SPREAD SPURIOUS ATTRIBUTE: IMPROVING WORST-GROUP ACCURACY WITH SPURIOUS ATTRIBUTE ESTIMATION

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Paper under double-blind review

ABSTRACT

The paradigm of worst-group loss minimization has shown its promise in avoiding to learn spurious correlations, but requires costly additional supervision on spurious attributes. To resolve this, recent works focus on developing weaker forms of supervision—e.g., hyperparameters discovered with a small number of *validation samples* with spurious attribute annotation—but none of the methods retain comparable performance to methods using full supervision on the spurious attribute. In this paper, instead of searching for weaker supervisions, we ask: Given access to a fixed number of samples with spurious attribute annotations, what is the best achievable worst-group loss if we "fully exploit" them? To this end, we propose a pseudo-attribute-based algorithm, coined Spread Spurious Attribute (SSA), for improving the worst-group accuracy. In particular, we leverage samples both with and without spurious attribute annotations to train a model to predict the spurious attribute, then use the pseudo-attribute predicted by the trained model as supervision on the spurious attribute to train a new robust model having minimal worst-group loss. Our experiments on various benchmark datasets show that our algorithm consistently outperforms the baseline methods using the same number of validation samples with spurious attribute annotations. We also demonstrate that the proposed SSA can achieve comparable performances to methods using full (100%) spurious attribute supervision, by using a much smaller number of annotated samples—from 0.6% and up to 1.5%, depending on the dataset.

1 INTRODUCTION

Machine learning models trained on datasets containing spurious correlation often end up learning such "shortcuts" instead of intended solutions (Geirhos et al., 2020). For example, consider an image classification dataset of 'cows' and 'camels,' in which most images of cows appear on grasslands and camels on deserts. When trained on such a dataset, models often learn to make predictions based on the landscape instead of the intended object (Beery et al., 2018). This phenomenon can lead to very low test accuracy on groups that are underrepresented in the training set.

Various approaches have been proposed to resolve this gap, and the idea of *minimizing the worst-group loss*—e.g., Sagawa et al. (2020)—has arisen as one of the most promising methods. This approach forces high performances on both the majority group (e.g., cows standing on grasslands) and the minority group which contradicts the spurious correlation (e.g., cows standing on deserts). Despite its effectiveness, the worst-case loss minimization approach has a drawback: The learner requires supervision on which group each training sample belongs. For example, the learner needs to know that sample belongs to both the 'cow' and the 'desert' categories to utilize such group information to perform worst-group loss minimization. Even if we put aside the issue of identifying the spuriously correlated attributes ('desert' and 'grass') in the first place, one still needs to collect additional annotation on such spurious attributes. Acquiring such fine-grained annotation is presumably more expensive to collect, as the annotator needs a clear understanding of both the target attribute ('cow' and 'camel') and the spurious attribute ('desert' and 'grass').

Acknowledging this difficulty, a recent line of works proposes worst-group loss minimization algorithms that require a smaller number of samples with spurious attribute annotations (Nam et al.,
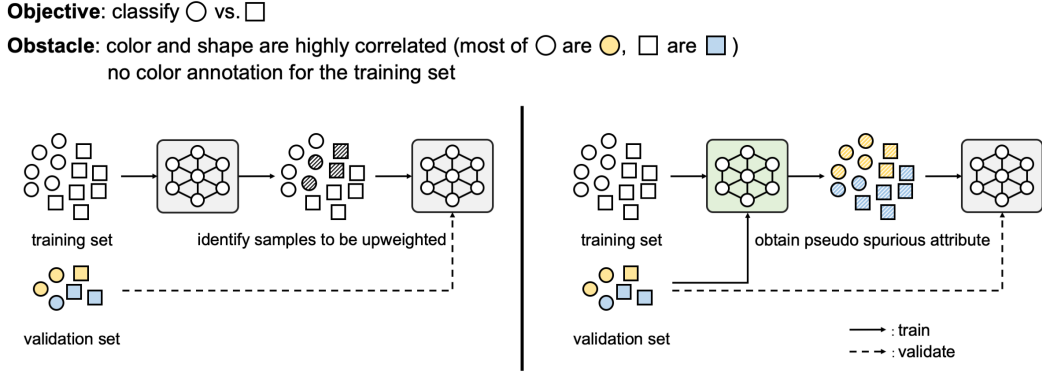
Figure 1: Comparison of prior approaches (left) and the proposed approach (right). **Left:** Existing works use samples with spurious attribute annotations only for tuning hyperparameters. **Right:** The proposed SSA uses the samples with spurious attribute annotation both for training the model and validation the trained model.

2020; Liu et al., 2021). At a high level, these works share a similar strategy (Fig. 1, Left): The methods first use a specialized mechanism to identify the minority group samples among the unannotated samples, and train a model in a way that puts more emphasis on identified-as-minority samples, e.g., by upweighting. A small set of annotated samples—which we will call *validation set*—are used to tune hyperparameters of this procedure; as Liu et al. (2021) shows, the final performance of these methods are very sensitive to these hyperparameters, indicating the high dependency of such algorithms on the availability of the validation set. Although these methods can achieve higher worst-group accuracy than completely annotation-free methods, e.g., Sohoni et al. (2020), they fail to perform comparably to the methods which use full annotations on spurious attributes, e.g., Sagawa et al. (2020). This performance gap gives rise to the following question: Can we closely achieve the full-annotation performance using a partially annotated dataset, if we use such annotations more *actively* than hyperparameter-tuning?

Contribution. This paper proposes a worst-group loss minimization algorithm, coined Spread Spurious Attribute (SSA). At a high level, SSA consists of two phases—*pseudo-labeling* phase and *robust training* phase—that is designed to make full use out of the validation set (Fig. 1, Right):

- *Pseudo-labeling:* SSA trains a spurious attribute predictor, using both the validation set samples and *training set* samples (i.e., samples lacking spurious attribute annotations). We find that group imbalances underlying the dataset can incur a severe *confirmation bias* detrimental to the performance (as in Kim et al. (2020)), and propose using *group-wise adaptive thresholds* to mitigate this problem. The predictions are used as pseudo-labels (Lee, 2013) on the training set.
- *Robust training:* Based on the pseudo-labeled training set, SSA trains a model which predicts the target attribute, using the worst-group loss minimization algorithms developed for fully supervised cases. We use Group DRO (Sagawa et al., 2020) as a default choice, and utilize the validation set for hyperparameter tuning.

