



Figure 5: Mode connectivity in the loss landscape when tuning CLIP for image classification. Interactive 3D figures are available in the supplementary material

A 3D VISUALIZATIONS OF CLIP’S LOSS LANDSCAPE

We propose here further visualizations of the mode connectivity between LoRA, RandLoRA and standard fine-tuning. To compute the loss value between the minimas reached by LoRA, RandLoRA and fine-tuning, define a 2D plane using 3 equidistant points representing LoRA, standard fine-tuning and RandLoRA and we then solve for interpolation coefficients $\alpha_{1..3}$ so that their sum equals 1. The weights of the model we evaluate is then $W_0 + \alpha_1 \text{LoRA} + \alpha_2 \text{FT} + \alpha_3 \text{RandLoRA}$. The loss is evaluated on a fixed 5% subset of the training set. Since the process of evaluating the loss at all coordinates on the plane is time consuming, we only perform this study for the CLIP-ViT-B/32 architecture where RandLoRA is especially successful. In all visualizations, the number of trainable parameters for LoRA and RandLoRA are the same. We clamp loss values 20% above the shallowest minima to improve visualization. 3D representation as well as the associated 2D elevation projection is provided in Figure 5. The interactive 3D figures are provided in the HTML format in the supplementary material.

B ADDITIONAL RESULTS

We report here further results on the General Language Understanding Evaluation (GLUE) (Wang et al., 2019) and End-to-end (E2E) (Novikova et al., 2017) generation benchmarks. While GLUE is a text classification task, E2E is a natural language generation task. We also report results comparing RandLoRA and LoRA with a prompt tuning baseline (Zhang et al., 2024b) for classification using CLIP’s vision backbone as in section 5.2 in appendix B.3

B.1 GLUE RESULTS

We report results for RandLoRA and compare with LoRA and VeRA on the SST-2, MRPC, COLA, QNLI, RTE and STS-N tasks. We report Matthew’s correlation for CoLA, Pearson correlation for STS-B, and accuracy for the remaining tasks. We report results using the RoBERTa network Liu et al. (2019) in the base and large configurations and perform 5 runs to report average performance and one standard deviation. Results are displayed in Table 5. We find that for the smaller RoBERTa-base architecture (125M parameters), all algorithms reach the same performance. For the larger RoBERTa-large variant (355M parameters), a larger gap is observed where RandLoRA improves over the performance of VeRA and LoRA. These findings are in line with the experiments in the main body of the paper where we find that RandLoRA provided larger improvements for larger models in Figure 3.

B.2 E2E RESULTS

We train RandLoRA and LoRA on the E2E dataset using the GPT-2 medium architecture (Radford et al., 2019) (355M parameters).

Table 5: Results on GLUE datasets with the RoBERTa-base and RoBERTa-large models.

RoBERTa-base								
Method	Params	SST-2	MRPC	COLA	QNLI	RTE	STS-N	Average
VeRA-1024	0.26M	95.8 \pm 0.3	89.3 \pm 1.2	65.3 \pm 1.1	94.1 \pm 0.3	81.6 \pm 0.8	91.8 \pm 0.1	86.3 \pm 0.3
LoRA-4	0.7M	94.4 \pm 0.5	87.3 \pm 0.2	58.4 \pm 0.8	92.7 \pm 0.2	71.5 \pm 1.2	90.5 \pm 0.1	82.4 \pm 0.3
RandLoRA-64	0.7M	92.2 \pm 0.3	88.0 \pm 1.5	59.4 \pm 2.1	91.3 \pm 0.4	74.7 \pm 1.9	90.3 \pm 0.2	82.6 \pm 0.5
RoBERTa-large								
VeRA-256	0.26M	95.8 \pm 0.3	89.3 \pm 1.2	65.3 \pm 1.1	94.1 \pm 0.3	81.6 \pm 0.8	91.8 \pm 0.1	86.3 \pm 0.3
LoRA-4	1.8M	95.5 \pm 0.2	87.2 \pm 0.7	64.7 \pm 1.2	94.5 \pm 0.1	83.6 \pm 0.4	91.8 \pm 0.1	86.2 \pm 0.3
RandLoRA-100	1.8M	95.5 \pm 0.3	90.1 \pm 0.4	67.4 \pm 0.3	94.1 \pm 0.3	84.5 \pm 0.3	91.4 \pm 0.6	87.2 \pm 0.1

B.3 COMPARISON WITH PROMPT-TUNING

Prompt tuning is a popular alternative to PEFT where learnable tokens are appended to human-designed prompts and optimized on to improve accuracy. We choose to report the Maple Khattak et al. (2023a) + DePT Zhang et al. (2024b) state-of-the-art configuration as it is shown in Zhang et al. (2024b) to be a highly competitive configuration for image classification. Table 6 reports the results for 4 and 16 shots over the 11 datasets used in Zhang et al. (2024b). We train on ViT-B/32 with all algorithms training approximately 3M parameters. We report that although competitive for low shots, prompt tuning struggles to keep up in the 16-shot setting. We note in particular that prompt tuning struggles on datasets that require more adaptation (e.g. FGVCaircraft) whereas LoRA and RandLoRA in particular manage to more largely improve results. We additionally report that Maple + DePT requires a much longer training time and VRAM usage. For example, 16-shots on ImageNet requires 3.5h and 18GB of VRAM for Maple + DePT while it requires 2 minutes and 4.5GB of VRAM for RandLoRA. Because prompt tuning is largely orthogonal to LoRA-type weight updates we suggest that future research should study how to combine these approaches together.

Table 6: Comparison of LoRA and RandLoRA with a state-of-the-art prompt tuning algorithm. CLIP ViT-B/32.

Shots	Method	ImageNet	Caltech101	OxfordIIITPet	Cars	Flowers102	Food101	FGVCaircraft	SUN397	DTD	EuroSAT	UCF101	Average
4	LoRA-16	64.9	92.0	88.2	63.9	87.9	82.6	30.3	68.2	61.1	89.4	74.7	73.0
	RandLoRA-10	63.9	91.7	86.4	67.0	89.9	80.8	34.0	69.7	62.4	84.4	74.9	73.2
	Maple + DePT	62.1	95.0	89.5	68.7	90.5	79.6	28.3	70.2	61.7	81.4	76.6	73.1
16	LoRA-16	65.8	91.7	89.5	80.1	94.9	81.8	42.5	73.5	72.0	91.2	81.5	78.6
	RandLoRA-10	66.3	95.6	91.1	77.4	94.5	84.0	45.0	73.7	72.5	94.1	81.7	79.6
	Maple + DePT	67.7	96.0	90.5	79.1	96.3	81.7	36.9	74.5	70.3	90.3	82.1	78.7

C IMPLEMENTATION DETAILS

C.1 CLASSIFICATION DATASETS

We fine-tune vision architectures on 22 vision datasets (21 for pure vision backbones where ImageNet is removed for brevity). We train for 10 epochs on the few-shot experiments and increase the number of epochs according to dataset constraints for 50% and 100% fine-tuning. Table 7 reports details of the 22 datasets we use as well as the number of epochs used as in (Zhang et al., 2024a).

