

# CAT: Closed-loop Adversarial Training for Safe End-to-End Driving

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1       **Abstract:** Driving safety is a top priority for autonomous vehicles. Orthogonal  
2 to prior work handling accident-prone traffic events by algorithm designs at the  
3 policy level, we present a general iterative learning framework called Closed-loop  
4 **Adversarial Training (CAT)** for safe end-to-end driving. CAT aims to continu-  
5 ously improve safety performance by training the driving agent on safety-critical  
6 scenarios that are dynamically generated over time. A novel resampling technique  
7 is developed to turn normal real-world driving scenarios into safety-critical ones  
8 through probabilistic factorization, where the adversarial traffic flow is cast as the  
9 product of standard motion prediction sub-problems. Consequently, CAT is able  
10 to utilize pre-trained motion forecasting models to launch more effective phys-  
11 ical attacks with significantly less computational cost compared to existing safety-  
12 critical scenario generation methods. We incorporate CAT into the MetaDrive  
13 simulator and validate our approach on hundreds of driving scenarios imported  
14 from real-world driving datasets. Experimental results demonstrate that CAT can  
15 generate effective safety-critical scenarios countering the agent being trained. Af-  
16 ter training, the agent can achieve superior driving safety in both normal and ad-  
17 versarial traffic scenarios on the hold-out test set. The demo video is available in  
18 the supplementary materials.

19       **Keywords:** Safety-Critical Scenario Generation, Adversarial Training, End-to-  
20 End Driving

## 21 1 Introduction

22 While end-to-end driving has achieved promising performance in urban piloting [1] and track rac-  
23 ing [2], safely handling accident-prone traffic events is still one of the crucial capabilities for both  
24 human driving and autonomous driving (AD). It is important to ensure AI driving safety in risky sit-  
25 uations before real-world deployment [3]. However, it is insufficient to train or evaluate the safe end-  
26 to-end driving agents on safety-critical scenarios only collected from real-world traffic datasets [4, 5]  
27 since such events of interest are extremely rare [6, 7].

28 Prior work improves the driving agent against safety-critical scenarios through rule-based reason-  
29 ing [8], motion verification [9], constrained reinforcement learning [10], etc. Orthogonal to the  
30 elaborate algorithm designs at the policy level, recent studies obtain robust driving policies at the  
31 environmental level by creating accident-prone scenarios as augmented training samples [11, 12].  
32 Nevertheless, the learned policy may easily overfit a fixed set of safety-critical events but fail to han-  
33 dle unknown hazards. The alternative is to dynamically generate challenging scenarios that match  
34 the current capability of the driving agent in a closed-loop manner. However, the state-of-the-art  
35 safety-critical scenario generation methods [11, 12, 13] are not yet applicable for that purpose due  
36 to the following reasons: (i) *Scene generalizability*: probabilistic graph methods like CausalAF [11]  
37 require human prior knowledge of each scene graph and thus cannot scale to large and complex  
38 driving datasets; (ii) *Model dependency*: kinematics gradient methods like KING [12] relies on the

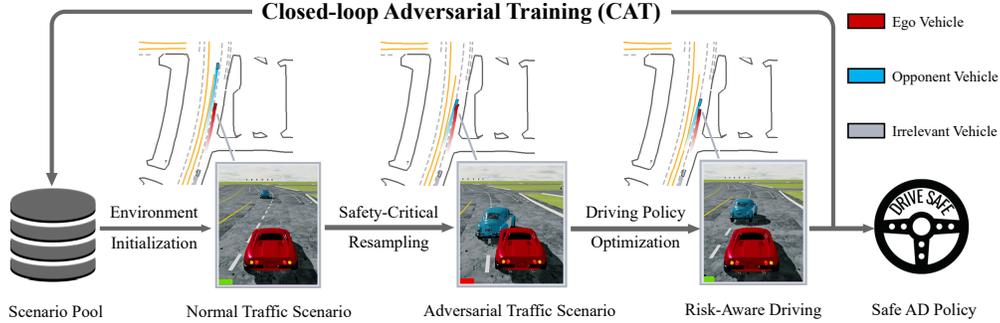


Figure 1: CAT iterates over safety-critical scenario generation and driving policy optimization in a closed-loop manner. In this example, the safety-critical resampling technique alters the behavior of the opponent vehicle (blue car) such that it suddenly cut into the lane of the ego vehicle (red car), enforcing the agent to learn risk-aware driving skills such as deceleration and yielding.

39 forward simulation of the running policy and the backward propagation based on the vehicle kine-  
 40 matics, which might not be accessible in the model-free end-to-end driving; (iii) *Time efficiency*:  
 41 autoregression-based generation methods like STRIVE [13] take minutes to optimize the adversarial  
 42 traffic per scenario, which is time prohibitive for large-scale training with millions of episodes.

43 In this paper, we present the Closed-loop Adversarial Training (CAT) framework for safe end-to-end  
 44 driving. As shown in Fig. 1, CAT imports driving scenarios from real-world driving logs and then  
 45 generates safety-critical counterparts as adversarial training environments tailored to the current  
 46 driving policy. The agent continuously learns to address emerging challenges and improves risk  
 47 awareness in closed-loop training. Given that CAT directly launches physical attacks against the  
 48 estimated ego trajectory, the proposed framework is thus agnostic to the policy used by the agent  
 49 and is compatible with a wide range of end-to-end learning approaches, including reinforcement  
 50 learning (RL) [14], imitation learning (IL) [15], human-in-the-loop feedback (HF) [16], etc.