Our experimental results suggest that SSA is a general yet effective framework of worst-case loss minimization. On various benchmark datasets, SSA consistently achieves performances comparable to fully supervised Group DRO and outperforms other baseline methods even when using only 5% of the validation set compared to the baselines. To be more specific, SSA requires less than 1.5%, and as little as 0.6% of attribute annotated samples—993 out of 182637 on CelebA, and 4123 out of 288637 on MultiNLI—to achieve similar worst-group accuracy to that of 100% usage. Moreover, we find that such benefits of SSA persist when combined with other robust training methods, such as supervised contrastive learning (SupCon; Khosla et al. (2020)). Finally, we also empirically observe that the group-wise adaptive thresholding technique—which we proposed for better pseudo-labeling—enjoy a broader usage for addressing the general problem of semi-supervised learning under class imbalance; existing pseudo-labeling techniques (Kim et al., 2020; Wei et al., 2021) require certain assumptions in datasets to work well for the task, while ours does not.

2 RELATED WORKS

Improving worst-group accuracy with group annotations. It has been known in various literature that machine learning models often perform significantly worse on the samples from groups with a relatively small number of training samples than on samples from the majority class. The *class imbalance* problem (Japkowicz, 2000; Johnson & Khoshgoftaar, 2019) is one of the representative cases of this phenomenon. Here, class labels naturally define the group identities and thus do not require any additional group annotations. In this context, popular strategies to improve worst-group performances are using *re-weighted loss* for each group (Huang et al., 2016; Khan et al., 2017) and *re-sampling* the given dataset to balance the group distribution of the training dataset (Chawla et al., 2002; He & Garcia, 2009). In contrast, this paper considers a setup where the group is defined as a combination of label and spuriously correlated attributes; unlike the class imbalance literature, the availability of the full group identity information is not guaranteed, as spurious attributes may not have proper annotations. Whenever the annotations for spurious attributes are available for all samples, Sagawa et al. (2020) shows promising results for improving robustness to spurious correlations with an online optimization algorithm for minimizing worst-group loss.

Improving worst-group accuracy without group annotations. Recently, a series of works aimed to train a robust model without requiring group annotation for the training samples to reduce additional annotation costs. These works utilize a model trained with standard procedure to identify samples that disagree with spurious correlations. Nam et al. (2020) train a model to be intentionally biased by minimizing generalized cross entropy, and use it to identify-and-upweight the high-loss samples to train another model. Liu et al. (2021) train a standard ERM model for a few epochs and upweight samples misclassified by this model to train the second model. Although these approaches do not use any group information for training, they still use a small number of group-annotated samples for hyperparameter tuning, which is critical to their worst-group performance. In this paper, we design algorithms to utilize such annotated samples more efficiently to boost performance. We note that, in the class imbalance literature, another line of works proposes to use group annotated validation samples more actively; they use validation samples for determining sample weights for the training set through meta-learning (Ren et al., 2018) or training a model to predict sample weights (Shu et al., 2019).

3 PROBLEM SETUP

We consider the task of learning a classifier in the presence of spurious correlations in the training set. Following the prior work of Sagawa et al. (2020), we cast this problem as minimizing the worst-group loss, where the group identity is determined by the target attribute (that we want to predict), and the spurious attribute (that we want to ignore). We assume that we do not know the spurious attributes of the samples in the training set, but have an access to additional set of samples—which we call *validation set*, in accordance with notations of Liu et al. (2021)—that are annotated with both the spurious attribute and the target attribute.

More formally, we assume that each sample is a triplet consisting of an *input* $x \in \mathcal{X}$, a *target attribute* $y \in \mathcal{Y}$, and a *spurious attribute* $a \in \mathcal{A}$. Our goal is to train a parameterized model $f_\theta : \mathcal{X} \to \mathcal{Y}$ that minimizes the worst-group expected loss on test samples; for the purpose of avoiding learning spurious correlations, we define the *group* as an attribute pair $g := (y, a) \in \mathcal{Y} \times \mathcal{A} =: \mathcal{G}$. In other words, we aim to minimize

$$R(\theta) = \max_{g \in \mathcal{G}} \mathbb{E}_{(x,y,a) \sim P_g}[\ell(f_\theta(x), y)], \tag{1}$$

for some loss function $\ell : \mathcal{Y} \times \mathcal{Y} \to \mathbb{R}$, where P_g denotes the group-conditioned data-generating distribution. Note that as we focus on the group defined by the attribute pairs, P_g is deterministic on y and a, and stochastic only on x.

We assume that the learner has access to two types of samples for training: The *training set* consists of n samples without spurious attribute annotations, i.e., $\mathcal{D}_{\text{train}} := \{(x_1, y_1), \ldots, (x_n, y_n)\}$, and the *validation set* consists of m samples with spurious attribute annotations, i.e., $\mathcal{D}_{\text{val}} := \{(\tilde{x}_1, \tilde{y}_1, \tilde{a}_1), \ldots, (\tilde{x}_m, \tilde{y}_m, \tilde{a}_m)\}$. We assume that these samples annotated with spurious attributes are much more costly to collect, i.e., $n \gg m$.

4 Spread Spurious Attribute

We now describe the algorithm we propose, Spread Spurious Attribute (SSA). At a high level, SSA consists of two phases: *pseudo-labeling phase*, and *robust training phase*. In the pseudo-labeling phase, SSA trains a model to predict the spurious attribute. In particular, we use *both* training and validation set to generate pseudo-labels on the training data (explained in detail in Section 4.1), using the adaptive thresholding technique for balancing the number of samples for each group (Section 4.2). Then, in the robust training phase, SSA uses the generated pseudo-label to train a model that predicts the target attribute with a small worst-group loss (Section 4.3). We use Group DRO (Sagawa et al., 2020) as a default method, but as we will show in Section 5.3, our approach also performs well when combined with other existing algorithms that use full spurious label supervisions, e.g., modified SupCon loss (Zhang et al., 2021).

