# 2 Appendix

# **3 A Materials and Methods**

### 4 A.1 Natural Scenes Dataset

Here, we briefly summarize the data acquisition and preprocessing steps that are described in detail 5 elsewhere []]. Scanning was conducted at 7T using whole-brain gradient-echo EPI at 1.8-mm 6 resolution and 1.6-s repetition time. Images were taken from the Microsoft Common Objects in 7 Context (COCO) database [2], square cropped, and presented at a size of  $8.4^{\circ}$  x  $8.4^{\circ}$ . A special 8 set of 1,000 images were shared across subjects; the remaining images were mutually exclusive 9 across subjects. Images were presented for 3 s with 1-s gaps in between images. Subjects fixated 10 centrally and performed a long-term continuous recognition task on the images. The fMRI data were 11 pre-processed by performing one temporal interpolation (to correct for slice time differences) and one 12 spatial interpolation (to correct for head motion). A general linear model was then used to estimate 13 single-trial beta weights. Cortical surface reconstructions were generated using FreeSurfer, and 14 both volume- and surface-based versions of the beta weights were created. Estimated beta weights 15 provided in the subject-native space (func1pt8mm) were used in all of our experiments. Every 16 stimulus considered in this study had 3 repetitions. We averaged single-trial betas after z-scoring 17 18 every voxel within each scan session to create our voxel responses.

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# 20 A.2 Response-optimized Model Training Routine

Response-optimized models for each visual area were trained for a maximum of 100 epochs using Adam with a learning rate of 1e-4, a batch size of 16 and early stopping (patience = 20) based on the Pearson's correlation coefficient between the predicted and measures responses on the validation set. The target signals for each model comprised the image stimuli and voxel-level response vector for each ROI. The loss is computed as the following:

$$\mathcal{L} = \sum_{i \in \text{Batch}} \sum_{s=1}^{S} \sum_{v=1}^{n_s} \mathbb{1}_{i \in I_s} (r_{s,v}^{pred} - r_{s,v}^{meas.})^2,$$

where  $1_{i \in I_s}$  is the indicator variable specifying if image *i* was shown to subject *s*,  $r_{s,v}^{pred}$  and  $r_{s,v}^{meas.}$ are the predicted and measured response at subject *s*, voxel *v*. This masked squared error loss allowed us to backpropagate errors through the shared convolutional backbone even if the subjects were not exposed to common stimuli. The other response-optimized baseline model (denoted as 'Response-optimized (no rotation symmetries)' in the main text) is optimized following the same training procedure as defined above.

# 27 A.3 Details of the task-optimized DNN models evaluated

Table A.2 lists all DNN models used as baselines against response-optimized models for quantitative 28 comparisons. All pre-trained models, except CORnet-S were downloaded from the official PyTorch 29 Model Zoo. CORnet-S was obtained from the official github repository of the project [3]. For 30 evaluation of all models except CORnet-S, we downsample convolutional layers by applying an 31 avgpool layer so that the resulting feature map has dimension at most 9K. We found that further 32 33 decreasing it (e.g. to 1K) only decreased the prediction accuracy on the validation set. For CORnet-S, we do not perform layer selection for each of the 5 visual regions, rather we pre-select the layer 34 homologous to each visual region, i.e., layers V1, V2 and V4 are used for modeling responses to 35 voxels in V1, V2 and V4 respectively. We further use the layer IT for modeling responses to LO 36 and VO. The pre-selection of convolutional layers further allows us to employ a spatial x features 37 factorized linear readout for the CORnet-S model to enable a fairer comparison with the proposed 38 response-optimized encoding models. We further resize the convolutional output of the CORnet-S 39 model to have spatial dimensions of  $28 \times 28$  (same as the response-optimized model). 40

