495 Appendix

⁴⁹⁶ The appendix is structured as follows:

497	• Related Works (Section A) provides an overview of the previous works related to bench-
498	marking MU.
499	• Datasets (Section B) contains information about the datasets, data augmentations, and
500	hyper-parameters used to train the Original and Retrained models.
501	• Neural Network Architectures (Section C) provides information about ResNet18 and
502	TinyViT used throughout our benchmark.
503	• Privacy Evaluation (Section D) gives the descriptions of the U-MIA and U-LiRA evaluation
504	metrics.
505	• Per Dataset Results (Section E) shows some experimental results in terms of accuracy,
506	retention, privacy metrics, and runtime efficiency per dataset for the 9 combinations of
507	datasets and DNN architectures considered in our work.
508	• Per Architectures Ranking (Section F) provides Performance Retention Deviation and
509	Indiscernibility Rankings separated for ResNet18 and TinyViT.
510	• L2 Distances between Model Weights (Section G) shows L2 distances computed between
511	the Unlearned, Original, and Retrained models.
512	• Requirements (Section H) which describes the compute resources.
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513 A Related Works

514 A.1 Machine Unlearning

Machine Unlearning is often first associated with the work from Cao et al. [11], followed by Bourtoule 515 et al. [9], which proposes SISA (Sharded, Isolated, Sliced, Aggregated) as an exact unlearning method. 516 For a recent overview of MU, we refer to the survey from Xu et al. [50], which provides a taxonomy of 517 common unlearning methods. Furthermore, Zhang et al. [52] review MU through privacy-preserving 518 and security lenses. The authors cover the Confidentiality, Integrity, and Availability security triad 519 and the need for Data Lineage, which relates to following the movement of data in a machine learning 520 pipeline and understand from where it originates, where it is stored, and how it percolates in the 521 system through transformation. Some might have information on common MU verification methods, 522 privacy evaluation metrics, and datasets, we defer to the work of Nguyen et al. [39], and Shaik et 523 524 al. [43].

In the following, we focus on the MU taxonomy from Xu et al. [50], which considers Data Reorganization and Model Manipulation:

(1) Data Reorganization methods focus on directly modifying the data to perform unlearning. It is
 divided into Data Obfuscation, Data Pruning, and Data Replacement.

Data Obfuscation refers to modifying the dataset to obscure the influence of the data to be unlearned:
 random relabeling and retraining [28], SRL (Successive Random Labels), and Saliency Unlearning
 (SalUN).

Data Pruning usually relies on dividing the dataset into multiple sub-datasets and training sub-models
 on these subsets. This is the category to which SISA [9] relates. Our work does not consider methods
 associated with this setting as they assume the training process.

Data Replacement attempts to unlearn by replacing the original dataset with transformed data that simplifies unlearning specific samples. For instance, Cao et al. [11], replace the training data with summations of efficiently computable transformations. Like data pruning, these methods tend to make strong assumptions about the training process.

(2) Model Manipulation methods directly adjust the model parameters to remove the influence of
 specific data points. Model manipulation is divided into Model Shifting, Model Replacement, and
 Model Pruning.

Model Shifting directly updates the model parameters to offset the influence of the unlearned samples,
such as using a single step of Newton's method on model parameters [30] or decremental updates
[40], in our benchmark Fisher Forgetting (FF), Influence Unlearning (IU), and SalUN would represent
these approaches.

546 *Model Replacement* uses pre-calculated parameters that do not reflect the data to forget to replace 547 parts of the trained model. For instance, when using decision trees, one can replace nodes affected by 548 the forget set by pre-calculated node [41]. These methods often make strong assumptions about the 549 training process and the overall model.

⁵⁵⁰ *Model Pruning* prunes specific parameters from the trained models to remove the influence of certain ⁵⁵¹ samples [34] or Prune-Reinitialize-Match-Quantize (PRMQ) [4] which prunes the model via L1 ⁵⁵² pruning, reinitializes parts of the model then train the model on \mathcal{D}_R .

