

## 572 Appendix Outline

573 . This appendix is organized as follows:

- 574 • In [Appendix A](#), we provide more detailed results on additional datasets for the different  
575 components discussed in [Section 4](#). Specifically, in subsections [Appendices A.1 to A.7](#), we  
576 present results on batch size, data augmentation, model architectures, pre-training, SSL,  
577 Sharpness-Aware Minimization, and label smoothing. These subsections delve into the  
578 specific effects and outcomes of each component.
- 579 • In [Appendix A.8](#), we examine the relationship between the training and test distributions  
580 in imbalanced training. We explore the optimal balance of training data and discuss the  
581 potentially destructive impact of collecting additional majority samples.
- 582 • In [Appendix A.9](#), we present additional and extended experimental results that compare the  
583 methods proposed in our paper with the baseline methods.
- 584 • In [Appendix A.10](#), we provide additional experimental results that illustrate how the training  
585 process evolves for imbalanced data.
- 586 • In [Appendix A.11](#), we include decision boundary visualizations for imbalanced training.  
587 Specifically, we demonstrate that Sharpness-Aware Minimization (SAM-A) helps decision  
588 regions take up similar volumes, whereas standard training routines tend to shrink-wrap the  
589 decision boundaries around minority samples.
- 590 • In [Appendix B](#), we provide detailed information on the hyperparameters, datasets, and  
591 architectures used in our experiments.
- 592 • In [Appendix C](#), we discuss the limitations of our study. This section addresses potential  
593 constraints, challenges, and areas for improvement in our research.
- 594 • Lastly, in [Appendix D](#), we discuss the broader impact of our work. This section explores the  
595 implications, significance, and potential applications of our findings beyond the scope of the  
596 immediate study.

## 597 A Additional Experiments

### 598 A.1 Batch Size

599 To investigate the impact of batch size in the context of class imbalance, we train networks across  
600 various training ratios using different batch sizes. In order to compare the accuracy for each training  
601 ratio, we calculate the percentage improvement over the baseline (set as the best batch size of 128).  
602 Specifically, if we denote  $Acc_b^\rho$  as the accuracy on the imbalanced dataset with training ratio  $\rho$  and  
603 batch size  $b$ , we define the adjusted accuracy  $new_{Acc_b^\rho}$  as

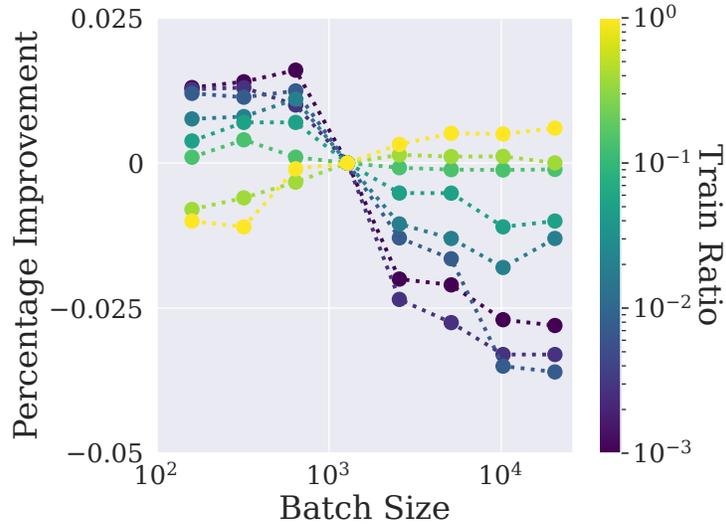
$$\bar{Acc}_b^\rho = \frac{Acc_b^\rho - Acc_{128}^\rho}{Acc_b^\rho}. \quad (1)$$

604 Positive values represent higher accuracy compared to the baseline, while negative values denote  
605 lower accuracy. This normalization allows us to examine the relative effect of batch size. As shown  
606 in the main text and [Figure 6](#), data with a high degree of class imbalance tends to benefit from smaller  
607 batch sizes, despite the fact that small batches often do not contain any minority samples.

### 608 A.2 Data Augmentation

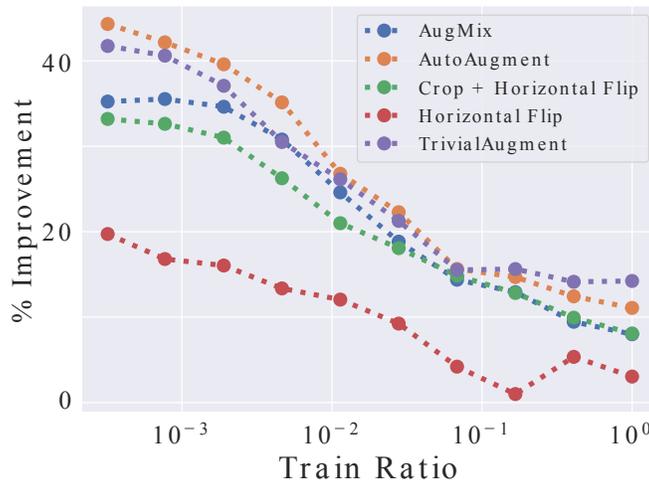
609 In order to evaluate and compare the effectiveness of various popular augmentation tech-  
610 niques—including horizontal flips, random crops, AugMix [28], TrivialAugmentWide [49], and  
611 AutoAugment [11]—we investigate their impact on the accuracy of minority and majority classes  
612 across a range of training ratios.