Table 7: Vision datasets used for the image classification experiments

#	Datasets	Classes	Splits			Epochs
			<i>train</i>	<i>val</i>	<i>test</i>	
(1)	Cars	196	7,330	814	8,041	35
(2)	DTD	47	3,384	376	1,880	76
(3)	EuroSAT	10	21,600	2,700	2,700	12
(4)	GTSRB	43	23,976	2,664	12,630	11
(5)	MNIST	10	55,000	5,000	10,000	5
(6)	RESISC45	45	17,010	1,890	6,300	15
(7)	SUN397	397	17,865	1,985	19,850	14
(8)	SVHN	10	68,257	5,000	26,032	4
(9)	CIFAR10	10	45,000	5,000	10,000	5
(10)	CIFAR100	100	45,000	5,000	10,000	6
(11)	ImageNet	1,000	1,276,167	5,000	50,000	10
(12)	STL10	10	4,500	500	8,000	4
(13)	Food101	101	70,750	5,000	25,250	15
(14)	Caltech101	101	6,941	694	1,736	10
(15)	Caltech256	257	22,037	2,448	6,122	8
(16)	FGVCAircraft	100	3,334	3,333	3,333	60
(17)	Flowers102	102	1,020	1,020	6,149	40
(18)	OxfordIIITPet	37	3,312	368	3,669	5
(19)	CUB200	200	5,395	599	5,794	20
(20)	PascalVOC	20	7,844	7,818	14,976	10
(21)	Country211	211	31,650	10,550	21,100	15
(22)	UCF101	101	7,639	1,898	3,783	20

C.2 CLIP

We utilize the pytorch AdamW optimizer with weight decay 0.1 and a cosine decaying learning rate schedule. To accommodate the full batch size on a single A100 GPU for the ViT-L/14 and ViT-H/14 CLIP architectures, we accumulate 2 batches of 64. This is excepted for the standard fine-tuning of the ViT-H/14 for standard fine-tuning where we need to accumulate 4 batches of 32 due to increasing memory costs. We acquire the pretrained weights from the openclip repository (Cherti et al., 2023) where the use the "openai" weights from ViT-B/32 and ViT-L/14 and the "laion2b_s32b_b79k" weights for ViT-H/14.

C.3 PURE VISION BACKBONES

For pure vision backbones, we use the same configuration as vision and language fine-tuning of CLIP except that we increase the learning rate to 10^{-2} for LoRA and RandLoRA. We train RandLoRA-6 for ViT-B/32 and RandLoRA-8 for Dinov2’s ViT-B/14 and CLIP’s ViT-L/14.

Table 8: Hyper-parameters for different algorithms. Multiple values for hyperparameters denote variances across the ViT-B/32, ViT-L/14 and ViT-H/14 architectures respectively.

Algorithm	FT	LoRA	NoLA	VeRA	RandLoRA
Batch size	128/64/32			128/64/64	
Learning Rate (LR)	1e-5	1e-3	1e-3	1e-2	1e-3
Scaling coefficient	1	$\frac{1}{r}$	$\frac{1}{r}$	$\frac{1}{r}$	$\frac{10}{r}$
Basis rank (r)	—	32	1	256/256/1024	6/8/10
Number of basis (n)	—	—	1024	1	128

C.4 COMMONSENSE REASONING

Our evaluation protocol assesses the model’s versatility and reasoning capabilities across eight diverse datasets: BoolQ (Clark et al., 2019) (yes/no question answering), PIQA (Bisk et al., 2020) (physics commonsense questions), SIQA (Sap et al., 2019) (social implications reasoning), HellaSwag (Zellers et al., 2019) (multi-choice scenario completion), WinoGrande (Sakaguchi et al., 2021) (binary sentence completion), ARC-c and ARC-e (Clark et al., 2018) (challenging and easy science questions at a grade-school level), and OBQA (Mihaylov et al., 2018) (multi-step reasoning). These datasets collectively pose a wide range of challenges, from natural language understanding

Table 9: LLM fine-tuning hyper-parameters for different algorithms. Multiple values for hyper-parameters denote variances across the Qwen2 -0.5b, Phi3-8b and LLama3-8b architectures respectively.

Algorithm	LoRA	NoLA	VeRA	RandLoRA
Batch size			16/8/4	
Learning Rate (LR)			10^{-4}	
Scaling coefficient	2	$\frac{2}{\sqrt{n}}$	2	$\frac{2}{\sqrt{n}}$
Basis rank (r)	32	1	256/1024/1024	6/10/15
Number of basis (n)	–	1024	1	149/153/136

and commonsense reasoning to physical and social inference. For further details on these datasets, we refer readers to the survey by Hu et al. (Hu et al., 2023). We train using the huggingface² transformers library and follow the implementation³ of Liu et al (Liu et al., 2024). We train for 3 epochs using a learning rate of 1×10^{-4} and a base scaling coefficient of 2 for the weight update. To prevent overfitting, we add a dropout layer in each of the adapter’s layers with a dropout probability of 0.05 and perform early stopping using the same validation set of size 120, drawn from the training set. We maintain hyper-parameters the same across architectures and algorithms except for the scaling ratio of the weight update for NoLA and RandLoRA which we further multiply by $1/\sqrt{n}$ where n is the number of bases to account for the increasing norm of the sum of random matrices.

C.5 TRAINING TIME, MEMORY CONSUMPTION AND RANDOM BASES

C.5.1 REDUCING MEMORY CONSUMPTION

Basis sharing across layers RandLoRA aims to preserve the memory efficiency and training speed advantages of LoRA. As shown in Section 4, although RandLoRA trains an amount of parameters comparable to LoRA we still have to store N large random bases for each weight update. We first note that as observed in previous research, (Koohpayegani et al., 2024; Kopiczko et al., 2024) random bases can be shared across layers. In practice, we generate one pair of random matrices $B_i \in \mathbb{R}^{N \times D_m \times r}$ and $A_0 \in \mathbb{R}^{r \times d_m}$, where D_m and d_m represent the largest D and d across all network layers. During forward and backward passes on a layer of size $D \times d$, we select the first D rows of B and d columns of A to perform the weight update. This strategy stores only the largest B and A matrices, which would have to be fit in memory at some point during training anyways. Note that although we do not study this case, this strategy directly generalizes to having different ranks r across layers as has been proposed in AutoLoRA (Zhang et al., 2024c) for example. This strategy allows us to avoid increasing memory as network depth increases, meaning that RandLoRA become more efficient when network depth increases.

Efficient back-propagation with a single random A basis We evidence in section 4.2 that the A_i matrices do not need to be N dimensional and that a single A matrix modified by $N \Gamma_i$ is enough to achieve full rank. We can thus optimize the backward pass when computing the gradient of Λ_i and Γ_i so that we only have to store one matrix $A \in \mathbb{R}^{r \times d}$ for the backward pass, further reducing memory consumption.

Efficient matrix multiplication in the forward pass We adopt the notations from Section C.5.1 to optimize the matrix multiplication of $X \in \mathbb{R}^{B \times D}$ during the forward and backward passes: XW . Given the pre-trained weight $W_0 \in \mathbb{D} \times$, LoRA computes $Y = XW_0 + XBA$ where we compute $Y = XW_0 + \sum_{i=1}^N (XB_i)(\Lambda_i A_i \Gamma_i)$. These equations suggest RandLoRA would be N times slower to run than LoRA but in practice, the XW_0 operation dominates the matmul time and the N of RandLoRA operations are naturally parallelized by the CUDA kernel. In practice we observe a 13% training time increase for the smaller ViT-B-32 models and up to 100% in the worst case for larger models with large weight matrices such as LLama3.

²<https://huggingface.co>

³https://github.com/NVlabs/DoRA/tree/main/commonsense_reasoning

C.6 SPARSE RANDOM BASES

We continue here the discussion on the possible collinearity of sparse bases. We remind here that we construct the random bases B_i and A_i by assigning

$$\begin{cases} -1, & \text{with probability } \frac{1}{s} \\ 0, & \text{with probability } 1 - \frac{2}{s} \\ 1, & \text{with probability } \frac{1}{s} \end{cases}$$

where s an integer in $[2, \sqrt{D}]$ for $W \in \mathbb{R}^{D \times d}$. Because of the ternary nature of these matrices, there is a non-zero probability that two row are collinear across all random matrices, resulting in non full rank. If we can show that is probability is negligible then the full rank constraint will be preserved in practice. We compute that the probability of drawing the same size d row twice equates to $p = 2 \times \left(\frac{s^2 - 4s + 6}{s^2}\right)^d$. Taking the example of the ViT-B/32 architectures with $W \in \mathbb{R}^{768 \times 768}$ and for the largest recommended optimal sparsity ($s = \sqrt{768}$) we compute $p = 2 \times 10^{-49}$. The probability of drawing at least two collinear row over N matrices of is $p_2 = (N+D)(N+D-1)p$. In the RandLoRA-6 configuration for ViT-B, $N = 128$ resulting in $p_2 = 8 \times 10^{-44}$ meaning these events are negligible in practice even with a large number of sparse bases and that the full rank constraint is preserved.