553 A.2 Machine Unlearning for Deep Neural Networks

Initially, MU research primarily focused on linear models such as linear regression and logistic models. Such models allow for the design of methods that assume the convexity of the loss function, rendering them less practical for DNN-based approaches. Since DNNs are able to memorize parts of their training data, they are particularly relevant targets for MU, even more so when they have been trained on large amounts of potentially personal data. For Deep Learning models, unlearning raises additional challenges: 1) the non-convexity of the loss function of Deep Neural Networks [15], 2) the size of the models inducing large computational costs, 3) the randomness coming from the model's training process, such as the initialization seed, randomness in the mini-batch generation process, and 4) the fact that any model update impacts subsequent versions of the models, namely the weights at epoch n + 1 directly depend on the weights at update n.

When considering MU for DNN, Xu et al. [50] notes that a standard scheme DNN is to focus only on the final layer, as it is expected for this layer to be the most relevant for the downstream task, and stems from the early works MU. Nonetheless, Goel et al. [24] showed that simply modifying the final layer is often insufficient to remove information related to D_f . However, other approaches, such as those from Golatkar et al. [25, 26, 27], attempt to unlearn the full model via methods derived from Information Theory. For instance, weight scrubbing on trained models can be done by approximating the Fisher information matrix.

571 A.3 Post-Hoc Machine Unlearning

While proactively designing deep-learning pipelines with built-in unlearning methods such as SISA can greatly simplify the unlearning process, many contemporary services relying on DNNs were not deployed with unlearning in mind. This motivates searching for methods that can unlearn from already trained models without making assumptions about the training process.

Thus, we focus on *post-hoc MU*, a scenario where we assume that the unlearning method is agnostic 576 to the original training process of the model. Under such a scenario, differences exist in terms of 577 data availability at unlearning time. For instance, whether one has access to the original training 578 data \mathcal{D} , the retain set \mathcal{D}_R , the forget set \mathcal{D}_F , or even some external set such as the validation set \mathcal{D}_V . 579 Therefore, careful consideration should be given to the data requirement associated with an unlearning 580 method. Indeed, some might require having access to both \mathcal{D}_R and \mathcal{D}_F at the unlearning time, while 581 others assume that \mathcal{D}_R is no longer available [17] making them more practical in real-world scenarios. 582 Throughout our benchmark, we make the same assumption as the NeurIPS2023 Unlearning Challenge 583 [45], where the unlearning methods had access to $f_O, \mathcal{D}_R, \mathcal{D}_F, \mathcal{D}_V$ 584

585 A.4 Machine Unlearning and Differential Privacy

We based our Unlearning definition on Sekhari et al. [42] and refer to their work on the distinction between Differential Privacy and the objective of Machine Unlearning. Differential privacy, in a high-level picture, is a method for publicly sharing aggregated information about a population by describing the patterns discovered among the groups within the dataset while withholding specific information about individual data points. A randomized algorithm \mathcal{A} is (ε, δ) -differentially private if for all datasets D_1 and D_2 that differ on a single data point, and all $S \subseteq \text{Range}(\mathcal{A})$,

$$\Pr[\mathcal{A}(D_1) \in S] \le e^{\varepsilon} \cdot \Pr[\mathcal{A}(D_2) \in S] + \delta.$$
(7)

In this definition, ε (epsilon) is a non-negative parameter that measures the privacy loss, with smaller values indicating stronger privacy. The parameter δ represents the probability of breaking differential privacy, ideally close to or equal to 0.

Despite enabling provable error guarantees for Unlearning methods, Differential Privacy requires
 strong model and algorithmic assumptions, making MU, derived from it, potentially less effective
 against practical adversaries [34].

598 **B** Datasets

CIFAR-10 CIFAR-10 is a widely used dataset in computer vision and machine learning. It comprises 60,000 32x32 color images in 10 different classes, with 6,000 images per class. The dataset is divided into 50,000 training images and 10,000 testing images. CIFAR-10 represents a diverse range of everyday objects, such as airplanes, automobiles, birds, and cats, making it a challenging task for image classification. The simplicity of the images combined with the variety of categories
 makes CIFAR-10 a suitable dataset to test the efficacy of machine unlearning algorithms in effectively

⁶⁰⁵ unlearning information without compromising the model's performance on the remaining data.

