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# PyTorch-Geometric Edge – a library for learning representations of graph edges

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## Abstract

Machine learning on graphs (GraphML) has been successfully deployed in a wide variety of problem areas, as many real-world datasets are inherently relational. However, both research and industrial applications require a solid, robust, and well-designed code base. In recent years, frameworks and libraries, such as PyTorch-Geometric (PyG) or Deep Graph Library (DGL), have been developed and become first-choice solutions for implementing and evaluating GraphML models. These frameworks are designed so that one can solve any graph-related task, including node- and graph-centric approaches (e.g., node classification, graph regression). However, there are no edge-centric models implemented, and edge-based tasks are often limited to link prediction. In this extended abstract, we introduce PyTorch-Geometric Edge (PyGE), a deep learning library that focuses on models for learning vector representations of edges. As the name suggests, it is built upon the PyG library and implements edge-oriented ML models, including simple baselines and graph neural networks, as well as corresponding datasets, data transformations, and evaluation mechanisms. The main goal of the presented library is to make edge representation learning more accessible for both researchers and industrial applications, simultaneously accelerating the development of the aforementioned methods, datasets and benchmarks.

## 1 Introduction

Nowadays, one of the most prominent research areas in machine learning is representation learning. Solving classification, regression, or clustering tasks by means of popular machine learning models, like decision trees, SVMs, logistic regression, linear regression, or feed-forward neural networks, requires the presence of object features in the form of real-valued number vectors (also called embeddings, or representation vectors). Representation learning aims at finding algorithms and models that can extract such numeric features from arbitrary objects (images, texts, or graphs) in an automated and reliable way. In terms of machine learning on graphs (GraphML), these models / algorithms are called *graph representation learning (GRL)* methods. In recent years, GRL methods have been successfully deployed in a wide variety of domains, including social networks, financial networks, and computational chemistry [1–4].

This wide adoption of graph-based models led to the creation of publicly available implementations, often in the form of frameworks or libraries with standardized APIs, which describe data formats, model building blocks, and scalable parameter optimization techniques. First-choice solutions are currently frameworks like PyTorch-Geometric (PyG) [5] or the Deep Graph Library (DGL) [6]. They include most of the existing graph neural networks and some traditional models, as well as datasets, preprocessing transformations, and basic evaluation mechanisms. This simplifies both production-ready model development and conducting GraphML research.

The implemented design choices allow solving any graph-related task (e.g., node classification, graph regression). Nevertheless, the main focus in these libraries is on node- and graph-centric models and tasks, whereas edge-based tasks are often limited to link prediction.

41 **Present work.** We aim to fill the gap for edge-centric GRL models and tasks. In this extended  
 42 abstract, we introduce PyTorch-Geometric Edge (PyGE), a deep learning library focused on  
 43 models for learning vector representations of graph edges. We build upon the PyTorch-Geometric  
 44 (PyG) library and provide implementations: (1) for edge-centric models, including simple baselines  
 45 and graph neural networks, (2) edge-based GNN layers, (3) datasets and corresponding preprocessing  
 46 functions (in a PyTorch- and PyG-compliant format), and (4) evaluation mechanisms for edge tasks.  
 47 PyGE should make edge representation learning more accessible for both researchers and industrial  
 48 applications, simultaneously accelerating the development of edge-centric methods, datasets and  
 49 benchmarks. **Disclaimer:** Please note that the introduced library is still under active development.  
 50 We provide a summary of our planned work in Section 4.

51 **Contributions.** We summarize our contributions as follows: (C1) We publicly release<sup>1</sup>  
 52 PyTorch-Geometric Edge, the first deep learning library for edge representation learning. (C2)  
 53 We implement a subset of available edge-based models, graph neural network layers, datasets, and  
 54 corresponding data transformations.

## 55 2 Preliminaries

56 We start by introducing definitions for basic concepts covered in our presented library and explore  
 57 the current state of node and edge embedding approaches, as well as GraphML software.

58 **Graph.** A graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$  describes a set of nodes  $\mathcal{V}$  that are connected (pairwise) by a set of  
 59 edges  $\mathcal{E} \in \mathcal{V} \times \mathcal{V}$ . An **attributed** graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathbf{X}, \mathbf{X}^{\text{edge}})$  extends this definition by a set of node  
 60 attributes:  $\mathbf{X} \in \mathbb{R}^{|\mathcal{V}| \times d_{\text{node}}}$ , and optionally also edge attributes:  $\mathbf{X}^{\text{edge}} \in \mathbb{R}^{|\mathcal{E}| \times d_{\text{edge}}}$ .

