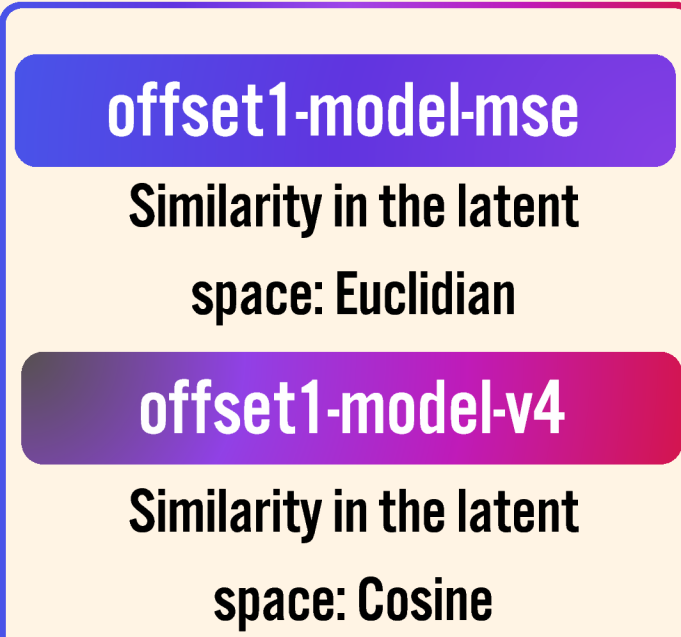
Datasets



Language Embedding Models



CEBRA



Pipeline:

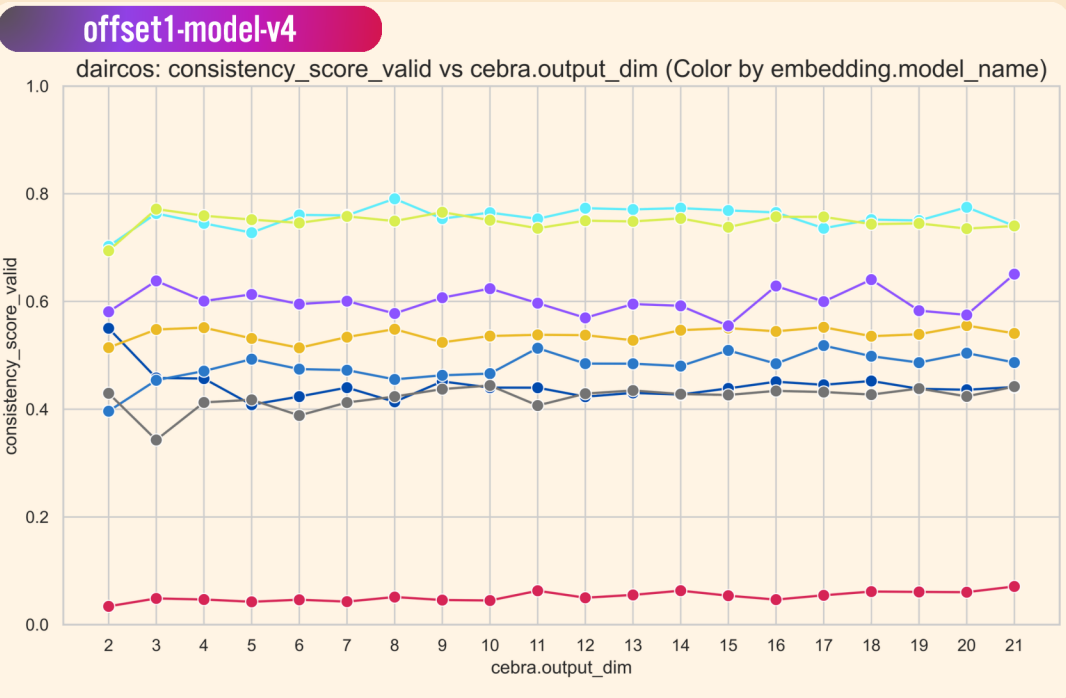
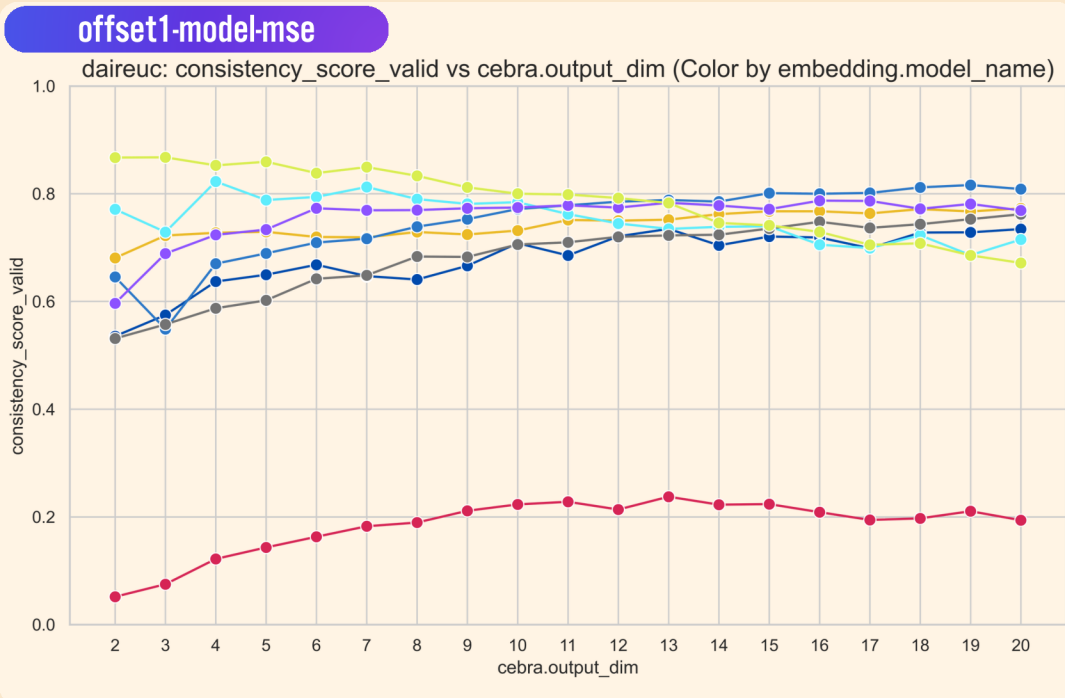
1. Extract high-dimensional embeddings from datasets.
2. Train CEBRA with discrete emotion labels as a AUX.