51 One crucial component of the proposed framework is a novel factorized safety-critical resampling  
 52 technique that efficiently turns normal driving scenarios into safety-critical ones during training.  
 53 Specifically, we cast the safety-critical traffic generation as the risk-conditioned Bayesian probability  
 54 maximization and decompose it into the multiplication of standard motion forecasting sub-problems.  
 55 Thus, we can utilize off-the-shelf motion forecasting models [17, 18] as the learned prior to generate  
 56 adversarial scenarios with high fidelity, diversity, and efficiency. Compared to previous safety-  
 57 critical traffic generation methods, the proposed technique obtains a higher attack success rate while  
 58 significantly reducing the computational cost, making the CAT framework effective and efficient for  
 59 end-to-end training.

60 To demonstrate the efficacy of our approach, we incorporate the proposed CAT framework into the  
 61 MetaDrive simulator [19] and compose adversarial traffic environments from a hundred complex  
 62 driving scenarios in a closed-loop manner to train RL-based driving agents without any ad hoc  
 63 safety designs. Experimental results show that CAT brings realistic and challenging physical attacks  
 64 during training, and the resulting agent obtains superior driving safety in both normal and adversarial  
 65 traffic scenarios on the hold-out test set. The contributions of this paper are summarized as follows:

- 66 i) We present the closed-loop adversarial training framework for end-to-end safe driving, which  
 67 is agnostic to the policy learning method and the policy function design.
- 68 ii) We propose an efficient safety-critical scenario generation technique tailored to end-to-end  
 69 policy learning, which balances attack success rate and computation cost by resampling the  
 70 learned traffic prior.
- 71 iii) We incorporate our approach into the MetaDrive simulator and demonstrate it generates effec-  
 72 tive adversarial samples during training and substantially improves driving safety in complex  
 73 testing scenarios imported from the real world.

## 74 2 Related Work

75 **Adversarial Training for Autonomous Driving.** Deep neural networks (DNNs), pervasively used  
76 in learning-based AD systems, are found vulnerable to adversarial attacks [20, 21]. Recent stud-  
77 ies tend to manipulate the physical environment to generate realistic yet adversarial observation  
78 sequences from LiDAR inputs [22], camera inputs [23], and other physical-world-resilient ob-  
79 jectives [24]. Compared to the above work focusing on perception, adversarial training for AD  
80 decision-making is much less explored. Ma et al. [25] first investigate the adversarial RL on an  
81 autonomous driving scenario. Wachi [26] employ the multi-agent DDPG algorithm [27] to enforce  
82 the competition between player and non-player vehicles. In addition to algorithmic level designs, a  
83 more natural but less explored approach is to iteratively propose challenging scenarios during train-  
84 ing [28]. There is a line of works on evolving training environments in RL [29, 30]. However,  
85 existing approaches are evaluated only in simplified environments like bipedal walker and heuristi-  
86 cally modify the terrain or static barriers, which is not meaningful for AD tasks. In this work, we  
87 focus on generating realistic and safety-critical traffic scenarios to facilitate closed-loop adversarial  
88 training for end-to-end driving.

89 **Safety-critical Traffic Scenario Generation.** Safety-critical traffic scenario generation is of great  
90 value in adaptive stress testing [31] and corner case analysis [32] for the research and development of  
91 autonomous vehicles. L2C [33] learns to place and trigger a cyclist to collide with the target vehicle  
92 via RL algorithms, but it is insufficient to model complex vehicle interactions in real-world scenes.  
93 For robust imitation learning, kinematics gradients [12] and black-box optimization [22] can be used  
94 to magnify traffic risks. However, it relies on the forward simulation of the running policy and the  
95 backward propagation based on the vehicle kinematics, which might not be accessible in model-free  
96 end-to-end driving. CausalAF [11] builds scenario causal graphs to uncover behavior of interest and  
97 generates additional training samples to improve the robustness of driving policies. Nevertheless,  
98 the evaluations are limited to three scenarios since it requires human prior knowledge of each scene  
99 and thus hardly scale to the larger dataset. STRIVE [13] constructs a latent space to constrain  
100 the traffic prior and searches for the best responsive mapping via gradient-based optimization on  
101 that dense representation. Despite its impressive results on realistic traffic flows, the autoregression  
102 on raster maps takes several minutes to optimize the adversarial traffic for each scene, which brings  
103 about a costly computational burden for periodic policy optimization. We refer to the survey [34] for  
104 more details. Different from the above literature, we propose a novel adversarial traffic generation  
105 algorithm for real-world scenarios with an admissible time consumption, making it viable for large-  
106 scale policy iterations involving millions of episodes.

## 107 3 Closed-loop Adversarial Training Framework

108 We present the Closed-loop Adversarial Training (CAT) framework for safe end-to-end driving. As  
109 shown in Fig. 1, CAT iterates over safety-critical scenario generation and driving policy optimization  
110 in a closed-loop manner. In this section, we first formulate the closed-loop adversarial training  
111 as a min-max problem and then introduce the factorization of adversarial traffic and the practical  
112 implementation of CAT.

### 113 3.1 Problem Formulation

114 Although CAT is designed to accommodate a range of driving policies, we focus on RL-based AD in  
115 this work which is formulated as Markov Decision Process (MDP) [35] in the form of  $(S, A, R, f)$ .  
116  $S$  and  $A$  denote the state and action spaces, respectively. The reward function  $R = d - \alpha c$  wherein  $d$   
117 is the displacement toward the destination and  $c$  is a boolean indicating collision with other objects.  
118  $\alpha$  is a hyper-parameter for the reward shaping.  $f$  is the transition function to describe the dynamics  
119 of the traffic scenario. The goal is to maximize the expected return  $J(\pi) = \mathbb{E}_{\tau \sim \pi} [\sum_{t=0}^T R(s_t, a_t)]$   
120 the driving policy  $\pi$  receives within the time horizon  $T$ , where  $\tau \sim \pi$  is short handed for  $a_t \sim$   
121  $\pi(\cdot | s_t), s_{t+1} \sim f(\cdot | s_t, a_t)$ .