61 **Edge representation learning.** The goal is to find a function  $f_{\theta} : \mathcal{E} \rightarrow \mathbb{R}^{d_{\text{edge}}}$  that maps an edge  
 62  $e_{(u,v)} \in \mathcal{E}$  into a low-dimensional ( $d_{\text{edge}} \ll \dim(\mathcal{E})$ ) vector representation (embedding)  $\mathbf{z}_{uv}$  that  
 63 preserves selected properties of the edge (e.g., features or local structural neighborhood information).

64 **Edge-based tasks.** Evaluation tasks for edge embeddings include: (1) link prediction – binary  
 65 classification problem of the existence (future appearance) of an edge; (2) edge classification –  
 66 label/type prediction of an existing edge (e.g., kind of social network relation); (3) edge regression –  
 67 prediction a numerical edge feature (e.g., bond strength in a molecule).

68 **Node representation learning methods.** Early approaches were built around the transductive  
 69 setting with an enormous **trainable lookup-embedding matrix**, whose rows denote representation  
 70 vectors for each node. The optimization process would preserve structural node information. For  
 71 instance, DeepWalk [7], and its successor Node2vec [8] use the Skipgram [9] objective to model  
 72 random walk-based co-occurrence probabilities. TADW [10] extended this approach to attributed  
 73 graphs and reformulated the model as a matrix factorization problem. Other early approaches include:  
 74 LINE [11], SDNE [12], or FSCNMF [13]. Recent methods are based on **Graph Neural Networks**  
 75 (GNNs) – trainable functions that transform feature vectors of a node and its neighbors to a new  
 76 embedding vector (inductive setting). These functions can be stacked to create a deep (graph) neural  
 77 network. The most popular ideas include: a graph reformulation of the convolution operator (GCN  
 78 [14]), neighborhood sampling and aggregation of sampled features (GraphSAGE [15]), attention  
 79 mechanism over graph structure (GAT [16]) or modeling injective functions (GIN [17]).

80 **Edge representation learning methods.** This area is still underdeveloped, i.e., only a handful of  
 81 proposed models and algorithms exists. Most early approaches are **node-based transformations**,  
 82 i.e., the edge embedding  $\mathbf{z}_{uv}$  is computed from two node embeddings  $\mathbf{z}_u$  and  $\mathbf{z}_v$ . There are simple  
 83 **non-trainable binary operators** [8], such as the average ( $\mathbf{z}_{uv} = \frac{\mathbf{z}_u + \mathbf{z}_v}{2}$ ), the Hadamard product  
 84 ( $\mathbf{z}_{uv} = \mathbf{z}_u * \mathbf{z}_v$ ), or the weighted L1 ( $\mathbf{z}_{uv} = |\mathbf{z}_u - \mathbf{z}_v|$ ) or L2 ( $\mathbf{z}_{uv} = |\mathbf{z}_u - \mathbf{z}_v|^2$ ) operators.  
 85 NRIM [18] proposes trainable transformations as two kinds of neural network layers: **node2edge**  
 86 ( $\mathbf{z}_{uv} = f_{\theta}([\mathbf{z}_u, \mathbf{z}_v, \mathbf{x}_{uv}^{\text{edge}}])$ ) and **edge2node** ( $\mathbf{z}_u = f_{\omega}([\sum_{v \in \mathcal{N}(u)} \mathbf{z}_{uv}, \mathbf{x}_u])$ ). Another group of  
 87 edge embedding methods **directly** learn the edge embeddings, i.e., without an intermediate node

<sup>1</sup>The link to the repository will be included in the final version and is now omitted due to double-blind policy.  
 We include an anonymized version of our library in the attachments on OpenReview.

88 embedding step. **Line2vec** [19] utilizes a line graph transformation (converting nodes into edges  
 89 and vice versa), applies a custom edge weighting method and runs Node2vec on the line graph.  
 90 The loss function extends the Skipgram loss with a so-called *collective homophily* loss (to ensure  
 91 closeness of neighboring edges in the embedding space). This method is inherently transductive (due  
 92 to Node2vec) and completely ignores any attributes. Those problems are addressed by **AttrE2vec**  
 93 [20]. It samples a fixed number of uniform random walks from two edge neighborhoods ( $\mathcal{N}(u)$ ,  
 94  $\mathcal{N}(v)$ ) and aggregates feature vectors of encountered edges (using average, exponential decaying, or  
 95 recurrent neural networks) into summary vectors  $\mathbf{S}_u$ ,  $\mathbf{S}_v$ , respectively. An MLP encoder network  
 96 with a self-attention-like mechanism transforms the summary vectors and the edge features into the  
 97 final edge embedding. AttrE2vec is trained using a contrastive cosine learning objective and a feature  
 98 reconstruction loss. **PairE** [21] utilizes two kinds of edge feature aggregations: (1) concatenated node  
 99 features (*self features*), (2) concatenation of averaged neighbor features for both nodes (*agg features*).  
 100 An MLP encoder with skip-connections transforms these two vectors into the edge embedding. Two  
 101 shallow decoders reconstruct the feature probability distribution. The resulting PairE autoencoder is  
 102 trained using the sum of the KL-divergences of the *self* and *agg* features. Other methods include:  
 103 EGNN [22], ConPI [23] or Edge2vec [24].