Evaluation:

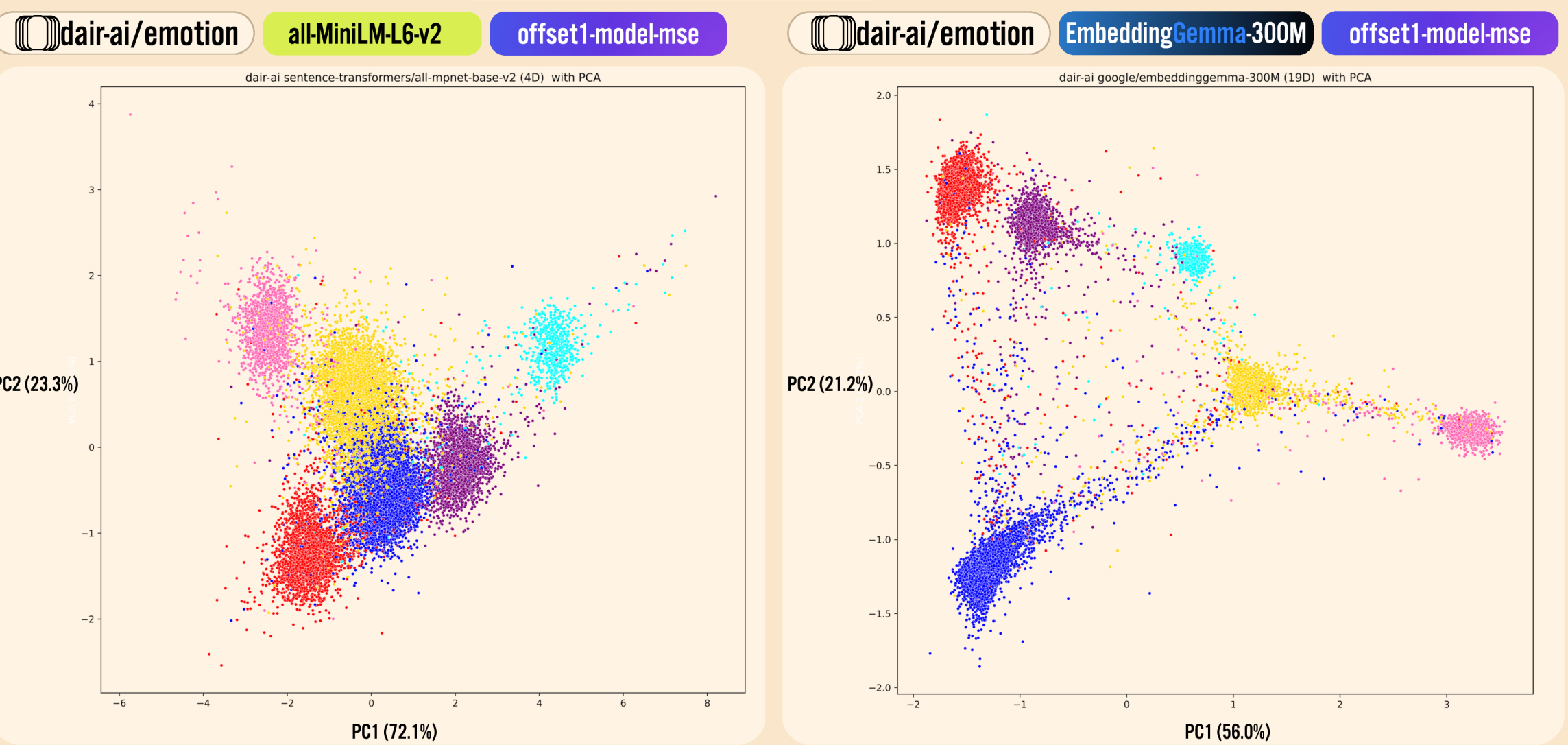
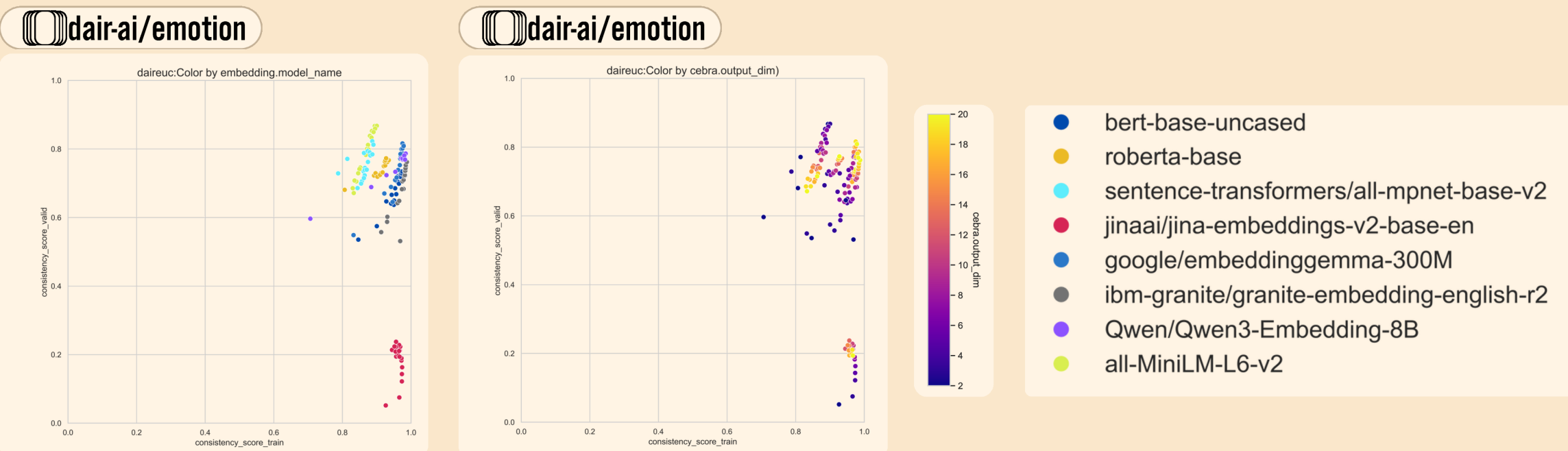
We measure Consistency across 5 random seeds using R^2 scores of linear regressions between learned embeddings.