122 When importing a real-world traffic scenario, CAT manipulates original traffic trajectories to mag-  
 123 nify the possibility of traffic collisions with the agent itself ( $\mathbb{E}[c] \uparrow$ ). Consequently, the modified  
 124 adversarial traffic dynamics  $s_{t+1}^{Adv} \sim f^{Adv}(\cdot|s_t, a_t)$  naturally hinders total rewards the agent receives  
 125 ( $\mathbb{E}[\Sigma R] \downarrow$ ). CAT aims to enhance the robustness of the learning agent via the following adversarial  
 126 optimization:

$$\max_{\pi} \min_{f^{Adv}} J(\pi, f^{Adv}). \quad (1)$$

### 127 3.2 Factorized Safety-Critical Resampling

128 The fundamental problem is to construct  $f^{Adv}$  by generating compliant future traffic trajectories  
 129 that are prone to collisions with the agent’s rollout. To formalize the traffic collisions, we denote  
 130 the vehicle controlled by the learning agent as the ego vehicle (EV) and other vehicles as opponent  
 131 vehicles (OVs) and represent a traffic scenario as a tuple  $(M, S_{1:T}^{EV}, \mathbf{S}_{1:T}^{OV})$  with duration  $T$  time  
 132 steps. Here, the High-Definition (HD) road map  $M$  consists of road shapes, traffic signs, traffic  
 133 lights, etc.  $S_{1:t}^{EV}$  denotes the past states of the EV.  $\mathbf{S}_{1:t}^{OV}$  is an  $N$ -element array  $[S_{1:t}^{OV_1}, \dots, S_{1:t}^{OV_N}]$ ,  
 134 wherein each element stands for the past states of the corresponding OV. For simplicity, we denote  
 135  $X = (M, S_{1:t}^{EV}, \mathbf{S}_{1:t}^{OV})$  as the information cutoff by step  $t$  and  $Y^{EV} = S_{t:T}^{EV}$ ,  $\mathbf{Y}^{OV} = \mathbf{S}_{t:T}^{OV}$  are the  
 136 future trajectories of EV and OVs starting from  $t$ , respectively.  $Y^{EV}$  is conditioned on the RL agent  
 137  $\pi$ . The cutoff step  $t$  is fixed. We define a binary random variable  $Coll = \{True, False\}$  to denote  
 138 whether  $Y^{EV}$  collides with  $\mathbf{Y}^{OV}$ . Consequently, the optimization of  $f^{adv}$  can be cast as trajectory  
 139 posterior probability maximization under the condition of any collision:

$$\min_{f^{Adv}} J(\pi, f^{Adv}) \Leftrightarrow \max_{\mathbf{Y}^{OV}} \mathbb{P}(\mathbf{Y}^{OV} | Coll = True, X). \quad (2)$$

140 Considering that the opponent vehicle must launch effective attacks based on the potential ego be-  
 141 havior while the agent’s future action sequence is also responsive and even defensive to the malicious  
 142 traffic flow, the opponents’ trajectories  $\mathbf{Y}^{OV}$  and the ego vehicle’s trajectory  $Y^{EV}$  are not independ-  
 143 ent. Therefore, it only makes sense to model  $\mathbf{Y}^{OV}$  and  $Y^{EV}$  simultaneously and estimate the joint  
 144 traffic distribution of safety-critical scenarios:

$$\mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X). \quad (3)$$

145 Under some mild assumptions in Theorem 1, we can factorize Eq. (3) with the Bayesian formula.

146 **Theorem 1.** *Suppose that the EV’s reaction depends on the future traffic unidirectionally, then we*  
 147 *have  $\mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \propto \mathbb{P}(\mathbf{Y}^{OV} | X) \mathbb{P}(Y^{EV} | \mathbf{Y}^{OV}, X) \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV})$ .*

148 *Proof.* See the Appendix. □

149 Note that the safety-critical scenario generation objective of CAT, namely  $\min_{f^{Adv}} J(\pi)$ , is to mag-  
 150 nify the probability of traffic collisions with the agent as possible. Thus, after the factorization, we  
 151 can search the best responsive  $\mathbf{Y}^{OV}$  through the marginal distribution given as:

$$\begin{aligned} & \max_{\mathbf{Y}^{OV}} \mathbb{P}(\mathbf{Y}^{OV} | Coll = True, X) \\ &= \max_{\mathbf{Y}^{OV}} \sum_{Y^{EV}} \mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \\ &= \max_{\mathbf{Y}^{OV}} \underbrace{\mathbb{P}(\mathbf{Y}^{OV} | X)}_{1st \ Term} \sum_{Y^{EV}} \underbrace{\mathbb{P}(Y^{EV} | \mathbf{Y}^{OV}, X)}_{2nd \ Term} \underbrace{\mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV})}_{3rd \ Term}. \end{aligned} \quad (4)$$

152 It is beneficial to perform the above safety-critical traffic probability factorization since each term in  
 153 Eq. (4) features a specific meaning and is tractable to handle. Each term is interpreted as follows:

154 i) **Traffic prior.** The 1st term is the standard motion prediction problem in which we can lever-  
 155 age arbitrary probabilistic traffic models [17, 36, 37, 38] to portray the multi-modal trajectory  
 156 distribution. Taking the pre-trained model as the traffic prior enables the attack plausibility in  
 157 complex scenarios without human specifications.

