

541 **A Inconsistent Practice of the Evaluation for Trajectory Prediction**

542 Previous research in the area of trajectory forecasting, i.e. trajectory prediction, has focused on
543 multiple datasets for quantitative evaluation. However, we notice that the evaluation settings of
544 previous works are inconsistent thus making noisy and unfair comparisons in the benchmarks we
545 usually refer to.

546 **A.1 Inconsistent evaluation convention on ETH/UCY**

547 The ETH/UCY [20, 33] dataset, comprising five subsets of data, serves as the primary benchmark for
548 human trajectory prediction. It is not proposed as a single dataset in the first place but merges many
549 different resources. Therefore, there are no official guidelines for data splitting and model evaluation
550 metrics. Consequently, previous studies employ different evaluation conventions and falsely confuse
551 results from different conventions together for benchmarking.

552 The benchmark widely adopted by the research community was initially proposed by Social-
553 GAN [11]. It adheres to the following principles:

- 554 1. Utilizing data with a sampling rate of 10 FPS in all subsets.
- 555 2. Employing a leave-one-out approach for splitting, where the model is trained on four subsets
556 and tested on the remaining one subset.
- 557 3. Dividing the raw trajectory samples into specific train, eval, and test sets.

558 Subsequent works like Trajectron++ [39], AgentFormer [52], and EqMotion [50] have widely
559 embraced this benchmarking and evaluation setting.

560 However, not all studies adhere to this benchmark. To identify examples, we conducted a review of
561 recent open-access conference papers, which reveals the following divergence.

562 **1. Sampling Rate on ETH dataset.** There are two widely used sampling rates for the evaluation of
563 the ETH dataset. While Social-GAN [11] utilized the data with a sampling rate of 10FPS (SR=10),
564 other works, such as SR-LSTM [53], V2Net [46], SocialCircle [47], STAR [51], PCCSNet [42],
565 Stimulus Verification [41], and MG-GAN [5], used the version with a sampling rate of 6FPS (SR=6).
566 The SR=6 version contains more data, with a total of 8,908 frames, whereas the SR=10 version
567 consists of only 5,492 frames. Based on our experience, the same model tends to yield higher
568 evaluation scores (ADE/FDE) on the SR=6 version compared to the SR=10 version.

569 **2. Data Splitting.** Social-GAN follows a specific scheme and ratio for splitting the data into
570 train/val/test sets, while some works have adopted different conventions. For instance, Sophie [38]
571 selected fewer training scenes, MG-GAN [5] used the complete training scene data for training while
572 separating a portion of the test set for evaluation. Also, works that choose the SR=6 version data
573 in the ETH dataset adopt different splitting conventions, because they do not share the same raw
574 trajectory data samples with Social-GAN, which uses the SR=10 version data.

575 **3. Inconsistent Data Pre-processing.** Some other studies, such as Y-Net [25], Introvert [40], and
576 Next [23], provide processed data without the raw data and the processing scripts. The provided
577 processed data for val/test sets does not align with the Social-GAN benchmark.

578 **A.2 Inconsistent evaluation convention on SDD**

579 Compared to ETH/UCY, SDD [36] is a more recent dataset consisting of 20 scenes captured in bird’s
580 eye view. SDD contains various moving agents such as pedestrians, bicycles, and cars.

581 Most works follow the setting of TrajNet [37] which comes from a public challenge. However,
582 some works adopt different evaluation way compared to TrajNet. SimAug [22] reprocesses the raw
583 videos and gets a set of data files different from TrajNet’s. Besides, it uses a different data splitting
584 convention. Subsequent works such as V2Net [46] and SocialCircle [47] follow the same setting
585 that SimAug starts. DAG-Net [30] shared the same data file with TrajNet, but used a different data
586 splitting approach. Social-Implicit [29] followed its setting.

587 Therefore, there are multiple different evaluation protocol conventions on the ETH/UCY and SDD
588 datasets. Because the data splitting for training/test and evaluation details are different, putting the
589 evaluation numbers from them together provides misleading quantitative observations, which the
590 community has been using for a while. We point it out and make a complete summary of these
591 misalignments, wishing future research aware of this to avoid potential continuity of the mis-practice
592 and provide a fair comparison.

Table 5: minADE/minFDE of worst- N predictions on UNIV dataset. By adding augmented data along with their corresponding cluster centers, our method significantly improves the performance on the corner cases.