613 We measure the relative improvement in performance by comparing the accuracy achieved with data  
614 augmentation to that achieved without it. We thus plot the percentage improvement as a function of  
615 the training ratio in [Figure 7](#).



**Figure 6: Batch size matter more for imbalanced data where small batch sizes are best, whereas the curve corresponding to balanced data is flat.** Percentage improvement in test accuracy over the default batch size of 128 at different training ratios. Experiments conducted on CIFAR-10.

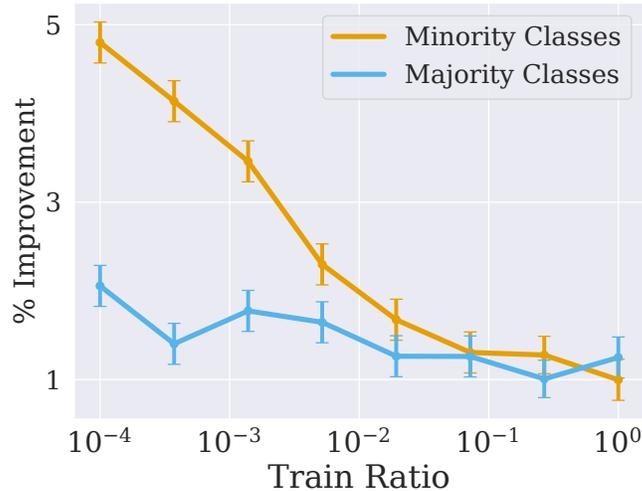
616 Our findings reveal that while the newer TrivialAugment method exhibits superior performance on  
 617 balanced training data, the older AutoAugment method yields better results on highly imbalanced  
 618 data.



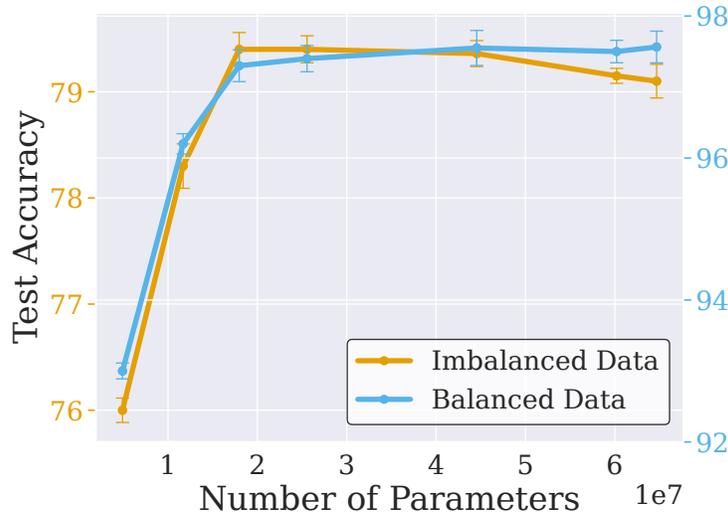
**Figure 7: Optimal augmentations depend on the imbalance ratio.** We plot the percent improvement in test accuracy for different augmentations compared to training without augmentations across train ratios for different augmentations. We see that TrivialAugment, which is known to outperform AutoAugment on class-balanced data, actually performs worse when data is severely imbalanced. Experiments conducted on CIFAR-100.

619 **A.3 Model architecture**

620 In Figure 9, we illustrate the impact of model size on the performance of the CIFAR-10 dataset with  
 621 a training ratio of 0.001. The trend observed is similar to the results discussed in the main text, where  
 622 increasing the model size leads to overfitting in the case of imbalanced training.



**Figure 8: Strong augmentations are particularly effective at improving minority class accuracy under severe class imbalance.** The percent improvement in test accuracy of TrivialAugment compared to training without any augmentation as a function of the training ratio. Experiments conducted on CIFAR-10. Error bars represent one standard error over 5 trials.

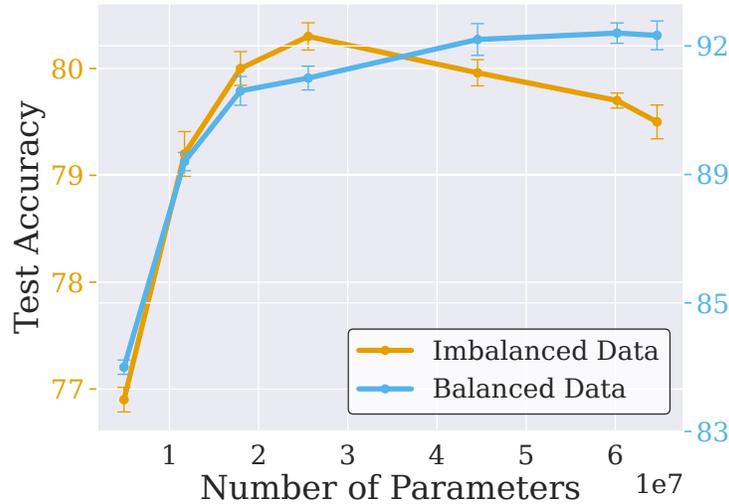


**Figure 9: Bigger architectures overfit on class-imbalanced data.** Experiments conducted on CIFAR-10. Error bars represent one standard error over 5 trials.