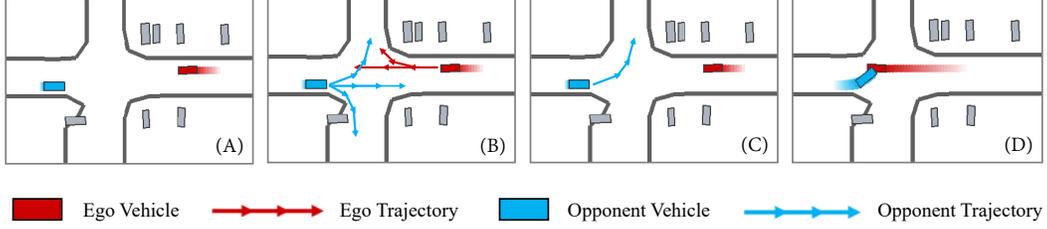


Figure 2: Illustration of Factorized Safety-Critical Resampling. (A) We initialize 1s traffic history with the dense map representation. (B) We then predict the traffic prior as well as the agent’s reaction. (C) The most accident-prone trajectory of the opponent vehicle is selected. (D) The generated scene is thus expected to be safety-critical.

- 158 ii) **Ego estimation.** The 2nd term denotes the interactive ego trajectory yielding to the current state  
 159 and upcoming traffic flow. The transition can be deterministic if the world model is learned or  
 160 accessible under model-based settings [12]. As for the inference of real-world-compliant traffic  
 161 flows, we can employ an interactive motion predictor [18] conditioned on known surrounding  
 162 vehicles’ trajectories to better reflects the ego compliance under risky interactions.
- 163 iii) **Collision likelihood.** The 3rd term reflects the likelihood of a collision in the compositional  
 164 future, which can be treated as a typical binary classifier to fit [39].

165 As shown in Fig. 2, it is possible to approach the near-optimal adversarial trajectory via numerical  
 166 optimization after each term is calculated.

### 167 3.3 Implementation Details

168 We summarize the overall implementation of the CAT framework for safe end-to-end driving in  
 169 **Algorithm 1.** Recalling the training objective of CAT in Eq. (1), we need to perform iterative opti-  
 170 mization of policy learning and adversarial environment generation synchronously in a closed loop.  
 171 The policy optimization can be achieved by arbitrary end-to-end driving policy learning approaches,  
 172 and we employ a vanilla RL algorithm.

173 Below, we focus on the adversarial environment generation, where we utilize the proposed factorized  
 174 safety-critical resampling in Eq. (4). Note that we make a simplification in CAT by enforcing a single  
 175 rival to launch the attack in each generated scene while simply maneuvering the other vehicles  
 176 to avoid self-collisions. This is reasonable since most traffic accidents are caused by two traffic  
 177 participants rather than involving multiple vehicles.

178 We first predict the traffic prior  $\mathbb{P}(Y^{OV}|X)$  using a pre-trained probabilistic traffic forecasting model  
 179  $\mathcal{G}$ . Considering the strong performance and the ease of sampling, we adopt DenseTNT [17], an  
 180 anchor-free goal-based motion predictor, in this work. Specifically, we propose  $M$  possible candi-  
 181 dates  $\{(Y_i^{OV}, P_i^{OV})\}_{i=1}^M$  in parallel. The component  $Y_{i,k}^{OV}$  in the  $k$ -th time step consists of the  
 182 predicted position and yaw of the opponent vehicle. The probability of the trajectory  $P_i^{OV}$  coincides  
 183 with the probability of the corresponding destination goal.

184 We then tackle the ego estimation term  $\mathbb{P}(Y^{EV}|Y^{OV}, X)$ . Considering the non-stationary policy  
 185 during training, we notice that the ego behavior does not necessarily match the logged behavior in  
 186 the dataset. Consequently, directly utilizing the pre-trained traffic estimator derived from natural  
 187 traffic flows [18] to provide ego trajectory probability has a severe bias. Alternatively, we record the  
 188 latest  $N$  rollouts of EV in each scenario formed as  $\{(Y_j^{EV}, P_j^{EV})\}_{j=1}^N$  and recompute the likelihood  
 189 of visited state sequences deduced by the current policy  $\pi$ :  $P_{j,k+1}^{EV} = P_{j,k}^{EV} \cdot \pi(a_k|s_k)$ .

190 At last, we empirically estimate the collision likelihood  $\mathbb{P}(Coll|Y^{EV}, Y^{OV})$ . Given the specific  
 191 compositional future of  $Y_j^{EV}$  and  $Y_i^{OV}$ , we compute the minimal distance between their bounding  
 192 boxes in the following steps and set the collision likelihood as  $P_{i,j}^{Coll} = \alpha^k$  if the closest gap is 0  
 193 at timestep  $k$ . Here,  $\alpha \in (0, 1]$  is a heuristic decay factor to reflect the uncertainty of traffic models  
 194 with the increasing prediction horizon.

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**Algorithm 1:** Closed-loop Adversarial Training (CAT) for Safe End-to-End Driving.

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**Input:** Initial driving policy  $\pi$ , Learning algorithm  $\mathcal{T}$ , Traffic Motion Predictor  $\mathcal{G}$ **Output:** Robust driving policy  $\pi^*$ 

```
1 Initialize the scenario pool  $\mathcal{D} = \{X_1, X_2, \dots, X_{|\mathcal{D}|}\}$  from real-world datasets.
2 while  $\pi$  is not converged do
3   Randomly sample normal traffic  $X$  from the scenario pool  $\mathcal{D}$ 
4    $\{(Y_i^{\text{OV}}, P_i^{\text{OV}})\}_{i=1}^M \sim \mathcal{G}(X)$  // Compute the traffic prior.
5   for  $i$  in  $1, 2, \dots, M$  do
6     for  $j$  in  $1, 2, \dots, N$  do
7        $P_{ij}^{\text{Coll}} = \alpha^k \cdot \mathbb{I}[\text{BBox}(Y_{j,k}^{\text{EV}}) \cap \text{BBox}(Y_{i,k}^{\text{OV}}) \neq \emptyset \exists k]$ 
8        $P(Y_i^{\text{OV}} | \text{Coll}, X) = P_i^{\text{OV}} \sum_{j=1}^N P_j^{\text{EV}} P_{ij}^{\text{Coll}}$  // Compute the posterior probability.
9        $*Y^{\text{OV}} = \arg \max_{Y_i^{\text{OV}}} P(Y_i^{\text{OV}} | \text{Coll}, X)$  // Select the best response.
10      obs = simulator.reset( $X, *Y^{\text{OV}}$ ) // Compose the adversarial environment.
11      for  $t$  in  $1, 2, 3, \dots, |T|$  do
12        act  $\sim \pi(\cdot | \text{obs})$ 
13        obs = simulator.step(act) // Policy execution.
14         $Y_{1:t}^{\text{EV}} = Y_{1:t-1}^{\text{EV}} \oplus Y_t^{\text{EV}}$ 
15         $P_{1:t}^{\text{EV}} = P_{1:t-1}^{\text{EV}} \cdot \pi(\text{act} | \text{obs})$ 
16       $\pi \leftarrow \mathcal{T}(\pi)$  // Policy optimization.
17       $\{(Y_i^{\text{EV}}, P_i^{\text{EV}})\}_{i=1}^N = \{(Y_i^{\text{EV}}, P_i^{\text{EV}})\}_{i=2}^N \oplus (Y^{\text{EV}}, P^{\text{EV}})$  // Update ego rollout queue.
```