C.6.1 TRAINING TIME

We report in Table 10 the relative training time of RandLoRA compared to LoRA and standard fine-tuning on a single RTX4090 GPU (A100 for LLama3 and ViT-H/14). Since we do not have ressources to fully fine-tune LLama3, we report LoRA as the memory baseline. In addition to Table 10 we report up to 212% increase over LoRA-64 training time for the best performing RandLoRA-15 configuration for LLama3-8b. This number should be put in perspective with DoRA leading to a 220% increase in all configurations for LLama3-8b.

Model	Architecture	LoRA-32	DoRA-32	RandLoRA	FT
CLIP-ViT-B/32	Training Time	90	–	113	100%
	Memory	81	–	78	100%
CLIP-ViT-L/14	Training Time	95	–	128	100%
	Memory	72	–	71	100%
CLIP-ViT-H/14	Training Time	96	–	122	100%
	Memory	54	–	51	100%
LLama3-8B	Training Time	100	220	167	–
	Memory	100	102	102	–

Table 10: Comparison of training times for LoRA, RandLoRA, and FT on vision-language or language architectures.

D MATHEMATICAL DERIVATIONS AND PROOFS

D.1 THEOREM 4.1

In this section we would like to give the details of the proof of theorem 4.1 from the main paper. In order to do so we will start by proving a few lemmas.

Our method consider decompositions similar to those given in equation 1 and equation 2 that are built from random matrices instead of the left and right singular vectors. A key observation is that such decompositions and their sums will yield high rank matrix approximations. The following two lemmas explains why this is the case.

Lemma D.1. Let $B = [B_1, \dots, B_n]$ denote a matrix where each $B_j \in \mathbb{R}^{D \times r}$ and let $A = [A_1, \dots, A_n]$ denote a matrix where each $A_j \in \mathbb{R}^{d \times r}$. Assume $nr \leq \min(D, d)$ and assume that the columns of B are linearly independent and the columns of A are linearly independent. Define

$$C = \sum_{j=1}^n B_j A_j^T \quad (9)$$

Then we must have that $\text{rank}(C) = nr$.

Proof. We first observe that using the inequality $\text{rank}(X + Y) \leq \text{rank}(X) + \text{rank}(Y)$ we get that $\text{rank}(C) \leq nr$ because each term $B_j A_j^T$ has rank r , since the columns of A and B are linearly independent, and there are n of them.

Then observe that we can rewrite C as

$$C = B A^T \quad (10)$$

Using Sylvester's rank inequality: If $X \in \mathbb{R}^{D \times l}$ and $Y \in \mathbb{R}^{l \times d}$ then

$$\text{rank}(X) + \text{rank}(Y) - l \leq \text{rank}(XY) \quad (11)$$

we have that

$$\text{rank}(C) = \text{rank}(B A^T) \quad (12)$$

$$\geq \text{rank}(B) + \text{rank}(A^T) - kj \quad (13)$$

$$= 2nr - nr \quad (14)$$

$$= nr \quad (15)$$

and the proof is complete. \square

Lemma D.2. Let $\{X_1, \dots, X_n\}$ denote n vectors in \mathbb{R}^N where $n \leq N$ drawn i.i.d from a Gaussian or uniform distribution. Then with probability 1 $\{X_1, \dots, X_n\}$ will be linearly independent.

Proof. We first note that any measure defined via a Gaussian or Uniform probability distribution is absolutely continuous with respect to the Lebesgue measure. Meaning they have the same sets of measure zero as the Lebesgue measure.

We then prove the case that $\{X_1, \dots, X_n\}$ are vectors of unit length. Since the vectors were drawn independently, we can first assume we drew X_1 . The probability that this is the zero vector is 0 w.r.t the Lebesgue measure on the closed unit ball $B_N(0)$ about the origin in \mathbb{R}^N and hence any other measure absolutely continuous to it. Then draw X_2 and note that the probability that X_2 lies in $\text{span}\{X_1\} \cap B_N(0)$ is also 0 since $\text{span}\{X_1\} \cap B_N(0)$ forms a set of 0 Lebesgue measure in $B_N(0)$. Continuing in this way we find that $\{X_1, \dots, X_n\}$ will be linearly independent with probability 1.

For the general case where $\{X_1, \dots, X_n\}$ are not drawn to have unit length i.e. drawn on the sphere in \mathbb{R}^N , we simply note that we can draw each one and then divide by its norm producing one of unit length. Since normalizing by the norm doesn't affect linear independence we get by the above case that $\{X_1, \dots, X_n\}$ must be linearly independent with probability 1. \square

Lemmas D.1 and D.2 show that if we were to i.i.d draw n random vectors A_1, \dots, A_n in \mathbb{R}^D and n vectors B_1, \dots, B_n using a Gaussian or uniform distribution for $n \leq \min(D, d)$. Then the matrix $Q = A B^T$ would have rank n , where $A = [A_1, \dots, A_n]$ and $B = [B_1, \dots, B_n]$.

We note that lemma D.1 is still true if we were to consider products of the form $B \Lambda A \Gamma$, where Λ and Γ are diagonal matrices with non-zero diagonal entries.

Using the above two lemmas we can now give a proof of theorem 4.1 from the main paper.

Proof. The fact that each $B_i \Lambda_i A_i \Gamma_i$ has rank r with probability 1 follows from lemmas D.1 and D.2. In order to estimate the difference $\|W - \sum_{j=1}^n B_j \Lambda_j A_j \Gamma_j\|$, we use equation 2 to write

$$W = \sum_{j=1}^n U_j \Sigma_j V_j^T. \quad (16)$$

We can then estimate

$$\|W - \sum_{j=1}^n B_j \Lambda_j A_j \Gamma_j\|_F = \|\sum_{j=1}^n U_j \Sigma_j V_j^T - \sum_{j=1}^n B_j \Lambda_j A_j \Gamma_j\|_F \quad (17)$$

$$= \|\sum_{j=1}^n U_j \Sigma_j V_j^T - B_j \Lambda_j A_j \Gamma_j\|_F \quad (18)$$

$$\leq \sum_{j=1}^n \|U_j \Sigma_j V_j^T - B_j \Lambda_j A_j \Gamma_j\|_F \quad (19)$$

$$\leq n \cdot \epsilon \quad (20)$$

where the last inequality follows from the assumption equation 6. \square

D.2 LoRA’S LOW BOUND

We demonstrate here the short derivation leading to the results of equation equation 8.

Proof. By definition, the forbenius norm of a matrix $X \in \mathbb{R}^{n \times n}$, $\|X\|_F$ is invariant under left and right multiplications by any orthogonal matrices $P \in \mathbb{R}^{n \times n}$ and $Q \in \mathbb{R}^{n \times n}$, i.e. $\|X\|_F = \|PXQ\|_F$. Then, given the k-truncated SVD of $M = U \Sigma_k V^T$ with $U, V \in \mathbb{R}^{n \times n}$ and $\Sigma_k \in \mathbb{R}^{n \times n}$ diagonal with elements above the k -th being 0, U and V are orthogonal matrices by definition. We then have the following,

$$\|X - M\|_F = \|U(X - M)V^T\|_F \quad (21)$$

$$= \|\Sigma - \Sigma_k\|_F \quad (22)$$

$$= \sum_{j=k+1}^r \sigma_j^2 \quad (23)$$

where $\Sigma \in \mathbb{R}^{n \times n}$ is diagonal and contains the n singular values of X by decreasing order and σ_j denotes the j -th element of Σ .

