REDUCING COMPUTATION IN RECURRENT NETWORKS BY SELECTIVELY UPDATING STATE NEURONS

Anonymous authors
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ABSTRACT

Recurrent Neural Networks (RNN) are the state-of-the-art approach to sequential learning. However, standard RNNs use the same amount of computation at each timestep, regardless of the input data. As a result, even for high-dimensional hidden states, all dimensions are updated at each timestep regardless of the recurrent memory cell. Reducing this rigid assumption could allow for models with large hidden states to perform inference more quickly. Intuitively, not all hidden state dimensions need to be recomputed from scratch at each timestep. Thus, recent methods have begun studying this problem by imposing mainly a priori-determined patterns for updating the state. In contrast, we now design a fully-learned approach, SA-RNN, that augments any RNN by predicting discrete update patterns at the fine granularity of independent hidden state dimensions through the parameterization of a distribution of update-likelihoods driven entirely by the input data. We achieve this without imposing assumptions on the structure of the update pattern. Better yet, our method adapts the update patterns online, allowing different dimensions to be updated conditional to the input. To learn which to update, the model solves a multi-objective optimization problem, maximizing accuracy while minimizing the number of updates based on a unified control. Using publicly-available datasets we demonstrate that our method consistently achieves higher accuracy with fewer updates compared to state-of-the-art alternatives. Additionally, our method can be directly applied to a wide variety of models containing RNN architectures.

1 INTRODUCTION

Recurrent Neural Networks (RNN) are the state-of-the-art approach to many sequential learning problems including speech recognition (Graves et al., 2013), machine translation (Bahdanau et al., 2015), and sequence generation (Graves, 2013; Xu et al., 2015). However, RNNs typically rely on the computationally-taxing update of their entire hidden states at each timestep, a cost that grows as hidden states get bigger. As demonstrated by the success of gating methods such as the GRU (Cho et al., 2014) or LSTM (Hochreiter & Schmidhuber, 1997), all dimensions rarely need to be re-computed from scratch at each timestep. By discretely selecting which dimensions to update at each timestep via a learned update pattern, RNNs with a large hidden state can be trained with lower computational requirements (Bengio et al., 2013), inference in long RNNs can be expedited (Campos et al., 2018), and hidden representations may be made more robust to misleading inputs such as outliers or noise.

Selective neuron activation in RNNs has recently gained attention in the literature (Koutnik et al., 2014; Neil et al., 2016; Shen et al., 2019; Jernite et al., 2017; Campos et al., 2018). The most popular methods hand-craft specific update patterns, dictating which dimensions of the hidden state will update at which timesteps according to prior knowledge of a task (Koutnik et al., 2014; Neil et al., 2016). This imposes undue challenges in implementation, limits extensibility, and ignores the data-driven curation of information-flow through the RNN, a signature property of recurrent memory cells (Hochreiter & Schmidhuber, 1997; Cho et al., 2014). More recent methods learn to react to input data but impose strict relationships between the update patterns across both hidden dimensions and time (Shen et al., 2019; Jernite et al., 2017; Campos et al., 2018). While applicable to tasks with clear hierarchical components, such as modeling character-level text (Chung et al., 2017), these assumptions limit the expressiveness of the learned update patterns.
Specifically, we study the problem of generating a binary update-pattern for the hidden states learned by an RNN. The learned update-pattern defines which dimensions of the hidden state to update at each timestep, similar to the motivation for Residual Networks (He et al., 2016; Wang & Tian, 2016) and Highway Networks (Srivastava et al., 2015; Zilly et al., 2017). Ideally, only a small subset of the hidden state’s dimensions needs to be updated at each timestep, especially with high-dimensional hidden states. This way, representations can be learned while solving a sequential learning task while minimizing the number of updates, subsequently reducing compute time. A solution to this multi-objective optimization problem should have a comparable accuracy to a traditional constantly-updating RNN but save the majority of computation steps along the way, ultimately accelerating inference and training.