Quantitative fit (response predictivity)					
Analysis	Probe/evaluation	Metrics for evalua- tion	Baselines		
NSD (i) Generaliza-	dataset Held-out stimuli-		Catagory ideal sharmen		
tion to <i>novel stimuli</i>		Prediction accuracy	Category ideal observer, ImageNet-trained mod-		
(in-distribution)	response pairs from the same NSD sub-	(Pearson's R)	els (AlexNet, CORnet-S,		
(III-distribution)	jects		ResNet-50, DenseNet121) and MS-COCO-trained (ResNet-50) task-optimized		
			models)		
(ii) Generalization to	Held-out stimuli-				
novel subjects	response pairs from 4				
(iii) Generalization to	novel NSD subjects 'NSDsynthetic'				
OOD stimuli	stimuli-response				
	pairs				
Generalization to	Algonauts 2019,	RSA (Kendall's $\tau$ )	Comparison among		
novel fMRI datasets	BOLD5000, Inani-		response-optimized models		
mate objects dataset           Characterizing neural response properties by probing response-optimized models					
Characterizing spatial	Measured pRF maps	Pearson's R (Ec-			
tuning	from NSD Retino-	centricity); Circular			
8	topy experiment	correlation coeffi-			
		cient (Polar angle)			
Characterizing fea-	NSD-meadows multi-	RSA (Kendall's $\tau$ )	Comparison among		
ture representations	arrangement task		response-optimized models		
(i) Alignment with human perception					
(ii) Separability of	THINGS, ImageNet-	RSA (Kendall's $\tau$ )			
category information	16, NSD	Roff (Rendult 57)			
(iii) Single voxel tun-	_	_			
ing (maximally acti-					
vating images) (iv) shape v/s texture	ImageNet-16, Silhou-	Tranfer performance	MS-COCO-trained multi-		
bias	ette and Geirhos Style	(classification accu-	label object classification		
	Transfer dataset	racy), shape bias	network, task-optimized encoding model (AlexNet)		

 Table A.1: Summary of model evaluation and interpretability techniques employed in this study

Name	Number of parameters	Layers selected for evaluation
AlexNet	0.61M	conv1, conv2, conv3, conv4, conv5, fc6, fc7
CORnet-S	53.4M	V1, V2, V4, IT
ResNet-50	25.6M	Last layer of every residual stage (res1, res2, res3, res4) and avgpool
DenseNet-121	8M	Last layer of every dense block (denseblock1, denseblock2, denseblock3, denseblock4)
ResNet-50 backbone (FasterRCNN, MS-COCO)	41.7M	Last layer of every residual stage (res1, res2, res3, res4) and avgpool

Table A.2: Details of the task-optimized DNNs used as baselines

#### 42 A.4 Characterizing the spatial tuning of early visual areas: Polar angle agreement

We measured the agreement between the polar angles estimated from the learned encoding model against the polar angle measurements from the independent pRF experiment using the circular correlation coefficient between measured and predicted polar angle arrays in an ROI of *n* voxels, respectively denoted by  $\{a_m^1, ..., a_m^n\}$  and  $\{a_p^1, ..., a_p^n\}$ , called *'polar angle agreement'*, is calculated as,

$$r = \frac{\sum_{i=1}^{n} \sin(a_m^i - T_m) \sin(a_p^i - T_p)}{\sqrt{\sum_{i=1}^{n} \sin^2(a_m^i - T_m) \sum_{i=1}^{n} \sin^2(a_p^i - T_p)}},$$

where  $T_m$  and  $T_p$  are the circular mean angles of the measured and predicted polar angle vectors, respectively,

$$T_m = \left(\frac{1}{n}\sum_{i=1}^n \sin a_m^i, \frac{1}{n}\sum_{i=1}^n \cos a_m^i\right), T_p = \left(\frac{1}{n}\sum_{i=1}^n \sin a_p^i, \frac{1}{n}\sum_{i=1}^n \cos a_p^i\right)$$

#### 45 A.5 Noise ceiling estimation

<sup>46</sup> Noise ceiling for every voxel represents the performance of the "true" model underlying the generation <sup>47</sup> of the responses (the best achievable accuracy) given the noise in the fMRI measurements. They <sup>48</sup> were computed using the standard procedure followed in [1] by considering the variability in voxel <sup>49</sup> responses across repeat scans. The dataset contains 3 different responses to each stimulus image <sup>50</sup> for every voxel. In the estimation framework, the variance of the responses,  $\sigma_{response}^2$ , are split into <sup>51</sup> two components, the measurement noise  $\sigma_{noise}^2$  and the variability between images of the noise free <sup>52</sup> responses  $\sigma_{signal}^2$ .