Since by the SVD definition, the best rank- k approximation of W is M , given LoRA’s rank- k approximation of W by the matrix multiplication BA where $B \in \mathbb{R}^{n \times k}$ and $A \in \mathbb{R}^{k \times n}$ we have

$$\|X - M\|_F \leq \|X - BA\|_F \quad (24)$$

$$\sum_{j=k+1}^r \sigma_j^2 \leq \|X - BA\|_F. \quad (25)$$

\square

E DETAILED RESULTS

E.1 VISION LANGUAGE: CLIP

We report per dataset accuracies for NoLA, VeRA, LoRA, standard fine-tuning (FT) and RandLoRA in for the CLIP ViT-B/32 ViT-L/14 and ViT-H/14 architectures on 22 datasets in Tables 11, 12 and 13 respectively.

E.2 VISION ONLY: DINO V2

Table 14 reports detailed results when fine-tuning DinoV2 on 21 datasets. We use the pretrained ViT-B/14 architecture and train a linear classifier together with the feature extractor. Compared to the CLIP results ImageNet was removed to promote brevity of the experiments.

E.3 COMMONSENSE REASONING

Table 15 reports detailed accuracy results for the Qwen2, Phi3 and LLama3 language models trained on the commonsense tasks. See C.4 for details on the datasets and the hyper-parameters used.

Table 11: Detailed accuracy results per dataset, fine-tuning the vision and language backbones of CLIP-ViT-B/32. Highest performance and those within a range of 0.1 in each section are highlighted in bold.

Method		Cars	DTD	EuroSAT	GTSRB	MNIST	RESISC45	SUN397	SVHN	CIFAR10	CIFAR100	ImageNet	STL10	Food101	Caltech256	FGVC Aircraft	Flowers102	OxfordIIITPet	CUB200	PascalVOC	Country211	Caltech101	UCF101	Average
1 shot	NoLA	51.6	44.5	72.8	54.3	76.3	64.1	53.8	31.1	81.3	62.7	49.7	90.4	61.9	76.6	19.0	62.5	69.7	41.8	69.1	5.3	84.9	61.4	58.4
	VeRA256	60.9	47.7	76.8	47.4	71.7	67.4	64.9	47.5	90.4	71.7	63.7	97.4	83.5	83.3	22.1	68.5	88.3	54.4	77.6	17.6	87.5	64.9	66.1
	LoRA32	51.9	46.3	73.2	61.4	73.7	67.9	53.9	30.6	79.8	63.9	51.7	89.5	63.5	78.1	19.1	65.3	69.9	43.0	67.1	5.6	85.2	63.5	59.3
	RandLoRA6	53.6	50.3	73.1	61.4	78.5	72.6	59.3	29.4	80.8	67.1	57.4	92.6	69.8	81.5	21.7	71.3	75.0	48.5	67.6	8.5	88.3	67.0	62.5
	FT	51.4	46.8	67.3	62.8	77.4	69.9	57.2	20.0	68.3	61.1	52.2	83.0	66.7	79.5	19.0	68.7	70.0	46.5	59.0	7.4	86.1	66.6	58.5
2 shots	NoLA	57.1	54.3	82.8	63.6	83.2	69.7	57.9	32.2	80.3	68.5	51.0	92.2	67.2	80.4	24.3	72.7	80.8	47.3	57.9	7.4	85.2	65.4	62.8
	VeRA256	62.1	49.5	71.0	50.5	72.2	68.1	64.8	50.7	91.7	73.1	63.7	97.5	84.2	84.0	22.1	69.9	89.2	54.8	73.8	17.7	89.2	65.0	66.6
	LoRA32	53.7	56.9	82.0	62.6	82.8	71.9	60.1	36.8	84.2	71.5	52.9	94.1	73.6	82.8	22.4	73.8	84.2	48.0	61.7	9.0	87.8	67.4	64.6
	RandLoRA6	59.5	60.4	83.4	73.7	85.2	74.9	62.0	30.0	82.6	72.0	57.7	94.5	72.0	83.8	28.6	80.8	83.7	54.3	62.3	9.8	89.0	71.7	66.9
	FT	58.5	57.7	82.9	76.7	84.8	74.4	60.3	23.0	69.4	68.3	53.9	87.3	69.1	83.0	26.2	81.0	79.1	55.2	53.2	9.3	89.2	71.6	64.3
4 shots	NoLA	60.1	58.1	86.9	67.7	87.5	75.0	61.0	45.3	87.2	69.3	51.4	91.3	72.3	81.2	26.0	80.7	84.1	51.6	69.0	9.3	87.3	68.0	66.8
	VeRA256	61.8	49.6	79.7	52.5	73.2	69.6	64.9	52.2	92.3	73.9	64.2	97.5	84.9	83.8	21.9	70.4	89.5	54.9	75.8	17.8	89.4	65.6	67.5
	LoRA32	57.0	60.4	86.7	59.0	86.5	73.5	62.3	46.4	87.1	71.1	52.5	93.6	76.3	83.2	24.2	77.2	84.7	50.9	69.5	11.2	88.4	67.1	66.8
	RandLoRA6	63.1	63.2	87.9	77.4	88.2	80.3	65.0	47.8	87.6	72.9	55.8	93.2	74.8	84.1	31.1	87.8	85.0	58.8	70.3	10.7	89.8	75.3	70.4
	FT	65.2	60.3	85.4	82.5	87.0	80.1	64.1	41.1	78.9	70.8	54.0	84.3	72.0	83.2	34.1	89.5	80.1	60.1	62.5	10.0	89.6	73.8	68.6
16 shots	NoLA	66.2	66.5	92.3	73.6	91.2	81.2	64.4	74.9	92.1	74.3	54.0	95.0	77.3	84.0	30.4	86.0	89.6	61.1	73.5	12.0	88.2	73.7	72.8
	VeRA256	62.9	51.4	82.4	53.2	75.8	70.5	66.3	57.0	93.3	73.9	64.6	97.9	85.2	85.6	22.3	71.6	90.9	55.8	76.4	18.1	89.2	65.7	68.6
	LoRA32	69.6	64.8	87.5	61.2	91.2	79.8	65.0	71.6	93.0	75.7	54.9	95.8	77.3	85.8	33.7	83.3	89.6	64.4	75.2	12.1	88.5	76.3	72.6
	RandLoRA6	71.9	70.2	94.2	81.5	94.1	84.9	67.6	73.7	92.0	77.0	56.8	95.0	80.1	86.9	35.1	91.3	89.3	68.6	75.5	12.2	90.9	79.3	75.8
	FT	74.0	69.8	93.2	87.5	94.3	86.7	67.2	74.1	89.8	76.3	56.2	92.7	78.6	86.9	39.1	93.2	89.0	70.1	74.9	12.1	90.9	78.9	76.2
50%	NoLA	69.7	68.9	98.6	93.9	98.7	91.6	64.9	93.0	97.1	79.0	56.9	97.8	81.0	86.3	44.2	81.9	89.6	62.3	85.6	14.4	88.9	78.0	78.3
	VeRA256	63.7	62.4	95.5	79.2	92.8	81.1	66.3	75.6	95.2	76.3	64.6	97.9	85.6	87.9	25.6	72.1	88.8	56.6	85.4	18.1	93.3	70.7	74.3
	LoRA32	71.9	71.3	98.4	94.7	98.8	93.0	65.6	93.7	97.4	81.5	59.5	97.7	85.4	88.1	45.3	85.8	89.2	65.2	86.5	14.1	88.5	80.2	79.6
	RandLoRA6	78.0	73.6	98.5	95.5	99.0	94.0	67.4	94.6	97.7	84.4	62.4	97.9	87.6	89.5	56.3	88.5	90.0	70.3	86.5	14.6	95.3	82.5	82.0
	FT	78.0	72.4	98.7	96.2	99.1	94.5	67.0	95.0	97.6	84.8	62.1	98.0	86.6	89.2	57.4	89.1	91.1	69.0	87.2	14.6	94.9	81.8	82.0
100%	NoLA	73.6	73.5	98.8	95.2	99.0	93.3	66.4	94.2	97.6	80.3	57.5	98.1	82.0	87.5	51.1	89.1	90.8	67.1	86.5	15.9	90.1	78.4	80.3
	VeRA256	63.7	62.5	95.2	79.5	92.2	80.6	66.3	75.4	95.2	76.2	64.6	98.1	85.6	87.8	25.4	77.3	90.6	56.8	85.9	18.1	93.8	70.3	74.6
	LoRA32	77.3	76.7	98.6	95.3	99.1	94.4	67.1	95.2	97.9	83.8	60.5	98.4	87.8	89.2	59.5	91.4	91.1	70.7	87.7	15.9	89.6	82.0	82.2
	RandLoRA6	83.1	78.9	99.0	96.1	99.3	95.4	69.5	95.5	98.1	87.0	63.8	98.4	89.4	90.9	67.1	93.7	91.0	75.2	88.0	16.8	95.6	85.1	84.4
	FT	84.4	77.7	98.9	96.8	99.2	96.0	69.0	96.0	97.9	86.9	63.7	98.5	88.8	90.8	68.1	94.8	91.2	74.8	88.0	16.3	95.8	84.6	84.5