Despite the potential for reducing computation required by RNNs, learning update patterns for RNNs is a challenging problem. First, binary-output neurons making discrete decisions (whether or not to update a hidden state dimension, for example) in the interior of a neural network is a classic challenge to gradient-based learning since such decisions are non-differentiable and therefore backpropagation cannot be directly used to update the weights. Second, the quality of a learned update pattern is unsupervised and thus the only feedback is task-driven. This discourages a priori assumptions of relationships between update patterns of different hidden dimensions.

To address the aforementioned challenges, we propose the selective activation RNN, or SA-RNN, which parameterizes a distribution of update-likelihoods, one per hidden state dimension, from which update-decisions can be made at each timestep. We augment an RNN with an update coordinator that adaptively controls the coordinate directions in which to update the hidden state on the fly. The coordinator is modeled as a lightweight neural network that observes incoming data at each timestep and makes a discrete decision of whether or not enough information is stored in each individual hidden dimension to warrant an update. Subsequently, each hidden dimension is computed by the RNN or copied from the previous timestep. The coordinator’s architecture is kept as simple as possible so the complexity of the RNN can scale without simply outsourcing computation to another network, similar to the controller in Ha & Schmidhuber (2018). Most notably, in contrast to other recent approaches (Koutnik et al., 2014; Jernite et al., 2017; Neil et al., 2016; Campos et al., 2018; Shen et al., 2019; Liu et al., 2018) we impose no assumptions of which individual hidden dimensions should update (or not update) together. Instead, we show that using an entirely-learned approach still results in complex task-specific update patterns. On three publicly-available datasets, we show that our low-bias approach achieves higher accuracy with far fewer updates than recent state-of-the-art approaches (Koutnik et al., 2014; Jernite et al., 2017; Neil et al., 2016; Campos et al., 2018). These results indicate that predicting RNN update-patterns solely with respect to a task is not only feasible and low-bias, but also is favorable in a variety of settings.

2 RELATED WORK

Recurrent neuron update patterns have gained much interest in the recent literature (Koutnik et al., 2014; Jernite et al., 2017; Neil et al., 2016; Chung et al., 2017; Shen et al., 2019; Liu et al., 2018), all of which boast fewer updates to the hidden states than standard RNN architectures. However, there are several limitations of these methods, two of which are summarized as follows.

First, the most popular methods rely on extensively-handcrafted update patterns consisting of periodic neuron activations (Koutnik et al., 2014; Neil et al., 2016; Liu et al., 2018). This requires either prior knowledge of either sampling frequencies or seasonal patterns present in the data, reducing the potential extension to many sequential learning problems. These methods rely on input-agnostic periodic neuron updates which are fixed prior to learning. The choice of update periods heavily impacts the performance of the model, and sequences with irregular information flow cannot be modeled using these data without massive state representations.

Second, the most recent works allow for data-reactive update patterns (Jernite et al., 2017; Shen et al., 2019; Campos et al., 2018) but assume temporal hierarchies in the input sequences and study settings where this effect is exceedingly obvious (for example, character-level sentence modeling (Chung et al., 2017)). In many real-world settings, temporal hierarchies are often subtle and forcing this assumption into the architectural design may limit its applications.
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Figure 1: Overview of SA-RNN. \( h_{t-1} \) is the hidden state at timestep \( t-1 \). Prior to computing \( h_t \), the update coordinator decides which hidden dimensions will be updated according to \( x_t \) and its previous update decisions. According to the decision in this figure, for example, hidden dimension 1 is updated while hidden dimension 2 remains unchanged.

Additionally, our approach is related to conditional computation, which predicts subsets of neural networks to activate (Bengio et al., 2015; Shazeer et al., 2017; Cheng et al., 2017). In many cases, when a particular concept can be represented using only a sub-network present in a larger neural network, computation can be preserved by learning the structure of said sub-network (Schmidhuber, 2012).