104 **GraphML software.** The backbone of all modern deep learning frameworks are tools for automatic  
 105 differentiation, such as: Tensorflow [25] or PyTorch [26]. GraphML libraries are mostly built upon  
 106 these tools, e.g., PyG uses PyTorch, GEM [27] and DynGEM [28] use Tensorflow, DGL can be  
 107 used both with Tensorflow and PyTorch, whereas some like KarateClub [29] are using a custom  
 108 backend. All of these libraries are focused on node- and graph-centric models. Our proposed  
 109 PyTorch-Geometric Edge library is the first one that focuses on edge-centric models and layers.  
 110 It adapts the PyG library API and uses PyTorch as its backend.

### 111 3 PyTorch-Geometric Edge

112 **Relation to PyG.** Our proposed PyGE library re-uses the API and data format implemented in  
 113 PyTorch-Geometric. The graph is stored as a Data() object with edges in form of a sparse COO  
 114 matrix (edge\_index). Other fields include: x (node attributes), edge\_attr (edge attributes), y  
 115 (node/edge labels). We also keep a similar layout of the library package structure, i.e., we have a  
 116 module for datasets, models, neural network layers (nn), data transformations (transforms) and  
 117 data samplers (samplers). The forward() method in all implemented models/layers accepts two  
 118 parameters: x (node or edge features) and edge\_index (adjacency matrix). Hence, the implemented  
 119 models/layers can be integrated with other PyG models/layers and vice versa (we show that in the  
 120 examples/ folder in the repository). The same applies for the datasets.

#### 121 3.1 Current state of implementation

122 We now show the current state of the library and what is already implemented. Please refer to Section  
 123 4 where we explain our future plans.

124 **Datasets.** We currently include 5 datasets (Cora, PubMed, KarateClub, Dolphin and Cuneiform)  
 125 that were originally used for evaluation of the implemented methods. We summarize their statistic in  
 126 Table 1. Note most of them also require preprocessing steps (see: AttrE2vec [20] for details) for the  
 127 edge classification evaluation – we implement appropriate data transformations.

**Table 1:** Summary of included datasets. The \* symbol denotes the number of edge classes after applying an appropriate data transformation.

Name	$ \mathcal{V} $	$ \mathcal{E} $	$d_{\text{node}}$	$d_{\text{edge}}$	classes
KarateClub [30]	34	156	-	-	4*
Dolphin [31]	62	318	-	-	5*
Cora [32]	2 708	10 556	1 433	-	8*
PubMed [33]	19 717	88 648	500	-	4*
Cuneiform [34]	5 680	23 922	3	2	2

128 **Models and layers.** We implement most of the edge representation learning methods discussed  
 129 in Section 2 into our proposed PyGE library (see: Table 2). Nevertheless, more of them will be  
 130 implemented in future versions.

**Table 2:** Models and layers implemented in PyGE.

Method	Type	Inductive	Attributed	Characteristics
Node pair operator [8]	layer	✓	✗	non-trainable
node2edge [18]	layer	✓	✓	trainable
Line2vec [19]	model	✗	✗	line graph, random-walk
AttrE2vec [20]	model	✓	✓	contrastive, AE, random-walk
PairE [21]	model	✓	✓	AE, KL-div

131 **Embedding evaluation.** We implement a ready-to-use edge classification evaluator class, which  
 132 takes edge embeddings and edge labels, applies a logistic regression classifier and returns typical  
 133 classification metrics, like ROC-AUC, F1 or accuracy. This is a widely adopted technique in  
 134 unsupervised learning, called the *linear evaluation protocol* [35].

135 **Example usage.** In the repository, we provide an end-to-end script showing the usage of a given  
 136 model/layer. Every script: (1) loads a dataset and applies the required data transformations (prepro-  
 137 cessing), (2) prepares the data split of edges into train and test sets, (3) builds a model, (4) trains the  
 138 model for a certain amount of epochs, (5) evaluates the learned edge embeddings. We provide also an  
 139 example script in this extended abstract – see Section A.