Table 12: Detailed accuracy results per dataset, fine-tuning the vision and language backbones of CLIP-ViT-L/14. Highest performance and those within a range of 0.1 in each section are highlighted in bold.

Method	Cars	DTD	EuroSAT	GTSRB	MNIST	RESISC45	SUN397	SVHN	CIFAR10	CIFAR100	ImageNet	STL10	Food101	Caltech256	FGVC Aircraft	Flowers102	OxfordIIITPet	CUB200	PascalVOC	Country211	Caltech101	UCF101	Average	
1 shot	NoLA	72.7	61.1	81.5	76.4	89.3	78.6	67.3	76.1	94.0	77.9	70.3	98.8	87.5	88.3	41.1	85.0	90.4	63.4	71.7	18.0	90.4	76.6	75.3
	VeRA256	78.5	55.6	75.3	55.0	88.8	73.2	68.8	67.8	96.6	80.5	75.5	99.4	93.2	88.9	34.3	80.6	93.8	64.2	78.8	32.0	86.8	73.6	74.6
	LoRA32	74.9	62.3	81.0	76.5	91.7	79.5	68.3	74.7	92.8	78.9	71.4	98.6	87.9	89.4	44.0	89.5	88.7	66.3	68.5	19.3	90.3	77.7	76.0
	RandLoRA10	76.8	63.1	83.5	72.5	92.7	81.6	74.7	74.2	95.0	83.0	76.2	99.3	91.6	92.1	43.2	89.1	91.0	68.8	74.9	27.2	90.3	82.7	78.3
	FT	73.6	62.4	81.2	78.4	92.8	83.8	71.5	68.3	91.0	81.3	73.2	98.6	88.4	91.6	41.8	90.5	88.7	68.9	66.1	23.0	90.7	82.5	76.7
2 shots	NoLA	74.0	66.7	81.1	81.2	93.2	82.4	68.0	78.3	93.3	80.8	66.3	98.2	88.0	89.4	39.6	92.5	93.9	64.8	75.2	20.5	91.2	76.6	77.1
	VeRA256	78.1	55.8	75.3	55.7	90.0	73.5	68.6	67.0	96.6	81.3	75.6	99.4	93.2	89.0	34.8	81.5	94.4	64.0	79.2	32.2	86.8	74.1	74.8
	LoRA32	77.3	68.1	84.7	82.7	95.2	84.2	69.9	78.5	92.4	81.6	68.7	97.8	88.7	90.0	46.4	94.5	91.8	69.3	72.6	21.0	91.7	79.5	78.5
	RandLoRA10	78.5	70.4	85.1	80.4	94.7	85.8	74.9	78.2	95.9	84.1	74.4	99.5	91.9	92.5	46.1	94.5	93.9	71.5	75.8	28.1	91.7	83.6	80.5
	FT	79.6	70.5	83.8	84.0	94.0	86.5	73.7	78.1	92.5	82.7	72.1	99.2	89.2	91.6	47.2	96.5	93.1	73.5	72.7	24.1	91.9	84.1	80.0
4 shots	NoLA	75.2	70.0	87.4	85.5	95.5	84.4	69.2	82.5	94.8	82.2	66.2	97.9	89.3	89.7	44.5	93.1	94.2	67.3	77.0	23.0	91.3	77.2	79.0
	VeRA256	77.9	56.7	77.8	56.0	91.3	74.1	69.8	68.0	96.9	81.4	75.9	99.5	93.2	89.1	35.1	81.1	94.6	64.2	79.3	32.1	86.9	74.2	75.2
	LoRA32	77.2	71.8	88.4	86.2	95.9	86.3	70.5	84.3	95.1	82.4	68.7	97.5	90.2	90.8	47.4	95.5	93.7	70.6	75.8	23.2	91.8	81.4	80.2
	RandLoRA10	79.3	73.6	89.2	85.2	96.4	87.8	74.6	80.9	97.3	85.1	72.6	99.3	92.4	92.4	47.1	93.7	94.8	71.0	79.1	29.2	91.7	84.6	81.7
	FT	79.7	74.6	90.0	90.1	96.0	88.8	73.5	82.5	94.2	84.2	71.6	98.1	89.8	92.7	43.3	97.3	93.7	76.0	78.2	25.3	92.3	84.8	81.7
16 shots	NoLA	82.8	72.0	93.7	86.4	96.7	87.3	72.2	87.8	97.0	84.2	69.1	98.7	90.5	93.0	53.5	96.2	94.6	78.8	83.7	23.6	90.3	82.7	82.5
	VeRA256	80.5	56.1	82.6	56.2	93.9	74.4	71.9	69.8	97.2	83.0	76.3	99.5	93.5	90.3	38.3	82.3	94.8	68.3	80.2	32.8	89.1	77.2	76.7
	LoRA32	85.7	74.8	94.2	88.1	97.1	88.9	73.3	88.7	96.9	85.8	70.9	99.0	91.2	93.2	56.7	97.5	94.2	82.6	82.1	23.6	90.8	85.5	83.7
	RandLoRA10	86.6	76.0	94.9	87.4	97.2	89.4	76.5	86.4	97.0	86.5	74.5	99.2	92.3	94.4	57.4	97.8	95.3	83.9	82.4	25.3	91.7	88.5	84.6
	FT	87.5	78.4	95.7	91.7	97.7	91.2	75.6	87.4	94.6	87.3	73.5	98.3	91.4	94.1	61.1	98.4	94.2	85.0	82.3	25.8	92.9	88.2	85.1
50%	NoLA	84.4	78.0	98.6	96.4	99.3	95.2	72.7	96.3	99.1	89.2	73.0	99.5	93.0	94.4	57.9	96.3	95.6	79.3	91.5	26.7	91.3	87.0	86.1
	VeRA256	81.7	68.8	95.8	88.5	97.0	86.8	71.8	90.5	98.1	85.0	76.2	99.5	93.9	93.8	44.5	87.7	94.4	70.2	88.6	32.9	94.3	80.9	82.8
	LoRA32	88.2	81.2	98.8	96.9	99.1	96.0	74.1	96.5	99.2	90.3	75.4	99.5	94.4	95.6	68.4	97.2	94.9	83.2	91.0	25.5	94.1	88.4	87.6
	RandLoRA10	89.9	82.3	98.8	96.8	99.4	96.0	76.7	96.8	99.2	91.6	78.3	99.5	94.7	95.6	69.0	96.9	95.7	83.9	92.1	27.5	96.9	90.5	88.5
	FT	89.7	79.0	99.1	96.3	99.3	96.8	76.0	97.0	99.2	91.2	77.3	99.4	94.3	95.8	69.6	97.1	95.0	84.6	91.9	26.8	96.9	90.8	88.3
100%	NoLA	87.5	82.5	99.0	96.8	99.3	96.3	75.0	96.6	99.3	90.4	73.6	99.7	93.8	95.2	74.0	98.5	95.1	83.2	91.5	28.5	93.9	88.0	88.1
	VeRA256	81.6	67.9	96.1	88.6	97.2	85.8	71.7	90.2	98.2	85.1	77.0	99.5	93.8	93.9	44.5	93.0	94.9	70.3	89.2	32.8	96.4	81.5	83.1
	LoRA32	89.2	83.9	99.2	97.4	99.3	96.8	75.9	95.8	99.3	91.4	76.1	99.7	95.2	95.8	78.6	98.4	95.2	85.3	91.7	27.9	96.1	90.2	89.0
	RandLoRA10	90.8	84.6	99.0	96.6	99.5	96.9	77.8	97.0	99.4	92.8	79.0	99.7	95.4	96.5	79.6	98.9	95.4	87.1	92.5	30.4	96.8	93.1	90.0
	FT	90.4	84.4	99.1	97.1	99.3	97.2	77.2	97.3	99.2	92.4	78.1	99.6	94.9	96.2	81.5	99.1	94.8	86.9	92.6	29.3	97.0	92.6	89.8