Results

CEBRA learns low-dimensional latent structures highly consistent across random initializations
Euclidean similarity generally yields higher consistency than cosine similarity as a similarity metric of latent space.



The choice of language embedding model strongly influences the the learned latent structure;
Sentence-Transformer models tend to produce more consistency with low dimensional output.



Discussions

CEBRA reflect stable, label-relevant factors inherent in the data:

CEBRA produces latent embeddings with clear and well-separated cluster structures aligned with the emotion labels.

The arrangement of clusters are highly consistent :

Label-related organization may reflect a stable latent structure associated with the data-generating process.

Choice of auxiliary variables with minimal inductive bias

Can we move beyond explicit labels to achieve identifiability in a more unsupervised manner?

Interpretation of indeterminacy up to a linear transformation:

How can we define robust and meaningful metrics on the relative geometric structure.

Geometrical structure of latent space:

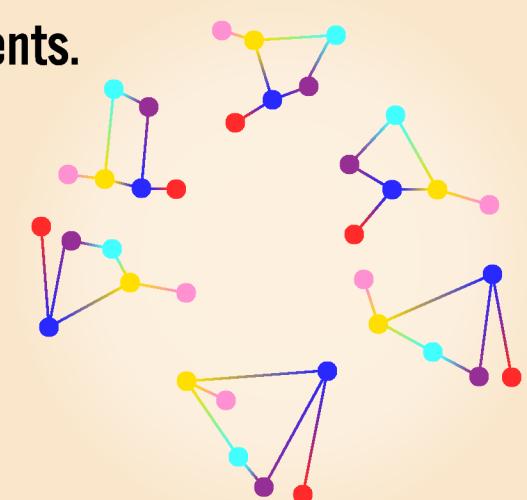
Analyzing distance/similarity patterns and relative geometric arrangements.

Topological structure of latent space:

Examining cluster relationships, connectivity patterns, and manifold-level organization.

Extensions to Multimodal and Neural Domains:

Future work will apply this framework to multimodal data (image,audio) and to neural data, probing whether similar identifiable structures emerge in biological brains.



Acknowledgements

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