3 Selective Neuron Activation for RNNs

We introduce the Selective-Activation RNN, or SA-RNN, a broadly-applicable augmentation to RNNs which minimizes the computation required for RNNs by facilitating unimpeded information-flow across timesteps for individual dimensions of the hidden state. At its core, SA-RNN learns a data-driven strategy for discretely reading and writing information to the latent state space through the learned parameterization of an update-likelihood distribution. Despite leaving hidden dimension update patterns independent from one another, complex strategies still arise naturally depending on the sequential learning task at hand. In this section, we describe the training process of SA-RNN with \( D \)-dimensional hidden states on sequences of length \( T \) for input data \( x \) with \( V \) variables. We omit biases from affine transformation equations and use notation for one training instance for ease of readability. An overview of the forward pass through SA-RNN is shown in Figure 1.

3.1 Computing Hidden States

RNNs compute a sequence of hidden states one timestep at a time (Elman, 1990), each computed by a recurrence function \( R(\cdot) \): \( h_t = R(h_{t-1}, x_t | \theta) \). The result is a sequence of vector representations \( H = \{ h_1, \ldots, h_T \} \) where ideally each \( h_t \in \mathbb{R}^D \) represents temporal dynamics of the time series up to timestep \( t \) with respect to a task, preserving not only temporal dependencies but also the ordering of the inputs.

A popular and powerful augmentation to the RNN, as it was originally proposed, is the Gated Recurrent Unit (GRU) (Cho et al., 2014), which adds a series of gates between \( h_{t-1} \) and \( h_t \) to aid in the vanishing gradient problem (Bengio et al., 1994):

\[
\begin{align*}
    r_t &= \sigma(W_r h_{t-1} + U_r x_t) \\
    z_t &= \sigma(W_z h_{t-1} + U_z x_t) \\
    s_t &= \phi(W_c x_t + U_c (r_t \odot h_{t-1})) \\
    \hat{h}_t &= (1 - z_t) \odot h_{t-1} + z_t \odot s_t
\end{align*}
\]
where $W_s$ and $U_s$ are matrices of learnable parameters of shape $D \times D$ and $D \times V$ respectively, $x_t \in \mathbb{R}^V$ is the input data at timestep $t$, $\odot$ represents the element-wise multiplication, $\sigma$ represents the sigmoid function, and $\phi$ represents a non-linearity, traditionally the hyperbolic tangent function. Its design is motivated heavily by the LSTM (Hochreiter & Schmidhuber, 1997). Traditionally, the GRU performs soft read/write operations, recomputing the entire vector $h_t$ at each timestep since gate $z \in [0, 1]^D$, the space of vectors with values inclusively between 0 and 1. Instead, we propose that all dimensions do not need to be updated at each timestep, as the position of the hidden state in some dimensions already encodes much of the modeled input. Note that the output of the recurrence function is referred to as $\hat{h}_t$. In the next section, we describe how to compute $h_t$, the final hidden state for timestep $t$ which is subsequently used for computing $h_{t+1}$ or the task.

### 3.2 Selective Neuron Activation

To reduce computation required to generate state representations, we assume updating state representations to be a sequence of binary decisions – either a neuron will be updated, or it will not at each timestep. Thus, we propose a learned update coordinator, which generates a binary mask for each neuron, forecasting which neurons will need to be updated at the next timestep. First, an update-likelihood $\tilde{u}_t$ is computed for each neuron, informed by both the data observed at the current timestep and the previous update-likelihoods: $\tilde{u}_t = \sigma(W_u h_{t-1} + W_i x_t)$ where $W_u \in \mathbb{R}^{D \times D}$ is a diagonal matrix of learnable parameters which dictate the linear relationship between $h_{t-1}$ and $\tilde{u}_t$. $W_i$ is kept diagonal to maintain relationships between update-decisions of the same dimension while avoiding the extensive computation of a fully-connected layer, similar to the hidden state decay in Che et al. (2018). $W_i \in \mathbb{R}^{D \times V}$ encodes the influence of the input data on the current update-likelihood and $\sigma(\cdot)$ represents the sigmoid function, bounding $\tilde{u}$. Thus $\tilde{u}_t \in [0, 1]^D$, with one update-likelihood per dimension of the hidden state.