$$\hat{\sigma}_{\text{response}}^2 = \hat{\sigma}_{\text{signal}}^2 + \hat{\sigma}_{\text{noise}}^2$$

An estimate of the variability of the noise is given as  $\hat{\sigma}_{noise}^2 = \frac{1}{n} \sum_{i=1}^{n} Var(\beta_i)$ , where i denotes the image (among *n* images) and Var( $\beta_i$ ) denotes the variance of the response across repetitions of the

same image. An estimate of the variability of the noise free signal is then given as,

$$\hat{\sigma}_{\text{signal}}^2 = \hat{\sigma}_{\text{response}}^2 - \hat{\sigma}_{\text{noise}}^2$$

Since the measured responses were z-scored,  $\hat{\sigma}_{response}^2 = 1$  and  $\hat{\sigma}_{signal}^2 = 1 - \hat{\sigma}_{noise}^2$ . The noise ceiling (n.c.) expressed in correlation units is thus given as  $n.c. = \sqrt{\frac{\hat{\sigma}_{signal}^2}{\hat{\sigma}_{signal}^2 + \hat{\sigma}_{noise}^2}}$ . The models were evaluated in terms of their ability to explain the average response across 3 trials (i.e., repetitions) of the stimulus. To account for this trial averaging, the noise ceiling is expressed as  $n.c. = \sqrt{\frac{\hat{\sigma}_{signal}^2}{\hat{\sigma}_{signal}^2 + \hat{\sigma}_{noise}^2/3}}$ . We computed noise ceiling using this formulation for every voxel in each subject and expressed the noise-normalized prediction accuracy (R) as a percentage of this noise ceiling.

# 62 A.6 Principal components analysis for characterizing features in high-level visual area VO

We implemented a principal components analysis on the predicted activity patterns in the anterior 63 ventral stream ROI VO to all 26,107 images from the THINGS dataset [4]. This also enables us to 64 find a compressed representation of thousands of voxels in VO (across 4 subjects). We found that the 65 first 2 principal components explained a large proportion of the variance in voxel responses (main text 66 Figure 5D). We examined the 2 discovered components by ordering exemplars along each component 67 dimension for intuitive exposition. Specifically, we extracted the top and bottom 100 images for each 68 PC dimension. We extracted the top 5 concepts that had the highest frequency in each of the top and 69 bottom image sets (the THINGS dataset comprises a total of 1,854 diverse concepts) and visualized 70 the two images within each of these concept categories that elicited the highest/lowest response along 71 the PCs. These images are shown in the main text Figure 5D [left]. We also plotted all images in the 72 2-dimensional space spanned by the PCs and colored them based on the animate/inanimate labels 73 provided along with the THINGS dataset (as part of the Top-Down WordNet Category ). 74

#### 75 A.7 Generalization to held-out NSD subjects

For each of the 4 held-out NSD subjects, the dataset comprised brain responses to 5,445 stimuli with 76 3 repetitions (remaining stimuli had either 1 or 2 repetitions and were discarded from analysis). To 77 assess generalization of response-optimized models in terms of predicting responses on held-out 78 NSD subjects, we fixed the weights of the shared convolutional backbone and used data from new 79 NSD participants to train their linear readouts. We varied the size of the training set for learning 80 81 readout weights from a mere 100 stimulus-response pairs from every new participant to a large set of 4,500 pairs. The readouts had the same architecture as the original models, i.e., they were factorized 82 83 into spatial and feature dimensions. The readouts were trained independently for each subject, each training set size and each visual ROI for 100 epochs with an early stopping criterion (patience of 20). 84 For task-optimized and category ideal observer models, we fit linear regression models (as described 85 above for the original 4 subjects) using these restricted sample sizes. The regularization parameter 86 for both semantic and task-optimized models was optimized independently for each training set size, 87 each subject and for voxels in each visual area by testing among 8 log-spaced values in [1e-4, 1e4]. 88

#### 89 A.8 Category ideal observer model

We fit a category ideal observer model using category annotations for NSD images. The input to the categorical model is an 80-D binary vector corresponding to the 80 object categories annotated in the MS-COCO database, where each element indicates whether the corresponding category was present in the image or absent. The weights corresponding to different categories for every voxel are optimized by fitting a  $l_2$  regularized linear regression model. The regularization parameter for this model was optimized independently for each subject and for voxels in each visual area by testing among 8 log-spaced values in [1e-4, 1e4].