---

## 195 4 Experiments

### 196 4.1 Experiment Setup

197 We import 100 real-world traffic scenarios involving complex vehicle interactions from the Waymo  
198 Open Motion Dataset (WOMD) [4] as the raw data. Each scene in WOMD contains a traffic partic-  
199 ipant labeled as *Object of Interest*, which is also designated as the opponent vehicle (OV) in our  
200 experiments. All the experiments are conducted in MetaDrive [19], an open-source and lightweight  
201 AD simulator. The detailed hyper-parameter settings can be referred to the Appendix. Here, we  
202 point out some pivotal parameters. Each scene lasts 9s, in which we take the first 1s traffic history  
203 as  $X$  and manipulate the following 8s to generate the adversarial trajectory  $Y^{\text{OV}}$ . We set  $M = 32$   
204 as the number of OV trajectory candidates,  $N = 5$  as the length of ego rollout queue during training  
205 and  $\alpha = 0.99$  to penalize the uncertainty of motion forecasting.

### 206 4.2 Evaluation of Safety-critical Traffic Generation in CAT

207 The factorized safety-critical resampling is the crucial component of CAT to generate adversarial  
208 training environments. We provide qualitative and quantitative comparisons with the following  
209 baselines: **(A) Raw Data:** Replaying the recorded real-world traffic. **(B) M2I (adv)** [18]: The in-  
210 teractive traffic motion prediction is similar to our factorized formulation and thus can be modified  
211 as an adversarial scenario generator. **(C) STRIVE** [13]: The state-of-the-art safety-critical scenario  
212 generation methods performing gradient-based optimization on the latent code.

213 **Qualitative analysis.** In Fig. 3, we present 9 different types of safety-critical scenarios that CAT  
214 generates from raw scenes, according to the pre-crashed traffic categorized by the National Highway  
215 Traffic Safety Administration (NHTSA). It can be concluded that CAT is able to generate adversarial  
216 traffic given arbitrary real-world raw scenes. Meanwhile, the generated trajectories are in line with  
217 human driver behavior, even though we don't specify prior knowledge of that scene. In Fig. 4, we  
218 compare the generated adversarial traffic of the four methods on the same intersection. In the raw  
219 scene, the leading vehicle turns preferentially and does not cross the path of the ego vehicle. The  
220 opponent attempts to collide with the agent at the intersection through the safety-critical generation.  
221 However, M2I (adv) has a bias in estimating the reaction of the ego vehicle, which does not cause the  
222 expected accident. STRIVE finds the solution to enforce a crash, but it is still cumbersome to tweak  
223 the multinomial loss function to balance the goal of colliding as soon as possible and reasonable

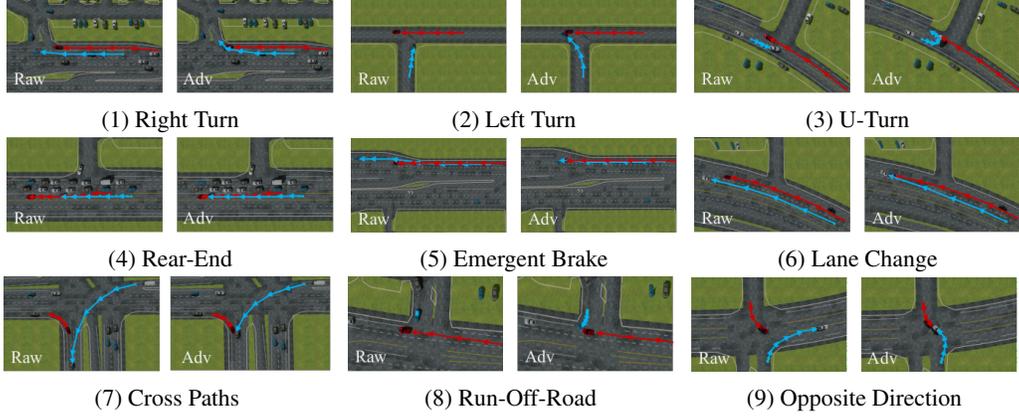


Figure 3: Qualitative results on the diversity of safety-critical scenarios generated by CAT. In each subfigure, the left and right are the raw scene and the adversarial counterpart. The ego and adversarial trajectories are highlighted with red and blue arrows, respectively.