To discretize $\tilde{u}_t$, thus allowing information to flow unimpeded, an element-wise binarization function is applied:

$$u_t = \text{binarize}(\tilde{u}_t), \text{ where}$$

$$\text{binarize}(a) = \begin{cases} 
1 & \text{if } a > 0.5, \\
0 & \text{otherwise.}
\end{cases}$$

We apply this final discrete update decision as a binary gating mechanism since $u_t \in \{0, 1\}^D$:

$$h_t = u_t \odot \tilde{h}_t + (1 - u_t) \odot h_{t-1}$$

As written, this equation requires the pre-computation of $\tilde{h}_t$. However, in practice, through masking the computation can be directed at only the needed updates upon calculation of $u_t$. Thus when $\tilde{u}_t^n$, the update decision for the $n$-th dimension in $h$, is 1 $h_{t}^n$ is updated according to the new information present in $\tilde{h}_t^n$. We note that this update-decision strategy does not impose the inter-neuron assumptions of Jernite et al. (2017); Shen et al. (2019); Koutnïk et al. (2014) while still allowing such strategies to be learned if they are found to be optimal by the model since decisions are made with respect to previous decisions, similar to Campos et al. (2018). We hypothesize that updating neurons together may generally be beneficial since complex temporal dependencies often require representations evolving in blocks of multiple neurons, as discussed in Koutnïk et al. (2014).

Since binary-output neurons are inherently non-differentiable, barring the use of back-propagation, we approximate the gradient of the binarization function using the straight-through gradient estimator (Bengio et al., 2013) paired with slope-annealing (Chung et al., 2017) during training:

$$\frac{\partial \text{binarize}(x)}{\partial x} = 1.$$ 

By estimating the gradient in this way we avoid additional loss terms and end up with empirically-reasonable approximations in comparison to other high-variance methods, such as REINFORCE (Williams, 1992; Chung et al., 2017; Campos et al., 2018). After computing the sequence of state representations $\{h_1, \ldots, h_T\}$, $h_T$ is projected into the output space depending on the task at hand.

### 3.3 Training

All weights of SA-RNN are updated together using back-propagation to minimize one loss function. For readability we gather all weights into one parameter matrix $\theta$. Our loss function $J(\theta)$ consists of
two parts: a task-driven loss (denoted as $L_{\text{task}}$) and an update-budget. The task-driven component maybe be cross entropy for classification or mean squared error for regression. The update-budget encourages the model to update the hidden dimensions more sparsely, as shown in Equation 9 where $N$ is the number of training examples, $\hat{y}$ is the prediction, and $y$ is the label.

$$J(\theta) = \frac{1}{N} \sum_{i=1}^{N} \left( L_{\text{task}}(y_i, \hat{y}_i) + \lambda \sum_{t=1}^{T} \tilde{u}_t^i \right)$$

(9)

$\lambda$ tunes the emphasis on the minimization of $\tilde{u}$, the update probability, and in practice it is reasonable to set $\lambda = 0$, encouraging the model to make update decisions should be made solely with respect to the learning task. As $\lambda$ is increased and update likelihoods decrease, the hidden dimension is update fewer times until eventually $h_0 = h_T$ where the hidden state is not updated with respect to the data.

4 Experiments

4.1 Datasets

We conduct our evaluation using three classification tasks on the following datasets, each being publicly-available.

Seizures$^1$ (Andrzejak et al., 2001): From 11,800 178-timestep time series, the task is to detect which EEGs contain evidence of epileptic seizure activity. Since there are only 2,300 cases of such activity, we down-sample an equal number from the negative class, resulting in a balanced dataset with 4,600 time series. Finally, we center the time series around zero and compute the mean value of every 10-timestep chunk, summarizing each series into 17 final timesteps.

