THE FAIRNESS-ACCURACY LANDSCAPE OF NEURAL CLASSIFIERS

Anonymous authors

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Abstract

That machine learning algorithms can demonstrate bias is well-documented by now. This work confronts the challenge of bias mitigation in feedforward fullyconnected neural nets from the lens of causal inference and multiobjective optimisation. Regarding the former, a new causal notion of fairness is introduced that is particularly suited to giving a nuanced treatment of datasets collected under unfair practices. In particular, special attention is paid to subjects whose covariates could appear with substantial probability in either value of the sensitive attribute. Next, recognising that fairness and accuracy are competing objectives, the proposed methodology uses techniques from multiobjective optimisation to ascertain the fairness-accuracy landscape of a neural net classifier. Experimental results suggest that the proposed method produces neural net classifiers that distribute evenly across the Pareto front of the fairness-accuracy space and is more efficient at finding non-dominated points than an adversarial approach.

1 INTRODUCTION

There is increasing concern over the ethics of machine learning algorithms. The issue of machine bias was prominently featured in ProPublica's 2016 eponymous article (Angwin et al., 2016) where the investigation uncovered prejudice against African-Americans in COMPAS (Correctional Offender Management Profiling for Alternative Sanctions), a recidivism prediction tool developed by Northpointe.

Efforts to mitigate machine bias has received steadily increasing attention from stakeholders in a wide array of arenas including academia, industry research labs, and advocacy groups. A number of works focus on defining the very concept of fairness (Dwork et al., 2012; Chouldechova, 2016; Joseph et al., 2016). But given its nascent nature, there is no single agreed-upon definition of fairness in the algorithmic fairness community. For instance, Corbett-Davies et al. (2017) and Dieterich et al. (2016) argue that COMPAS is indeed fair with respect to certain fairness notions. Works such as Hardt et al. (2016) and Kleinberg (2018) have shed light on this apparent contradiction by showing that certain fairness criteria cannot be simultaneously satisfied.

Most works in algorithmic fairness attempt to answer the question "is the algorithm unfair?" and then to find ways to impose constraints that can make the algorithm more fair (Hardt et al., 2016; Joseph et al., 2016; Zafar et al., 2017b;a). Recent works can handle very complex algorithms such as neural networks (Beutel et al., 2017; Wadsworth et al., 2018; Madras et al., 2018; Manisha & Gujar, 2018). However none of the works in the literature can give a holistic view of the fairness-accuracy landscape of the algorithm.

What we mean is this, while it is desirable that the neural network maintain high predictive accuracy while simultaneously remaining fair with regards to a sensitive variable, these two objectives often compete. Given this, it is essential to cast the balancing act between fairness and accuracy as a multi-objective optimisation task and look at the fairness-accuracy *Pareto front*. This can give a bird's eye view of the algorithm and can be useful for comparing two algorithms based on, say, the "volume" of the Pareto front (Li et al., 2015). In this work, we propose a methodlogy for estimating the fairness-accuracy Pareto front of a feedforward fully-connected network.

Contributions This is the first work in algorithmic fairness that specifically addresses estimation of the fairness-accuracy Pareto front of a feedforward network. The framework presented is flexible

enough to allow for user-supplied accuracy and fairness measures. Although the framework is general, we will investigate one particular fairness notion. Namely, we introduce a causal measure of fairness which emphasises subjects with the most overlap in observed covariates across the different values of a sensitive attribute. The motivation for doing this is to avoid selection bias in the datasets we typically observe in algorithmic fairness. Furthermore, the methodology can be used to enforce fairness in all intermediate representations of the neural network. This has potential benefits for downstream tasks that may involve transfer learning.

2 Related work

In this section, we review the broad categories of existing methods in algorithmic fairness. The major discernible classes of fair learning methods can be trifurcated according to the stage during which action is taken. The first class of methods attempts to remove bias from the input data itself. These methods rest on the premise that once proper preprocessing is accomplished, any classifier can be used to subsequently produce fair predictions (Kamiran & Calders, 2012; Feldman et al., 2015; Calmon et al., 2017; Johndrow & Lum, 2019), among others.

Then there are methods that directly intervene at the stage of training the learning algorithm. Many of these methods are specific to certain classifiers and certain notions of fairness. Generally speaking, train-time methods minimise predictive error while enforcing some fairness constraint (Agarwal et al., 2018; Narasimhan, 2018; Zafar et al., 2017a;b;c; Kamishima et al., 2011; Calders & Verwer, 2010; Bechavod & Ligett, 2017).

Our proposed methodology falls into this category. However, rather than placing fairness constraints on the output of the classifier, our method nudge internal representations in the neural network to be less biased. In this way, it's almost as if we are performing a sequence of supervised pre-processing to the input data, one in each layer of the neural net. This is in contrast to agnostic pre-processing that is performed in the preprocessing methods.

Another class of methods that operate at train time employs concepts from adversarial learning. These include Beutel et al. (2017) and Ganin et al. (2016) in which hidden layers are encouraged to promote fairness. The adversarial approach to fairness can also involve an adversary that tries to predict the sensitive attribute from the output of the predictor in (Wadsworth et al., 2018; Zhang et al., 2018).

Finally, post-processing techniques directly operate on the classifier output and are amenable to any classifier. The technique in Hardt et al. (2016) for instance seeks to learn a monotone transformation of the classifier's output to remove unfairness with regard to either demographic parity or equalised odds.

3 THE FAIRNESS-ACCURACY PARETO FRONT

This section introduces the fairness-accuracy Pareto front of a general learning algorithm which attempts to learn an accurate mapping while also remaining fair with respect to a sensitive attribute. Suppose the inputs live in some space \mathbb{X} , the sensitive attribute in \mathbb{A} , and the responses in \mathbb{Y} . Let $(\mathbb{X}, \mathbb{A}, \mathbb{Y})$ be a measurable space and P be a probability measure on it. Let \mathcal{F} be a class of functions from \mathbb{X} to \mathbb{Y} . Given a loss function $\mathcal{L} : \mathbb{Y} \times \mathbb{Y} \to \mathbb{R}$, we may define the expected loss, $R(f; P) = \mathbb{E}_{(\mathbf{x}, \mathbf{a}, \mathbf{y}) \sim P} \mathcal{L}(f(\mathbf{x}), \mathbf{y})$, also known as the risk.

Suppose \mathcal{F} is chosen to be the family of functions $f_{\theta} : \mathbb{X} \to \mathbb{Y}$ parametrised by a deep feedforward fully-connected neural network with parameters $\theta \in \Theta$. For a probability measure P on $(\mathbb{X}, \mathbb{A}, \mathbb{Y})$, define $R(\theta; P) = R(f_{\theta}; P)$. Let $U(\theta; P)$ be a measure of the *unfairness* of f_{θ} , in a manner to be made precise in Section 4. Since we wish for the learning algorithm f_{θ} to be both accurate and fair, we wish to minimise, over θ , the *vector* objective function

$$\begin{bmatrix} R(\theta; P) \\ U(\theta; P) \end{bmatrix}.$$
 (1)

Unfortunately, the situation is made difficult by the fact that classification accuracy and fairness are often competing objectives. Take for instance the extreme of performing classification completely at random, then the resulting classifier will certainly be fair with respect to the sensitive attribute, by

almost all measures of fairness. The other extreme might be a perfect classifier; but in datasets where the targets are collected in a biased way, this will result in the classifier being unfair. For instance, if police routinely target a certain group then a recidivism dataset would contain a disproportionate number of re-offenses amongst that group.