#### 623 A.4 Pre-training

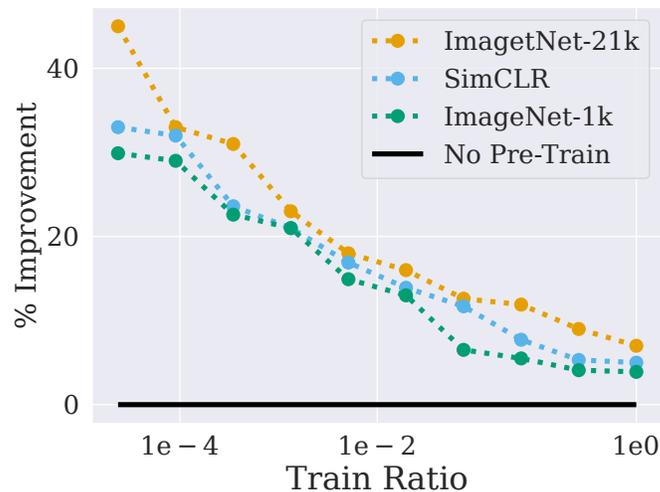
624 To assess the effectiveness of pre-training, we fine-tune several pre-trained models on downstream  
 625 datasets with varying training ratios. In addition to the main body, Figure 11 illustrates the percentage  
 626 improvement in test accuracy compared to random initialization for supervised pre-training on  
 627 ImageNet-1k and ImageNet-21k, as well as SimCLR on ImageNet-1k (which is a Self-Supervised  
 628 Learning (SSL) method), measured by downstream performance on CIFAR-10. This comparison is  
 629 made across different training ratios (Figure 4). Let  $Acc_{\text{Rand}}^\rho$  denote the accuracy of the model trained  
 630 from random initialization at a training ratio  $\rho$ . The relative improvement is then defined by:

$$Acc_b^\rho = \frac{Acc_b^\rho - Acc_{\text{Rand}}^\rho}{Acc_{\text{Rand}}^\rho} \quad (2)$$



**Figure 10: Bigger architectures overfit on class-imbalanced data.** Experiments were conducted on CINIC-10 with an imbalanced train ratio of 0.001. Error bars represent one standard error over 5 trials.

631 Positive values indicate an improvement in performance compared to random initialization. It is  
 632 clear that all pre-training methods improve performance when compared to random initialization.  
 Interestingly, these improvements are significantly more pronounced under imbalanced conditions.



**Figure 11: Pretraining yields bigger improvements on more imbalanced data.** The improvement in the test accuracy compared to training from random initialization. Experiments conducted on CIFAR-10.

633

### 634 A.5 SSL

635 Self-supervised learning (SSL) has gained substantial traction as a method of representation learning  
 636 across multiple domains, including computer vision, natural language processing, and tabular data  
 637 [10, 36, 55]. Networks pretrained using SSL often demonstrate more transferable representations  
 638 than those pretrained with supervision [21]. Pre-training traditionally consists of a two-stage process:  
 639 initial learning on an upstream task followed by fine-tuning on a downstream task. However, the  
 640 limitation in many use-cases is the lack of large-scale pretraining datasets. In order to solve this  
 641 problem, our approach diverges from this two-stage process by merging supervised learning with an

642 auxiliary self-supervised loss function during from-scratch training, effectively eliminating the need  
 643 for any pertaining.

644 For this, we employ the Variance-Invariance-Covariance Regularization (VICReg) objective [4]:

645 Given two batches of embeddings,  $\mathbf{Z} = [f(\mathbf{x}_1), \dots, f(\mathbf{x}_B)]$  and  $\mathbf{Z}' = [f(\mathbf{x}'_1), \dots, f(\mathbf{x}'_B)]$ , each of  
 646 size  $(B \times K)$ , where  $\mathbf{x}_i$  and  $\mathbf{x}'_i$  are two distinct random augmentations of a sample  $I_i$ , we derive the  
 647 covariance matrix  $\mathbf{C} \in \mathbb{R}^{K \times K}$  from  $[\mathbf{Z}, \mathbf{Z}']$ .

648 Consequently, the VICReg loss can be articulated as:

$$\mathcal{L}_{SSL} = \frac{1}{K} \sum_{k=1}^K \left( \alpha \max \left( 0, \gamma - \sqrt{\mathbf{C}_{k,k} + \epsilon} \right) + \beta \sum_{k' \neq k} (\mathbf{C}_{k,k'})^2 \right) + \gamma \|\mathbf{Z} - \mathbf{Z}'\|_F^2 / N.$$

In our experiments, the total loss is given by

$$L_{Joint-SSL} = L_{SSL} + \lambda L_{Supervised}.$$

649 Note that the SSL loss function is independent of the class-imbalanced labels.

## 650 A.6 SAM

651 Sharpness-Aware Minimization [18] is an optimization technique that seeks to find “flat” minima  
 652 of the loss function, often leading to improved generalization. This method consists of taking an  
 653 initial ascent step followed by a descent step, aiming to find parameters that minimize the increase  
 654 in loss resulting from the ascent step. Huang et al. [33] demonstrate that flat minima correspond to  
 655 wide-margin decision boundaries.