TwitterBuzz$^2$ (Kawala et al., 2013): To predict buzz events on Twitter, we work with 77-dimensional time series, labeled indicating whether or not a spike in tweets on a particular topic is observed. Starting with over 140,000 timesteps, we compute the mean of every five steps, center the time series around zero, and break the resulting 28,000 timesteps into 2,800 length-15 sequences. We then extract the 776 time series containing any buzz events and balance the dataset by randomly selecting an equal number of no-buzz time series, resulting in a balanced dataset of 1552 time series.

Yahoo$^3$: We re-frame this outlier detection dataset as a classification problem – whether or not a sequence contains an anomaly. We begin by chunking the time series into subsequences of length 25. Then, we create a balanced dataset by selecting all subsequences with anomalies present along with an equal number of randomly-selected subsequences with no anomalies to serve as our negative class. Thus we end up with a dataset containing 418 length-25 time series.

4.2 Settings

Baselines.

To quantify the performance of selective activation in RNNs, we compare our method with five recent state-of-the-art related methods.

- **Random Updates**: This method is effectively the random version of our proposed method. At each step, random hidden dimensions are updated. This is similar to Zoneout (Krueger et al., 2017) however we maintain random updating during testing.

- **Clockwork RNN** (Koutnik et al., 2014): Hidden dimensions are updated in groups at pre-determined “clock” rates. For example, the first five dimensions in the hidden state may update every step while the second five neurons update every 3 steps.

- **Phased LSTM** (Neil et al., 2016): Hidden dimensions are updated independently at sampled “clock” rates where the user defines the distribution from which to sample. Each hidden dimension has its own update pattern.

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$^2$http://ama.liglab.fr/resourcestools/datasets/buzz-prediction-in-social-media/
$^3$https://webscope.sandbox.yahoo.com/catalog.php?datatype=s&did=70
Figure 2: Sample skipping patterns from compared methods for the Seizures task with 50-dimensional state representations. Black squares indicate update while white squares indicate skip.

- **SkipRNN** (Campos et al., 2018): Hidden dimensions update in lock-step with one another, with the entire hidden state being either being modified or left unchanged at each step. Additionally, the update likelihoods increase monotonically, regardless of input data.

- **VC-GRU** (Jernite et al., 2017): A value $p \in [0, 1]$ is predicted at each step indicating the proportion of the representation to update. Then, the first $p \ast D$ neurons are updated, imposing a hierarchical structure to the update patterns.

**Implementation Details.**

For all experiments, we use a 80% training, 10% validation, and 10% testing dataset splits. The training data are used to tune the parameters of the models, the validation data are used to validate hyperparameter selection, and the testing data are used to report final performances. We randomly repeat this process ten times to compute confidence intervals for performance metrics. Across all models we fix the size of state representations to be fifty neurons. Keeping this number fixed allows us to purely compare performance of the update-patterns observed in alternative algorithms. For $\lambda$ selection in SkipRNN and our proposed method, SA-RNN, we search in a log-space ranging from $0$ to $0.1$ in 11 steps. For all methods, we choose the same learning rate of $1e^{-03}$ from a log-space search ranging from $1e^{-05}$ to $1e^{-01}$, likely due to similarities behind the core of the sequential learning (RNNs with equal state representation sizes). We optimize all models using Adam (Kingma & Ba, 2014). The code for our method is available at https://hiddenforreview.com.