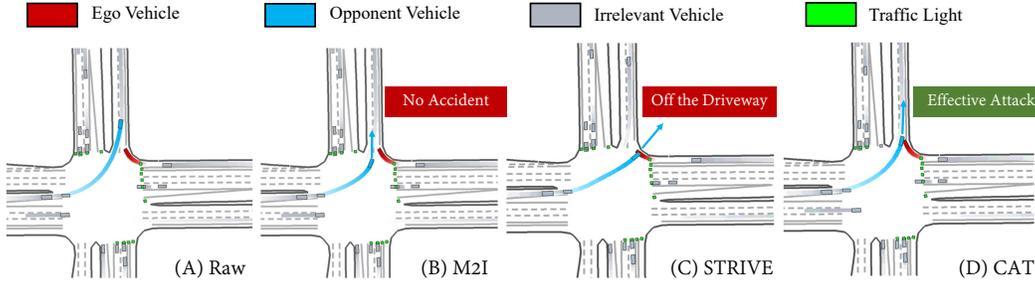


Figure 4: Qualitative results on the plausibility of safety-critical scenarios generated by CAT. The attack is regarded as effective only if leading traffic accidents are consistent with real-world events.

224 driving behavior, like keeping the vehicle in the driveway. By contrast, our factorized safety-critical  
 225 resampling leverages the learned motion prior to regularize the opponent’s trajectory, magnifying  
 226 the traffic risk while preserving its plausibility. More visualization can be found in Appendix.

227 **Quantitative analysis.**

228 In Table 1, we conduct the comparative study mainly on two metrics.  
 229 The first metric of interest is the attack success rate as the driving policies are responsive and  
 230 even defensive to the traffic flow.  
 231 We adopt three kinds of agents with fixed policies to validate: (i)  
 232 *Replay Agent*: Replay the original trajectory of the ego vehicle  
 233 logged in real-world data-set. (ii)  
 234 *IDM Agent*: A heuristic controller well-adopted in AD tasks [40]. (iii) *Pre-trained Agent*: A pre-trained RL policy on WOMD. We  
 240 find that M2I (adv) is insufficient for ego prediction and attacks less effectively especially against  
 241 low-level policy, which is fatal for end-to-end driving. CAT collects ego rollouts to enhance the con-  
 242 fidence of ego estimation during training ( $N = 5$ ) and testing ( $N = 1$ ) which significantly improves  
 243 the attack success rate and is competitive with the SOTA method STRIVE. The second metric of  
 244 interest is the time consumption per scene, which is non-negligible considering the large number of  
 245 scenario iterations during training. We find that STRIVE generally requires 2-3 minutes to process  
 246 a single scene due to its autoregression procedure on the raster map, which means it takes days to  
 247 train the agent in a closed loop involving thousands of episodes. By contrast, our approach best  
 248 balance the attack success rate and computational time compared and enjoys a privileged advantage  
 249 in closed-loop adversarial training for end-to-end driving.  
 250

Table 1: Comparison of adversarial traffic generation algorithms on 100 scenes.

Methods	Attack Success Rate $\uparrow$			Per Scene Creating Time $\downarrow$
	Replay	IDM	Pretrained	
Raw Data	0%	34%	14%	/
M2I (adv)	47%	41%	19%	$0.41 \pm 0.03s$
STRIVE	85%	82%	66%	$153.10 \pm 47.33s$
CAT ( $N = 1$ )	91%	71%	62%	$0.66 \pm 0.09s$
CAT ( $N = 5$ )	<b>91%</b>	<b>86%</b>	<b>69%</b>	$3.34 \pm 0.41s$

Table 2: Performance of end-to-end driving policies with different training pipelines.

Metrics	No Adv	Heuristic	Open-loop	Closed-loop
Train Attack Num $\uparrow$	7546 $\pm$ 506	9881 $\pm$ 810	18541 $\pm$ 2172	<b>24997 <math>\pm</math> 2437</b>
Test Crash Rate (Raw) $\downarrow$	19.7% $\pm$ 1.37%	16.8% $\pm$ 0.43%	15.1% $\pm$ 1.45%	<b>11.2% <math>\pm</math> 2.48%</b>
Test Crash Rate (Adv) $\downarrow$	49.6% $\pm$ 2.11%	41.4% $\pm$ 1.73%	29.9% $\pm$ 2.08%	<b>20.0% <math>\pm</math> 3.11%</b>

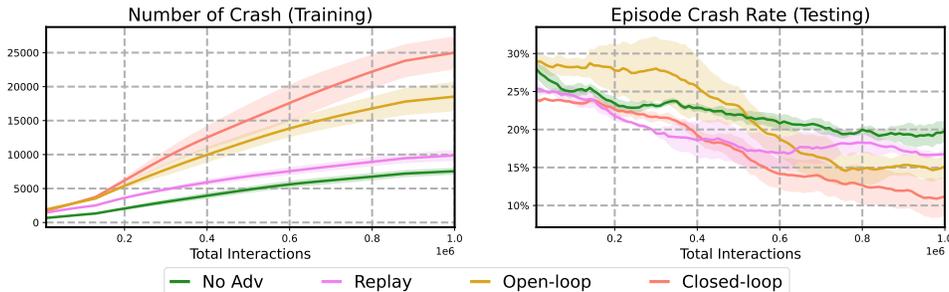


Figure 5: The learning curves with different training pipelines.

### 251 4.3 Evaluation of Closed-loop Adversarial Training in CAT

252 We show how CAT improves AI driving safety in accident-prone driving scenarios. We split the  
 253 100 scenes into 70 training and 30 testing scenarios. We train a TD3 [41] driving policy from  
 254 scratch with 4 types of training pipelines: **(A) No Adv**: Remove the opponent vehicle. **(B) Replay**:  
 255 Replay the human behaviors stored in the dataset. **(C) Open-loop**: Use CAT to manipulate the  
 256 opponent trajectory against the log-replayed ego rollout, instead of the ego trajectory of RL agent.  
 257 **(D) Closed-loop**: Use CAT to generate adversarial scenario dynamically against the learning agent.  
 258 We evaluate the driving policies trained from different pipelines with three metrics. The first metric  
 259 is the number of effective attacks occurred during adversarial training, describing the total number of  
 260 collision with the surrounding vehicles. We also evaluate the crash rate, the ratio of the episodes that  
 261 the ego vehicle crashes into others, on the hold-out testing scenarios with log-replay traffic (*Raw*) or  
 262 with CAT generated traffic (*Adv*).