656 Given a model parameterized by weights  $\theta$  and a loss function  $L(\theta)$  that we aim to minimize, SAM  
 657 performs two steps in each iteration:

658 1. **First step (gradient ascent):** Perform a scaled gradient ascent step from the current model  
 659 weights  $\theta$ :

$$\theta' = \theta + \rho |\nabla L(\theta)|_2 \frac{\nabla L(\theta)}{|\nabla L(\theta)|_2} \quad (3)$$

660 2. **Second step (weight update):** Update the weights from  $\theta$  in the negative direction of the  
 661 gradient computed at the post-ascent parameter vector:

$$\theta = \theta - \eta \nabla L(\theta') \quad (4)$$

662 In the above steps,  $\eta$  represents the learning rate,  $\rho$  is a hyperparameter determining the size of the  
 663 neighborhood around the current weights, and  $|\cdot|_2$  denotes the Euclidean norm.

664 SAM was initially developed for balanced datasets, where the decision boundaries for each class have  
 665 comparable areas. However, this assumption does not hold true for imbalanced datasets. To address  
 666 this, we adapted SAM for use with class-imbalanced datasets by increasing the flatness specifically  
 667 for minority class loss terms. We propose a new method - SAM-Asymmetric (SAM-A). Our method  
 668 adjusts the ascent step size ( $\rho$ ) in SAM’s inner loop for minority classes by employing a step size  
 669 inversely proportional to the classes’ proportions.

670 Let  $p_i$  be the proportion of class  $i$  in the training set. We define the class-conditional ascent step size  
 671 as:

$$\rho_i = \frac{\rho}{1 - p_i}, \quad (5)$$

672 where  $\rho$  is a scaling factor.

673 By doing this, we widen the margins around under-represented classes, potentially improving  
 674 generalization in imbalanced datasets.

675 **A.7 Label Smoothing**

676 Label smoothing is a regularization technique often used in training deep learning models. It  
677 mitigates the model’s excessive confidence in class labels, which can improve generalization and  
678 reduce overfitting. However, traditional label smoothing assumes a balanced class distribution, which  
679 is not always the case in real-world datasets.

680 To adapt label smoothing for imbalanced training, we propose a class-conditional label smoothing  
681 technique. Instead of using a uniform smoothing parameter  $\epsilon$ , we use a different  $\epsilon_i$  for each class  $i$ ,  
682 which is proportional to the inverse of the class’s proportion within the dataset.

683 Let  $p_i$  be the proportion of class  $i$  in the training set. We define the class-conditional smoothing  
684 parameter as:

$$\epsilon_i = \frac{\epsilon}{1 - p_i}, \tag{6}$$

685 where  $\epsilon$  is a scaling factor.

686 We then apply label smoothing as follows. Let  $p$  be the model’s output probability distribution over  
687  $K$  classes, and let  $q_i$  be the target distribution for class  $i$ . The smoothed target distribution is:

$$q_{i,j} = (1 - \epsilon_i)I_{y=j} + \frac{\epsilon_i}{K}, \tag{7}$$

688 where  $j \in 1, 2, \dots, K$ ,  $y$  is the true class, and  $I$  is the indicator function.

689 During training, we minimize the cross-entropy loss between the model’s predictions  $p$  and the  
690 class-conditional smoothed labels  $q_i$ :

$$L = - \sum_{i=1}^K q_{i,y} \log p_y \tag{8}$$

691 By using class-conditional label smoothing, we apply more smoothing to the minority classes and  
692 less to the majority classes, which can help the model generalize better when the class distribution is  
693 imbalanced.

694 **A.8 Data Curation**

695 Common intuition dictates that training on data that is more balanced than the testing distribution  
696 can improve representation learning by preventing overfitting to minority samples [22, 8, 24]. In this  
697 section, we put that intuition to the test by examining the optimal balance of training data. Moreover,  
698 while minority class samples may be scarce, a practitioner may be able to collect additional majority  
699 class training samples at will, so we also examine the potentially destructive impact of collecting  
700 additional majority samples.

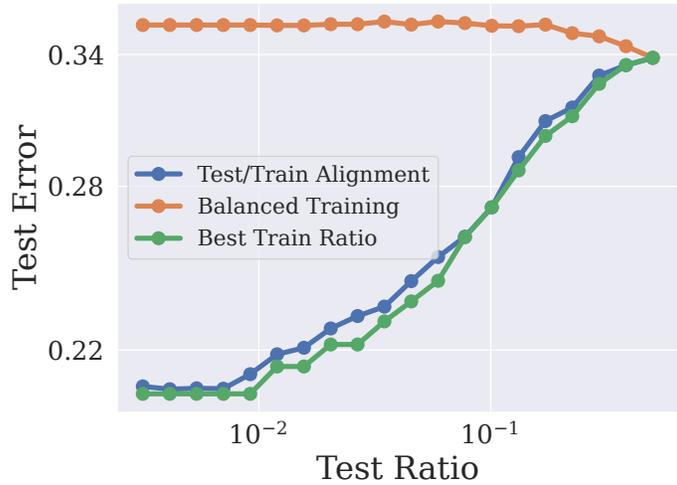
701 **A.8.1 The Relationship Between Train-Time and Test-Time Imbalance**

702 The literature on training routines for class imbalance in machine learning is filled with methods  
703 designed for scenarios in which training data is highly imbalanced but testing data is balanced.  
704 However, data encountered during deployment is typically also imbalanced. Therefore, we disentangle  
705 training and testing balances and investigate how sensitive models are to discrepancies between  
706 the two. This study may be particularly important if one considers collecting training data for a  
707 downstream application. Should we gather training data with the same balance we anticipate during  
708 testing? How worried should we be if the data we encounter during deployment is more or less  
709 balanced than the training data we gathered?