When the individual components of a vector function compete, as they do in equation 1, it is unlikely that a parameter value exists which simultaneously minimises the individual objectives. This lack of total ordering necessitates optimisation according to a *partial order*. For $a, b \in \mathbb{R}^p$, we say $a \leq b$ if and only if every component of a is less than or equal to the corresponding component of b. Suppose we have p objective functions J_1, \ldots, J_p where each is a function from the parameter space Θ to \mathbb{R} . Then $\theta \in \Theta$ is *Pareto optimal* if and only if there does not exist any $\tilde{\theta} \in \Theta$ such that $(J_1(\tilde{\theta}), \ldots, J_p(\tilde{\theta})) \leq (J_1(\theta), \ldots, J_p(\theta))$ with at least one strict inequality. The **Pareto front** is the set of all Pareto optimal points.

A basic technique for approximating the Pareto front is to first scalarise the vector objective function. Let $\lambda \in [0, 1]$. One possible scalarisation scheme for equation 1 is to minimise, with respect to θ , the convex combination $(1 - \lambda)R(\theta; P) + \lambda U(\theta; P)$. An important caveat is that scalarisation in this manner only allows for recovery of points on the *convex hull* of the Pareto front (Das & Dennis, 1997). A scalarisation scheme that avoids this issue is the so-called Chebyshev method (Ehrgott, 2000; Giagkiozis & Fleming, 2015) which results in the scalar optimisation

$$\theta^{\lambda} = \underset{\theta}{\operatorname{arg\,min}} \max\{(1-\lambda)R(\theta; P), \lambda U(\theta; P)\}.$$
(2)

The resulting set $\{\theta^{\lambda} : \lambda \in [0, 1]\}$ are members of the Pareto front and it is this set that we will attempt to approximate. The Chebyshev scalarisation enjoys many properties. It guarantees solutions that are at least *weakly Pareto optimal* for any $\lambda \in [0, 1]$. The term weakly refers to replacing the non-strict inequality in the Pareto optimal definition with a *strict* inequality. A further property of the Chebyshev scalarisation is that any Pareto optimal solution can be obtained for some λ .

Estimation of the Pareto front Now we describe a general technique for estimating the set $\{\theta^{\lambda} : \lambda \in [0,1]\}$. Let $(\mathbf{x}_1, \mathbf{a}_1, \mathbf{y}_1), \ldots, (\mathbf{x}_n, \mathbf{a}_n, \mathbf{y}_n)$ be independent copies of $(\mathbf{x}, \mathbf{a}, \mathbf{y})$ drawn from (unknown) distribution P_{model} . Define the empirical measure as $\hat{P}_{\text{data}} = \frac{1}{n} \sum_{i=1}^{n} \delta_{(\mathbf{x}_i, \mathbf{a}_i, \mathbf{y}_i)}$. Let $R(\theta; \hat{P}_{\text{data}})$ be the plug-in estimator of $R(\theta; P_{\text{model}})$, i.e. $R(\theta; \hat{P}_{\text{data}}) = \mathbb{E}_{(\mathbf{x}, \mathbf{a}, \mathbf{y}) \sim \hat{P}_{\text{data}}} L(f(\mathbf{x}), \mathbf{y}) = \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}(f(\mathbf{x}_i), \mathbf{y}_i)$. Similarly let $U(\theta; \hat{P}_{\text{data}})$ be an estimate of $U(\theta; P_{\text{model}})$, but not necessarily a plug-in estimator. Then we consider the empirical version of equation 2 to obtain $\hat{\theta}_n^{\lambda} = \arg\min_{\theta} \max\{(1 - \lambda)R(\theta; \hat{P}_{\text{data}}), \lambda U(\theta; \hat{P}_{\text{data}})\}$.

To assess the quality of our Pareto front approximation, it will be helpful to have unbiased estimators of $R(\hat{\theta}_n^{\lambda}; P_{\text{model}})$ and $U(\hat{\theta}_n^{\lambda}; P_{\text{model}})$. We are in luck if we have a testing set $\mathbb{V} = \{(\mathbf{x}_i^*, \mathbf{y}_i^*)\}$ where $(\mathbf{x}_1^*, \mathbf{y}_1^*), \dots, (\mathbf{x}_m^*, \mathbf{y}_m^*)$ are another set of independent copies of $(\mathbf{x}, \mathbf{a}, \mathbf{y})$ drawn from distribution P_{model} . Define the corresponding empirical measure as $\hat{P}_{\text{test}} = \frac{1}{m} \sum_{i=1}^m \delta_{(\mathbf{x}_i^*, \mathbf{y}_i^*)}$. The risk of $\hat{\theta}_n^{\lambda}$ can be assessed using the out-of-sample average loss $R(\hat{\theta}_n^{\lambda}; \hat{P}_{\text{test}}) = \mathbb{E}_{(\mathbf{x}, \mathbf{a}, \mathbf{y}) \sim \hat{P}_{\text{test}}} \mathcal{L}(f(\mathbf{x}; \hat{\theta}_n^{\lambda}), \mathbf{y}) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(f(\mathbf{x}_i^*; \hat{\theta}_n^{\lambda}), \mathbf{y}_i^*)$. The unfairness can be also assessed on the test set, let's denote it $U(\hat{\theta}_n^{\lambda}; \hat{P}_{\text{test}})$.

In summary, the Pareto front of $(R(\theta; P_{\text{model}}), U(\theta; P_{\text{model}}))$ will be approximated by the set $\{\hat{\theta}_n^{\lambda} : \lambda \in [0, 1]\}$. The quality of the approximation will be assessed by evaluating $\{(R(\hat{\theta}_n^{\lambda}; \hat{P}_{\text{test}}), U(\hat{\theta}_n^{\lambda}, \hat{P}_{\text{test}})) : \lambda \in [0, 1]\}$.

The appropriate loss function $R(\theta; P_{\text{model}})$ will be context-specific; since we will be interested in binary classification, we will limit future discussion to the cross entropy loss. How fairness should be defined is much more controversial. We will discuss various existing notions of fairness in the next section and advocate for a new causal measure of fairness that is especially adept at handling inherent biases in the dataset.

4 A NEW CAUSAL FAIRNESS MEASURE

Notions of fairness in the algorithmic fairness literature can be divided into two camps. On one hand, we have non-causal fairness notions which typically operate by conditioning on the levels of the sensitive variable and thus revolve around conditional distributions, e.g. $p(f_{\theta}(\mathbf{x}) | \mathbf{a} = a, \mathbf{x} = x)$. For instance, enforcing equalised odds (Hardt et al., 2016) on a classifier amounts to enforcing two conditional distributions are the same.

