

Table 5: Detection accuracy in the AUC measure. The distance-based metrics, denoted by DISTANCE, are further categorized depending on whether the Euclidean distance or the cosine similarity is used. RECURVE adopts the curvature-based metric. If the inter-class embedding distance between two classes is shorter than a certain threshold, the change between the two classes is categorized as *gradual*. Here, the threshold is set so that gradual changes constitute 20% of all changes. Abrupt changes are excluded when measuring AUC-Gradual, and vice versa. In conclusion, RECURVE can support both gradual and abrupt changes, and it is more effective in handling gradual changes.

Methods	Repr.	$p$	AUC-Gradual $\uparrow$				AUC-Abrupt $\uparrow$			
			WISDM	HAPT	mHealth	50salads	WISDM	HAPT	mHealth	50salads
DISTANCE (Euclidean)	TPC	5	0.690 $\pm$ 0.008	0.516 $\pm$ 0.029	0.519 $\pm$ 0.005	0.596 $\pm$ 0.005	0.694 $\pm$ 0.009	0.716 $\pm$ 0.010	0.696 $\pm$ 0.010	0.622 $\pm$ 0.027
		10	0.690 $\pm$ 0.008	0.520 $\pm$ 0.029	0.521 $\pm$ 0.005	0.599 $\pm$ 0.005	0.695 $\pm$ 0.009	0.717 $\pm$ 0.010	0.699 $\pm$ 0.010	0.624 $\pm$ 0.027
		20	0.691 $\pm$ 0.009	0.527 $\pm$ 0.028	0.521 $\pm$ 0.005	0.603 $\pm$ 0.005	0.696 $\pm$ 0.008	0.718 $\pm$ 0.009	0.700 $\pm$ 0.010	0.628 $\pm$ 0.027
	TNC	5	0.715 $\pm$ 0.012	0.692 $\pm$ 0.022	0.706 $\pm$ 0.017	0.556 $\pm$ 0.057	0.720 $\pm$ 0.008	0.846 $\pm$ 0.007	0.839 $\pm$ 0.028	0.630 $\pm$ 0.011
		10	0.724 $\pm$ 0.014	0.698 $\pm$ 0.022	0.708 $\pm$ 0.017	0.558 $\pm$ 0.056	0.735 $\pm$ 0.009	0.849 $\pm$ 0.007	0.847 $\pm$ 0.028	0.632 $\pm$ 0.011
		20	0.734 $\pm$ 0.017	0.708 $\pm$ 0.022	0.709 $\pm$ 0.017	0.561 $\pm$ 0.056	0.754 $\pm$ 0.011	0.854 $\pm$ 0.007	0.849 $\pm$ 0.029	0.636 $\pm$ 0.011
DISTANCE (Cosine)	TPC (=TS-CP <sup>2</sup> )	5	0.807 $\pm$ 0.014	0.602 $\pm$ 0.023	0.546 $\pm$ 0.015	0.671 $\pm$ 0.010	0.838 $\pm$ 0.009	0.746 $\pm$ 0.021	0.631 $\pm$ 0.011	0.703 $\pm$ 0.039
		10	0.811 $\pm$ 0.014	0.606 $\pm$ 0.023	0.548 $\pm$ 0.014	0.674 $\pm$ 0.010	0.845 $\pm$ 0.010	0.747 $\pm$ 0.021	0.636 $\pm$ 0.011	0.706 $\pm$ 0.035
		20	0.814 $\pm$ 0.015	0.613 $\pm$ 0.022	0.550 $\pm$ 0.011	0.677 $\pm$ 0.009	0.847 $\pm$ 0.010	0.747 $\pm$ 0.020	0.637 $\pm$ 0.010	0.714 $\pm$ 0.037
	TNC	5	0.779 $\pm$ 0.013	0.774 $\pm$ 0.013	0.789 $\pm$ 0.017	0.594 $\pm$ 0.022	0.794 $\pm$ 0.012	<b>0.945<math>\pm</math>0.006</b>	0.892 $\pm$ 0.023	0.681 $\pm$ 0.010
		10	0.787 $\pm$ 0.012	0.783 $\pm$ 0.012	0.803 $\pm$ 0.015	0.594 $\pm$ 0.032	0.808 $\pm$ 0.011	0.946 $\pm$ 0.004	0.901 $\pm$ 0.022	0.685 $\pm$ 0.010
		20	0.814 $\pm$ 0.013	0.799 $\pm$ 0.014	0.846 $\pm$ 0.009	0.601 $\pm$ 0.032	0.846 $\pm$ 0.011	0.950 $\pm$ 0.004	0.928 $\pm$ 0.017	0.687 $\pm$ 0.010
RECURVE	TPC	5	<b>0.888<math>\pm</math>0.004</b>	<b>0.886<math>\pm</math>0.009</b>	0.939 $\pm$ 0.003	<b>0.712<math>\pm</math>0.006</b>	<b>0.923<math>\pm</math>0.003</b>	<b>0.945<math>\pm</math>0.002</b>	0.985 $\pm$ 0.004	<b>0.729<math>\pm</math>0.055</b>
		10	<b>0.893<math>\pm</math>0.005</b>	<b>0.891<math>\pm</math>0.009</b>	0.940 $\pm$ 0.003	<b>0.715<math>\pm</math>0.006</b>	<b>0.927<math>\pm</math>0.002</b>	0.948 $\pm$ 0.002	0.988 $\pm$ 0.004	<b>0.731<math>\pm</math>0.054</b>
		20	<b>0.894<math>\pm</math>0.005</b>	<b>0.896<math>\pm</math>0.009</b>	0.941 $\pm$ 0.003	<b>0.722<math>\pm</math>0.006</b>	<b>0.927<math>\pm</math>0.002</b>	0.955 $\pm$ 0.002	0.988 $\pm$ 0.004	<b>0.734<math>\pm</math>0.051</b>
	TNC	5	0.867 $\pm$ 0.007	0.773 $\pm$ 0.038	<b>0.975<math>\pm</math>0.003</b>	0.551 $\pm$ 0.034	0.901 $\pm$ 0.006	0.931 $\pm$ 0.002	<b>0.988<math>\pm</math>0.006</b>	0.600 $\pm$ 0.016
		10	0.875 $\pm$ 0.007	0.779 $\pm$ 0.038	<b>0.977<math>\pm</math>0.003</b>	0.553 $\pm$ 0.034	0.910 $\pm$ 0.006	0.933 $\pm$ 0.002	<b>0.989<math>\pm</math>0.006</b>	0.602 $\pm$ 0.016
		20	0.890 $\pm$ 0.008	0.791 $\pm$ 0.038	<b>0.977<math>\pm</math>0.004</b>	0.558 $\pm$ 0.033	<b>0.927<math>\pm</math>0.006</b>	0.939 $\pm$ 0.002	<b>0.990<math>\pm</math>0.006</b>	0.606 $\pm$ 0.015