710 We begin by illustrating three scenarios in Figure 12: (1) identical training and testing ratios, (2)  
711 balanced training, and (3) the training ratio with the lowest test error (optimal training ratio). We see  
712 that training on data with the same imbalance as the testing data is superior to training on balanced  
713 data, and the two strategies only approach equal performance when the testing data becomes balanced.  
714 We share additional results over different datasets and models in Figure 20, Figure 21, and Figure 22.

715 We then plot for each test ratio the corresponding train ratio that results in the lowest test error in  
 716 [Figure 13](#). If the two ratios are perfectly aligned, then points will lie on the diagonal. Indeed, the  
 717 points are close to the diagonal, indicating that it is best to train with a very similar imbalance ratio to  
 718 the test dataset, especially for highly imbalanced testing scenarios.

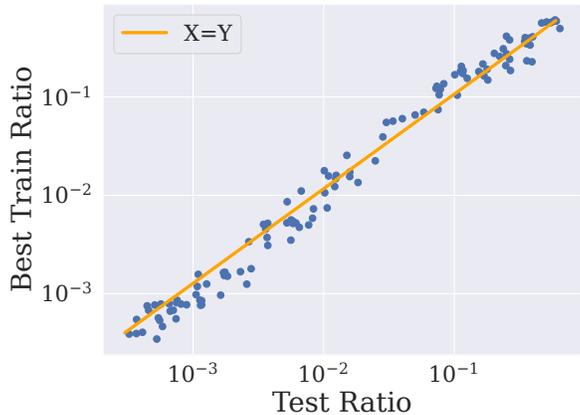
719 In these previous experiments, we fixed the size of the training set, but what happens as we gather  
 720 more and more training data? In [Figure 16](#), we train and evaluate a network on different imbalance  
 721 ratios across training set sizes, and we plot the misalignment between the train and test ratios, referring  
 722 to the average distance between the optimal train ratio and the specified test ratio. As the amount of  
 723 training data increases, we see that the optimal training ratio becomes more and more close to the  
 724 ratio of the test data.



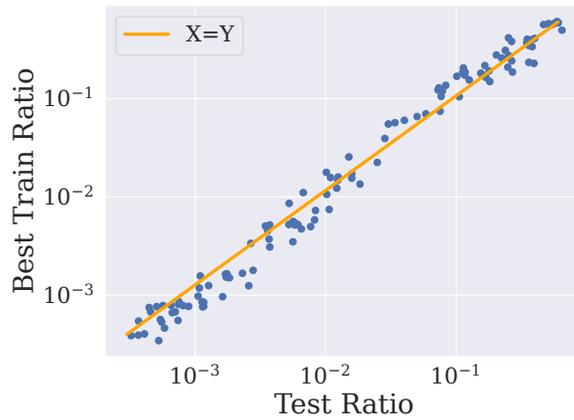
**Figure 12: Imbalanced training data is optimal for imbalanced testing scenarios.** Test accuracy as a function of the test ratio for different training setups. Experiments conducted on CIFAR-100.

725 **A.8.2 When More Data Degrades Performance**

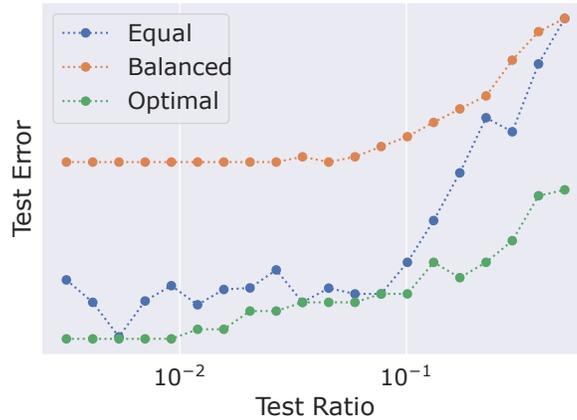
726 In practice, a practitioner may not have precise control over the data they collect. Will collecting  
 727 additional samples always help performance? Instead of fixing the total number of samples and



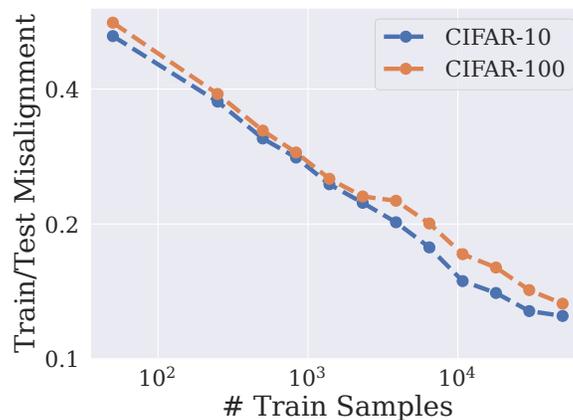
**Figure 13: The optimal train ratio is closely aligned with the test ratio.** Experiments conducted on CIFAR-100.