### 97 A.9 Maximally activating images

98 We performed k-means clustering (k=4) on model-predicted voxel-level responses of each visual ROI to locate 'representative' voxels (cluster medians) for visualization, rather than randomly selecting 99 these voxels. Following [5], we start with a random noise input  $x_0$  for each model neuron i 100 and iteratively update the input along the gradient  $\frac{\partial a_i}{\partial x}$  to synthesize inputs that would result in 101 higher and higher predicted activation  $a_i$  for that neuron. For visualization purposes, since we were 102 interested in *featural* tuning, we discarded the spatial mask in the readout of every voxel and used 103 the learned feature tuning of every voxel to create an additional 1x1 convolutional layer, so that 104 every voxel is represented by an independent unit in this convolutional layer and synthesized inputs 105 to activate individual units in this convolutional voxel layer instead. Most visualization techniques 106 further employ an *image prior* in the form of a regularizer to encourage stable results [6, 7]. This 107 visualization technique is commonly employed in neural network interpretability research to find the 108 features that drive model neurons. Formally, the goal of finding the maximally activating image  $x^*$  is 109 then expressed as the following optimization problem. 110

$$x^* = \underset{x \in \mathbb{R}^{H \times W \times C}}{A_{ij}(\theta, x)} + \mathcal{R}(x)$$

where  $A_{(i,j)}(\theta, x)$  denotes the activation of unit *i* from layer *j* in the neural network to input *x* 111 (H: Height, W: Width, C: Channels), and  $\theta$  denotes the parameters of the network. The latter are 112 fixed during the above optimization procedure.  $\mathcal{R}(x)$  denotes the regulariser. In order to generate 113 maximally activating image for the *j*th voxel, we set *i* to the output voxel layer and *j* to be the index 114 of the model neuron in the output layer that emulates voxel j. We find a local solution for the above 115 optimization problem by performing gradient ascent in the input space and updating x iteratively in 116 the direction of the gradient of  $A_{ij}(\theta, x) + \mathcal{R}(x)$ . We employed a very weak form of regularization, 117 where we stochastically jitter (up to 3 px)) the image before each optimization step to avoid high 118 frequency noise. We also blurred the image after every gradient ascent step using a Gaussian filter 119 to avoid high-frequency effects. The images are optimized starting from random noise with Adam 120 optimizer for 1000 steps using a step size of 1. 121

### 122 A.10 Shape bias analysis

**Training baseline object classification model on MS-COCO** We train a baseline DNN for multilabel object classification on the entire MS-COCO dataset. The dataset comprises 82,081 training and

40,137 validation images, with most images containing multiple objects at once. Since NSD images 125 were drawn from the MS-COCO dataset, this serves as a useful control for assessing features that 126 may arise simply due to the dataset distribution. The model employs the same backbone architecture 127 as the proposed rotation-equivariant response-optimized model comprising 4 convolutional blocks 128 with E(2)-steerable convolutions. The convolutional output is downsampled to a spatial resolution of 129  $4 \times 4$  and is mapped on to an 80-D output using a linear layer. The model is optimized for multi-label 130 131 classification using a Binary Cross-Entropy loss with an Adam optimizer (learning rate of 0.001). The model is trained for 30 epochs and achieves a mean Average Precision (mAP) measure of 66.7% 132 on the validation set, which is within the range of competitive CNN models, although on the lower 133 end of that range [8]. 134

Mapping predicted voxel-wise responses to ImageNet-16 category labels and measuring transfer 135 **performance** We use the proposed response-optimized models to extract the *predicted* responses 136 137 of voxels in every region to stimuli from a small subset of the large-scale ImageNet-16 dataset. This 138 subset comprised 500 images from each of the 16 categories, resulting in a total of 8,000 images (same samples were used in the RDM analyses shown in the main text Figure 5B). The predicted 139 voxel-wise responses for every visual area constitute the *representational space* of that ROI. We 140 randomly split the 8,000 images into training (70%), validation (5%) and test sets (25%) and fitted 141  $l_2$  regularized linear classification models (known as ridge classifiers) on top of this ROI-specific 142 representational space to predict the category label of test images from the ImageNet-16 subset. The 143 predicted labels were compared against the ground truth labels to compute the ImageNet-16 transfer 144 performance. Error bars are computed over 5 random splits. This approach is akin to supervised 145 linear probes [9], where linear classifiers are trained independently of the models to probe their neural 146 representations. The classification accuracy provides a quantitative measure of the ability of each 147 ROI-specific neural representational space to support object classification. As demonstrated in the 148 main text, this classification capacity increases along the ventral visual hierarchy 4 149

