Unveiling The Mask of Position-Information Pattern Through the Mist of Image Features

A Implementation Details

2 A.1 Architecture and Feature Alignments

VGG19	Regular Padding	Optimal Padding Feature Size (Fo) Principal Point (Po)	Top/Left Margin = Po-Pr	Feature Alig <u>Bottom/Right Margin</u> = Fo - (Po-Pr) - Fr	nment PPP Alignment
Input Crop	460x460				
2 x Conv2d(k=3, s=1)		460x460 (229.5, 229.5)	118	118	
MaxPool2d(k=2, s=2)					
2 x Conv2d(k=3, s=1)					1st Layer of Intere
MaxPool2d(k=2, s=2)			56	56	FR - FO[56:-56, 56:-56]
4 x Conv2d(k=3, s=1)	50x56 (27.5, 27.5)				2nd Layer of Intere
MaxPool2d(k=2, s=2)			24		FR - FO[24:-24, 24:-24]
4 x Conv2d(k=3, s=1)					3rd Layer of Intere
MaxPool2d(k=2, s=2)					FR – FO[8:-8. 8:-8]
4 x Conv2d(k=3, s=1)					4th Layer of Intere
AdaptiveAvgPool2d	14x14 (6.5, 6.5)	14x14 (6.5, 6.5)			FR – FO

ResNet50	Regular Padding	Optimal Padding	Feature Alignment		
	Feature Size (Fr) Principal Point (Pr)	Feature Size (Fo) Principal Point (Po)	$ \underline{ \textbf{Top/Left Margin}}_{= Po \cdot Pr} \underline{ \textbf{Bottom/Right Margin}}_{= Fo \cdot (Po \cdot Pr) \cdot Fr} $	PPP Alignment	
Input Crop	613x613				
Conv2d (k=3, s=2)	224x224 (96, 96)		209 180 +		
MaxPool2d(k=2, s=2)	112x112 (48, 48)	306x306 (152, 152)			
ResBlock(k=3, s=1)	56x56 (24, 24)	153x153 (76, 76)			
2 x ResBlock(k=3, s=1)	56x56 (24, 24)			1st Layer of Interest	
ResBlock(k=3, s=2)	56x56 (24, 24)		49 42 4	FR - FO[49:-42, 49:-42]	
3 x ResBlock(k=3, s=1)				2nd Layer of Interest	
ResBlock(k=3, s=2)	28x28 (12, 12)	67x67 (33, 33)		FR - FO[21:-18, 21:-18]	
5 x ResBlock(k=3, s=1)	14x14 (6, 6)			3rd Layer of Interest	
ResBlock(k=3, s=2)	14x14 (6, 6)			FR - FO[5:-4. 5:-4]	
2 x ResBlock(k=3, s=1)				4th Layer of Interest	
AdaptiveAvgPool2d	7x7 (3, 3)	7x7 (3, 3)		FR – FO	
	1X1				

Figure 1: The architecture for VGG19 and ResNet50 used in the paper. We mark the calculation of optimal padding in orange arrows and principal point in blue arrows. We label the layers of interest that are used in the paper. The red [†] indicates where a principal point shift is identified.

Submitted to 36th Conference on Neural Information Processing Systems (NeurIPS 2022). Do not distribute.



Figure 2: **The architecture for EfficientNet used in the paper.** We mark the calculation of optimal padding in orange arrows and principal point in blue arrows. We label the layers of interest that are used in the paper. The red † indicates where a principal point shift is identified.

3 A.2 PPP Feature Misalignment

There are several pitfalls in visualizing and quantifying PPP. We identify two critical pitfalls from
 the architectures we implemented. However, these may not be sufficient to cover all potential issues

6 while integrated into other architectures. Therefore one must be alerted to any unusual behavior

7 (e.g., Figure 2(d) in the main paper) throughout their implementation.