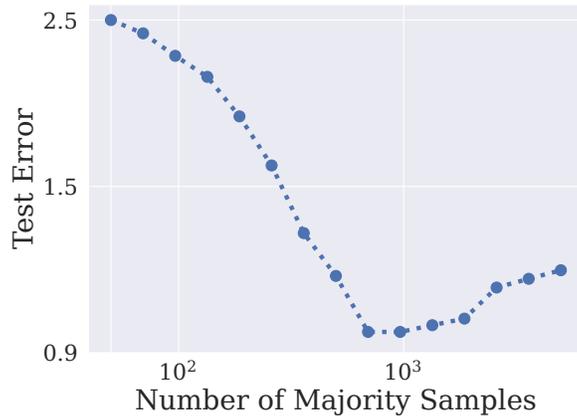
**Figure 14:** The optimal train ratio is closely aligned with the test ratio. Experiments conducted on CINIC-10.



**Figure 15:** Test accuracy on the minority classes as a function of the test ratio for different training setups. ‘Equal’ denotes the same balance between training and testing, and ‘Optimal’ is the optimal trainset balance amongst the ratios we try. Experiments conducted on CIFAR-10.



**Figure 16:** Alignment between train and test proportions improves as the number of training samples increases. *Train/test misalignment* is calculated by taking the mean over test ratios of the difference between the best train ratio (train ratio that gives maximum test accuracy) and the test ratio. If misalignment is 0, then the best train ratio is always the same as the test ratio.



**Figure 17: The potentially destructive effects of adding majority class samples.** We fix the number of minority samples to be 200 and vary the number of majority samples. Experiments conducted on CIFAR-100.

**Table 5: Our training routines exceed previous state-of-the-art or improve existing methods when combined.** Split class accuracy for classes with Few, Med and Many examples of WideResNet-28×10 on long-tailed CIFAR-100 and CINIC-10. Error bars correspond to one standard error over 5 trials.

Method	CINIC-10			CIFAR-100		
	Few	Med	Many	Few	Med	Many
ERM	40.5 ± 0.4	64.1 ± 0.3	90.1 ± 0.5	20.1 ± 0.3	42.3 ± 0.3	70.5 ± 0.6
Reweighting	36.6 ± 0.5	63.1 ± 0.3	87.8 ± 0.3	17.1 ± 0.4	39.3 ± 0.3	67.1 ± 0.4
Resampling	37.4 ± 0.5	63.6 ± 0.6	87.9 ± 0.4	18.4 ± 0.2	38.1 ± 0.2	68.9 ± 0.3
Focal Loss	39.1 ± 0.2	63.9 ± 0.2	88.2 ± 0.5	19.8 ± 0.4	39.0 ± 0.5	69.3 ± 0.6
LDAM-DRW	40.1 ± 0.4	64.3 ± 0.4	89.8 ± 0.3	20.8 ± 0.5	42.1 ± 0.3	70.6 ± 0.4
M2m	42.8 ± 0.7	64.1 ± 0.6	90.3 ± 0.4	20.1 ± 0.6	41.8 ± 0.4	69.4 ± 0.5
SAM-A	43.2 ± 0.3	62.3 ± 0.6	89.7 ± 0.3	22.5 ± 0.4	40.3 ± 0.3	70.1 ± 0.4
Joint-SSL + SAM-A	43.9 ± 0.4	63.3 ± 0.5	90.4 ± 0.5	22.9 ± 0.3	41.3 ± 0.6	69.9 ± 0.6
Joint-SSL + SAM-A + M2m	44.1 ± 0.3	64.2 ± 0.4	90.9 ± 0.3	23.9 ± 0.4	42.3 ± 0.2	70.4 ± 0.3

728 varying their imbalance ratio, we now fix the number of samples from the minority class and vary the  
729 number of total majority class samples.

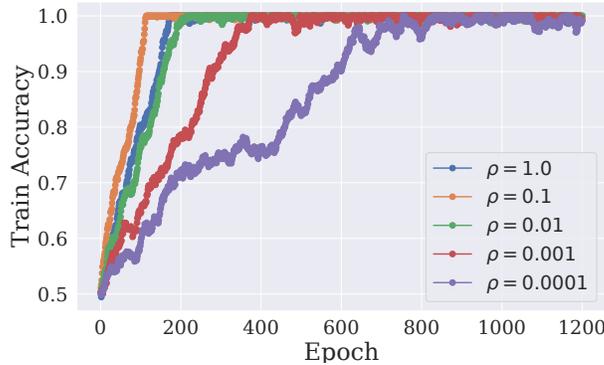
730 In Figure 17, we see that increasing the number of samples from the majority class initially boosts  
731 performance on a balanced test set. Nevertheless, in both cases, the performance reaches an optimum  
732 before the growing training data imbalance eventually degrades test accuracy. Thus, adding training  
733 data can help, but if we add enough majority samples, we must be careful not to cause too sharp a  
734 mismatch between training and testing distributions. Notably, the optimal training set ratio is nearly  
735 balanced, matching the test set, even when we are allowed to gather extra samples from one class  
736 without having to forego samples from another.