We also used the response-optimized models to extract the model-*predicted* responses of voxels in every region to 160 images (10 per category) from the Silhouettes dataset [10]. The predicted responses were mapped onto the 16 category labels using the linear classifier weights estimated with the ImageNet-16 dataset (as described above) without any additional fitting. This also helps us assess how well the prediction function generalizes to out-of-domain stimuli, such as image silhouettes. The classification performance on this dataset is termed 'Silhouettes transfer performance'.

Shape bias evaluation (a) Response-optimized 156 models: Finally, we use the response-optimized mod-157 els to extract the model-predicted responses of vox-158 159 els in every region to 1200 images from the Geirhos cue-conflict dataset [10]. We map these predicted 160 responses onto the 16-class-ImageNet categories us-161 ing the linear classifier weights estimated with the 162 ImageNet-16 subset (as described above). Each im-163 age from this dataset has a texture and a shape label. 164 The shape bias of each response-optimized model is 165 then computed as the percentage of times it classi-166 fies images from the cue-conflict dataset according 167 to shape, provided it classified either shape or texture 168 correctly. 169

(b) Task-optimized models: We can also compute 170 the shape bias of task-optimized encoding models 171 (here, we assess the AlexNet model) by extracting 172 173 their predicted voxel-wise responses to the images from the Geirhos cue-conflict dataset and mapping 174 these responses to the 16-class-ImageNet categories. 175 For the mapping, we follow the same procedure as 176 employed in the case of response-optimized models, 177 wherein a linear classifier is first trained to map the 178 predicted responses to 16 classes using the 8,000 179 images from the ImageNet-16 subset. The transfer 180



Figure A.1: **A.** Transfer performance of different task-optimized encoding models on ImageNet-16 dataset. **B.** Fraction of shape vs. texture decisions for stimuli with cue conflict. Bar plots on the right display the proportion of correct decisions (either shape or texture recognized correctly) as a fraction of all trials for human observers as well as responseoptimized and task-optimized models of LO.



Figure A.2: *Voxel-wise prediction accuracy* (R) of the proposed response-optimized model across all voxels in all the 5 visual ROIs depicted on cortical flatmaps for each subject. High prediction accuracy (> 0.6) is obtained across large swathes of the cortex, well beyond early visual cortex (V1-V4) into LO and VO as well.

- 181 performance in this case is much higher than the
- 182 transfer performance of response-optimized models,
- as shown in Supplementary Figure A.1. This gap is
- 184 perhaps unsurprising given that the task-optimized

encoding models inherit feature representations *optimized* for ImageNet classification. The shape

bias is evaluated using the same approach as response-optimized models. As shown in the main
 text Figure 4B[bottom], these models exhibit a strong texture bias. This is also not surprising given

that the task-optimized encoding model is more likely to reflect the biases of supervised ImageNet training [10].

# 190 B Supplemental Results

### 191 B.1 Voxel-wise prediction accuracy on cortical surface

Supplementary Figure A.2 depicts the raw voxel-wise prediction accuracy of the proposed response optimized models on the cortical surface for each of the 4 NSD participants analyzed in the main
 study.