Data Augmentations: random cropping to 32x32 with 4-pixel padding, 50% random horizontal flipping, and per-channel normalization with a mean of [0.4919, 0.4822, 0.4465] and standard deviation

 $_{608}$ of [0.2023, 0.1994, 0.2010]. At test time, we resize to 32x32 and normalize.

CIFAR-100 CIFAR-100 is a more complex extension of CIFAR-10, containing 100 classes with 600 images per class, split into 500 training images and 100 testing images per class. Each class is 1 labeled with a "fine" label and grouped into 20 "coarse" labels, adding another layer of classification 612 difficulty. The increased number of classes and finer granularity make CIFAR-100 an intriguing 613 dataset for machine unlearning benchmarks. It poses a more significant challenge for models to forget 614 specific classes or groups while retaining knowledge of others, thus testing the unlearning algorithms' 615 precision and effectiveness in handling more granular and complex datasets.

Data Augmentations: random cropping to 32x32 with 4-pixel padding, 50% random horizontal flipping, and per-channel normalization with a mean of [0.5071, 0.4865, 0.4409] and standard deviation of [0.2673, 0.2564, 0.2762]. At test time, we resize to 32x32 and normalize.

MNIST The MNIST dataset is a well-known benchmark in handwritten digit recognition. It comprises 70,000 grayscale images of handwritten digits (0-9), 60,000 used for training, and 10,000 for testing. Each image is 28x28 pixels in size. We consider MNIST due to its simplicity and extensive research and development history. The simplicity of MNIST allows researchers to focus on the fundamental aspects of unlearning techniques without the additional complexity introduced by color or high resolution, providing a clear assessment of the effectiveness of unlearning algorithms in a controlled setting.

Data Augmentations: conversion to 3 channels, resizing to 32x32 such that both ResNet18 and TinyViT use the same input resolution, 50% random horizontal flipping, and per-channel normalization with a mean of [0.1307, 0.1307, 0.1307] and standard deviation of [0.3081, 0.3081, 0.3081]. We convert to 3 channels at test time, resize to 32x32, and normalize.

Fashion MNIST Fashion MNIST is a more challenging replacement for MNIST. It contains 70,000 grayscale images of fashion items in 10 categories: shirts, trousers, and sneakers. Like MNIST, each image is 28x28 pixels, but the increased complexity and variability of clothing items make it a more challenging classification task. Fashion MNIST provides a more realistic and intricate dataset than MNIST, testing the unlearning algorithms' ability to handle real-world-like variability and ensuring that they can effectively remove learned information while maintaining performance on a moderately complex dataset.

Data Augmentations: conversion to 3 channels, resizing to 32x32, 50% random horizontal flipping, and per-channel normalization with a mean of [0.2860, 0.2860, 0.2860] and standard deviation of [0.3560, 0.3560, 0.3560]. We convert to 3 channels at test time, resize to 32x32, and normalize.

UTKFace UTKFace is a large-scale face dataset containing over 20,000 images of faces with annotations of age, gender, and ethnicity. The images vary in size and cover a wide range of ages, from 0 to 116. UTKFace is particularly interesting due to the sensitive nature of the data and the need for privacy-preserving techniques.

Data Augmentations: resizing to 224x224, and per-channel normalization with a mean of [0.485, 0.456, 0.406] and standard deviation of [0.229, 0.224, 0.225]. We apply the same transformation at test time.

For each dataset, the Original and Retrained models are trained using the same hyper-parameters(provided in Table 3)

Dataset	Model	Epochs	Learning Rate	Batch Size
FashionMNIST	ResNet18	50	0.1	256
1 asmonivity 15 1	TinyViT	50	0.1	256
MNIST	ResNet18	50	0.1	256
	TinyViT	50	0.1	256
	ResNet18	182	0.1	256
CIFAR-10	(LiRA) ResNet18	91	0.1	256
	TinyViT	182	0.1	256
CIEAD 100	ResNet18	182	0.1	256
CIFAR-100	TinyViT	182	0.1	256
LITKEnce	ResNet18	50	0.1	128
UIKFace	TinyViT	50	0.1	128

Table 3: Summary of the number epochs, learning rate, and batch size for each dataset and model used to train the Original and Retrained models.