4.1 Pseudo-labeling using training and validation samples

Using both validation set $\mathcal{D}_{\text{val}}$ and training set $\mathcal{D}_{\text{train}}$, we train a model to predict spurious attributes on the training set. The predictions will be used to generate artificial spurious attribute labels on the training set, called pseudo-labels (Lee, 2013). We emphasize that we also use $\mathcal{D}_{\text{train}}$ for *training* the model, instead of training solely based on $\mathcal{D}_{\text{val}}$. In fact, as we shall see in Section 5.2, the additional use of training set brings a significant performance boost. More specifically, we first partition both the validation set and training set into two:

$$\mathcal{D}_{\text{val}} = \mathcal{D}_{\text{val}}^{\circ} \cup \mathcal{D}_{\text{val}}^{\bullet}, \quad \mathcal{D}_{\text{train}} = \mathcal{D}_{\text{train}}^{\circ} \cup \mathcal{D}_{\text{train}}^{\bullet}. \tag{2}$$

The sets $\mathcal{D}_{\text{val}}^{\circ}, \mathcal{D}_{\text{train}}^{\circ}$ are used to *train* the model that predicts the spurious attribute on the remaining training set $\mathcal{D}_{\text{train}}^{\bullet}$, which will be validated using the samples in $\mathcal{D}_{\text{val}}^{\bullet}$.[1]

To train the spurious attribute predictor, we use the loss function consisting of two terms: the supervised loss for the samples in $\mathcal{D}_{\text{val}}^{\circ}$, and the unsupervised loss for samples in $\mathcal{D}_{\text{train}}^{\circ}$. For the supervised loss, we use the standard cross entropy loss. For the unsupervised loss, we use the cross-entropy loss between the prediction and the *pseudo-labels*, i.e., labels generated by taking the $\arg\max$ of predictions. Following prior works (e.g., Sohn et al. (2020)), we apply the loss only if the confidence of the prediction exceeds some threshold $\tau \geq 0$. More formally, let us denote the class probability estimate of the predictor on the attribute a given the input x as $\hat{p}(a|x)$, and the pseudo-label from this prediction as $\hat{a}(x) = \arg\max_{a \in \mathcal{A}} \hat{p}(a|x)$. Then, the supervised and unsupervised losses are

$$\ell_{\text{sup}}(x, y, a) = \text{CE}(\hat{p}(\cdot|x), a), \quad \ell_{\text{unsup}}(x, y) = \mathbf{1}\Big\{ \max_{a \in \mathcal{A}} \hat{p}(a|x) \geq \tau \Big\} \cdot \text{CE}\left(\hat{p}(\cdot|x), \hat{a}(x)\right), \tag{3}$$

where $\text{CE}(\hat{p}(\cdot|x), a)$ denotes the cross-entropy loss between the prediction $\hat{p}(\cdot|x)$ and label a. As we will describe with more detail in Section 4.2, we use group-wise adaptive thresholds for pseudo-labeling. The thresholds are determined in a way that balances the *pseudo-group* (i.e., the pair $\hat{g} = (y, \hat{a}(x))$) population of the samples with confidence exceeding the group-wise threshold. This strategy helps the model to avoid making a pseudo-label prediction biased toward the majority group.

We note that running this procedure once does not generate pseudo-labels for all samples in $\mathcal{D}_{\text{train}}$, even when we set $\tau = 0$. This is because we make predictions only on samples in $\mathcal{D}_{\text{train}}^{\bullet}$ and not on samples in $\mathcal{D}_{\text{train}}^{\circ}$. To make a full use of $\mathcal{D}_{\text{train}}$, we run this procedure multiple times using a different split of $\mathcal{D}_{\text{train}}^{\circ}, \mathcal{D}_{\text{train}}^{\bullet}$. Detailed experimental setups are given in Appendix A.1.

4.2 Balancing generated pseudo-labels via adaptive thresholds

As we train the pseudo-labeling model with the loss described in Eq. (3), the prediction confidence of the model on each sample gradually increases. This growth affects the pseudo-group population ratio of the highly-confident samples (i.e., with confidence greater than some threshold). If the underlying group population is severely imbalanced—as is very common with spurious attributes— samples belonging to the majority group often attains the high prediction confidence significantly faster than samples in minority groups, by receiving more frequent gradient updates. This imbalance in learning leads to an even more severe imbalance in the pseudo-labels, which have detrimental effects on the subsequent training steps.

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[1]We write $\circ$ to denote that samples are "visible" during the training phase, and $\bullet$ to denote that they are not.

To resolve this *confirmation bias*, we set different threshold for each pseudo-group, so that the same number of (either training or validation set) samples from each group is used for training with Eq. (3). To do this, we first set a fixed threshold $\tau_{g_{\min}}$ for the *group with the smallest population* in the training split of the validation set, i.e., the group defined as

$$g_{\min} = \arg\min_{g \in \mathcal{Y} \times \mathcal{A}} |\mathcal{D}_{\text{val}}^{\circ}(g)|, \qquad \text{where } \mathcal{D}_{\text{val}}^{\circ}(g) := \left\{ (x, y, a) \in \mathcal{D}_{\text{val}}^{\circ} \mid g = (y, a) \right\}. \tag{4}$$

Next, we count the number of samples in $\mathcal{D}_{\text{train}}^{\circ}$ that (a) belongs to $g_{\min}$ after pseudo-labeling, and (b) the prediction confidence exceeds $\tau_{g_{\min}}$. Then, we set thresholds for other groups to have same number of samples from each group. More concretely, let $\mathcal{D}_{\text{train}}^{\circ}(g, \tau_g)$ be the set of samples in the training split of the training set with the pseudo-group g and confidence greater than equal to τ_g, i.e.,

$$\mathcal{D}_{\text{train}}^{\circ}(g, \tau_g) := \left\{ (x, y) \in \mathcal{D}_{\text{train}}^{\circ} \mid g = (y, \hat{a}(x)), \quad \max_{a \in \mathcal{A}} \hat{p}(a|x) \geq \tau_g \right\}. \tag{5}$$

Then, for each group $g \neq g_{\min}$, we set τ_g to be the smallest real number such that

$$|\mathcal{D}_{\text{val}}^{\circ}(g)| + |\mathcal{D}_{\text{train}}^{\circ}(g, \tau_g)| \leq |\mathcal{D}_{\text{val}}^{\circ}(g_{\min})| + |\mathcal{D}_{\text{train}}^{\circ}(g_{\min}, \tau_{g_{\min}})|. \tag{6}$$

With this group-wise adaptive threshold, we use the unsupervised loss revised as

$$\ell_{\text{unsup}}(x, y) = \mathbf{1}\left\{ \max_{a \in \mathcal{A}} \hat{p}(a|x) \geq \tau_{(y, \hat{a}(x))} \right\} \cdot \text{CE}\left(\hat{p}(\cdot|x), \hat{a}(x) \right). \tag{7}$$

We show the effectiveness of this group-wise adaptive threshold in Section 5.2, and further applicability to class-imbalance problem in Section 5.4.