4.3 **EXPERIMENTAL RESULTS**

**Contrasting update patterns of alternative algorithms.**

First, we inspect the update-patterns generated by each baseline algorithm, as shown in Figure 4. Both PhasedLSTM and VC-GRU use “partial updates”, and do not make fully-binary update decisions. For this visualization we binarize their update patterns using a ceiling function on non-zero update decisions since the neurons are still updated. Importantly, all algorithms are subject to update-budgets, which clearly effect the observed patterns. For example, since the SkipRNN updates all neurons at the same time, deciding to update has a large cost, eating through the update budget quickly. Meanwhile, other methods such as our own SA-RNN and the PhasedLSTM take much smaller bites into the update budget since the neurons are updated independently. From these visuals, it is clear that our method is the only method which can update neurons for many steps at a time adaptively, according to the data. Thus, some neurons may update a few times in the middle of the sequence instead of at the beginning or end, a decision which is driven directly by the data. This allows our method to spend its computational budget in a more informed way, choosing to activate some neurons many times in a row, while leaving others unchanged.
Method √Acc. × Skip% Skip(%) Accuracy (%) FLOPS
GRU (Cho et al., 2014) 0 0 84.7 (0.8) 257550
CW-RNN (Koutnik et al., 2014) 73.7 81 67.1 (0.4) 16150
PhasedLSTM (Neil et al., 2016) 74.9 69 81.4 (1.4) 106454
VC-GRU (Jernite et al., 2017) 68.7 66 71.6 (3.4) 89284
SkipRNN (Campos et al., 2018) 69.2 82 58.4 (5.5) 48042
Random Updates 62.3 76 51.1 (0.1) 61812
SA-RNN 78.8 76 81.6 (0.6) 63512

Table 1: Performance on the Seizures task. √Accuracy × Skip% is the geometric mean of Accuracy and Skip Percent. The first section contains the baseline GRU, the second contains non-reactive methods, the third contains learned methods, and the fourth is our proposed method and random baseline. For SA-RNN we use $\lambda = 2e^{-4}$.

Method √Acc. × Skip% Skip(%) Accuracy (%) FLOPS
GRU (Cho et al., 2014) 0 0 64.8 (1.6) 378750
CW-RNN (Koutnik et al., 2014) 68.2 81 57.4 (1.9) 23750
PhasedLSTM (Neil et al., 2016) 65.3 70 60.9 (4.0) 151500
VC-GRU (Jernite et al., 2017) 62.9 66 59.9 (2.8) 131300
SkipRNN (Campos et al., 2018) 69.2 88 54.4 (8.1) 47925
Random Updates 72.2 89 58.6 (1.9) 41662
SA-RNN 75.0 89 63.1 (1.8) 44162

Table 2: Performance on the Yahoo task. For SA-RNN we use $\lambda = 1e^{-3}$.

Comparing accuracy and update-frequency across methods.
Second, we show results from three classification tasks, described in Section 4.1. We measure four properties of each method. 1) Skip Percent – the proportion of neurons which are not updated across all timesteps. To make a fair comparison between all methods, we tune their hyperparameters so that their skip percents are as close together as possible. This allows us to better analyze the effects of the differences in update patterns instead of changing the hidden state dimension sizes. 2) Accuracy – the accuracy achieved on the task. For each task we use balanced datasets, so the lower bound is 50%. 3) $\sqrt{\text{Accuracy} \times \text{Skip\%}}$ – the geometric mean of a model’s accuracy and skip percent. The measure allows comparison of all methods since they do not all update the same number of time. Thus, this is the key performance metric, the upper and lower limits of which are 1.0 and 0.0, respectively. 4) FLOPS – as in Campos et al. (2018) we compute the FLOPS for each method as a surrogate for wall-clock time, which is hardware-dependent and often fluctuates dramatically in practice.

Across all tasks, SA-RNN achieves on average higher accuracy with fewer updates, shown across Tables 1, 2, and 3. In Yahoo and TwitterBuzz, SA-RNN maintains by far the closest accuracy to that of the baseline GRU, which updates every hidden dimension at every timestep. In Seizures, both SA-RNN and PhasedLSTM are similar to the GRU, possibly due to periodic dynamics in the data. We also show in Tables 1 and 3, the accuracy of Random Updates is far worse than SA-RNN, indicating that the benefits of our proposed update-strategy comes strongly from the learning. The benefits of adaptive update patterns are not present in the Clockwork RNN or PhasedLSTM.