Table 13: Detailed accuracy results per dataset, fine-tuning the vision and language backbones of CLIP-ViT-H/14. Highest performance and those within a range of 0.1 in each section are highlighted in bold.

Method		Cars	DTD	EuroSAT	GTSRB	MNIST	RESISC45	SUN397	SVHN	CIFAR10	CIFAR100	ImageNet	STL10	Food101	Caltech256	FGVC Aircraft	Flowers102	OxfordIIITPet	CUB200	PascalVOC	Country211	Caltech101	UCF101	Average
1 shot	NoLA	92.0	71.8	80.9	78.7	90.1	82.2	70.6	60.2	95.1	82.7	73.1	98.0	88.0	90.3	46.4	91.5	91.2	76.2	69.7	17.5	91.5	78.1	78.0
	VeRA1024	93.8	69.4	73.8	65.1	90.0	73.2	74.9	54.2	98.2	85.5	77.6	99.1	92.8	91.5	46.4	81.6	92.0	82.2	80.0	29.9	89.7	79.2	78.2
	LoRA32	92.7	70.4	84.6	79.8	88.2	84.7	71.2	59.9	95.6	83.3	71.9	96.7	87.5	90.6	49.0	95.2	90.4	76.6	70.2	18.4	91.8	79.8	78.6
	RandLoRA10	93.0	71.0	79.8	79.6	90.2	84.3	78.3	55.8	97.2	85.9	78.0	98.1	90.9	92.5	49.9	94.3	92.2	78.3	66.1	26.4	92.3	82.1	79.8
	FT	92.2	69.9	81.7	79.8	88.2	85.3	76.2	56.2	95.8	83.3	73.3	97.6	89.1	91.7	49.8	95.6	90.6	76.9	66.1	24.6	91.9	82.4	79.0
2 shots	NoLA	92.8	71.7	89.3	87.8	91.2	83.2	71.8	75.1	96.0	84.3	68.9	95.5	88.6	91.0	50.7	94.6	92.3	79.4	71.7	20.8	91.6	78.8	80.3
	LoRA1024	93.8	71.1	89.7	67.0	90.3	74.3	78.2	74.3	98.1	85.8	77.3	99.0	92.9	91.7	47.0	82.1	92.3	81.7	80.8	30.1	89.5	79.4	80.3
	LoRA32	93.1	71.9	93.2	84.9	92.2	86.0	72.3	77.4	96.9	83.5	70.4	94.6	87.7	91.9	51.9	97.2	91.8	77.5	75.5	20.8	92.9	83.6	81.2
	RandLoRA10	93.9	75.8	90.7	89.3	93.5	86.9	78.2	79.0	97.5	86.5	74.8	98.1	91.3	92.5	53.6	97.4	93.2	81.0	72.6	27.2	93.7	84.1	83.2
	FT	93.1	74.0	90.8	89.9	93.7	86.1	74.3	74.0	95.4	85.2	71.2	97.2	90.1	92.0	46.9	97.4	92.6	78.2	71.5	25.1	93.3	84.5	81.7
4 shots	NoLA	93.1	73.7	92.9	86.3	94.4	85.1	72.6	80.3	96.8	84.2	69.2	97.2	89.4	91.0	55.2	95.8	92.7	80.7	78.7	23.5	91.6	82.4	82.1
	VeRA1024	93.9	71.4	92.4	67.3	92.5	74.2	76.6	78.0	98.3	86.1	72.9	99.1	92.8	92.8	47.6	82.0	94.0	82.7	82.2	30.8	89.9	79.6	80.8
	LoRA32	93.9	73.7	94.2	89.5	95.6	87.8	72.5	80.9	97.1	85.3	70.8	97.3	89.1	92.3	56.9	97.8	92.4	82.4	78.5	23.3	91.9	84.8	83.1
	RandLoRA10	94.1	78.6	95.5	89.5	95.7	89.8	76.5	80.5	98.1	87.4	73.5	99.0	91.6	92.7	57.5	98.1	93.7	83.1	78.1	28.6	93.3	86.9	84.6
	FT	93.8	78.1	94.0	88.5	95.8	89.4	75.5	77.1	96.2	86.5	72.8	97.7	90.5	93.5	51.8	98.4	92.8	81.5	77.2	25.2	93.0	86.3	83.4
16 shots	NoLA	93.3	76.0	95.7	90.3	96.7	88.6	75.3	87.1	98.0	87.3	71.6	98.7	90.0	92.8	61.5	98.1	93.7	86.0	81.5	23.8	92.2	85.9	84.7
	VeRA1024	94.2	77.4	94.3	81.7	94.4	85.1	77.1	82.0	98.4	87.8	73.8	99.3	91.7	94.0	61.1	94.6	94.5	86.4	81.2	25.7	93.2	88.1	84.4
	LoRA32	93.5	77.7	95.3	92.5	96.6	90.2	75.7	86.8	98.2	88.3	73.2	98.5	90.4	93.9	65.5	98.8	92.9	86.8	80.9	23.2	92.2	87.7	85.4
	RandLoRA10	94.4	79.8	95.9	92.3	96.9	91.7	78.1	87.4	98.1	88.6	75.6	99.0	91.2	94.6	64.5	99.0	94.0	87.8	80.7	25.2	92.2	89.1	86.2
	FT	94.3	80.0	95.8	94.1	96.5	91.7	77.5	85.6	97.8	87.6	75.0	98.6	90.8	94.5	64.7	98.7	93.7	87.1	81.9	25.2	93.3	89.6	86.1
50%	NoLA	93.0	80.8	99.1	96.7	99.2	95.2	75.2	96.2	99.2	90.7	74.7	99.3	93.0	95.3	70.5	97.5	94.5	85.2	90.9	25.9	91.7	87.4	87.8
	VeRA1024	93.8	82.0	99.2	96.2	99.3	96.1	76.9	96.2	99.2	91.9	76.3	99.5	93.6	96.2	72.7	98.3	95.2	86.7	90.5	25.7	95.8	89.4	88.7
	LoRA32	92.7	82.1	98.8	96.5	99.3	96.2	75.7	96.5	99.3	91.9	77.0	99.4	94.2	96.0	74.0	97.2	94.5	86.4	89.5	25.9	96.2	90.5	88.6
	RandLoRA10	94.8	82.8	98.8	96.6	99.3	96.4	77.7	96.8	99.3	93.0	79.1	99.5	94.6	96.5	77.2	98.7	94.7	87.3	91.3	28.1	96.0	90.4	89.5
	FT	94.5	82.0	98.8	96.8	99.3	96.6	76.7	96.8	99.0	91.8	77.0	99.4	94.2	96.4	77.9	98.1	94.6	86.7	90.8	27.6	95.5	91.4	89.2
100%	NoLA	93.3	84.2	99.3	96.7	99.4	96.2	76.6	96.8	99.2	91.5	74.8	99.5	93.7	95.5	77.2	98.7	94.4	86.9	91.4	28.2	95.0	89.8	89.0
	VeRA1024	94.3	85.0	99.0	97.2	99.4	97.0	78.0	96.8	99.3	92.6	76.7	99.6	94.3	95.9	79.7	99.3	95.0	87.7	91.3	27.3	96.4	91.3	89.7
	LoRA32	93.1	85.8	99.1	97.3	99.5	97.2	77.6	97.2	99.3	93.0	77.9	99.5	94.9	96.6	83.7	99.0	94.4	87.5	91.8	28.3	95.9	91.5	90.0
	RandLoRA10	94.7	86.0	99.0	97.0	99.4	97.1	79.4	97.3	99.3	93.5	80.1	99.5	95.2	97.1	84.1	99.3	95.1	88.6	91.7	31.2	96.5	92.7	90.6
	FT	94.9	84.2	98.8	97.5	99.5	97.6	78.7	97.3	99.2	92.8	77.9	99.5	94.8	96.8	84.4	99.3	95.3	88.3	91.8	30.1	96.6	93.0	90.4