## 737 A.9 Benchmarking Results

738 In Table 5, we present additional experimental results that compare the methods proposed in our  
739 paper with the baseline methods. In accordance with Kang et al. [34], we also report the accuracy  
740 across three distinct subsets: (1) Many-shot classes, which contain more than 100 training samples.  
741 (2) Medium-shot classes, comprising 20 to 100 samples, and (3) Few-shot classes, including classes  
742 with fewer than 20 samples.

743 **A.10 Regularization and Overfitting**

744 In order to determine whether the performance differences among various methods stem from their  
745 optimization abilities or their generalization to unseen test samples, we evaluate the training error  
746 without any regularization or specialized optimization method. Specifically, we train a ResNet-50  
747 network on CIFAR-10 and CIFAR-100 datasets using SGD with an initial learning rate of 0.5 and  
748 cosine annealing, across different levels of training data imbalance. As seen in Figure 18, although  
749 fitting all training examples takes longer as we increase the imbalance ratio of our datasets, the  
750 empirical risk minimization successfully fits all training data eventually, including minority samples.



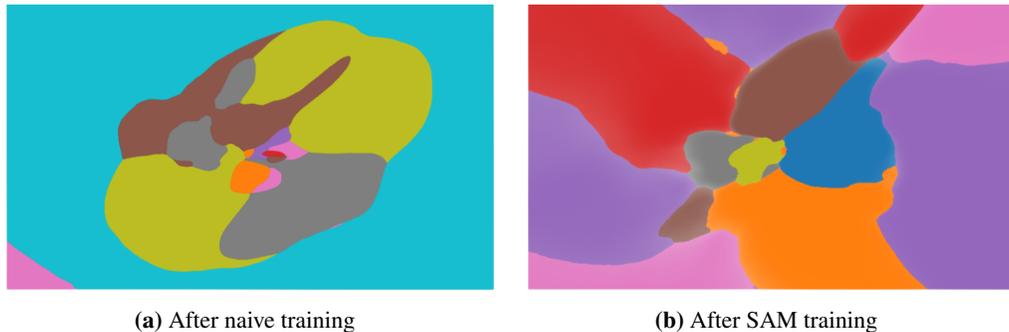
**Figure 18: Imbalanced data is harder to fit.** Training accuracy every epoch for imbalanced training with various imbalance ratios. Experiments conducted on CIFAR-10.

751 **A.11 Decision Boundary Visualizations**

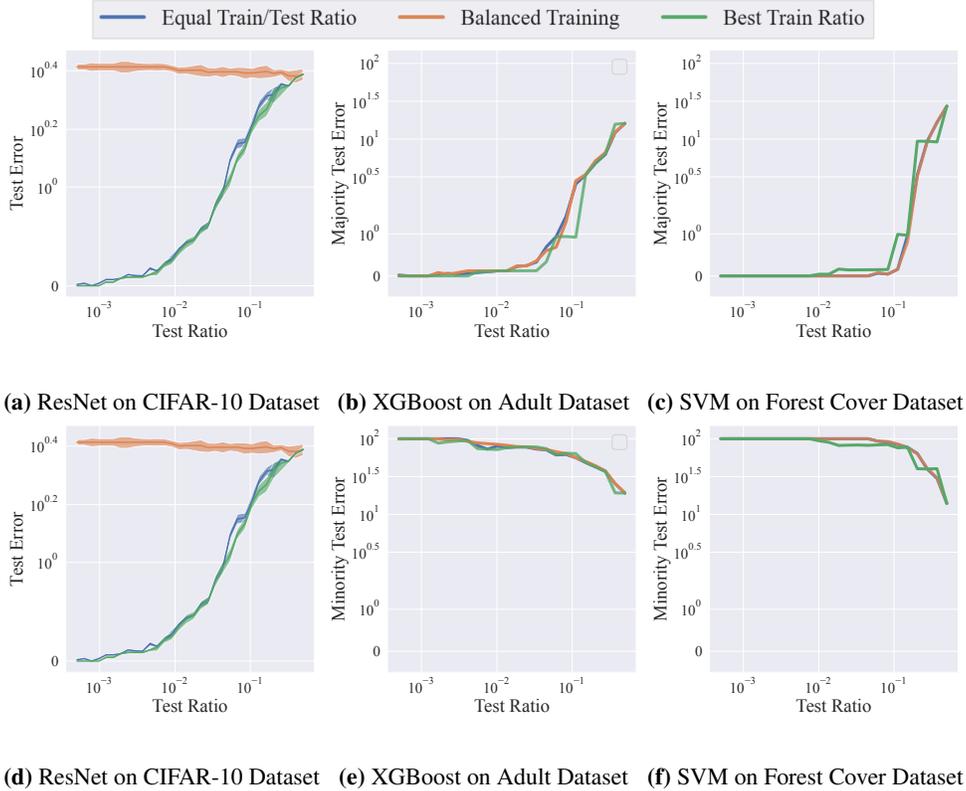
752 To explore the differences between classifiers trained on imbalanced data, we visualize their decision  
753 boundaries. A variety of methods have been established for visualizing the decision boundaries of  
754 deep learning models, offering valuable insights into their intricate internal operations. Apart from  
755 the methods discussed in the main text, we utilize the approach introduced by Somepalli et al. [56]  
756 to visualize the decision boundaries of a ResNet-50 network trained on the CIFAR-10 dataset. In  
757 Figure 19, we display the decision boundaries resulting from standard training (right), which yields  
758 narrow margins around minority classes (green, grey, and orange), and SAM-A (left), which notably  
759 broadens these margins and all the classes occupy similar area in input space.