SA-RNN has nearly-equivalent FLOPS to the other methods that learn update patterns since each adds another affine transformation to map data to update decisions. As shown in Table 3, adapting the update decisions according to the input data adds a significant amount of computation with high-dimensional inputs. To improve this, update patterns may be predicted for multiple steps concurrently, depending on the input data. Given the same number of updates, the FLOPS are roughly equivalent between our method, VC-GRU, and SkipRNN. As in (Campos et al., 2018), it may be possible to only observe the previous hidden state, however this results in a perpetual-lag as information fills the hidden state. CW-RNN consistently has extremely low FLOPS since there is no data-driven decision making, instead hard-coding everything beforehand.
Table 3: Performance on the TwitterBuzz task. For SA-RNN we use $\lambda = 2^{-3}$.

<table>
<thead>
<tr>
<th>Method</th>
<th>$\sqrt{\text{Acc.} \times \text{Skip}}$</th>
<th>Skip (%)</th>
<th>Accuracy (%)</th>
<th>FLOPS</th>
</tr>
</thead>
<tbody>
<tr>
<td>GRU (Cho et al., 2014)</td>
<td>0</td>
<td>0</td>
<td>82.8 (2.2)</td>
<td>569250</td>
</tr>
<tr>
<td>CW-RNN (Koutnik et al., 2014)</td>
<td>72.1</td>
<td>81</td>
<td>64.2 (0.8)</td>
<td>35910</td>
</tr>
<tr>
<td>PhasedLSTM (Neil et al., 2016)</td>
<td>70.2</td>
<td>70</td>
<td>70.5 (1.8)</td>
<td>227700</td>
</tr>
<tr>
<td>VC-GRU (Jernite et al., 2017)</td>
<td>61.9</td>
<td>66</td>
<td>58.1 (2.2)</td>
<td>197340</td>
</tr>
<tr>
<td>SkipRNN (Campos et al., 2018)</td>
<td>72.2</td>
<td>87</td>
<td>60.0 (1.1)</td>
<td>75487</td>
</tr>
<tr>
<td>Random Updates</td>
<td>61.2</td>
<td>76</td>
<td>49.4 (0.7)</td>
<td>130927</td>
</tr>
<tr>
<td>SA-RNN</td>
<td>76.1</td>
<td>77</td>
<td>75.4 (3.0)</td>
<td>252120</td>
</tr>
</tbody>
</table>

Effects of budgeting neuron updates.

Finally, we assess how the performance of SA-RNN depends on its hyperparameter $\lambda$, which budgets the number of permitted updates. We investigate $\lambda$ values from 0 to 0.1 on a log-scale, since empirically no updates were allowed with $\lambda > 0.1$. Interestingly, the relationship between accuracy and $\lambda$ depends heavily on the task, as demonstrated in the first row of Figure 3. For example, on the Twitter task, we observe a smooth transition from random guessing (when no updates are allowed) to our peak accuracy (no constraint on updates). Meanwhile, on the Seizures task, there is a sharp increase from random predictions to near-peak predictions. This could be a feature of the parameter search space, but with already-small changes to $\lambda$ this indicates high-sensitivity. Additionally, we consider both accuracy and how many neurons are skipped, as shown in the second row of Figure 3. Interestingly, there are steep elbows where very few updates are needed to observe near-peak accuracy. This bolsters the intuition behind Residual Networks and related methods: many hidden dimensions often already capture enough information to warrant copying directly.

5 CONCLUSIONS

In this paper, we study the problem of reducing the number of updates to the state representations learned by RNNs. This allows for less computation at each timestep. We propose an augmentation to general RNN models, called SA-RNN, which is carefully crafted to skip neurons while maintaining accuracy through the parameterization of a distribution of neuron update-likelihoods, making binary decisions for each neuron at each step. We conduct extensive experiments on three real-world publicly-available time series datasets and show that our method achieves on average higher accuracy with fewer neuron updates compared to recent state-of-the-art alternatives. Our results demonstrate that updating state representations without imposing high-bias decisions on the update-patterns is not only easier to train, but preferable in terms of performance.
REFERENCES


6 Appendix

6.1 Hyperparameter Selection

We employ the validation set to select hyperparameters for compared models, as described in Section 3.2 of the submitted paper.