Taking the causal approach means replacing the question "is the learning algorithm (conditionally) dependent on the sensitive attribute?" with the question "does the sensitive attribute have a *causal effect* on the algorithm's predictions?" In an ideal world, we could intervene on the sensitive attribute by manipulating their values in an experiment and recording the outcomes. Causal inference is designed to handle situations where this direct intervention is not possible. In particular, causal inference tools attempt to glean causal effects from observational data. The tools are based on posing hypothetical questions about counterfactuals or potential outcomes: "what would have been the prediction outcome in a parallel universe where the only thing that changed about this subject was the value of the sensitive attribute?"

Let us first review some existing notions of fairness before introducing our new causal measure. In the non-causal category, two fundamental definitions of fairness are demographic parity and conditional parity. The classifier $f_{\theta}(\mathbf{x})$ is said to exhibit **demographic parity** with the sensitive attribute a if $f_{\theta}(\mathbf{x}) \perp \mathbf{a}$, where the shorthand \perp means independence. Intuitively, demographic parity assesses if the predicted score does not depend on the sensitive variable. For example, a classifier predicting if a convicted criminal will re-offend exhibits demographic parity with respect to race if the distribution of $f_{\theta}(\mathbf{x})$ is the same irrespective of race. The drawbacks to demographic parity are well-documented (Hardt et al., 2016; Kleinberg, 2018). Essentially, when the base rates differ across values of the sensitive attribute, satisfying demographic parity can come at the cost of discrimination.

A more flexible framework of fairness is given by conditional parity, a term coined in Ritov et al. (2017). Let u be a random vector. The prediction score $f_{\theta}(\mathbf{x})$ is said to exhibit **conditional parity** with sensitive attribute a conditional on u if $f_{\theta}(\mathbf{x}) \perp \mathbf{a} \mid \mathbf{u}$. Under the umbrella of conditional parity, Ritov et al. (2017) unified various measures of fairness. For instance, the notion of equalized odds, introduced in Hardt et al. (2016), is recovered by setting u to the true target class membership itself.

Intuitively, conditional parity asks for class predictions that are independent of the sensitive variable a conditioned on **u**. For example, one could consider a classifier predicting if an applicant should be admitted to graduate school. Here, one may desire admission decisions generally independent of sex (demographic parity), or, for conditional parity, independent of sex *conditional* on a particular university department. That the notions of demographic and conditional parity can strongly differ and may lead seemingly paradoxical results was strikingly illustrated in Bickel et al. (1975) for graduate admissions at UC Berkeley.

4.1 CAUSAL FAIRNESS IN THE OVERLAP POPULATION

We have seen that satisfying demographic parity can come at the cost of discrimination. On the other hand, conditional parity concepts such as equalised odds can be problematic if the labels in the training set are biased themselves. In response to these issues, a growing line of work employs causal notions of fairness (Kusner et al., 2017; Kilbertus et al., 2017; Khademi et al., 2019). A good review on causal inference tools for algorithmic fairness can be found in Loftus et al. (2018).

Our approach differs from previous works mainly in the causal estimand we use. We also note that we do not make use of structural equation models. Our new causal fairness notion is based on the weighted average treatment effect (WATE) (Hirano et al., 2003) which derives its name from the fact that in many situations due to selection bias, the study population may be different from the target population. Then, to make valid causal inference, we might weight the samples according to the covariate distributions of the target population. Specifically, WATE is a class of causal estimands

parametrised by a function $g: \mathbb{R}^p \to \mathbb{R}$ as follows

$$\tau_g(\mathbf{h}) = \frac{\mathbb{E}_{(\mathbf{x}, \mathbf{a}, \mathbf{y}) \sim P_{\text{model}}}[g(\mathbf{x})(\mu_1(\mathbf{x}) - \mu_0(\mathbf{x}))]}{\mathbb{E}_{(\mathbf{x}, \mathbf{a}, \mathbf{y}) \sim P_{\text{model}}}[g(\mathbf{x})]}$$
(3)

where $\mu_1(x) = (\mathbf{h}(1) | \mathbf{x} = x)$ and $\mu_0(x) = \mathbb{E}(\mathbf{h}(0) | \mathbf{x} = x)$. This form reveals WATE is indeed a measure of the causal effect in the target population specified by g(x). Note when g(x) = 1for all values of x, WATE reduces to the standard conditional average treatment effect (CATE), $\tau_{CATE} = \mathbb{E}_{(\mathbf{x},\mathbf{a},\mathbf{y})\sim P_{\text{model}}}(\mathbf{h}(1) - \mathbf{h}(0) | \mathbf{x} = x)$.

Henceforth, we focus our discussion on the case when g(x) = e(x)(1 - e(x)) where

 $e(x) = P(\mathbf{a} = 1 \mid \mathbf{x} = x)$

is also known as the propensity score. The propensity score is typically understood to be the probability of *treatment* given the covariate **x**. (Recall in our case, the sensitive variable **a** plays the role of treatment.) The WATE corresponding to g(x) = e(x)(1-e(x)) shall be called the *average treatment effect for the overlap population* (ATO) after Li et al. (2018a) who introduced the terminology. The ATO articulates the causal effect among the **overlap population** which consists of subjects whose covariates could appear with substantial probability in either value of the sensitive attribute.

We will use WATE to measure and then penalise the causal link between the sensitive attribute and an intermediate representation of the neural network. Suppressing the dependence on the layer, let **h** denote values in the hidden layer. Note **h** is itself a function of $(\mathbf{x}, \mathbf{a}, \mathbf{y})$. Adopting the potential outcome framework of Imbens & Rubin (2015), each intermediate representation **h** takes on one of two potential outcomes, $\mathbf{h}(0)$, $\mathbf{h}(1)$ depending on whether $\mathbf{a} = 0$ or $\mathbf{a} = 1$. Note that $\mathbf{h} = \mathbf{ah}(1) + (1 - \mathbf{a})\mathbf{h}(0)$, i.e. we can only ever observe one of the two potential outcomes.

Let $\hat{e}(x)$ be an unbiased estimator of the propensity score function; the estimation will be discussed further in the next section. An unbiased estimator of the ATO (Li et al., 2018b) based on $\{(\mathbf{x}_i, \mathbf{a}_i, \mathbf{h}_i)\}_{i=1}^n$ is

$$\hat{\tau}_{ATO}(\mathbf{h}) = \frac{\sum_{i=1}^{n} \mathbf{a}_{i} \mathbf{h}_{i} w_{i}}{\sum_{i=1}^{n} \mathbf{a}_{i} w_{i}} - \frac{\sum_{i=1}^{n} (1 - \mathbf{a}_{i}) \mathbf{h}_{i} w_{i}}{\sum_{i=1}^{n} (1 - \mathbf{a}_{i}) w_{i}}$$
(4)

where w_i are the so-called overlap weights (Li et al., 2018a) given by

$$w_i = \begin{cases} 1 - \hat{e}(\mathbf{x}_i) & \text{if } \mathbf{a}_i = 1\\ \hat{e}(\mathbf{x}_i) & \text{if } \mathbf{a}_i = 0. \end{cases}$$

Overlap weights derive their name from an emphasis on subjects with the most overlap in observed covariates x across the treatments (in our case the treatment is the sensitive attribute). The weights smoothly down-weight subjects in the tails of the propensity score distribution.