### 195 B.2 Generalization to novel datasets

We also compared the representational similarity structure captured by response-optimized models of 196 different ROIs to novel stimuli from other well-known fMRI datasets besides NSD. Here, we wanted 197 to assess whether the models indeed captured ROI-specific features that could generalize in explaining 198 representational geometries of similar visual ROIs in different datasets. While the ROI definitions 199 and nomenclature can vary substantially across these datasets because of the different protocols 200 201 involved in their localization, we expected the response-optimized models to capture representational geometry of voxel responses in ROIs that lie in a roughly similar anatomical location as any of the 202 5 ROIs considered in this study. We first performed this generalization analysis using the classical 203 RSA framework (without any fitting) on the following two widely-used fMRI datasets: (1) Cichy 204 et al. dataset [11] comprises fMRI recordings while 15 human participants observed 92 images of 205 natural objects (this dataset was also used in the Algonauts 2019 Challenge Training Set): Here, the 206 subject-averaged RDMs of early ('EVC') and high-level visual ROIs ('IT') were already computed 207 and publicly distributed by the authors. Further details about the localization of these 2 ROIs are 208 provided in [11]. (2) BOLD5000 V2 (GLM-denoised) dataset [12] comprises fMRI recordings 209 from 4 subjects (CSI1-4), while they each viewed  $\sim$ 5,254 natural scene images. Subject CSI4 was 210 discarded from this analyses since this subject completed much fewer scan sessions. We restrict our 211 analyses to the 1,000 images within the BOLD5000 dataset that are shared with the NSD dataset. 212 213 This enables us to compute the match not just against model-predicted RDMs but also against RDMs 214 derived from *measured* responses in NSD subjects. Importantly, these 1,000 images are all part of the 215 test set and were not used in training any of the response-optimized models. We focus on two visual ROIs in this dataset, namely 'EarlyVis' and 'LOC', which had (at least) a partial overlap with some 216 of the 5 visual ROIs we modeled in our study. 217

For stimuli from each of the above datasets, we first extracted model-predicted responses from the response-optimized models of all 5 visual ROIs: [V1, V2, V4, LO, VO]. We then computed model RDMs separately for each ROI by computing the pairwise correlation distance between the model-predicted responses of all images in each dataset. We then computed the RDM similarity between model-predicted RDMs of each ROI against the observed-response RDMs (computed using



Figure A.3: *Generalization to the Cichy et al. and BOLD5000 datasets* assessed with classical RSA. A and B depict the RDM similarity between model-predicted RDMs (5 models corresponding to the 5 visual ROIs considered in this study) and fMRI RDMs from the Cichy et al. and BOLD5000 datasets, respectively. C depicts the model-predicted RDMs from each ROI model (V1-VO, center) as well as the fMRI RDMs of 'EVC' (left) and 'IT' ROIs (right)

the respective fMRI datasets). RDM similarities were computed using the Kendall's  $\tau$  coefficient. As 223 shown in Supplementary Figure A.3, response-optimized model RDMs captured the representational 224 geometry of respective ROIs in these novel fMRI datasets. For e.g., early visual ROI model RDMs 225 (V1-V4) better match fMRI RDMs of early visual areas ('EVC' in Cichy et al. and 'EarlyVis' in 226 BOLD5000) and higher-order ROI model RDMs (LO and VO) better match fMRI RDMs of higher-227 order visual areas ('IT' in Cichy et al. and 'LOC' in BOLD5000). This can also been qualitatively 228 in the model-predicted and fMRI RDMs for the Cichy et al. dataset (Supplementary Figure A.3C). 229 Importantly, we also had access to the measured responses in NSD participants to the restricted 230 BOLD5000 image set since the same stimuli were also shown to NSD participants. This enabled us 231 to compare subject-averaged measured RDMs (from observed responses of NSD participants) against 232 233 BOLD5000 observed RDMs. Intriguingly, this agreement against observed BOLD5000 RDMs was greater with *predicted* than *measured* NSD responses, likely highlighting the denoising quality of 234 encoding models (Figure A.3B). Further, the model-predicted RDM similarity follows the same 235 pattern as NSD-measured RDM similarity across ROIs, suggesting that the models indeed capture 236 features idiosyncratic to each visual ROI. 237