760 **B Experimental Details**

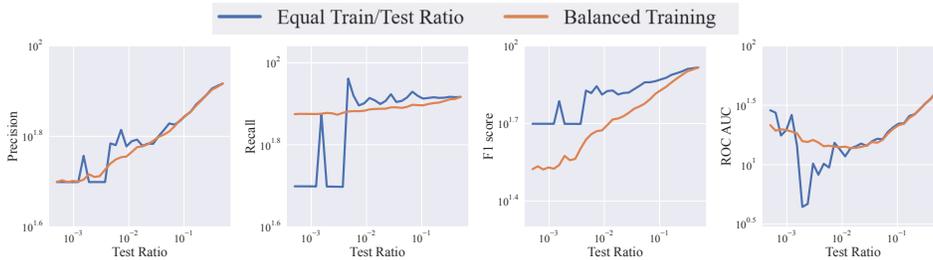
761 In this section, we provide additional implementation details that were not included in the main text.



**Figure 19: SAM-A makes decision regions take up similar volumes, whereas standard training routines shrink wrap the decision boundaries around minority samples.** Experiments conducted on a CIFAR-10 with ResNet-18.



**Figure 20:** Test error split by majority and minority classes for balanced test sets. We see similar trends across all models and datasets.



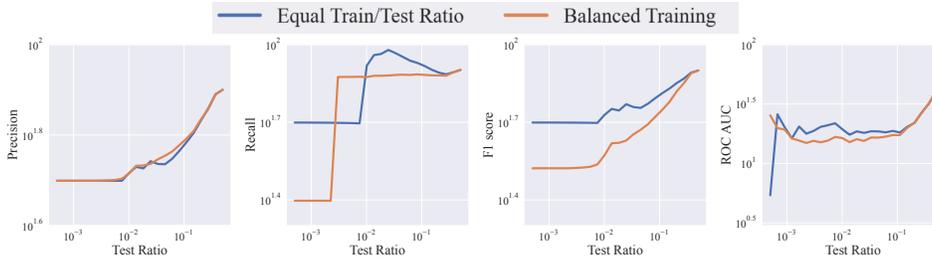
**Figure 21:** Additional metrics for XGBoost on the Adult dataset.

762 For the CIFAR-10, CIFAR-100, and CINIC-10 datasets, we follow the imbalanced setup proposed by  
 763 Liu et al. [45], using an exponential distribution to create imbalances between classes. Across all  
 764 methods, we use TrivialAugment [49] combined with CutMix as our augmentation policy, supple-  
 765 mented by label smoothing and an exponential moving weight average. Our model of choice is the  
 766 WideResNet-28×10 [62].

767 We employ the SGD optimizer with momentum 0.9 and weight decay coefficient  $210^{-4}$ . Our models  
 768 are trained for 300 epochs with cosine annealing and a linear warm-up of the learning rate. The  
 769 learning rate is initialized at 0.1.

770 For the APTOS 2019 Blindness Detection, SIIM-ISIC Melanoma Classification, and EuroSAT  
 771 datasets, we largely follow the approach detailed in Fang et al. [17], utilizing the ResNeXt-50-32×4d  
 772 model, which was identified as the best model for these datasets in the comparison by Fang et al.  
 773 [17].

774 Our implementation was done in PyTorch, utilizing the PyTorch Lightning library for training. All of  
 775 our models were trained on V100 GPUs.



**Figure 22:** Additional metrics for SVM on the Forest Cover dataset.

776

## 777 C Limitations

778 In our paper, we found that existing methods for class imbalance are unreliable on real-world datasets.  
 779 While our tuned routine was effective on the real-world datasets we considered, these general trends  
 780 raise the concern that solutions which are effective on some class-imbalanced datasets may fail on  
 781 others. A second limitation of our work is that some tools we utilize are only applicable in certain  
 782 domains. For example, data augmentations and self-supervised learning for tabular data are not  
 783 widely accepted.

## 784 D Broader Impacts

785 Across a wide variety of high-impact domains, ranging from credit card fraud detection to disease  
 786 diagnosis, data is severely class-imbalanced. Therefore, performance increases for class-imbalanced  
 787 data is highly valuable. With this potential for value also comes the potential that proposed methods  
 788 make false promises which won't benefit real-world practitioners and may in fact cause harm when  
 789 deployed in sensitive applications. For this reason, we release our numerical results across diverse  
 790 datasets, and we also include implementation details for the sake of transparency and reproducibility.  
 791 As with all new state-of-the-art methods, our improvements may also improve models used for  
 792 malicious intentions.