5 METHODOLOGY

In this section, we present a methodology for approximating the fairness-accuracy Pareto front of a feedforward fully-connected neural net classifier. The available data include a single binary sensitive variable a, input variables $\mathbf{x} \in \mathbb{R}^p$, and binary response \mathbf{y} indicating class membership. The input \mathbf{x} is further standardised to mean 0 and variance 1. All discrete variables are dummy encoded.

To define a multi-layer feedforward fully-connected neural network with L layers, let $w^{(l)} \in \mathbb{R}^{m_l \times m_{l-1}}$ and $b^{(l)} \in \mathbb{R}^{m_l}, l = 1, \ldots, L$ be the parameters in the *l*-th layer. Let $h^{(l)} : \mathbb{R}^{m_{l-1}} \to \mathbb{R}^{m_l}$ be the affine transformation

$$h^{(l)} = w^{(l)}v^{(l-1)} + b^{(l)}, l = 1, \dots, L$$

where $v^{(0)} = id$ is the identity function and $m_0 = p$. The activation function $\sigma^{(l)} : \mathbb{R}^{m_l} \to \mathbb{R}^{m_l}$ is applied to obtain

The activation function in the final layer, $\sigma^{(L)}$, is restricted to the sigmoid function since we wish the classifier to output scores between 0 and 1. We use the ReLU activation function in all other layers for our experiments. Let $\mathbf{h}_{i}^{(l)}$ be shorthand for the application of the function $h^{(l)}$ to input feature \mathbf{x}_{i} ,

i.e. $\mathbf{h}_i^{(l)} = h^{(l)}(\mathbf{x}_i)$. Collect all parameters $w^{(l)}$ and $b^{(l)}$ for l = 1, ..., L into the parameter vector θ . The multi-layer feed-forward neural network is simply the function $f_\theta : \mathbb{R}^p \to [0, 1]$ given by $f_\theta(x) = v^{(L)}(x)$.

We will employ the binary cross-entropy loss $\mathcal{L} : [0,1] \times \{0,1\} \to \mathbb{R}$ given by $\mathcal{L}(\hat{y},y) = y \log \hat{y} + (1-y) \log(1-\hat{y})$. For this loss, the risk becomes $R(\theta; P_{\text{model}}) = -\mathbb{E}_{(\mathbf{x},\mathbf{a},\mathbf{y})\sim P_{\text{model}}}(\mathbf{y} \log f_{\theta}(\mathbf{x})) + (1-\mathbf{y}) \log(1-f_{\theta}(\mathbf{x})))$.

Our object of interest is to determine, for the feedforward fully-connected network f_{θ} , the fairness-accuracy Pareto front associated to the (unknown) vector objective function

$$\begin{pmatrix} R(\theta; P_{\text{model}}) \\ U(\theta; P_{\text{model}}) \end{pmatrix} = \begin{pmatrix} -\mathbb{E}_{(\mathbf{x}, \mathbf{a}, \mathbf{y}) \sim P_{\text{model}}}(\mathbf{y} \log f_{\theta}(\mathbf{x})) + (1 - \mathbf{y}) \log(1 - f_{\theta}(\mathbf{x}))) \\ \tau_{ATO}(f_{\theta}(\mathbf{x})) \end{pmatrix}.$$
(5)

The first component measures classification error while the second component determines unfairness with respect to the ATO measure. (We would like both components to have low values.) To estimate the Pareto front of equation 5, we will use the strategy laid out in Section 3. Namely, we estimate each component of equation 5, scalarise the vector objective function using the Chebyshev method, and finally optimise the scalarised objective.

Estimation of $R(\theta; P_{\text{model}})$ is straightforward; we simply use the plug-in estimator $R(\theta; \hat{P}_{\text{data}}) = -\frac{1}{n} \sum_{i=1}^{n} [\mathbf{y}_i \log f_{\theta}(\mathbf{x}_i) + (1 - \mathbf{y}_i) \log(1 - f_{\theta}(\mathbf{x}_i))]$. Now we turn our attention to estimating $\tau_{ATO}((f_{\theta}(\mathbf{x})))$, the average effect of the sensitive attribute on the prediction for the overlap population. To achieve a low value for $\tau_{ATO}((f_{\theta}(\mathbf{x})))$, we could directly constrain the network to learn final predictions with low ATO. However, it may be preferable to penalise the ATO in the hidden layers of the network. This way, downstream analyses that involve transfer learning are also safeguarded against bias. See the exposition in Madras et al. (2018) for further benefits of learning fair internal representations. To keep the notation simple, let's say we penalise the hidden units in the some layer l. We then calculate the ATO in that layer to obtain

$$U(\theta; \hat{P}_{\text{data}}) = \left| \hat{\tau}_{ATO}(\mathbf{h}^{(l)}) \right| = \left| \frac{\sum_{i=1}^{n} \mathbf{a}_{i} \mathbf{h}_{i}^{(l)} (1 - \hat{e}(\mathbf{x}_{i}))}{\sum_{i=1}^{n} \mathbf{a}_{i} (1 - \hat{e}(\mathbf{x}_{i}))} - \frac{\sum_{i=1}^{n} (1 - \mathbf{a}_{i}) \mathbf{h}_{i}^{(l)} \hat{e}(\mathbf{x}_{i})}{\sum_{i=1}^{n} (1 - \mathbf{a}_{i}) \hat{e}(\mathbf{x}_{i})} \right|$$
(6)

We use the set $\{\hat{\theta}_n^{\lambda} : \lambda \in [0, 1]\}$ to approximate the Pareto front associated to equation 5 where

$$\hat{\theta}_{n}^{\lambda} = \operatorname*{arg\,min}_{\theta} \max\{(1-\lambda)R(\theta;\hat{P}_{\mathrm{data}}), \lambda U(\theta;\hat{P}_{\mathrm{data}})\}.$$
(7)

Ideally, we would finely sample λ in [0, 1]. However, the computational burden of solving equation 7 increases accordingly. Thus in situations where only a coarse grid of λ 's is possible, we have to make a decision which λ 's to sample from [0, 1]. It turns out that evenly distributed λ 's in the interval [0, 1] can often produce solutions that form clumps on the Pareto front, i.e. evenly distributed λ 's in [0, 1] do *not* produce evenly distributed points in the multi-objective space. Future work might seek to adaptively select the λ 's by implementing methods such as the Normal-Boundary-Interactive Das & Dennis (2000).