We also assesses model generalization to a challenging new fMRI dataset, namely the Inanimate 238 239 Objects dataset from Konkle et al. ([13]). As shown in [13], current SOTA supervised and 240 unsupervised models trained on ImageNet struggle to predict voxel responses to stimuli from this dataset. This dataset comprises fMRI responses from 10 participants to 72 everyday objects. We 241 focused on responses within two high-level visual ROIs in this dataset, namely posterior occipito-242 temporal cortex (pOTC), and the anterior occipito-temporal cortex. We extracted model-predicted 243 responses from the response-optimized models of all 5 visual ROIs: [V1, V2, V4, LO, VO] to each 244 of the 72 images in this dataset to construct the model representational space. Model-brain match 245 in this dataset was then measured using a voxelwise encoding RSA (veRSA) procedure, following 246 the same protocol described in 13 for consistency. Performance of competing models, namely 247 (i) a Supervised ImageNet-trained model and (ii) a self-supervised ImageNet-trained model, called 248 instance-prototype contrastive learning (IPCL) with an AlexNet architecture was already reported 249 in the main paper describing this dataset  $\begin{bmatrix} 13 \end{bmatrix}$  and is included in Supplementary Figure A.4 for 250 comparison. As shown in Supplementary Figure A.4, response-optimized models of high-level 251 visual ROIs (and not early visual ROIs) perform on par with these SOTA models in predicting neural 252 responses in both the high-level visual ROIs (pOTC and aOTC), serving as another useful model 253 class for studying high-level visual cortical representations. 254



Figure A.4: *Generalization to the Konkle et al. Inanimate Objects dataset* assessed with voxel-wise encoding RSA as described in [13]. Performance numbers for competing models (Supervised (ImageNet), IPCL (ImageNet)) as well as the noise ceiling are taken directly from the values reported in the main paper (details provided in [13].)

# 255 B.3 Models retain signatures of voxel-level idiosyncracies

We correlated the predicted response of every voxel (from the proposed response-optimized model) 256 against the measured response of every other voxel (across all 4 subjects in the main study) in each 257 ROI to obtain a voxel identifiability matrix per ROI. Visualizing this matrix helps us assess whether the 258 models indeed captured meaningful voxel-level idiosyncracies. We note that all response-optimized 259 models retain signatures of individual voxel-level idiosyncracies as indicated by the prominent 260 diagonal nature of the *voxel identifiability matrices* (Supplementary Figure A.5); this illustrates that 261 the predicted response for a voxel best matches the measured response for the same voxel in the same 262 subject. This enables us to perform population-level analysis with these predictive models. 263

# 264 B.4 Variability in voxel response predictivity is driven by the noise ceiling

We visualized the raw predictive accuracy (R) for every voxel, as achieved using the proposed response-optimized model, against that voxel's corresponding noise ceiling to see if there was a systematic trend. We observed that a large proportion of the variance in predictive accuracy across voxels is driven by their noise ceiling, as shown in Supplementary Figure [A.6].

# 269 B.5 Quantifying the complexity of synthesized images

We measured the complexity of synthesized images optimized to maximally activate individual voxels (as shown in Figure 4A) using a measure based on compression ratios, that was previously adopted to quantify complexity of synthesized images 14. Briefly, this metric, based on the discrete cosine transform, estimates the minimum number of coefficients (corresponding to different spatial frequencies) needed to accurately reconstruct an image, which in turn indicates the 'compressibility' (or inversely, complexity) of the image. We quantified the complexity of all images in Figure 4A as



Figure A.5: *Voxel identifiability matrix* for every ROI is computed by correlating the predicted response for every voxel against the measured response of every other voxel in that ROI. To account for higher variability in measured versus predicted responses, we normalize the rows and columns of this correlation matrix.



Figure A.6: Each scatter plot depicts the raw prediction accuracy (R) for all voxels (obtained using the proposed response-optimized model) belonging to one of the five ROIs against their corresponding noise ceiling.

the inverse of their respective compression ratios and found that the complexity does indeed increase along the ventral visual hierarchy [A.3].

We also extracted the top 3 natural images among the THINGS database ( $\sim 27,000$  images) that produce the highest predicted response for each V1 or VO voxel (the two ends of the hierarchy) visualized in Figure [4]A. The natural images contain similar featural configurations as their corresponding synthesized counterparts [A.7] the natural images for V1 voxels contain objects at specific orientations or high frequency spatial patterns reminiscent of the orientation preferences visible in the synthesizes images, whereas the images for VO contain complex shapes like concentric circles, rectangles and hexagons, again in agreement with their respective synthesized images.