263 As shown in Table 2 and Fig. 5, we find that CAT substantially increases safety-critical events compared  
 264 with other baselines during training, showing that CAT can generate challenging collision-prone  
 265 scenarios. On the other hand, the agent trained with CAT demonstrate superior safety performance  
 266 in testing time.

## 267 5 Conclusion and Discussion

268 In this paper, we propose the closed-loop adversarial training (CAT) framework for safe end-to-  
 269 end driving. The crucial component of CAT is an efficient adversarial traffic generation technique.  
 270 Empirical results demonstrate that CAT can provide realistic physical attacks during training and  
 271 enhance AI driving safety in the test time.

272 **Limitation**: Following limitations wait to be addressed in future work: (i) we only consider ad-  
 273 versarial vehicles in this work but the safety-critical behaviors of pedestrians and cyclists are also  
 274 of importance for safe driving and yet to be done, it requires the access to a different motion fore-  
 275 casting model; (ii) Experiment on one hundred scenes cannot cover all the accident-prone situa-  
 276 tions, thus there are other possible failure modes in the resulting agent; (iii) we only investigate  
 277 the RL-based driving policy but the adversarial scenarios should also benefit the human-in-the-loop  
 278 imitation learning [16, 42].

279 **Transferring to real-world driving**: The proposed adversarial training method and the comparison  
 280 with prior methods are evaluated in the simulation of one hundred complex traffic scenarios imported  
 281 from real-world driving dataset [4]. Thus, the evaluation contains realistic and complex vehicle  
 282 interactions and shows promise for transferring to real-world settings.

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402 ceedings, 2011.

403 **A Proof of Theorem 1**

404 **Theorem.** *Suppose that the EV's reaction depends on the future traffic unidirectionally, then we*  
 405 *have  $\mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \propto \mathbb{P}(\mathbf{Y}^{OV} | X) \mathbb{P}(Y^{EV} | \mathbf{Y}^{OV}, X_t) \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV})$ .*

406 *Proof.* According to Bayes theorem, we have

$$\mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \propto \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV}, X) \mathbb{P}(Y^{EV}, \mathbf{Y}^{OV}, X) \quad (\text{A.1})$$

407 Since  $Coll$  merely depends on  $Y_{t:t+l}^{EV}$  and  $\mathbf{Y}_{t:t+l}^{OV}$ , (A.1) is equivalent to

$$\mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \propto \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV}) \mathbb{P}(Y^{EV}, \mathbf{Y}^{OV}, X) \quad (\text{A.2})$$

408 Suppose that the AV's reaction depends on the future traffic unidirectionally; continuing with Bayes  
 409 theorem, we have

$$\begin{aligned} \mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \\ \propto \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV}) \mathbb{P}(Y^{EV} | \mathbf{Y}^{OV}, X) \mathbb{P}(\mathbf{Y}^{OV}, X) \\ \propto \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV}) \mathbb{P}(Y^{EV} | \mathbf{Y}^{OV}, X) \mathbb{P}(\mathbf{Y}^{OV} | X) \mathbb{P}(X) \end{aligned} \quad (\text{A.3})$$

410 Since the past state  $X$  is given, we can omit the last item  $\mathbb{P}(X)$  in (A.3). Therefore, it holds that

$$\mathbb{P}(Y^{EV}, \mathbf{Y}^{OV} | Coll = True, X) \propto \mathbb{P}(\mathbf{Y}^{OV} | X) \mathbb{P}(Y^{EV} | \mathbf{Y}^{OV}, X) \mathbb{P}(Coll = True | Y^{EV}, \mathbf{Y}^{OV}) \quad (\text{A.4})$$

411 The proof of Theorem 1 is completed. □

412 **B Hyper-parameter Settings**

Table 3: CAT		Table 4: TD3		Table 5: DenseTNT and M2I	
Hyper-parameter	Value	Hyper-parameter	Value	Hyper-parameter	Value
Scenario Horizon $T$	9s	Discounted Factor $\gamma$	0.99	Train Batch size	256
History Horizon $t$	1s	Train Batch Size	256	Train Epoches	30
# of OV candidates $M$	32	Critic Learning Rate	3E-4	Sub Graph Depth	3
# of EV candidates $N$	5	Actor Learning Rate	3E-4	Global Graph Depth	1
Penalty Factor $\alpha$	0.99	Policy Delay	2	NMS Threshold	7.2
Policy Training Steps	10E6	Target Network $\tau$	0.005	Number of Mode	32