We also found it necessary to make sure the two terms are comparable in scale, we standardised each term as follows. First, we ran the optimisation for $\lambda = 0$ and recorded the minimum R_{min} and maximum R_{max} of $R(\theta; \hat{P}_{data})$. Similarly we then ran the optimisation for $\lambda = 1$ to obtain U_{min} and U_{max} . The we standardised by $(R - R_{min})/(R_{max} - R_{min})$ for the expected loss and similarly for the unfairness measure.

Evaluation Suppose we have available to us a testing set $\{(\mathbf{x}_i^*, \mathbf{a}_i^*, \mathbf{y}_i^*)\}_{i=1}^m$. We assess the quality of the approximation by evaluating $\begin{bmatrix} R(\hat{\theta}_n^{\lambda}, \hat{P}_{\text{test}}) \\ U(\hat{\theta}_n^{\lambda}, \hat{P}_{\text{test}}) \end{bmatrix}$ where

$$R(\hat{\theta}_n^{\lambda}, \hat{P}_{\text{test}}) = -\frac{1}{m} \sum_{i=1}^m \left[\mathbf{y}_i^* \log f_{\hat{\theta}_n^{\lambda}}(\mathbf{x}_i^*) + (1 - \mathbf{y}_i^*) \log(1 - f_{\hat{\theta}_n^{\lambda}}(\mathbf{x}_i^*)) \right]$$
(8)

and

$$U(\hat{\theta}_{n}^{\lambda}, \hat{P}_{\text{test}}) = \left| \frac{\sum_{i=1}^{m} \mathbf{a}_{i}^{*} f_{\hat{\theta}_{n}^{\lambda}}(\mathbf{x}_{i}^{*})(1 - \hat{e}(\mathbf{x}_{i}^{*}))}{\sum_{i=1}^{m} \mathbf{a}_{i}^{*}(1 - \hat{e}(\mathbf{x}_{i}^{*}))} - \frac{\sum_{i=1}^{m}(1 - \mathbf{a}_{i}^{*}) - f_{\hat{\theta}_{n}^{\lambda}}(\mathbf{x}_{i}^{*})\hat{e}(\mathbf{x}_{i}^{*})}{\sum_{i=1}^{n}(1 - \mathbf{a}_{i}^{*})\hat{e}(\mathbf{x}_{i}^{*})} \right|.$$

We employ a neural net to estimate the propensity score e(x), the conditional probability of a for X = x. The output is then calibrated through the temperature scaling procedure of Guo et al. (2017) to provide proper probability estimates. This neural net is trained once and for all on the training set.

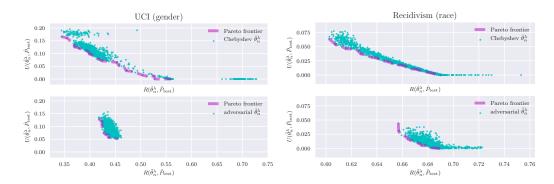


Figure 1: Each block of plots corresponds to a dataset and a sensitive attribute of interest. In all panels, we repeatedly split the data into training and testing sets, creating in total 100 sets of each. Then in each of the 100 training sets, for a collection of 15 λ 's in the interval [0, 1], we find $\hat{\theta}_n^{\lambda}$ according to the Chebyshev scalarisation scheme (left panel) and $\tilde{\theta}_n^{\lambda}$ according to the adversarial approach (right panel). The quality of the approximation is assessed using the corresponding test set. Lower values are better in both axes. Thus there are a total of 1500 learned θ 's in each plot and the magenta boundary is the Pareto frontier culled from these 1500 candidates. We can see the estimated Pareto front by the proposed methodology spans the fairness-accuracy space more than the adversarial approach.

6 EXPERIMENTS

In this section, we will apply the proposed methodology to two benchmarking datasets in the algorithmic fairness literature – the UCI adult income dataset and the ProPublica recidivism dataset. The two datasets are briefly summarised in Table 2. Missing values were pre-processed according to the accompanying code. Our goals are as follows. In the UCI dataset, we wish to predict whether an individual has income above 50,000 USD while remaining fair with respect to *gender*. Separately, we wish to perform the same prediction task while remaining fair with respect to *race*. In the recidivism dataset, we wish to predict whether an individual will recommit a crime in two years while remaining fair with respect to *race*.

We will achieve these goals by estimating the fairness-accuracy Pareto front of a binary classifier given by a feedforward fully-connected network. Note that we are conducting the analysis for the UCI dataset separately for race and gender. Future work should address fairness with respect to multiple sensitive attributes at the same time; this would require an extension of the ATO to multiple "treatments" which was suggested as feasible future work by the authors who proposed the ATO in Li et al. (2018a).

Each dataset is split into a training set and a held-out test set, with the split reported in Table 2. First, the propensity scores are estimated using a neural net. Details of the propensity score network are given in Appendix A. For the neural net architecture defining f_{θ} , the number of fully-connected layers and number of hidden nodes in each layer (held constant over the layers) were tuned for each dataset with the goal of not incurring over-fitting in the held-out test set. Each fully-connected layer is interspersed with a dropout layer with dropout probability 0.2. The resulting architecture is reported in Table 3. The ReLU activation function is used in all intermediate layers while the sigmoid function is used in the output layer.

To learn the network, we use the ADAM optimisation algorithm (Kingma & Ba, 2014). The initial learning is fixed throughout at 0.001. We reduce the learning rate when the training loss has stopped decreasing by using the ReduceLROnPlateau scheduler in PyTorch, setting the factor and patience variables to 0.9 and 10, respectively. All training took place over 500 epochs. Mini-batch size

was chosen to be around 5% of the training set size; 150 and 1000 minibatch sizes were used in the recidivism and UCI datasets, respectively.

For a given dataset and a sensitive attribute of interest, we repeatedly split the data into training and testing sets, creating in total 100 sets of each. Then, in each of the 100 training sets, we find $\hat{\theta}_n^{\lambda}$, according to equation 7, for a collection of 15 λ 's in the interval [0,1]. The quality of the approximation is assessed using the corresponding test set. Thus we produce a total of 1500 learned network parameters and each one can be plotted in the fairness-accuracy space. The left column of Figure 1 shows all 1500 $\hat{\theta}_n^{\lambda}$'s as well as the Pareto front culled from these 1500 Pareto candidates. The culling simply involves checking which of the 1500 points is dominated by any other point in the set; the Pareto front displayed in Figure 1 consists of all non-dominated points. As we sweep from the top-left corner to the bottom-right corner, we move from networks exhibiting high-accuracy-low-fairness to networks exhibiting low-accuracy-high-fairness. We also repeated this experiment by modifying the fairness measure to penalise intermediate representations in *all* layers, i.e. set $U(\theta; \hat{P}_{data}) = \sum_{i=1}^{L} |\hat{\tau}_{ATO}(\mathbf{h}^{(l)})|$, for which the results are reported and discussed in Appendix A.