Table 14: Detailed accuracy results per dataset, the DinoV2 ViT-B/14 vision backbone. Highest performance and those within a range of 0.1 in each section are highlighted in bold.

Method		Cars	DTD	EuroSAT	GTSRB	MINIST	RESISC45	SUN397	SVHN	CIFAR10	CIFAR100	STL10	Food101	Caltech256	FGVC Aircraft	Flowers102	OxfordIIITPet	CUB200	Pascal VOC	Country211	Caltech101	UCF101	Average
1 shots	NoLA	21.2	45.4	60.7	28.8	55.0	49.8	46.3	14.4	73.8	57.3	71.7	50.5	78.7	19.7	98.6	74.6	62.5	43.6	3.1	85.5	63.8	52.6
	VeRA256	22.5	45.6	57.9	20.1	50.7	44.6	46.7	12.9	76.5	55.8	64.4	51.9	78.6	19.1	98.7	75.5	62.9	36.2	3.4	84.7	63.1	51.0
	LoRA32	22.6	47.2	59.3	24.8	51.7	48.7	45.9	14.6	77.2	57.4	64.6	52.4	77.5	19.7	98.9	76.5	63.1	37.2	3.4	85.1	62.3	51.9
	RandLoRA6	21.5	47.8	57.9	34.5	61.6	44.9	44.1	16.2	56.8	54.0	66.0	47.2	76.4	19.6	97.8	71.8	59.9	43.4	3.0	86.1	62.8	51.1
	FT	20.8	45.5	67.8	25.7	52.3	45.2	45.3	15.5	70.2	54.7	75.8	50.1	75.2	19.4	98.3	70.8	60.0	36.9	3.1	84.7	60.3	51.3
2 shots	NoLA	41.4	57.8	64.1	43.1	73.5	65.4	58.1	16.2	90.0	74.5	93.9	64.5	84.9	28.0	99.6	83.0	73.3	51.4	4.1	90.0	72.7	63.3
	VeRA256	38.2	57.4	64.0	28.9	65.0	60.8	57.3	14.4	86.0	71.6	78.9	66.2	84.8	26.2	99.4	83.4	74.8	44.4	4.1	88.0	73.7	60.4
	LoRA32	41.1	58.4	68.3	37.7	71.4	64.7	58.2	14.7	89.6	74.8	87.0	66.1	85.3	27.0	99.5	86.7	73.0	52.1	5.0	89.2	72.1	63.0
	RandLoRA6	41.9	59.6	69.0	48.6	70.2	62.2	57.1	19.4	72.1	70.6	84.8	63.3	83.8	29.5	98.4	80.0	71.3	49.7	3.8	89.9	72.1	61.8
	FT	43.1	56.0	65.7	42.6	72.1	63.1	57.5	16.1	79.0	71.0	91.3	64.6	85.1	27.7	99.3	81.1	71.8	50.6	3.9	89.2	70.5	62.0
4 shots	NoLA	62.9	68.5	76.4	62.4	82.4	75.9	65.8	22.8	94.5	82.6	97.6	73.7	89.8	40.6	99.7	89.3	82.6	65.4	6.0	90.6	79.5	71.9
	VeRA256	56.1	64.2	71.5	43.2	76.1	71.6	64.8	17.6	91.4	80.9	88.7	74.7	89.3	36.0	99.7	91.0	82.1	53.5	6.2	89.8	77.7	67.9
	LoRA32	63.4	66.5	79.2	61.0	79.2	77.6	66.3	20.9	94.5	82.1	94.5	75.0	89.4	41.9	99.7	91.9	83.5	66.2	6.8	89.7	80.6	71.9
	RandLoRA6	64.6	65.3	72.2	66.6	86.4	77.0	65.0	24.8	84.0	79.4	93.1	73.0	89.8	43.9	99.6	86.6	82.4	63.8	5.9	91.7	78.6	71.1
	FT	65.5	67.3	73.0	62.7	85.6	73.8	66.0	20.9	88.0	81.3	94.0	73.6	90.2	41.4	99.6	88.9	82.6	61.3	6.0	91.7	79.3	71.1
16 shots	NoLA	86.4	79.5	91.0	88.2	94.0	87.8	75.1	56.9	97.2	89.4	99.0	85.1	93.1	64.0	99.7	93.9	88.8	82.2	12.2	95.3	87.0	83.1
	VeRA256	81.7	78.2	88.2	60.1	88.9	83.2	73.5	30.2	97.4	87.6	97.4	84.4	92.6	51.3	99.7	94.6	88.5	72.9	11.8	91.9	85.7	78.1
	LoRA32	87.1	80.5	93.9	86.4	93.0	87.2	75.1	44.8	97.4	88.8	99.4	85.6	93.5	65.2	99.7	94.2	88.5	80.5	12.4	94.6	87.6	82.6
	RandLoRA6	88.4	79.0	92.3	90.3	95.4	87.3	74.7	57.4	97.0	88.5	98.2	85.5	93.1	71.5	99.7	93.3	88.6	79.7	11.8	94.5	87.8	83.5
	FT	87.3	78.8	92.4	88.9	95.0	88.9	74.7	50.4	96.8	88.6	98.8	85.3	93.4	67.1	99.7	93.2	88.9	77.8	11.8	94.9	87.4	82.9
0.5 shots	NoLA	89.0	82.5	98.9	96.4	99.2	94.8	76.0	96.5	99.2	93.2	99.6	92.5	95.8	73.7	99.5	94.9	87.4	92.8	18.7	97.8	88.6	88.9
	VeRA256	84.0	80.1	97.3	89.7	97.7	92.0	74.8	88.2	99.0	92.2	99.4	91.7	94.7	68.4	99.5	95.1	86.9	89.9	17.6	96.0	87.5	86.7
	LoRA32	89.7	82.8	99.0	96.2	99.1	94.8	75.9	96.6	99.3	93.7	99.5	93.2	95.5	72.6	98.3	95.0	88.6	93.0	19.0	97.5	90.3	89.0
	RandLoRA6	89.7	83.2	98.7	97.1	99.3	95.5	75.8	97.2	99.2	93.4	99.6	93.3	95.5	75.2	99.7	94.9	87.5	92.8	19.6	97.6	89.3	89.2
	FT	90.3	81.5	98.8	96.6	99.3	95.8	76.2	96.6	99.2	93.4	99.3	93.0	95.7	75.3	98.9	95.0	87.4	92.4	19.9	97.3	90.6	89.2
1.0 shots	NoLA	92.5	85.4	98.8	96.9	99.3	96.1	77.8	96.8	99.4	94.1	99.7	93.4	96.2	81.8	99.7	95.9	90.2	93.6	22.3	98.2	90.2	90.4
	VeRA256	89.8	81.6	97.4	89.5	98.1	93.1	76.5	88.4	99.1	92.6	99.6	92.5	95.3	75.4	99.7	95.8	89.7	90.6	20.5	97.1	88.2	88.1
	LoRA32	92.7	84.6	99.1	96.3	99.3	96.0	78.2	97.2	99.3	94.2	99.7	93.7	96.3	83.3	99.7	95.7	90.4	92.7	20.6	97.8	91.5	90.4
	RandLoRA6	93.3	85.5	99.0	97.1	99.4	96.8	77.9	97.5	99.5	94.4	99.7	94.2	96.2	84.0	99.6	95.8	90.1	93.1	22.7	98.0	92.0	90.8
	FT	93.4	85.5	99.4	96.8	99.3	97.0	78.4	97.4	99.2	94.0	99.6	94.1	96.3	83.9	99.7	95.8	90.1	93.1	23.8	98.0	91.8	90.8