649 C Neural Network Architectures

We consider two families, ResNet (Residual Network) [32] and ViT (Vision Transformer) [19], which are prominent architectures in computer vision. We consider ResNet18 and a TinyViT[48] with approximately 11M learnable parameters for a fair comparison between two fundamentally different architectures. This provides insights into how architectural differences impact the unlearning process and helps understand the trade-offs between convolutional and transformer-based models regarding reliability and computational efficiency.

ResNet: ResNet18 Introduced by He et al. [32], it facilitates the training of deep networks through
 shortcut connections, which mitigates the problem of vanishing gradients. The ResNet18 is known
 for its balance between performance and computational efficiency.

ViT: TinyViT Vision Transformer (ViT), introduced by Dosovitskiy et al. [19], adapts the transformer architecture to image classification by treating images as sequences of patches. We consider
TinyViT from Wu et al. [48], as it is a compact version of ViT designed to be parameter-efficient
while maintaining high performance.

663 **D** Privacy Evaluation

664 D.1 Unlearning-Membership Inference Attack (U-MIA)

A common approach to evaluate the quality of unlearning methods is to attack the unlearned models 665 with a form of Membership inference Attack (MIA). Membership Inference Attacks attempt to 666 determine whether a specific data point was part of the model train data. The efficacy of the 667 Membership Inference Attack has been used as a metric to evaluate the success of unlearning 668 algorithms. A general approach to such an attack is as follows. Assume $f\theta$ is a trained model with 669 parameters θ , and let \mathcal{L} be a loss function, such as the cross-entropy loss. Then, compute the losses 670 for each sample from two sets of data A and B (of equal size) and train a binary classification model 671 such as logistic regression with labels $y_i^A = 1$ for points i in A and $y_i^B = 0$ for points i in B. An 672 accuracy score from the classifier close to 1.0 indicates that the classifier can perfectly distinguish 673 between samples from A and B based on the loss values. A score of 0.5 indicates that the ability to 674 distinguish is close to random. 675

676 D.2 Unlearning -Likelihood Ratio Attack (U-LiRA)

The performance of a general MIA can be improved by considering, *e.g.*, a per-sample attack such as LiRA [13, 31]. For any given point, we wish to determine whether the outputs from the unlearned models differ from those of models that have never seen the data point. To assess the attack robustly,

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
unlearner										
BT	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.99	0.50	9.76
CF-k	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.98	0.51	5.86
CFW	1.00	1.00	0.99	1.00	1.00	1.00	0.00	1.00	0.50	4.29
CT	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	5.83
EU-k	-	-	-	-	-	-	-	-	-	-
FCS	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	2.11
FF	-	-	-	-	-	-	-	-	-	27.64
FT	1.00	0.99	0.99	1.00	1.00	1.00	0.00	0.99	0.51	5.07
GA	0.98	0.98	0.97	0.98	0.99	0.98	0.04	0.99	0.51	33.97
IU	-	-	-	-	-	-	-	-	-	-
KDE	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	3.27
MSG	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	4.29
NG+	1.00	0.99	0.99	1.00	1.00	1.00	0.01	1.00	0.50	3.12
0	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.98	0.51	1.10
PRMQ	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	3.77
R	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	1.00	1.00	1.00	1.00	1.00	1.00	0.01	1.00	0.50	4.70
SCRUB	-	-	-	-	-	-	-	-	-	-
SRL	1.00	1.00	0.99	1.00	1.01	0.99	0.01	0.99	0.51	8.55
SalUN	1.00	1.00	0.99	1.00	1.00	0.99	0.01	0.99	0.50	3.19

Table 4: MNIST - ResNet18

we evaluate it across multiple models, using shadow models trained on various retain/forget sets. Specifically, we first train n models based on n splits of the training data. This train data is then split into 10 random retain and forget splits, and hence, we unlearn a total of 10n models. We then perform hyper-parameter sweeps, similar to what we do in the original results and unlearn using the optimal hyper-parameters, except that we consider $\frac{n}{2}$ sweeps and conduct 200 trials per sweep to determine the best hyper-parameters. In our setting, we set n = 64.