Comparison to alternatives We did not find other works in the algorithmic fairness literature that address the specific task of finding the fairness-accuracy Pareto front of a feedforward neural network. Given this, we instead looked for methods where there was some type of tuning parameter that controls the trade-off between fairness and accuracy. By dialling this tuning parameter, one could hope to sweep out a set of classifiers that live in different parts of the fairness-accuracy landscape.

Given the diversity of fairness methods, due in part to the fairness definition used, we decided to implement the adversarial training technique proposed in Louppe et al. (2017) which is not based on a specific fairness criterion. The idea is intuitive; the classifier and adversarial are engaged in a zero-sum game. The classifier network, call its parameters θ_{clf} , attempts to make the best binary classification. The adversary, on the other hand, attempts to make the best prediction of the binary sensitive attribute based on the classifier's prediction. Let θ_{adv} denote the parameters of the adversarial network. The overall objective is $\tilde{\theta}_n^{\lambda} = \arg \min_{\theta_{clf}} [Loss_{\mathbf{y}}(\theta_{clf}) - \lambda Loss_{\mathbf{a}}(\theta_{clf}, \theta_{adv})]$. where the first loss measures the prediction of \mathbf{y} and the second loss measures the prediction of the sensitive attribute \mathbf{a} . Both losses were chosen to be the binary cross-entropy loss.

Our implementation of Louppe et al. (2017) is based on GoDataDriven's post on fairness in machine learning with adversarial networks. Following their choice of epochs, we alternate the following steps over 200 epochs: (1) train the adversarial network for a *single epoch*, holding the classifier network fixed and (2) train the classifier network on a *single sampled mini batch*, holding the adversarial network fixed.

Details on the adversarial network architecture are provided in Appendix A. For the classifier network, we employed the same network as above in our proposed methodology and kept all training choices, such as the optimisation algorithm and mini-batch size, the same. The classifier was pretrained for 2 epochs.

We built on top of GoDataDriven's code base the ability to sweep $\tilde{\theta}_n^{\lambda}$ over the parameter λ . The result of the adversarial approach is shown in the right column of Figure 1. Once again, using the same 100 training and testing pairs as above, we find solutions to $\tilde{\theta}_n^{\lambda}$ for a set of 15 λ 's in [0, 1], for a total of 1500 Pareto candidates. We can immediately see that compared to the proposed methodology, the adversarial is less capable of finding a Pareto front that spans the fairness-accuracy space. Furthermore, a better Pareto front estimation method should find more non-dominated points. Indeed the set of dominated (non-dominated) points in the adversarial approach is larger (smaller) relative to the proposed approach, see Table 1.

Table 1: A comparison between the proposed methodology the adversarial technique for finding the Pareto front in each of the three data settings of Figure 1. Reported are the number of *non-dominated* points. Higher is better.

	UCI (gender)	UCI (race)	Recidivism
Proposed	44	33	89
Adversarial	13	9	27

REFERENCES

- Alekh Agarwal, Alina Beygelzimer, Miroslav Dudík, John Langford, and Hanna M. Wallach. A reductions approach to fair classification. In *Proceedings of the 35th International Conference* on Machine Learning, ICML 2018, Stockholmsmässan, Stockholm, Sweden, July 10-15, 2018, pp. 60–69, 2018. URL http://proceedings.mlr.press/v80/agarwal18a.html.
- J. Angwin, J. Larson, S. Mattu, and L. Kirchner. Machine bias. ProPublica, 2016. URL https://www.propublica.org/article/ machine-bias-risk-assessments-in-criminal-sentencing.
- Yahav Bechavod and Katrina Ligett. Learning fair classifiers: A regularization-inspired approach. *CoRR*, abs/1707.00044, 2017.
- Alex Beutel, Jilin Chen, Zhe Zhao, and Ed Huai hsin Chi. Data decisions and theoretical implications when adversarially learning fair representations. *CoRR*, abs/1707.00075, 2017.
- Peter J Bickel, Eugene A Hammel, and J William O'Connell. Sex bias in graduate admissions: Data from berkeley. *Science*, 187(4175):398–404, 1975.
- Toon Calders and Sicco Verwer. Three naive bayes approaches for discrimination-free classification. *Data Mining and Knowledge Discovery*, 21(2):277–292, Sep 2010. ISSN 1573-756X. doi: 10. 1007/s10618-010-0190-x. URL https://doi.org/10.1007/s10618-010-0190-x.
- Flavio Calmon, Dennis Wei, Bhanukiran Vinzamuri, Karthikeyan Natesan Ramamurthy, and Kush R Varshney. Optimized pre-processing for discrimination prevention. In I. Guyon, U. V. Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett (eds.), Advances in Neural Information Processing Systems 30, pp. 3992– 4001. Curran Associates, Inc., 2017. URL http://papers.nips.cc/paper/ 6988-optimized-pre-processing-for-discrimination-prevention.pdf.
- Alexandra Chouldechova. Fair prediction with disparate impact: A study of bias in recidivism prediction instruments. *Big Data*, 5, 10 2016. doi: 10.1089/big.2016.0047.
- Sam Corbett-Davies, Emma Pierson, Avi Feller, Sharad Goel, and Aziz Huq. Algorithmic decision making and the cost of fairness. In *Proceedings of the 23rd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, KDD '17, pp. 797–806, New York, NY, USA, 2017. ACM. ISBN 978-1-4503-4887-4. doi: 10.1145/3097983.3098095. URL http://doi.acm.org/10.1145/3097983.3098095.
- I. Das and J. E. Dennis. A closer look at drawbacks of minimizing weighted sums of objectives for pareto set generation in multicriteria optimization problems. *Structural optimization*, 14(1): 63–69, Aug 1997. ISSN 1615-1488. doi: 10.1007/BF01197559. URL https://doi.org/ 10.1007/BF01197559.
- Indraneel Das and J Dennis. Normal-boundary intersection: A new method for generating the pareto surface in nonlinear multicriteria optimization problems. *SIAM Journal on Optimization*, 8, 07 2000. doi: 10.1137/S1052623496307510.
- William Dieterich, Christina Mendoza, and Tim Brennan. Compas risk scales: Demonstrating accuracy equity and predictive parity. Technical report, Northpointe Inc., 2016.
- Cynthia Dwork, Moritz Hardt, Toniann Pitassi, Omer Reingold, and Richard Zemel. Fairness through awareness. In *Proceedings of the 3rd Innovations in Theoretical Computer Science Conference*, ITCS '12, pp. 214–226, New York, NY, USA, 2012. ACM. ISBN 978-1-4503-1115-1. doi: 10.1145/2090236.2090255. URL http://doi.acm.org/10.1145/2090236. 2090255.
- M. Ehrgott. *Multicriteria optimization*. Lecture Notes in Economics and Mathematical Systems. Springer-Verlag, 2000.