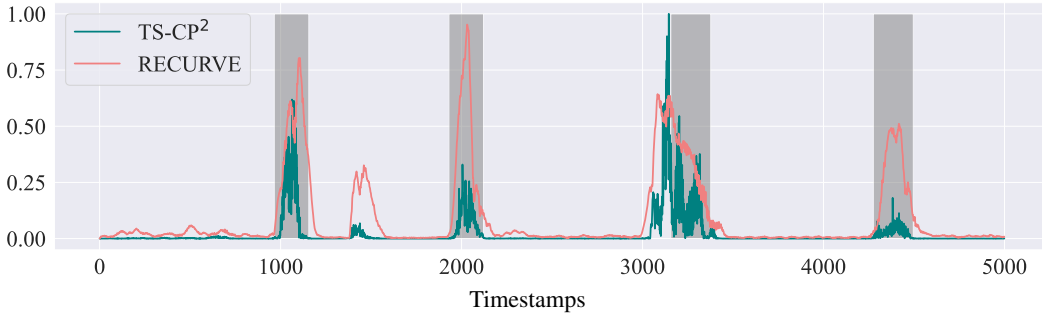


Figure 8: Change metric score from the HAPT dataset with the default configuration. A grey-shaded area represents inter-segment points between two class segments. Note that TS-CP<sup>2</sup> fluctuates rapidly during the changes and seems to have many false negatives at the rightmost boundary area. On the other hand, RECURVE indicates the inter-segment points much more clearly than TS-CP<sup>2</sup>.

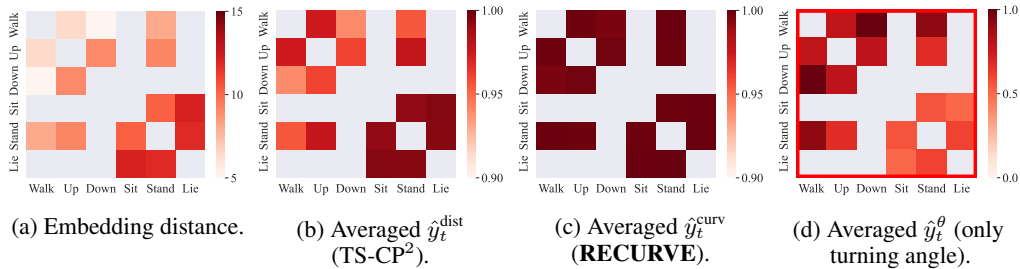


Figure 9: Heatmaps of the inter-class distances and values of the change metrics between the classes in the HAPT dataset. A grey box indicates no transition between two classes. Compared to Figure 6, Figure 9(d) is added here to investigate the *sole effect* of the turning angle  $\theta_t$ . For (d),  $\hat{y}_t^\theta = \text{MA}(\text{NORM}(2\pi - \theta_t))$ , where  $\theta_t$  is defined as Eq. (4). Interestingly,  $\hat{y}_t^\theta$  is greater for the transitions with smaller inter-class embedding distances. This additional result in (d) validates the rationale behind the effectiveness of RECURVE in handling gradual changes.