686 E Per dataset results

⁶⁸⁷ Here, we present the results for both ResNet18 and the TinyViT across datasets.

ResNet18 We provide the tables with Retain Accuracy (RA), Forget Accuracy (FA), Test Accuracy 688 (TA), Retain Retention (RR), Forget Retention (FR), Test Retention (TR), Performance Retention 689 Deviation (RetDev), Indiscinerbility concerning the Test Set (Indisc), U-MIA on the Test set (T-MIA) 690 and RunTime Efficiency (RTE) for every dataset using the ResNet18 model on MNIST (Table 4), 691 FashionMNIST (Table 5), CIFAR-10 (Table 6), CIFAR-100 (Table 7) and UTKFace (Table 8). In 692 general, CIFAR-100 provides the most visible differences, as the performance on the retain set is 693 much higher than on the test. Datasets such as MNIST and FashionMNIST tend to show smaller 694 differences between the methods as the performance on both the Retain and Test sets are similar, to 695 begin with. 696

TinyViT We provide the tables with RA, FA, TA, RR, FR, TR, RetDev, Indisc, T-MIA and RTE for
 MNIST (Table 9), FashionMNIST (Table 10), CIFAR-10 (Table 11) and CIFAR-100 (Table 12) using
 the TinyViT model.

700 F Per architectures rankings

Here, we present the rankings across datasets for ResNet18 (Table 13) and TinyVit (Table 14). We
 note that some methods, such as RNI or NG+, are less efficient on the ViT architectures regarding
 Indiscernibility. However, methods such as SCRUB are less efficient regarding Retention Deviation
 on the ViT architecture.

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	1.00	0.96	0.92	1.00	1.03	0.99	0.04	0.98	0.51	13.57
CF-k	0.98	0.97	0.91	0.98	1.05	0.98	0.09	0.92	0.54	16.31
CFW	1.00	0.95	0.92	1.00	1.02	0.99	0.03	0.97	0.51	4.90
CT	1.00	0.92	0.92	1.00	0.99	0.99	0.02	0.99	0.50	4.47
EU-k	-	-	-	-	-	-	-	-	-	-
FCS	0.98	0.93	0.91	0.98	1.00	0.98	0.04	0.98	0.51	2.79
FF	-	-	-	-	-	-	-	-	-	-
FT	1.00	0.95	0.92	1.00	1.02	1.00	0.02	0.98	0.51	4.29
GA	-	-	-	-	-	-	-	-	-	-
IU	1.00	1.00	0.93	1.00	1.08	1.00	0.08	0.87	0.56	14.97
KDE	1.00	0.93	0.92	1.00	1.00	1.00	0.01	0.99	0.50	3.22
MSG	1.00	0.93	0.91	1.00	1.00	0.99	0.01	0.98	0.51	3.32
NG+	0.99	0.94	0.91	0.99	1.01	0.99	0.03	0.99	0.49	3.21
0	1.00	1.00	0.93	1.00	1.08	1.00	0.08	0.87	0.56	1.11
PRMQ	0.98	0.93	0.91	0.98	1.00	0.99	0.04	0.98	0.51	3.77
R	1.00	0.93	0.92	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	0.98	0.93	0.91	0.98	1.00	0.98	0.04	0.98	0.51	3.25
SCRUB	0.95	0.93	0.90	0.95	1.00	0.98	0.08	0.97	0.51	5.62
SRL	1.00	0.97	0.92	1.00	1.04	1.00	0.05	0.98	0.51	24.85
SalUN	0.99	0.97	0.92	0.99	1.04	0.99	0.06	0.98	0.51	25.02