4.3 Worst-group loss minimization with estimated pseudo-groups

After training the model using the revised loss (Section 4.2), we generate final pseudo-labels for all samples in the training set. In other words, we generate

$$\widetilde{\mathcal{D}}_{\text{train}} = \left\{ (x, y, \hat{a}(x)) \mid (x, y) \in \mathcal{D}_{\text{train}} \right\}. \tag{8}$$

We emphasize that we put pseudo-labels on all samples without applying any threshold, which allows us to utilize the whole training set.

Then, in the robust training phase, we use the labeled datasets $\widetilde{\mathcal{D}}_{\text{train}}$ and $\mathcal{D}_{\text{val}}$ to perform worst-group loss minimization. We use Group DRO (Sagawa et al., 2020) as our default algorithm, using $\widetilde{\mathcal{D}}_{\text{train}}$ for training and $\mathcal{D}_{\text{val}}$ for validation purposes. We note that we can also use other worst-case loss minimization algorithms instead of Group DRO; indeed, in Section 5.3, we show that our framework performs well with SupCon as a surrogate for Group DRO.

5 Experiments

Here, we briefly describe the experiment setup that will be used throughout all experiments in this section, except for Section 5.4 where we consider a slightly different scenario.

Datasets. We evaluate SSA on two image classification datasets (Waterbirds, CelebA) and two natural language processing datasets (MultiNLI, CivilComments-WILDS) containing spurious correlations. Below, we briefly describe each dataset and the corresponding spurious correlations.

- *Waterbirds* (Sagawa et al., 2020): Waterbirds is an artificial dataset generated by combining bird photographs in the Caltech-UCSD Birds dataset (Wah et al., 2011) with landscapes from Places (Zhou et al., 2017). The goal is to classify the target attributes $\mathcal{Y} = \{\text{waterbird, landbird}\}$ given the spurious correlations with the background landscape $\mathcal{A} = \{\text{water background, land background}\}$.
- *CelebA* (Liu et al., 2015): CelebA dataset consists of the face pictures of celebrities, with various annotations on facial/demographic features. We use the hair color as the target attribute $\mathcal{Y} = \{\text{blond, non-blond}\}$, given the spurious correlations with the gender $\mathcal{A} = \{\text{male, female}\}$.

Table 1: Average and worst-group test accuracies evaluated on image classification datasets (Waterbirds, CelebA). For more rigorous comparison, we run SSA and Group DRO on 3 random seeds and report the average and the standard deviation. Other results are from Liu et al. (2021). Best performances (among methods using only validation set labels) are marked in bold.

Method	Amount of group label used	Waterbirds		CelebA	
		Avg.	Worst-group	Avg.	Worst-group
ERM	val. set	97.3	72.6	95.6	47.2
CVaR DRO (Levy et al., 2020)	val. set	96.0	75.9	82.5	64.4
LfF (Nam et al., 2020)	val. set	91.2	78.0	85.1	77.2
JTT (Liu et al., 2021)	val. set	93.3	86.7	88.0	81.1
SSA (Ours)	val. set	$92.2_{\pm0.87}$	$\mathbf{89.0}_{\pm0.55}$	$92.8_{\pm0.11}$	$\mathbf{89.8}_{\pm1.28}$
	5% of val. set	$92.6_{\pm0.15}$	$87.1_{\pm0.70}$	$92.8_{\pm0.34}$	$86.7_{\pm1.11}$
Group DRO (Sagawa et al., 2020)	train. & val. set	$91.8_{\pm0.48}$	$89.2_{\pm0.18}$	$93.1_{\pm0.21}$	$88.5_{\pm1.16}$

Table 2: Average and worst-group test accuracies evaluated on natural language datasets (MultiNLI, CivilComments-WILDS). For more rigorous comparison, we run SSA and Group DRO on 3 random seeds and report the average and the standard deviation. Other results are from Liu et al. (2021). Best performances (among methods using only validation set labels) are marked in bold.

Method	Amount of group label used	MultiNLI		CivilComments-WILDS	
		Avg.	Worst-group	Avg.	Worst-group
ERM	val. set	82.4	67.9	92.6	57.4
CVaR DRO (Levy et al., 2020)	val. set	82.0	68.0	92.5	60.5
LfF (Nam et al., 2020)	val. set	80.8	70.2	92.5	58.8
JTT (Liu et al., 2021)	val. set	78.6	72.6	91.1	69.3
SSA (Ours)	val. set	$79.9_{\pm0.87}$	$\mathbf{76.6}_{\pm0.66}$	$88.2_{\pm1.95}$	$\mathbf{69.9}_{\pm2.02}$
	5% of val. set	$80.4_{\pm0.62}$	$76.5_{\pm1.89}$	$89.1_{\pm1.09}$	$69.5_{\pm1.15}$
Group DRO (Sagawa et al., 2020)	train. & val. set	$81.4_{\pm1.40}$	$76.6_{\pm0.41}$	$87.7_{\pm1.35}$	$69.1_{\pm1.53}$

- *MultiNLI* (Williams et al., 2018): MultiNLI is a multi-genre natural language corpus where each data instance consists of two sentences and a label indicating whether the second sentence is entailed by, contradicts, or neutral to the first. We use this label as the target attribute (i.e., $\mathcal{Y} = \{\text{entailed, neutral, contradictory}\}$), and use the existence of the negating words as the spurious attribute (i.e., $\mathcal{A} = \{\text{negation, no negation}\}$).

- *CivilComments-WILDS* (Borkan et al., 2019; Koh et al., 2021): CivilComments-WILDS consists of comments generated by online users, each of which are labeled with the toxicity indicator $\mathcal{Y} = \{\text{toxic, non-toxic}\}$. We use demographic attributes of the mentioned identity $\mathcal{A} = \{\text{male, female, White, Black, LGBTQ, Muslim, Christian, other religion}\}$ as a spurious attribute for evaluation purpose. We note that a comment can contain multiple such identities, so that groups defined by $\mathcal{Y} \times \mathcal{A}$ can be overlapped. Therefore, we use $\mathcal{A}' = \{\text{any identity, no identity}\}$ as a spurious attribute for training, following Liu et al. (2021).