Principal point shifting. Conv2d has a hidden behavior that few people are aware of, the operation 8 is one-pixel skewed while applying a stride-two Conv2d on even-shaped features. To understand how 9 does the one-pixel shift happen, we first define the principal point of a feature map. We first define the 10 principal point of the last feature map as the center pixel (note that we define it as the middle-point 11 between the center-two pixels in case the last feature size is even). Then, we recursively define the 12 principal point of the (N-1)-th layer as the pixel that positions at the center of the Conv2d receptive 13 field that mainly forms the principal point of the N-th layer. In the case of optimally-padded features, 14 the principal points in every layer are the center of the feature map. But, as shown in Figure 2(a), 15 the principal point of algorithmically-padded features will have a one-pixel shift when a stride-2 16 convolution is applied to even-shaped features, which can be further amplified as more layers stack up. 17 Such a skew causes the principal points of algorithmically-padded features shift several pixels away 18 from the principal points of optimally-padded features. As PPP metrics use pixel-wise subtraction to 19 distinguish the image content from PPP, the misalignment becomes a critical issue, since the image 20 contents are no longer aligned and subtractable. 21

In Figure 1 and Figure 2, we show the procedure of calculating the principal point in blue arrows and marking the values impacted by principal point shift with red \dagger . For the ResNet50 architecture, the principal point shift accumulates to 16(=224/2-96) pixels in the early layers.

Fortunately, such a displacement can be fixed by adding corrections to how we calculate the feature margins. As shown in Figure 2(b), the concept of the margin correction is to make the two principal points overlapping each other after adding the margin. In the example, the left-right margins are
corrected to (209, 180) (instead of the more intuitive choice of (195, 194) or (194.5, 194.6)).

²⁹ We also show how the principal point shift visually looking like in Figure 2(c), notice the patterns

have right-bottom shifted 16 pixels. As shown in Figure 2(d), failing to identify the principal point
 shift will result in checkerboard artifacts while calculating PPP , and adding correction eliminates the
 artifacts.

Maxpooling misalignment. This is a hypothetical condition that may potentially happen but has not 33 been observed in the three architectures we tested. Consider a case of a Maxpooling layer of window 34 size 2 and stride 2, the sliding windows of each pooling operation have no overlap, therefore the 35 initial index of the first sliding window solely determines the spatial location of all sliding windows. 36 Accordingly, there is a chance that the initial condition of the optimally-padded features causes all of 37 its sliding windows are 1-pixel misaligned to the algorithmically-padded features. Fortunately, the 38 condition can be easily determined by calculating the top and left margin of the feature alignment 39 (similar to the aforementioned principal point shift calculation). For the case of a Maxpooling layer 40 of window size 2 and stride 2, the misalignment will not happen if the top and left margins are even 41 numbers, and that is exactly the case for both VGG19 and ResNet50, as shown in Figure ??. 42

43 A.3 Randn Padding

A critical implementation detail is that such a padding scheme must be applied before activation functions. Since the paddings are based on the distribution within sliding windows, activation functions such as ReLU, which clamps all negative values, can discard a significant amount of information beforehand. Instead of the traditional use of padding-convolution-normalization-activation, we modify the order to convolution-normalization-padding-activation. Note that such a change of order does not affect the behavior or results of other padding schemes.

50 A.4 Acknowledging Open-Source Contributors

51 Our implementation reuses codes from several open-source codebases, which greatly supports our

⁵² development. The repositories used in the paper are F-Conv [1], torchvision [2] and Pytorch-cifar [3].

B More PPP Visualizations



Figure 3: Visualization of Position-Information Pattern from Padding (PPP). The visualizations are calculated based on Eq. 3 over 480 GMap samples. The results show that the pretrained model significantly reinforces PPP compared to randomly initialized networks. Note that each image is normalized to [0, 1] separately, therefore the colors between images are not comparable.



Figure 4: Visualization of Position-Information Pattern from Padding (PPP). The visualizations are calculated based on Eq. 3 over 480 GMap samples. The results show that the pretrained model significantly reinforces PPP compared to randomly initialized networks. Note that each image is normalized to [0, 1] separately, therefore the colors between images are not comparable.



Figure 5: **Visualization of Position-Information Pattern from Padding (PPP).** The visualizations are calculated based on Eq. 3 over 480 GMap samples. The results show that the pretrained model significantly reinforces PPP compared to randomly initialized networks. Note that each image is normalized to [0, 1] separately, therefore the colors between images are not comparable.



Figure 6: Visualization of Position-Information Pattern from Padding (PPP). The visualizations are calculated based on Eq. 3 over 480 GMap samples. The results show that the pretrained model significantly reinforces PPP compared to randomly initialized networks. Note that each image is normalized to [0, 1] separately, therefore the colors between images are not comparable.

54 **References**

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