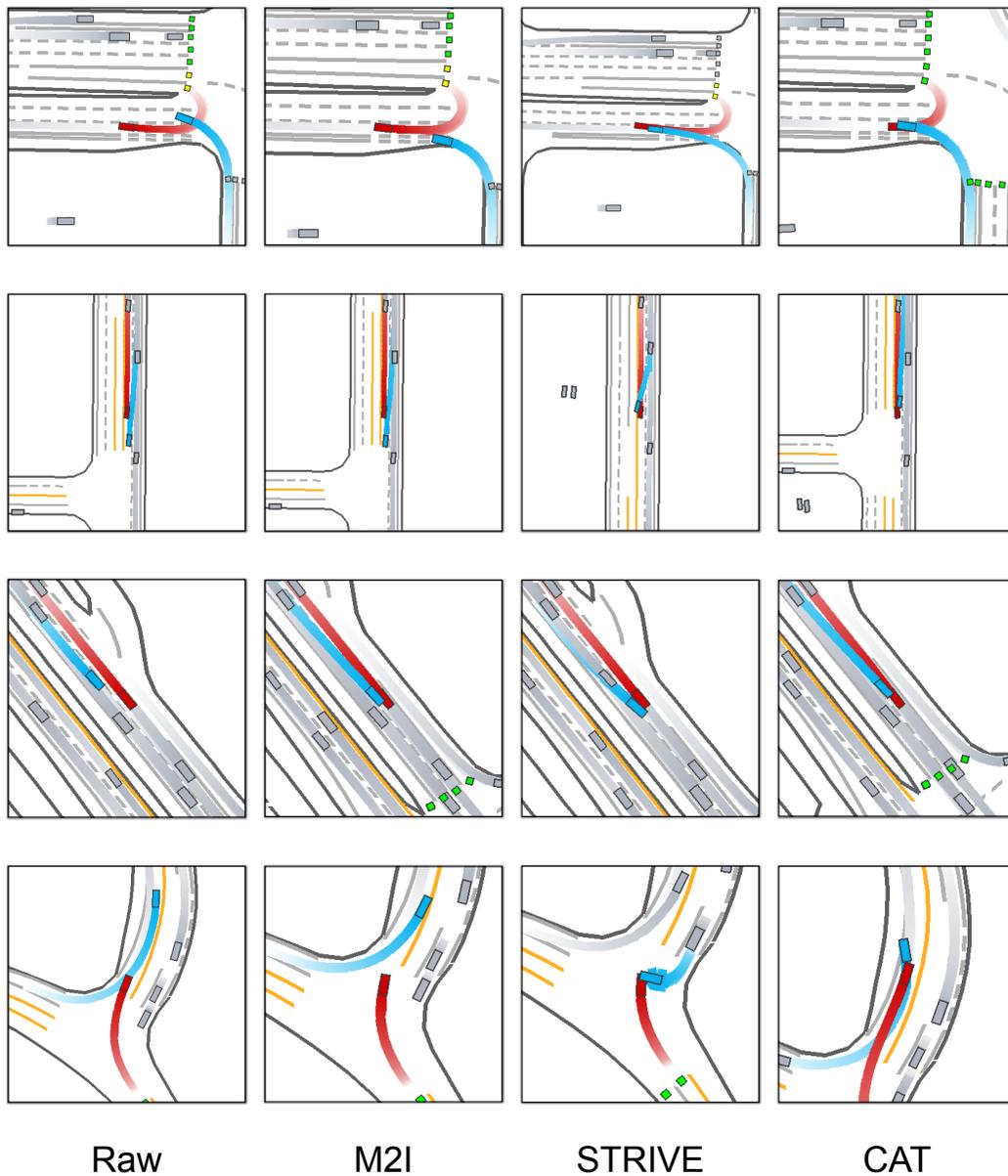


Figure 6: Comparing the different scenario generation methods. M2I and CAT both can determine the object of interest while STRIVE select the closest vehicle as the opponent. The red car is the ego vehicle and the blue car is the opponent vehicle.

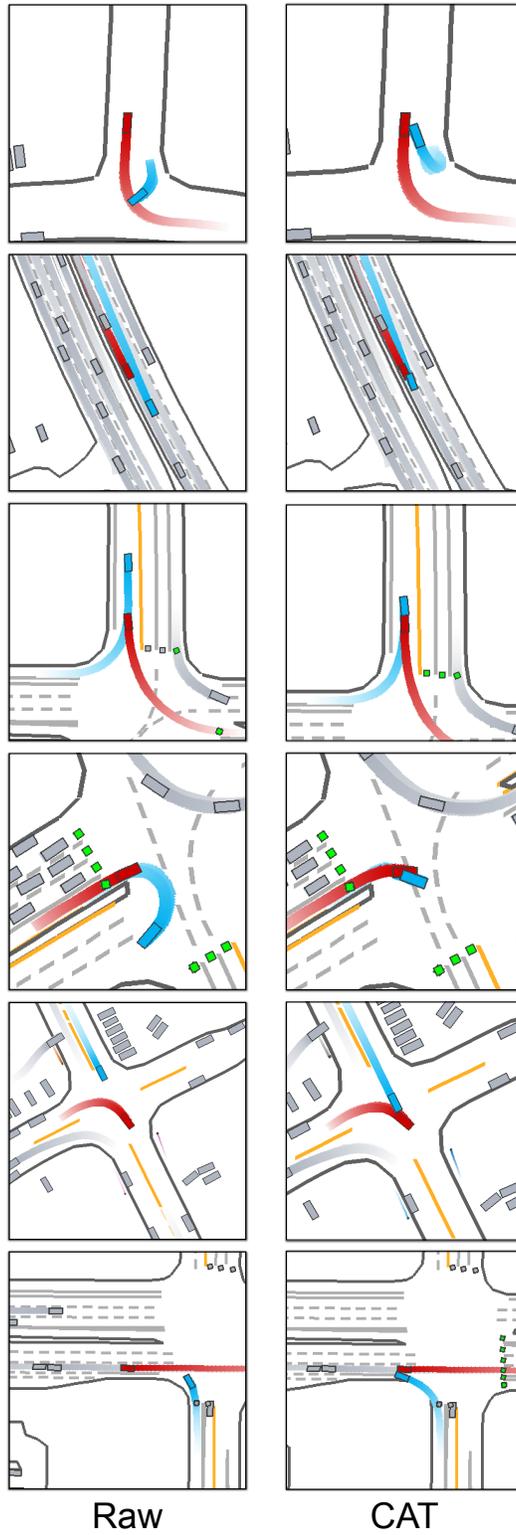


Figure 7: More comparison between the original scenarios in raw datasets and the safety-critical scenarios generated by our method. The red car is ego vehicle and the blue car is the opponent vehicle.