Models. For the all experiments on image classification datasets, we use ResNet-50 (He et al., 2016) starting from ImageNet-pretrained weights. For experiments on language datasets, we use pretrained BERT (Devlin et al., 2019). We use the same architecture for predicting the spurious attribute (in the pseudo-labeling phase) and the target attribute (in the robust training phase).

5.1 MAIN RESULTS

We compare the average and worst-case performance of the proposed SSA against the standard empirical risk minimization (ERM) and recent methods that tackles spurious correlation without group annotation for the training, including CVaR DRO (Levy et al., 2020), LfF (Nam et al., 2020), JTT (Liu et al., 2021), and Group DRO (Sagawa et al., 2020) requiring group annotation to minimize the worst-group loss.

In Table 1, 2, we report average accuracies and the worst-group accuracies on all datasets we consider. Our method consistently outperforms all the other apporaches that use spurious attribute annotated dataset for validation while using the same amount of spurious attribute annotation. Notably, our method shows comparable performance to Group DRO which uses full amount of spurious

Table 3: Worst-group accuracy on Waterbirds and CelebA with varying validation set size.

Method	Waterbirds				CelebA			
	100%	20%	10%	5%	100%	20%	10%	5%
JTT (Liu et al., 2021)	86.7	84.0	86.9	76.0	81.1	81.1	81.1	82.2
SSA (Ours)	89.0	88.9	88.9	87.1	89.8	88.9	90.0	86.7

Table 4: Group-wise accuracy for spurious attribute prediction on CelebA. Results of the worst-performing group are marked in bold.

Method	Amount of group label used	# (Blond, Male) in val set	Non-blond		Blond	
			Female	Male	Female	Male
Vanilla			90.2	90.3	97.0	**70.4**
Pseudo-labeling	10% of val set	18	94.2	95.5	98.8	**76.4**
+ Group-wise threshold			89.5	93.9	95.1	**83.6**
Vanilla			88.0	89.7	96.3	**68.7**
Pseudo-labeling	5% of val set	8	92.2	94.2	98.4	**67.8**
+ Group-wise threshold			83.3	90.6	92.7	**75.7**

attribute annotation for the training set, even outperforms on CelebA dataset. We also run our algorithm using only 5% of the default validation set to show efficiency of our algorithm to improve the worst-group accuracy. We further provide analysis on varying validation set size below.

Effect of validation set size. Although we focus on improving the worst-group performance with given amount of spurious annotation, reducing the amount of supervision is an important topic to discuss especially with high annotation cost. In the main results in Table 1, 2, we use the default validation sets provided by each dataset as $\mathcal{D}_{val}$. To further test whether SSA can achieve high worst-group accuracy with reduced amount of supervision, we run our algorithm with small fraction of the default validation sets. Following Liu et al. (2021), we run our method using 100%, 20%, 10%, 5% of the default validation set. In Table 3, we report the worst-group accuracy of JTT and our algorithm on Waterbirds and CelebA, with various validation set size. Surprisingly, we find that our method maintains high worst-group accuracy even with the 10% of the original validation set. Most notably, the number of attribute annotated samples used for training spurious attribute predictor is 58 in total, 6 for the worst-group in Waterbirds when we only use 10% of the default validation set.

5.2 DETAILED ANALYSIS ON THE PSEUDO-LABELING PHASE OF SSA

We now take a closer look at the pseudo-labeling phase of the proposed SSA. In particular, we focus on validating the effectiveness of the group-wise adaptive threshold we introduced in Section 4.2. The purpose of the adaptive threshold was to prevent the confirmation bias that may take place during the pseudo-labeling phase; the prediction confidence of the majority group samples may exceed the threshold faster than samples of minority group, increasing the contribution of majority-group samples on the loss even further. In the first set of experiments (Table 4), we perform ablation studies on the pseudo-labeling and the adaptive threshold to see their effects on the spurious attribute prediction performance of the SSA. In the second set of experiments (Table 5), we validate if the confirmation bias takes place indeed, and check that our adaptive threshold strategy successfully addresses the phenomenon.

Performance comparison. In Table 4, we report the group-wise spurious attribute prediction accuracies of SSA on CelebA dataset (using 5% or 10% of the validation split as the validation set) for following ablations: (1) *Vanilla*: Does not use any pseudo-labels and train the model using only the validation set samples. (2) *Pseudo-labeling*: Uses pseudo-labeling with a fixed threshold, and (3) *+Group-wise threshold*: Identical to SSA, using group-wise adaptive thresholds for pseudo-labeling. We find that using the group-wise threshold increases the spurious attribute prediction accuracy for the worst-group—$(y, a) = (\text{Blond}, \text{Male})$, providing 7% boost in both cases. Interestingly, we observe that pseudo-labeling with fixed thresholds can even slightly degrade the performance, when the validation set is too small (5%).

Table 5: Samples statistics during the training of spurious attribute predictor on CelebA with 5% of the default validation set.

Description	Non-blond		Blond		Fraction of (Blond, Male)
	Female	Male	Female	Male	
Number of training samples ($|\mathcal{D}_{\text{train}}^{\circ}|$)	47750	44617	15240	906	0.83%
Number of validation samples ($|\mathcal{D}_{\text{val}}^{\circ}|$)	213	206	71	4	0.81%
Pseudo-labeling					
Number of samples exceeding fixed threshold	45897	43201	15344	712	0.68%
Number of samples used for training	45897	43201	15344	712	0.68%
+ Group-wise threshold					
Number of samples exceeding fixed threshold	32926	34622	12733	712	0.88%
Number of samples used for training	501	528	681	716	29.5%

Table 6: Average and the worst-group accuracy of the proposed SSA algorithm, when combined with two different choices of supervised worst-case loss minimization algorithms.