N	FlowChain		Augment-MGF	
	ADE	FDE	ADE	FDE
10	3.13	6.54	0.75	1.30
50	2.40	4.90	0.90	1.57
100	2.06	4.29	1.07	1.86

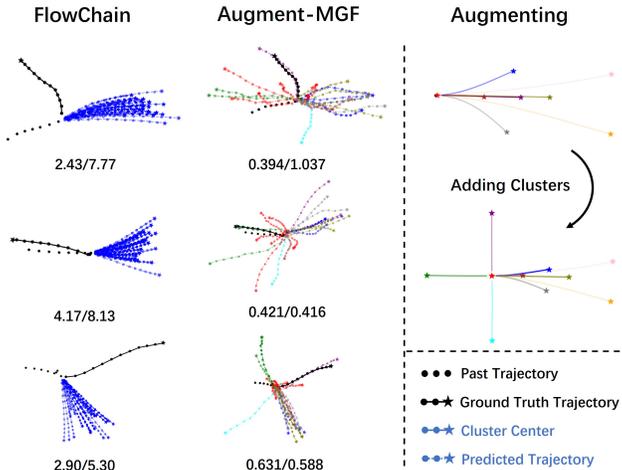


Figure 6: By adding augmented data along with their corresponding clusters into the construction of the mixed Gaussian prior, we could manipulate the generation patterns as we desire. For example, we could inject some under-represented trajectory patterns. Then the model can generate corner cases that existing models fail to generate in a reasonable probability. We selected three examples from the UNIV dataset, namely sharp left/right turns and U-turns. The left column shows the predictions from FlowChain, while the middle column shows the predictions of MGF with augmented priors

593 A.3 Summary and Our Practice

594 When comparing baseline results, many previous studies fail to meticulously verify whether they
 595 adhere to the same convention, thereby leading to unfair comparisons. To compare the performance of
 596 various models fairly, we follow the practice that the community adheres to the most: Social-GAN’s
 597 convention for ETH/UCY and TrajNet’s convention for SDD.

598 More specifically, for ETH/UCY dataset, we recommend to use the preprocessed data and dataloader
 599 from SocialGAN [11]/Trajectron++ [39]/AgentFormer [52]. For the SDD dataset, we recommend
 600 using the preprocessed data and dataloader from Y-Net [25]. Although their data processing methods
 601 may differ, they share the same data source and data splitting approach, facilitating fair comparisons.

602 We also note that, in the early version of Trajectron++, a misuse of the *np.gradient* function during
 603 computation resulted in the model accessing future information. Rectifying this bug typically leads
 604 to a significant decrease in scores. Consequently, several Trajectron++-based studies have achieved
 605 improved scores.

606 B Controllable generation by data augmentation

607 Besides the fashion of manipulating generation results given the good property of our constructed
 608 mixed Gaussian prior in the main paper, we also use data augmentation to alter the data patterns
 609 in our training set, thereby obtaining different priors. This enables our model to fix corner cases
 610 that are difficult to handle with traditional flow-based models like FlowChain. Taking Figure 6
 611 as an example, to generate the clusters representing green "U-turn", purple "left-turn", and cyan
 612 "right-turn" clusters in the right-middle figure, we duplicate and rotate the original future trajectory
 613 data by 180°, 90°, and -90°, respectively. Subsequently, we mix these rotated data with the original
 614 data in a fixed ratio to produce the augmented dataset (in this particular case, a 2:2:1:1 ratio is
 615 employed for the original:180°:90°:-90°). Then we apply k-means to the augmented dataset, thereby

616 obtaining the new augmented prior distribution (depicted in the right-middle figure). Finally, we
617 train the model using this augmented dataset. Compared to the generated results from FlowChain,
618 after using the augmented data to construct the mixed Gaussian prior, our method can generate the
619 under-explored trajectory patterns with a higher chance. After this manipulation, we could change
620 the mixed Gaussian prior as we desire, such as amplifying the chance of generating corner cases in
621 this example.

622 On the other hand, we quantitatively evaluate the ability to generate under-represented trajectory
623 patterns. Table 5 compares the ADE/FDE scores of their worst- N samples on the UNIV dataset.
624 Typically, the samples from the test set with the worst ADE/FDE relate to the under-represented
625 corner cases of future trajectories. The results demonstrate quantitatively that MGF can better
626 generate the under-represented motion patterns after injecting the desired corner cases on purpose by
627 manipulating the mixed Gaussian prior as mentioned above. We note that all the provided examples
628 of manipulating the mixed Gaussian prior to controlling the generation statistics do not require
629 fine-tuning or any operation to the normalizing flow itself. As manipulating the mixed Gaussian prior
630 is purely a parameter updating processing without any training and gradient backpropagation, all the
631 manipulation is very fast in practice. This suggests the good efficiency and flexibility of our proposed
632 method to achieve controllable generations.

633 **6 Limitations**

634 Limited by computing resources, we did not utilize the map information in our model. Some generated
635 trajectories may overlap with obstacles, thus decreasing the upper bound of MGF’s ability. Also, we
636 found that agents can occasionally collide with each other due to the limited ability of the history
637 encoder. Future works may take more consideration to the collision among agents or between agents
638 and the environment.