- Michael Feldman, Sorelle A. Friedler, John Moeller, Carlos Scheidegger, and Suresh Venkatasubraan. Certifying and removing disparate impact. In *Proceedings of the 21th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, KDD '15, pp. 259–268, New York, NY, USA, 2015. ACM. ISBN 978-1-4503-3664-2. doi: 10.1145/2783258.2783311. URL http://doi.acm.org/10.1145/2783258.2783311.
- Yaroslav Ganin, Evgeniya Ustinova, Hana Ajakan, Pascal Germain, Hugo Larochelle, François Laviolette, Mario Marchand, and Victor Lempitsky. Domain-adversarial training of neural networks. J. Mach. Learn. Res., 17(1):2096–2030, January 2016. ISSN 1532-4435. URL http://dl.acm.org/citation.cfm?id=2946645.2946704.
- I. Giagkiozis and P.J. Fleming. Methods for multi-objective optimization: An analysis. Information Sciences, 293:338 – 350, 2015. ISSN 0020-0255. doi: https://doi.org/10.1016/j. ins.2014.08.071. URL http://www.sciencedirect.com/science/article/pii/ S0020025514009074.
- Chuan Guo, Geoff Pleiss, Yu Sun, and Kilian Q. Weinberger. On calibration of modern neural networks. In *Proceedings of the 34th International Conference on Machine Learning Volume* 70, ICML'17, pp. 1321–1330. JMLR.org, 2017. URL http://dl.acm.org/citation.cfm?id=3305381.3305518.
- Moritz Hardt, Eric Price, and Nathan Srebro. Equality of opportunity in supervised learning. In *Proceedings of the 30th International Conference on Neural Information Processing Systems*, NIPS'16, pp. 3323–3331, USA, 2016. Curran Associates Inc. ISBN 978-1-5108-3881-9. URL http://dl.acm.org/citation.cfm?id=3157382.3157469.
- Keisuke Hirano, Guido W. Imbens, and Geert Ridder. Efficient estimation of average treatment effects using the estimated propensity score. *Econometrica*, 71(4):1161–1189, 2003. ISSN 00129682, 14680262. URL http://www.jstor.org/stable/1555493.
- Guido W. Imbens and Donald B. Rubin. *Causal Inference for Statistics, Social, and Biomedical Sciences: An Introduction.* Cambridge University Press, New York, NY, USA, 2015. ISBN 0521885884, 9780521885881.
- James E. Johndrow and Kristian Lum. An algorithm for removing sensitive information: Application to race-independent recidivism prediction. *Ann. Appl. Stat.*, 13(1):189–220, 03 2019. doi: 10. 1214/18-AOAS1201. URL https://doi.org/10.1214/18-AOAS1201.
- Matthew Joseph, Michael Kearns, Jamie H Morgenstern, and Aaron Roth. Fairness in learning: Classic and contextual bandits. In D. D. Lee, M. Sugiyama, U. V. Luxburg, I. Guyon, and R. Garnett (eds.), Advances in Neural Information Processing Systems 29, pp. 325-333. Curran Associates, Inc., 2016. URL http://papers.nips.cc/paper/ 6355-fairness-in-learning-classic-and-contextual-bandits.pdf.
- Faisal Kamiran and Toon Calders. Data preprocessing techniques for classification without discrimination. *Knowledge and Information Systems*, 33(1):1–33, Oct 2012. ISSN 0219-3116. doi: 10. 1007/s10115-011-0463-8. URL https://doi.org/10.1007/s10115-011-0463-8.
- Toshihiro Kamishima, Shotaro Akaho, and Jun Sakuma. Fairness-aware learning through regularization approach. In *Proceedings of the 2011 IEEE 11th International Conference on Data Mining Workshops*, ICDMW '11, pp. 643–650, Washington, DC, USA, 2011. IEEE Computer Society. ISBN 978-0-7695-4409-0. doi: 10.1109/ICDMW.2011.83. URL https://doi.org/10. 1109/ICDMW.2011.83.
- Aria Khademi, Sanghack Lee, David Foley, and Vasant Honavar. Fairness in algorithmic decision making: An excursion through the lens of causality. In *The World Wide Web Conference*, WWW '19, pp. 2907–2914, New York, NY, USA, 2019. ACM. ISBN 978-1-4503-6674-8. doi: 10.1145/ 3308558.3313559. URL http://doi.acm.org/10.1145/3308558.3313559.
- Niki Kilbertus, Mateo Rojas-Carulla, Giambattista Parascandolo, Moritz Hardt, Dominik Janzing, and Bernhard Schölkopf. Avoiding discrimination through causal reasoning. In *Proceedings of the 31st International Conference on Neural Information Processing Systems*, NIPS'17, pp. 656–666, USA, 2017. Curran Associates Inc. ISBN 978-1-5108-6096-4. URL http://dl.acm. org/citation.cfm?id=3294771.3294834.

- Diederik Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *International Conference on Learning Representations*, 12 2014.
- Jon Kleinberg. Inherent trade-offs in algorithmic fairness. In Abstracts of the 2018 ACM International Conference on Measurement and Modeling of Computer Systems, SIGMETRICS '18, pp. 40–40, New York, NY, USA, 2018. ACM. ISBN 978-1-4503-5846-0. doi: 10.1145/3219617. 3219634. URL http://doi.acm.org/10.1145/3219617.3219634.
- Matt J Kusner, Joshua Loftus, Chris Russell, and Ricardo Silva. Counterfactual fairness. In I. Guyon, U. V. Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett (eds.), *Advances in Neural Information Processing Systems 30*, pp. 4066–4076. Curran Associates, Inc., 2017. URL http://papers.nips.cc/paper/6995-counterfactual-fairness.pdf.
- Fan Li, Kari Lock Morgan, and Alan M. Zaslavsky. Balancing covariates via propensity score weighting. Journal of the American Statistical Association, 113(521):390–400, 2018a. doi: 10. 1080/01621459.2016.1260466. URL https://doi.org/10.1080/01621459.2016. 1260466.
- Fan Li, Laine E Thomas, and Fan Li. Addressing Extreme Propensity Scores via the Overlap Weights. American Journal of Epidemiology, 188(1):250–257, 09 2018b. ISSN 0002-9262. doi: 10.1093/aje/kwy201. URL https://doi.org/10.1093/aje/kwy201.
- Miqing Li, Shengxiang Yang, and Xiaohui Liu. A performance comparison indicator for pareto front approximations in many-objective optimization. In *Proceedings of the 2015 Annual Conference* on Genetic and Evolutionary Computation, GECCO '15, pp. 703–710, New York, NY, USA, 2015. ACM. ISBN 978-1-4503-3472-3. doi: 10.1145/2739480.2754687. URL http://doi. acm.org/10.1145/2739480.2754687.
- Joshua R. Loftus, Chris Russell, Matt J. Kusner, and Ricardo Silva. Causal reasoning for algorithmic fairness. *CoRR*, abs/1805.05859, 2018. URL http://arxiv.org/abs/1805.05859.
- Gilles Louppe, Michael Kagan, and Kyle Cranmer. Learning to pivot with adversarial networks. In I. Guyon, U. V. Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett (eds.), Advances in Neural Information Processing Systems 30, pp. 981–990. Curran Associates, Inc., 2017. URL http://papers.nips.cc/paper/ 6699-learning-to-pivot-with-adversarial-networks.pdf.
- David Madras, Elliot Creager, Toniann Pitassi, and Richard Zemel. Learning adversarially fair and transferable representations. In Jennifer Dy and Andreas Krause (eds.), *Proceedings of the 35th International Conference on Machine Learning*, volume 80 of *Proceedings of Machine Learning Research*, pp. 3384–3393, Stockholmsmssan, Stockholm Sweden, 10–15 Jul 2018. PMLR. URL http://proceedings.mlr.press/v80/madras18a.html.
- P. Manisha and Sujit Gujar. A neural network framework for fair classifier. *CoRR*, abs/1811.00247, 2018. URL http://arxiv.org/abs/1811.00247.
- Harikrishna Narasimhan. Learning with complex loss functions and constraints. In Amos Storkey and Fernando Perez-Cruz (eds.), *Proceedings of the Twenty-First International Conference on Artificial Intelligence and Statistics*, volume 84 of *Proceedings of Machine Learning Research*, pp. 1646–1654, Playa Blanca, Lanzarote, Canary Islands, 09–11 Apr 2018. PMLR. URL http: //proceedings.mlr.press/v84/narasimhan18a.html.
- Ya'acov Ritov, Yuekai Sun, and Ruofei Zhao. On conditional parity as a notion of nondiscrimination in machine learning. *To appear in Statistical Science*, 2017.
- Christina Wadsworth, Francesca Vera, and Chris Piech. Achieving fairness through adversarial learning: an application to recidivism prediction. *CoRR*, abs/1807.00199, 2018. URL http://arxiv.org/abs/1807.00199.
- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez-Rodriguez, and Krishna P. Gummadi. Fairness constraints: Mechanisms for fair classification. In *Proceedings of the 20th International*