Table 5: FashionMNIST - ResNet18

Table 6: CIFAR-10 - ResNet18

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	0.94	0.87	0.84	0.94	1.00	0.96	0.10	0.97	0.48	51.96
CF-k	-	-	-	-	-	-	-	-	-	-
CFW	1.00	0.81	0.80	1.00	0.92	0.92	0.16	1.00	0.50	4.67
CT	1.00	0.82	0.81	1.00	0.93	0.93	0.14	0.99	0.50	17.49
EU-k	-	-	-	-	-	-	-	-	-	-
FCS	0.99	0.86	0.84	0.99	0.98	0.96	0.07	0.98	0.49	22.53
FF	-	-	-	-	-	-	-	-	-	-
FT	1.00	0.84	0.82	1.00	0.96	0.95	0.09	1.00	0.50	8.15
GA	0.91	0.89	0.81	0.91	1.02	0.93	0.18	0.92	0.54	91.48
IU	0.95	0.94	0.84	0.95	1.08	0.97	0.16	0.91	0.55	64.61
KDE	0.98	0.84	0.80	0.98	0.96	0.92	0.15	0.97	0.52	6.33
MSG	1.00	0.85	0.83	1.00	0.97	0.95	0.08	0.99	0.51	6.80
NG+	0.97	0.89	0.85	0.98	1.02	0.97	0.07	0.98	0.51	12.89
0	0.96	0.96	0.85	0.96	1.10	0.98	0.16	0.89	0.55	1.08
PRMQ	1.00	0.86	0.83	1.00	0.98	0.95	0.07	0.98	0.51	4.93
R	1.00	0.87	0.87	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	1.00	0.83	0.81	1.00	0.95	0.93	0.12	0.99	0.50	3.60
SCRUB	0.99	0.85	0.85	0.99	0.97	0.98	0.07	0.99	0.50	2.57
SRL	0.99	0.93	0.84	0.99	1.06	0.97	0.10	0.98	0.49	5.52
SalUN	0.98	0.90	0.84	0.98	1.04	0.97	0.08	0.96	0.48	18.04

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	0.98	0.68	0.54	0.98	1.25	0.99	0.27	0.95	0.48	9.39
CF-k	1.00	0.83	0.56	1.00	1.53	1.02	0.55	0.73	0.63	5.91
CFW	0.98	0.43	0.43	0.98	0.79	0.78	0.44	1.00	0.50	6.17
CT	0.99	0.53	0.53	0.99	0.97	0.97	0.07	0.99	0.49	11.82
EU-k	-	-	-	-	-	-	-	-	-	-
FCS	0.98	0.54	0.55	0.98	0.99	1.01	0.04	0.92	0.54	3.02
FF	-	-	-	-	-	-	-	-	-	-
FT	0.98	0.55	0.54	0.98	1.02	0.98	0.05	0.99	0.50	5.16
GA	0.34	0.33	0.24	0.34	0.60	0.44	1.61	0.90	0.55	39.97
IU	-	-	-	-	-	-	-	-	-	-
KDE	0.99	0.52	0.51	0.99	0.95	0.94	0.11	0.99	0.50	3.98
MSG	0.91	0.38	0.38	0.91	0.69	0.69	0.71	1.00	0.50	4.49
NG+	0.89	0.59	0.49	0.89	1.08	0.89	0.29	0.98	0.49	12.14
0	0.98	0.98	0.56	0.98	1.81	1.02	0.85	0.53	0.73	1.10
PRMQ	0.97	0.47	0.46	0.97	0.86	0.85	0.32	1.00	0.50	4.34
R	1.00	0.55	0.55	1.00	1.00	1.00	0.00	0.99	0.49	1.00
RNI	0.99	0.45	0.45	0.99	0.83	0.82	0.36	0.98	0.49	3.65
SCRUB	0.97	0.50	0.53	0.97	0.91	0.96	0.15	0.98	0.51	3.81
SRL	1.00	0.55	0.52	1.00	1.00	0.95	0.06	0.98	0.49	3.67
SalUN	0.98	0.49	0.51	0.98	0.91	0.93	0.18	0.99	0.49	10.66

Table 7: CIFAR-100 - ResNet18. CIFAR-100 provides the most visible comparison as there is a large gap in performance between the Retain Set and Test set, this leads to much larger RetDev scores.