Method	Amount of group label used	Waterbirds		CelebA	
		Avg.	Worst-group	Avg.	Worst-group
ERM	val. set	97.3	72.6	95.6	47.2
JTT (Liu et al., 2021)	val. set	93.3	86.7	88.0	81.1
SSA w/ Group DRO (Ours)	val. set	$92.2_{\pm0.87}$	$89.0_{\pm0.55}$	$92.8_{\pm0.11}$	$89.8_{\pm1.28}$
Group DRO (Sagawa et al., 2020)	train. & val. set	$91.8_{\pm0.48}$	$89.2_{\pm0.18}$	$93.1_{\pm0.21}$	$88.5_{\pm1.16}$
SSA w/ SupCon (Ours)	val. set	$92.6_{\pm0.40}$	$89.2_{\pm0.24}$	$91.7_{\pm1.32}$	$87.6_{\pm0.32}$
SupCon (Khosla et al., 2020)	train. & val. set	$92.5_{\pm0.49}$	$90.0_{\pm0.56}$	$92.5_{\pm0.62}$	$87.4_{\pm0.85}$

Population comparison. In Table 5, we compare the populations of pseudo-labeled samples that contribute to the training, for pseudo-labeling using a fixed threshold ('Pseudo-labeling') and the adaptive threshold ('+Group-wise threshold'); for each method, we trained the spurious attribute predictor until the worst-group spurious attribute prediction accuracy reaches the highest point. We used CelebA dataset with only 5% of the validation split. From the experimental results, we find that naïve pseudo-labeling with a fixed threshold indeed leads to a confirmation bias, using only 0.68% of the minority group (male blond) for training while the true fraction of the group is over 0.8%. On the other hand, using the adaptive threshold successfully addresses this problem, lifting the fraction of blond male samples to 0.88%, which is close to the population level. More impressively, we observe that pseudo-labeling phase adaptive threshold uses relatively uniform number of samples from each group to training the spurious attribute predictor.

5.3 SSA COMBINED WITH SUPERVISED CONTRASTIVE LEARNING

We now examine whether the proposed SSA still remains to be beneficial when combined with a recent robust training procedure (Zhang et al., 2021) proposed as an alternative to Group DRO. More specifically, Zhang et al. (2021) considers a following procedure base on the supervised contrastive loss (Khosla et al., 2020): As in JTT (Liu et al., 2021), we first train a standard ERM model. Then, we use the contrastive loss to maximize the representational similarity between samples have the same target label but different ERM prediction, while minimizing the representational similarity of samples with different target attribute but same ERM prediction. This procedure can be smoothly combined the SSA framework, by replacing the ERM predictions with the pseudo-labels generated in the first phase of SSA.

In Table 6, we compare the performance of SSA using Group DRO or SupCon with the performance of the robust training methods using the full spurious attribute annotations on the training set. Both models learned with SSA significantly outperforms the baseline (JTT), and achieved comparable performance to the fully supervised counterparts. This result suggests that the benefit of SSA may not be constrained on a specific robust training method, and may be combined with more general classes of robust training algorithms. Also, we find that none of the robust training method consistently outperform the other; SupCon slightly outperforms Group DRO on Waterbirds, and Group DRO does better on CelebA.

Table 7: Comparison of classification performance (bACC/GM) on CIFAR-10 under 4 different sets of $(m_{\text{maj}}, n_{\text{maj}}, \gamma_{\text{lab}})$, where m_{maj} denotes number of labeled samples in to the largest class, n_{maj} denotes the number of unlabeled samples in the largest class, and γ_{lab} denotes the largest-to-smallest class ratio in the labeled set (we let $\gamma_{\text{unlab}} = 1$). The best results are indicated in bold.

	$(m_{\text{maj}}, n_{\text{maj}}, \gamma_{\text{lab}})$			
Algorithm	$(500, 4500, 100)$	$(500, 4500, 50)$	$(100, 4900, 50)$	$(100, 4900, 20)$
Vanilla	$42.1_{\pm0.66} / 25.5_{\pm1.16}$	$50.3_{\pm0.14} / 41.6_{\pm0.40}$	$28.0_{\pm0.97} / 13.0_{\pm1.90}$	$34.4_{\pm1.78} / 26.4_{\pm2.86}$
FixMatch (Sohn et al., 2020)	$65.6_{\pm0.35} / 26.8_{\pm0.82}$	$68.3_{\pm0.15} / 30.4_{\pm0.28}$	$56.4_{\pm0.23} / 14.9_{\pm1.21}$	$69.1_{\pm1.96} / 42.1_{\pm2.37}$
DARP (Kim et al., 2020)	$75.6_{\pm0.26} / 73.1_{\pm0.19}$	$78.2_{\pm0.14} / 76.5_{\pm0.26}$	$72.3_{\pm0.28} / 67.8_{\pm0.45}$	$77.5_{\pm0.47} / 75.2_{\pm0.71}$
CReST (Wei et al., 2021)	$77.4_{\pm0.36} / 61.6_{\pm2.11}$	$79.7_{\pm1.00} / 77.2_{\pm1.01}$	$67.4_{\pm0.70} / 34.7_{\pm3.23}$	$69.8_{\pm0.35} / 53.6_{\pm0.42}$
Adaptive thresholds (Ours)	$\mathbf{86.1}_{\pm0.44} / \mathbf{85.7}_{\pm0.47}$	$\mathbf{87.4}_{\pm0.03} / \mathbf{87.1}_{\pm0.02}$	$\mathbf{83.8}_{\pm0.19} / \mathbf{82.7}_{\pm0.43}$	$\mathbf{86.5}_{\pm0.16} / \mathbf{86.1}_{\pm0.16}$
Oracle	$93.6_{\pm0.18} / 93.5_{\pm0.18}$	$93.6_{\pm0.18} / 93.5_{\pm0.18}$	$93.6_{\pm0.15} / 93.6_{\pm0.15}$	$93.9_{\pm0.02} / 93.8_{\pm0.03}$

5.4 APPLICATION TO GENERAL SEMI-SUPERVISED LEARNING UNDER CLASS IMBALANCE

In Section 4.2, we proposed to use adaptive thresholding to mitigate confirmation bias when pseudo-labeling group-imbalanced datasets. Interestingly, it turns out that the benefit of this idea also extends (without any modification) to a more general scenario of semi-supervised learning (SSL) on datasets with class imbalances. In fact, two settings are quite similar, except that SSA aims to put pseudo-labels on spurious attributes while SSL methods estimate target attributes. To demonstrate this point, we evaluate adaptive thresholds under the SSL setup, and compare it with the performances of baseline pseudo-labeling-based SSL algorithms. FixMatch (Sohn et al., 2020) is a recent SSL method proposed without considerations on the class imbalance issue. DARP (Kim et al., 2020) and CReST (Wei et al., 2021) build on FixMatch to handle class imbalance, but are primarily designed under the assumptions that there exists sufficiently many labeled data at hand (to estimate the class imbalance ratio), and that class distributions of labeled and unlabeled datasets are identical, respectively.[2] In contrast, our method of adaptive thresholds does not rely on such assumptions to solve the same task.