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### 286 B.6 Human behavioral data from 'nsdmeadows'

We also employ the T-distributed Stochastic Neighbor Embedding (t-SNE) algorithm to visualize human behavioral data from the 'nsdmeadows' experiment where NSD participants performed a Multiple arrangement Task [1]. Supplementary Figure A.9 depicts the t-SNE visualization of the mean pairwise dissimilarity matrix across all 8 NSD subjects. The pairwise dissimilarity matrix (RDM) for



Figure A.7: **A** and **B** show the synthesized and natural images (among the THINGS database) that most highly activate each of the 4 individual voxels visualized in Figure  $\frac{1}{4}$ A, belonging to V1 and VO, respectively. The natural images are reminiscent of the patterns in their corresponding synthesized counterparts. For V1 voxels, we also visualize the Gabor filter (among a filter bank of 4 sine and cosine gabors) that produces the highest model-predicted response for each voxel.

Model ROI	Complexity
V1	0.439+/-0.041
V2	0.433+/-0.012
V4	0.449+/-0.034
LO	0.536+/-0.079
VO	0.637+/-0.012

Table A.3: Complexity of the synthesized images for each visual region.



Figure A.8: **pRF estimation with task-optimized CORnet-S encoding models**. A Scatter plots showing predicted and localizer-estimated retinotopic parameters for all voxels in all 4 subjects. Inset correlations are computed using voxels from all 4 subjects. C Agreement between estimated and measured retinotopic maps as a function of training examples (stimulus-response pairs) from novel subjects used to train their linear readout. Error bars depict the 95% CI around estimated mean.





each participant was released with NSD. We see that even qualitatively, pairwise similarities from
 human behavioral data appear remarkably similar to pairwise similarities estimated from model predicted VO responses (shown in the main text Figure 5A); in both cases, faces and scenes appear
 clustered together. This is in contrast to the pairwise similarities estimated from model-predicted V1
 responses, as shown below in Supplementary Figure [A.10]

### 296 C Supplemental Discussion

#### 297 C.1 Relationship to concurrent work

Concurrent with the present work, recent papers [15, 16] have demonstrated that when trained with 298 large amounts of data such as NSD, the response-optimization approach can perform competitively 299 with state-of-the-art task-optimized models. Khosla et al. [16] adopt similar neural network ar-300 chitectures and compare asymptotic performance and sample complexity in models of specialized 301 302 category-selective regions of the brain, such as FFA and EBA, and do not study the ventral visual 303 cortical hierarchy (the ROIs investigated in this study). St. Yves et al. [15] study the early to intermediate visual cortex (V1-V4), specifically the role played by the brain hierarchy in training 304 brain-optimized models that are not hierarchical by design, presenting alternate evidence against 305 the hierarchical nature of neural representations. Our work differs from these studies in several 306 respects: (i) We develop models for regions along the *entire* ventral visual hierarchy, including 307 higher-order ROIs like LO and VO (the human analogues of IT). (ii) We study the generalization 308 of response-optimized models to datasets beyond NSD and compare against a richer battery of 309 task-optimized models. (iii) We demonstrate the denoising capability of models, showing that the 310 predicted activity not only serves as a useful surrogate for the measured activity, but also yields a 311 better match to neural data in other datasets and human behavior. (iv) While St. Yves et al. [15] also 312 313 demonstrate the ability of response-optimized models to recover the retinotopic organization in early visual cortex, they do so at the qualitative level of capturing size-eccentricity relationships. In the 314 present study, we perform rigorous quantitative comparisons and sample complexity analysis on the 315 ability of response-optimized models to capture the precise spatial receptive field tuning of individual 316 voxels. (v) St. Yves et al. [15] focus on network architectures and ask if hierarchy, at the level of 317





model architecture, is needed to explain brain activity. Here, on the other hand, we ask: what features 318 emerge spontaneously in networks optimized to explain brain activity and what kinds of biases do 319 these networks exhibit (shape v/s texture)? We demonstrate increasing separability of categorical 320 information and alignment with human perception in the optimized models of ventral visual visual 321 stream regions, providing a model abstraction of this key neural phenomenon. In the future, we 322 hope these can be richly interrogated to generate mechanistic hypotheses. The strong shape bias in 323 response-optimized, but not task-optimized models, further has interesting implications for computer 324 vision models. Altogether, these studies and our work invite a shift from the task-optimized modeling 325 326 framework, providing an alternate modeling strategy to understand neural representations.

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