Conference on Artificial Intelligence and Statistics, AISTATS 2017, 20-22 April 2017, Fort Lauderdale, FL, USA, pp. 962–970, 2017a. URL http://proceedings.mlr.press/v54/zafar17a.html.

- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez Rodriguez, and Krishna P. Gummadi. Fairness beyond disparate treatment & disparate impact: Learning classification without disparate mistreatment. In *Proceedings of the 26th International Conference on World Wide Web*, WWW '17, pp. 1171–1180, Republic and Canton of Geneva, Switzerland, 2017b. International World Wide Web Conferences Steering Committee. ISBN 978-1-4503-4913-0. doi: 10.1145/3038912.3052660. URL https://doi.org/10.1145/3038912.3052660.
- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez-Rodriguez, Krishna P. Gummadi, and Adrian Weller. From parity to preference-based notions of fairness in classification. In *NIPS*, 2017c.
- Brian Hu Zhang, Blake Lemoine, and Margaret Mitchell. Mitigating unwanted biases with adversarial learning. *CoRR*, abs/1801.07593, 2018. URL http://arxiv.org/abs/1801.07593.

A APPENDIX

In this section, we provide additional details on the experiments conducted in Section 6. First, in Table 2, we summarise the datasets on which all experiments were conducted. The feedforward architecture used in the proposed methodology is given in Table 3 for each of the three data settings.

Next, we describe the neural net we employed to estimate the propensity scores $P(\mathbf{a} = 1 | X)$. We actually used the same neural net for all three data settings in Table 2. Each of the 3 fully-connected layer, with 32 hidden units each, is interspersed with a dropout layer with dropout probability 0.2. The ReLU activation function is used in all intermediate layers while the sigmoid function is used in the output layer. The cross-entropy loss is used between the estimated scores and the true labels dictated by \mathbf{a} . To learn the network, we use the ADAM optimisation algorithm (Kingma & Ba, 2014). The initial learning is fixed throughout at 0.001. Training took place over 100 epochs. Mini-batch size was chosen to be around 5% of the training set size; 150 and 1000 minibatch sizes were used in the recidivism and UCI datasets, respectively. After the propensity neural network is trained, we apply the calibration technique proposed in Guo et al. (2017) to calibrate the probability predictions. We used their GitHub code with no modification.

Figure 2 shows the additional output from the experiment that produced Figure 1 on the UCI dataset with race as the sensitive attribute. We also repeated the experiment in Section 6 by penalising the ATO in all layers. The results are shown in Figure 3. The adversarial approach we compared the proposed methodology against used a network with 4 hidden layers with 32 hidden units in each. ReLU activations were used throughout except in the final layer where the sigmoid function is used. The adversarial network was pretrained for 5 epochs. Optimisation used ADAM and minibatch sizes described in Table 2.

dataset features						
Dataset	$dim(\mathbf{x})$	binary outcome y	sensitive a	training size	testing size	minibatch size
Recidivism	12	Reoffend in 2 years?	binary race	3086	3086	150
UCI	93	Income above 50K?	binary race	15470	15470	1000
UCI	93	Income above 50K?	binary gender	15470	15470	1000

Table 2:	Dataset	descri	ptions
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	neural network features		
Dataset	layers L	hidden nodes	
Recidivism	4	4	
UCI	32	10	
UCI	32	10	

 Table 3: Network architecture

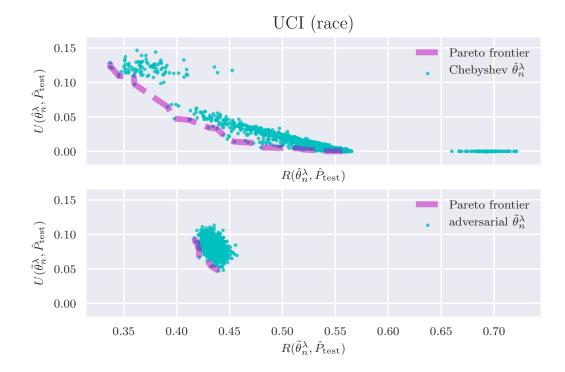


Figure 2: This reports the result for UCI (race) in the same experiment that produced Figure 1.

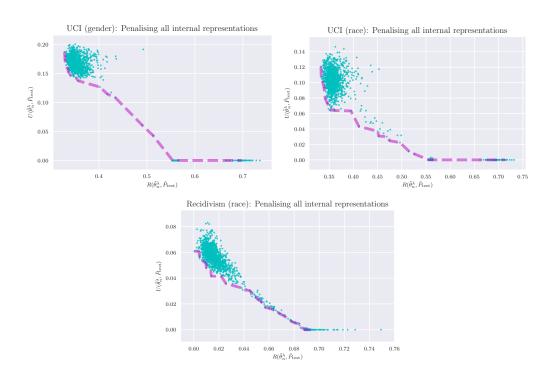


Figure 3: We repeated the experiment in Figure 1 changing only the fairness penalty to penalise the ATO in *all* layers. There is a drop in the quality of the Pareto front estimation compared to penalising just one internal layer. Namely, more of the candidate points are dominated points in this modified experiment where we've penalised ATO in all layers. It seems that we should have perhaps also tuned for a brand new architecture given this new penalty.