We consider a slightly more challenging experimental setup than in Kim et al. (2020): We construct an artificial labeled dataset from the CIFAR-10 (Krizhevsky et al., 2009) by controlling the number of samples in the majority class m_{maj} (i.e., the largest class) and the ratio between the largest and smallest class sizes $\gamma_{\text{lab}} \geq 1$.[3] In a similar manner, we construct an unlabeled dataset using some parameters n_{maj} and γ_{unlab}. We select these parameters so that the number of labeled samples is small, and the imbalance ratios of labeled and unlabeled sets have bigger discrepancies (We provide further details in Appendix A.4). In Table 7, we observe that empirical gains from both DARP and CReST are limited comparing to supervised learning with full ground-truth labels (oracle), due to the violation of their inherent assumptions in the experimental setups of our choice, i.e., limited labeled data and different class distribution between labeled and unlabeled datasets. However, our method successfully reduces such gap by effectively constructing the pseudo-labels for minority classes. Overall, these results implies that the proposed method has a potential to provide a more robust semi-supervised learning solution (despite its simplicity) in more realistic scenarios, which we think is an interesting direction to explore further in the future.

6 CONCLUSION

In this work, we present Spread Spurious Attribute (SSA), an algorithm for improving worst-group accuracy in the presence of spurious correlation. SSA framework uses a small amount of spurious attribute annotated samples to estimate group identities of the training set samples. With the generated attribute annotated training set, we successfully train a robust model using existing worst-case loss minimization algorithms. SSA is highly effective given a limited amount of the spurious attribute annotated samples, but still does not completely remove the need for supervision on spurious attributes which is an important future direction.

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[2]In fact, in the previous spurious attribute setups, adopting DARP/CReST methods did not provide much gain over naïve pseudo-labeling; we suspect the reason to be the violation of these assumptions.

[3]Larger γ_{lab} thus indicates a more severe imbalance.

ETHICS STATEMENT

This paper addresses the problem of mitigating the harmful effects of spurious correlations in the dataset, which is deeply intertwined with the topics of machine bias and fairness. By targeting demographic groups (e.g., gender, race) carefully, our method has a potential to be used for preventing the machine to make predictions on the basis of biases on such demographic identities. One possible pitfall, however, is that this group-based evaluation can provide a false sense of morality; as making a fair decision in terms of group cannot be equated with the individual fairness (even putting aside the issues of *gerrymandering*), our performance reports based on the worst-group performance should not be naïvely taken as a *measure of justice*. About the responsible research practice: We have used benchmark datasets, and thus believe that our research practice has not posed any foreseeable hazard in this regard.

REPRODUCIBILITY STATEMENT

We provide descriptions of the experimental setup and implementation details in Appendices A.1 to A.3. Also, we provide our (anonymized) source code as a part of the open-to-public supplementary materials.

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A EXPERIMENTAL DETAILS

A.1 DISCUSSIONS ON SPLITTING THE TRAINING AND VALIDATION SETS

Recall that in the pseudo-labeling phase of SSA (Section 4.1, we partition both the training set and the validation set into two subsets:

$$\mathcal{D}_{\text{val}} = \mathcal{D}_{\text{val}}^{\circ} \cup \mathcal{D}_{\text{val}}^{\bullet}, \quad \mathcal{D}_{\text{train}} = \mathcal{D}_{\text{train}}^{\circ} \cup \mathcal{D}_{\text{train}}^{\bullet}. \quad (9)$$

SSA then trains a spurious attribute predictor based on $\mathcal{D}_{\text{val}}^{\circ}, \mathcal{D}_{\text{train}}^{\circ}$, with hyperparameters tuned using $\mathcal{D}_{\text{val}}^{\bullet}$. The trained model is then used to make predictions on the samples in $\mathcal{D}_{\text{train}}^{\bullet}$.

Here, it is easy to see that, if we want to make a best prediction on a particular data point $x_\star \in \mathcal{D}_{\text{train}}$, then the optimal split would be the one that uses the largest number of training set samples for training the model, i.e.,

$$\mathcal{D}_{\text{train}}^{\circ} = \mathcal{D}_{\text{train}} \setminus \{x_\star\}, \quad \mathcal{D}_{\text{train}}^{\bullet} = \{x_\star\}. \quad (10)$$

However, such partitioning requires training $|\mathcal{D}_{\text{train}}|$ different models to label all samples in the training set, which is computationally infeasible. Thus, we propose partitioning the training dataset into K equally-sized subsets $\mathcal{D}_{\text{train}}^{(1)}, \ldots, \mathcal{D}_{\text{train}}^{(K)}$, and run the algorithm K times, using

$$\mathcal{D}_{\text{train}}^{\circ} = \cup_{\substack{j=1 \\ j \neq i}}^{K} \mathcal{D}_{\text{train}}^{(j)}, \quad \mathcal{D}_{\text{train}}^{\bullet} = \mathcal{D}_{\text{train}}^{(i)}, \quad (11)$$

for the i-th training iteration. For all experiments appearing in this paper, we used $K = 3$ for a simple evaluation; the empirical performance of SSA may improve if we use a larger value of K.

For the validation set, we do not require such trick. We simply partitioned the validation into two equally size subsets, and used one for training and another for validation. We kept the split fixed throughout the whole pseudo-labeling phase.

A.2 TRAINING DETAILS

Models. As we briefly discussed in the main text, we use pretrained ResNet-50 and BERT for image and natural language dataset experiments, respectively. For ResNet-50, we use the `torchvision` implementation. For BERT, we use the `huggingface` implementation.