Method	% Params	BoolQ	PIQA	SIQA	HellaSwag	WinoGrande	ARC-e	ARC-c	OBQA	Average + Δ
Qwen2 - Zero-shot										
Zero-shot	0	3.12	4.68	7.22	2.50	14.52	4.80	1.79	2.60	5.15
Qwen2 - 15k										
NoLA	0.05	54.16	56.91	47.65	17.36	45.46	46.55	32.51	39.80	42.55
VeRA1024	0.06	58.78	56.64	50.10	24.95	49.80	56.52	37.80	50.40	48.12
LoRA-16	1.18	62.14	62.13	58.24	27.86	49.96	62.46	44.97	58.20	53.25
RandLoRA-10	1.18	62.14	63.49	55.32	31.16	49.96	64.27	44.97	56.60	53.49 +0.24
LoRA-32	2.33	59.94	62.13	56.55	30.27	41.99	64.39	46.42	57.00	52.34
RandLoRA-5	2.33	62.81	63.82	54.86	30.00	48.07	64.81	43.34	55.40	52.89 +0.55
Qwen2 - 170k										
NoLA	0.05	55.99	52.50	55.07	23.74	50.51	55.64	38.91	46.80	47.40
VeRA1024	0.06	55.50	59.30	52.81	34.52	52.72	58.55	42.94	57.80	51.78
LoRA-16	1.18	53.39	68.12	66.33	46.46	58.72	59.97	43.77	62.20	57.37
RandLoRA-10	1.18	61.47	67.63	65.61	40.26	57.22	62.12	47.95	59.60	57.73 +0.36
LoRA-32	2.33	55.78	68.28	67.20	42.37	60.22	61.03	45.05	58.80	57.34
RandLoRA-5	2.33	63.46	65.72	66.43	42.90	56.20	61.49	47.53	59.20	57.86 +0.52
Phi3 - Zero-shot										
Zero-shot	0	62.26	79.82	65.81	56.29	19.89	89.86	77.65	71.40	65.37
Phi3 - 15k										
NoLA	0.005	66.24	85.15	73.49	78.29	73.95	95.33	85.15	85.20	80.35
VeRA1024	0.015	68.53	84.49	73.08	74.54	72.85	93.01	80.97	81.60	78.63
LoRA-16	0.57	69.51	85.36	75.44	80.15	75.85	95.37	86.09	86.60	81.80
RandLoRA-40	0.58	69.54	85.31	73.80	84.05	75.14	94.65	84.90	85.80	81.65 -0.15
LoRA-32	1.14	68.44	85.31	74.67	72.14	74.98	95.20	85.41	86.60	80.34
RandLoRA-20	1.16	69.20	85.42	75.33	83.98	75.77	95.50	85.92	87.60	82.33 +1.99
LoRA-64	2.28	69.88	85.75	74.97	74.45	75.30	95.54	87.12	88.00	81.37
RandLoRA-10	2.29	69.63	85.31	75.03	86.94	75.30	95.24	85.58	86.40	82.43 +1.06
Phi3 - 170k										
NoLA	0.005	68.87	85.15	77.18	85.13	77.90	95.20	85.58	83.60	82.33
VeRA1024	0.015	69.53	84.53	74.52	84.08	76.82	94.51	83.68	83.54	81.40
LoRA-16	0.57	70.83	84.39	78.45	89.94	82.87	95.45	86.09	89.00	84.63
RandLoRA-40	0.58	70.86	86.67	78.81	90.07	82.00	95.12	86.26	87.60	84.67 +0.04
LoRA-32	1.14	71.23	85.96	78.92	91.77	82.95	94.61	84.81	89.40	84.96
RandLoRA-20	1.16	71.62	87.43	79.48	91.48	82.79	95.16	86.01	87.80	85.22 +0.26
LoRA-64	2.28	71.93	86.13	79.58	90.14	83.74	92.68	81.74	87.80	84.22
RandLoRA-10	2.29	71.87	86.56	79.43	90.99	82.72	95.66	85.49	87.40	85.01 +0.79
LLama3 - Zero-shot										
Zero-shot	0	60.73	41.40	28.40	25.00	10.97	16.41	15.96	16.80	26.96
LLama3 - 15k										
NoLA	0.004	67.58	84.49	72.31	69.60	70.56	90.49	78.75	81.20	76.87
VeRA1024	0.014	63.36	84.39	74.10	77.70	71.35	89.48	76.54	80.20	77.14
LoRA-16	0.35	73.03	86.94	75.90	90.53	77.74	90.74	80.29	86.20	82.67
RandLoRA-60	0.36	71.19	84.22	75.59	83.82	74.98	91.12	81.31	86.00	81.03 -1.64
LoRA-32	0.7	74.22	86.40	75.79	91.90	77.35	90.61	80.80	87.60	83.09
RandLoRA-30	0.7	71.65	83.79	74.56	86.85	75.61	90.78	80.03	87.20	81.31 -1.78
LoRA-64	1.4	71.77	84.17	76.25	85.14	73.80	91.46	80.80	86.20	81.20
RandLoRA-15	1.4	70.98	86.02	75.44	89.74	76.80	91.29	81.66	83.80	81.96 +0.76
LLama3 - 170k										
NoLA	0.004	71.83	84.66	77.79	85.05	82.72	88.59	76.45	82.20	81.16
VeRA1024	0.014	70.55	85.69	79.27	92.14	82.64	87.33	73.38	82.20	81.65
LoRA-16	0.35	75.14	89.12	80.66	89.01	86.58	90.07	78.75	86.20	84.44
RandLoRA-60	0.35	75.26	87.98	79.63	94.66	85.64	90.03	79.44	84.40	84.62 +0.18
LoRA-32	0.7	75.08	88.85	80.25	95.42	86.19	90.28	80.29	85.60	85.24
RandLoRA-30	0.7	76.33	88.08	80.25	95.67	86.11	90.36	80.89	87.00	85.59 +0.45
LoRA-64	1.4	74.65	89.66	80.86	95.17	86.74	90.95	79.18	85.40	85.33
RandLoRA-15	1.4	72.63	87.98	81.37	95.68	87.77	91.33	80.89	89.00	85.83 +0.50

Table 15: Comparison of accuracy on commonsense reasoning datasets. We report accuracy delta of RandLoRA with LoRA for comparable amounts of trainable parameters.