### 140 3.2 Maintenance

141 An open-source library requires continuous maintenance. We host our code base at GitHub, which  
 142 allows to track all development progress and user-generated issues. We will build library releases and  
 143 announce them on GitHub and host them later on the Python Package Index (PyPI) to allow users  
 144 to simply run a `pip install torch-geometric-edge` command to install our library. We use  
 145 the MIT license to give potential users, researchers, and industrial adopters a good user experience  
 146 without worrying about the rights to use or modify our code base. Another aspect of software  
 147 development and maintenance is Continuous Integration. We use the GitHub Actions module to  
 148 automatically execute code quality checks and unit tests with every pull request to our library. This  
 149 prevents that a change will break existing functionality or lower our assumed code quality.

## 150 4 Summary and roadmap

151 In this extended abstract, we presented an initial version of PyTorch-Geometric Edge, the first  
 152 deep learning library that focuses on representation learning for graph edges. We provided information  
 153 about currently implemented models/layers and datasets. Our roadmap is extensive and includes: (I)  
 154 preparation of a complete documentation (right now: we rely on code quality checks and example  
 155 scripts on how to use particular models/layers), (II) addition of more datasets (e.g., Enron Email  
 156 Dataset<sup>2</sup>, FF-TW-YT<sup>3</sup>, among others), (III) implementation of other mentioned edge-centric models  
 157 (and a continuous extension of the literature review to find new methods), (IV) we want to add  
 158 more edge evaluation schemes, (V) in the full paper, we want to include an extensive benchmark  
 159 of all implemented models and compare them in different downstream tasks; moreover we want to  
 160 provide the entire reproducible experimental pipeline and pretrained models. With such an amount of  
 161 incoming work, we want to encourage readers interested in edge representation learning to contact  
 162 the authors and contribute to our library. We are convinced that edge representation learning can be  
 163 widely adopted in networked tasks, like message classification in social networks, connection/attack  
 164 classification in cybersecurity applications, to name only a few.

<sup>2</sup><https://www.cs.cmu.edu/~enron/>

<sup>3</sup><http://multilayer.it.uu.se/datasets.html>

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## 287 A Example: PairE model

288 Let’s explore how to use PyGE in practice. We will be using the PairE model to classify the citation  
289 type between academic papers (citation within a research area or cross citation; if the same research  
290 area, then which one). We start by loading the Cora dataset and extracting the target edge labels using  
291 our implemented `MatchingNodeLabelsTransform()` (if two node labels match, use this label, else  
292 use special label `-1`):

```
293 from torch_geometric_edge.datasets import Cora
294 from torch_geometric_edge.transforms import MatchingNodeLabelsTransform
295
296 data = Cora("/tmp/pyge/", transform=MatchingNodeLabelsTransform())[0]
```

297 Next, we split the edges into train and test sets:

```
298 import torch
299 from sklearn.model_selection import train_test_split
300
301 train_mask, test_mask = train_test_split(
302     torch.arange(data.num_edges),
303     stratify=data.y,
304     test_size=0.8,
305 )
```

306 Now, let’s create the PairE model:

```
307 from torch_geometric_edge.models import PairE
308
309 model = PairE(
310     num_nodes=data.num_nodes,
311     node_feature_dim=data.num_node_features,
312     emb_dim=128,
313 )
```

314 We can train our model using standard PyTorch training-loop boilerplate code. Note, that we only  
315 use training edges (`data.edge_index[:, train_mask]`).

```
316 optimizer = torch.optim.AdamW(model.parameters(), lr=1e-3)
317
318 model.train()
319 for _ in range(100):
320     optimizer.zero_grad()
321
```

```
322     x_self, x_aggr = model.extract_self_aggr(data.x, data.edge_index[:, train_mask])
323     h_edge = model(data.x, data.edge_index[:, train_mask])
324     x_self_rec, x_aggr_rec = model.decode(h_edge)
325
326     loss = model.loss(x_self, x_aggr, x_self_rec, x_aggr_rec)
327
328     loss.backward()
329     optimizer.step()
```

330 Finally, we can evaluate our model's edge embedding in the edge classification task using the  
331 `LogisticRegressionEvaluator`. The returned metrics will be prefixed to indicate the train/test  
332 split. Note that we use now all edges during inference:

```
333 from torch_geometric_edge.evaluation import LogisticRegressionEvaluator
334
335 model.eval()
336 with torch.no_grad():
337     Z = model(data.x, data.edge_index)
338
339     metrics = LogisticRegressionEvaluator(["auc"]).evaluate(
340         Z=Z,
341         Y=data.y,
342         train_mask=train_mask,
343         test_mask=test_mask,
344     )
345 print(metrics)
```