Hyperparameter Tuning - Overall. We separately tune the hyperparameters for the pseudo-labeling phase and the robust training phase. For the pseudo-labeling phase, the tuning criterion is the worst-group *spurious label* classification accuracy on $\mathcal{D}_{\text{val}}^{\bullet}$. For the robust training phase, the tuning criterion is the worst-group prediction accuracy of the trained target attribute classifier on the whole validation set $\mathcal{D}_{\text{val}}$.

Hyperparameter Tuning - Image. For Waterbirds and CelebA, we tuned the learning rate over {1e-3, 1e-4, 1e-5} and ℓ_2 regularization over {1e-1, 1e-4}. We used SGD optimizer with momentum 0.9 and batch size 64.

Hyperparameter Tuning - Natural Language. For MultiNLI and CivilComments-WILDS, we did not tune any hyperparameter and follow the details of Liu et al. (2021). For MultiNLI, we trained SSA and its baselines for 5 epochs with default tokenization and dropout, using the batch size 32 and the initial learning rate of 2e-5. We did not use any ℓ_2 regularization. For CivilComments-WILDS, we capped the number of tokens per example at 300 and used batch size 8, ℓ_2 regularization of 1e-2 and initial learning rate of 1e-5. We used AdamW optimizer with gradient clipping for both MultiNLI and CivilComments-WILDS.

Hyperparameter Tuning - Robust Training. For the robust model, we use hyperparameters to maximize worst-group accuracy on $\mathcal{D}_{\text{val}}$. Following Liu et al. (2021), we use learning rate of 1e-4 and ℓ_2 regurlarization 1e-1 for Waterbirds, learning rate of 1e-5 and ℓ_2 regularization 1e-1 for CelebA. We use SGD optimizer with momentum 0.9 and batch size 64 for both Waterbirds and CelebA. For MultiNLI and CivilComments, we use the same configuration as pseudo-labeling phase, except using batch size 16 for CivilComments.

A.3 DETAILS ON SUPERVISED CONTRASTIVE LEARNING

Given an anchor (x_i, y_i), original supervised contrastive loss uses same class samples $(y = y_i)$ as positive samples and different class samples $(y \neq y_i)$ as negative samples to maximize similarity of representation between samples belong to same class. Correct-N-Contrast (CNC; Zhang et al. (2021)) first trains ERM model as JTT and use ERM prediction as a surrogate to ground truth spurious attribute. With obtained ERM prediction, CNC uses supervised contrastive loss to maximize similarity of representation between samples having same target and different ERM prediction, while minimizing similarity of representation between samples having different target and same ERM prediction. Similar to the second stage of CNC, given an anchor (x_i, y_i, a_i), we use samples having same target and different spurious attribute as positive samples $(y^+ = y_i, a^+ \neq a_i)$ and samples having different target and same spurious attribute as negative samples $(y^- \neq y_i, a^- = a_i)$. To be specific, we sample M samples from each group. Given an anchor (x_i, y_i, a_i), we use samples from group (y_i, a^+) for $a^+ \neq a_i$ as a set of positive samples B^+ and samples from group (y^-, a_i) for $y^- \neq y_i$ as a set of negative samples B^-. In addition to standard cross entropy loss, we minimizes following supervised contrastive loss for each anchor x_i:

$$\frac{1}{|B^+|} \sum_{z^+ \in B^+} - \log \frac{\exp(z_i \cdot z^+/\tau)}{\sum_{z \in B^+ \cup B^-} \exp(z_i \cdot z/\tau)}, \tag{12}$$

where $z = g(x)$ is a representation of x and $g : \mathcal{X} \to \mathbb{R}^d$ is an encoder maps x to a representation, $f = h \circ g$, $\tau > 0$ is a scalar temperature hyperparameter.

We use $M = 16$ for both Waterbirds and CelebA. Except batch size, we follow Zhang et al. (2021) for other hyperparameters. For Waterbirds, we use temperature 0.1, contrastive weight 0.75, SGD optimizer with momentum 0.9, learning rate 1e-4, weight decay 1e-3 and use gradient accumulation to update model parameter every 32 batches. For CelebA, we use temperature 0.05, contrastive weight 0.75, SGD optimizer with momentum 0.9, learning rate 1e-5, weight decay 1e-1 and use gradient accumulation to update model parameter every 32 batches.

A.4 DETAILS ON CLASS-IMBALANCED SEMI-SUPERVISED LEARNING

We consider a classification problem with K classes. In other words, our goal is to train a predictor $\mathcal{X} \to \mathcal{Y}$ with $\mathcal{Y} = \{1, \ldots, K\}$. We assume that we have access to two types of datasets: labeled, and unlabeled. We let

$$\mathcal{D}_{\text{lab}} := \{(\tilde{x}_1, \tilde{y}_1), \ldots, (\tilde{x}_m, \tilde{y}_m)\}, \quad \mathcal{D}_{\text{unlab}} := \{x_1, \ldots, x_n\}. \tag{13}$$

The number of samples in some class $k \in \mathcal{Y}$ will be denoted by m_k and n_k, respectively, i.e., $\sum_{k=1}^{K} m_k = n$ and $\sum_{k=1}^{K} m_k = m$. Without loss of generality, we assume that the number of labeled data in each class is ordered in a descending order, i.e.,

$$m_{\text{maj}} =: m_1 \geq m_2 \geq \cdots \geq m_K. \tag{14}$$

We define the *imbalance ratio* of this labeled dataset as the ratio between the sample sizes of the largest class and the smallest class, i.e., $\gamma_{\text{lab}} = m_1/m_K \geq 1$. This quantity is used as a key parameter that controls the degree of class imbalance in the labeled dataset; higher the γ_{lab}, more severe the imbalance. To determine the number of samples in other classes, we use an exponential decay function, i.e., $m_k = m_1 \cdot \gamma_{\text{lab}}^{(-k-1)/(K-1)}$. We assume that the same ordering holds for the unlabeled samples, i.e., $n_1 \geq \cdots \geq n_K$, and let define the imbalance ratio as $\gamma_{\text{unlab}} = n_1/n_K$. For simplicity, we let $\gamma_{\text{unlab}} = 1$, i.e., all classes have the same number of unlabeled samples.

To evaluate the classification performance of models trained under the imbalanced dataset, we report two popular metrics: *balanced accuracy* (bACC) and *geometric mean scores* (GM), which are defined by the arithmetic and geometric mean over class-wise sensitivity, respectively. Mean and standard deviation are reported across three random trials, respectively.