- **Random Updates**: When training Random Updates, the one hyperparameter to tune is the probability of updating each hidden dimension. Our goal is to match the number updates in Random Updates to the number observed in our proposed method, SA-RNN. So after observing how many times SA-RNN updated, we simply create random binary masks with the same update proportions.

- **Clockwork RNN**: This method relies on hand-crafted update patterns. In order to have roughly 20% of the updates (to be similar to the other methods) with 50-dimension state representations, we use block-sizes of 5 (the number of dimensions whose updates are tied together) with exponentially-increasing clock rates as proposed in the original paper: \(\{1, 2, 4, 8, 16, 32, 64, 128, 256\}\). We choose this as it is the originally-intended use of the model and resulted in the proper number of updates. There is no variance in this method as it does not react to the input data.

- **PhasedLSTM**: This method employs the sampling of update periods for individual hidden dimensions. The distribution from which to sample update periods is left up to the user (along with the parameters of such distribution). As proposed in the paper, we sample update periods from a uniform distribution \(U\). To determine the lower and upper bounds of the distribution, we tried sampling update patterns from a uniform distribution of all combinations of integers between 0 and 6, finally choosing \(U(1, 3)\). We sample \(D\) values from this distribution, where \(D\) is the dimension of the state representation. We choose the shift as described in the original PhasedLSTM paper, sampling a value with an upper limit of the period for each neuron. These two settings, paired with \(r_{on} = 0.3\) led to a comparable number of updates.

- **VC-GRU**: This method predicts proportions of the state representation to update at each timestep. During the optimization, there is a loss term which adds a “target” proportion, penalizing deviations from this target value. As suggested in the original paper, we tried values of 0.1, 0.2, and 0.5 and selected 0.1, which resulted in a comparable number of updates.

- **SkipRNN**: This method predicts likelihoods of state updates at each timestep. In the loss function, there is one hyperparameter, \(\lambda\), which penalizes the number of updates. We use a log-space search, ranging from 0.0 to 0.1 in 11 steps, settling on \(1e-05\) for the Twitter task, and \(1e-04\) for the Seizures and Yahoo tasks. We found the number of updates to be extremely sensitive, skipping from roughly 13% to 100% between single log-space steps.

6.2 Visualizing Update Patterns

In Section 4.3 we visualize and contrast the update patterns between all described methods. PhasedLSTM and VC-GRU, however, do not propose fully-binary update patterns. PhasedLSTM softly opens and closes neurons, and VC-GRU approximates binary update-decisions using a soft mask, changing the proportion of updated-neurons at each timestep. In order to fairly compare them to all other methods, we employ ceiling functions to raise their update predictions to 1 (prior to this, their updates are between 0 and 1, similar to LSTM and GRU). In Figure 4, we display their update patterns prior to this ceiling function, to show their use as originally intended. We believe that this use of the ceiling function is fair, since such soft updates are still updates, which is the focus of our work.

6.3 Implementing SA-RNN

We implement our method (and all other methods) in PyTorch 1.0. Below, we provide some pseudocode to give a taste of how to approach implementing SA-RNN (at a high level). The pseudocode is loosely formatted similar to PyTorch for readability. In the pseudocode, `Discriminator` is simply
Figure 4: Raw update patterns. Each column is a state representation. White boxes indicate Skip, darker boxes indicate the degree to which a neuron is updated with darker being more updated. A black box indicates that a neuron is fully-updated.

In practice the next state does not need to be fully computed once the update decisions are computed.

```python
def forward(sequence):
    u_likelihoods = zeros  # Initialize update likelihoods as zeros
    state = initializeState()  # Create the initial state
    for t in range(len(sequence)):
        x = sequence[t]  # Extract one timestep of data
        u_likelihoods = Coordinator.forward(x, u_likelihoods)
        u_decisions = Binarize.forward(u_likelihoods)
        state_tilde = RNN.forward(x, state)
        state = u_decisions*state_tilde + (1-u_decisions)*state
    prediction = Discriminator.forward(state)
    return prediction
```