Table 8: UTKFace - ResNet18

	DA	E A		DD	ED	TD	D (D	T 1'	T) (I)	DTT
** 1	KA	FA	IA	KK	FK	IK	RetDev	Indisc	I-MIA	RIE
Unlearner										
BT	1.00	0.74	0.73	1.00	1.00	0.96	0.04	0.99	0.50	12.48
CF-k	1.00	1.00	0.75	1.00	1.34	0.99	0.35	0.70	0.65	5.35
CFW	1.00	0.76	0.76	1.00	1.02	1.00	0.02	1.00	0.50	5.54
СТ	1.00	0.75	0.76	1.00	1.01	1.00	0.01	0.99	0.50	13.34
EU-k	0.72	0.61	0.59	0.72	0.82	0.77	0.68	0.99	0.51	11.42
FCS	0.90	0.70	0.70	0.91	0.94	0.93	0.23	0.99	0.50	4.33
FF	-	-	-	-	-	-	-	-	-	-
FT	1.00	0.76	0.77	1.00	1.02	1.01	0.04	1.00	0.50	5.78
GA	0.49	0.47	0.40	0.49	0.63	0.53	1.34	0.92	0.54	235.10
IU	1.00	1.00	0.76	1.00	1.34	1.01	0.35	0.62	0.69	33.77
KDE	0.99	0.79	0.76	0.99	1.06	1.00	0.07	0.97	0.52	8.19
MSG	1.00	0.80	0.76	1.00	1.08	1.00	0.08	0.96	0.52	7.57
NG+	0.94	0.80	0.72	0.95	1.07	0.95	0.18	0.99	0.51	6.73
0	1.00	1.00	0.76	1.00	1.34	1.01	0.35	0.61	0.69	1.09
PRMQ	0.91	0.72	0.72	0.91	0.97	0.95	0.17	1.00	0.50	5.88
R	1.00	0.75	0.76	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	0.96	0.75	0.73	0.96	1.01	0.96	0.08	0.98	0.51	5.11
SCRUB	0.80	0.76	0.69	0.80	1.01	0.92	0.29	0.94	0.53	4.64
SRL	1.00	0.80	0.73	1.00	1.08	0.97	0.11	0.99	0.51	12.05
SalUN	0.97	0.79	0.73	0.98	1.06	0.96	0.12	0.97	0.52	36.80

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	1.00	1.00	0.99	1.00	1.01	1.00	0.01	1.00	0.50	4.39
CF-k	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.99	0.51	123.88
CFW	1.00	0.99	0.99	1.00	1.00	1.00	0.00	0.99	0.50	5.15
CT	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	5.92
EU-k	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.99	0.50	11.93
FCS	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.99	0.49	7.42
FF	-	-	-	-	-	-	-	-	-	-
FT	1.00	0.99	0.99	1.00	1.00	1.00	0.01	1.00	0.50	7.69
GA	0.97	0.97	0.96	0.97	0.98	0.97	0.08	0.99	0.51	390.99
IU	-	-	-	-	-	-	-	-	-	-
KDE	1.00	0.99	0.99	1.00	1.00	1.00	0.01	1.00	0.50	5.35
MSG	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	5.21
NG+	1.00	0.99	0.99	1.00	1.00	1.00	0.00	0.99	0.50	2.74
0	1.00	1.00	0.99	1.00	1.01	1.00	0.01	0.99	0.51	0.97
PRMQ	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	6.88
R	1.00	0.99	0.99	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	1.00	0.99	0.99	1.00	1.00	1.00	0.01	1.00	0.50	8.03
SCRUB	0.99	0.99	0.99	0.99	1.00	1.00	0.01	1.00	0.50	3.54
SRL	1.00	0.99	0.99	1.00	1.00	1.00	0.01	0.98	0.51	16.37
SalUN	1.00	1.00	0.99	1.00	1.01	0.99	0.01	0.99	0.50	43.67

Table 9: MNIST - TinyViT

Table 10: FashionMNIST - TinyViT

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	0.97	0.94	0.91	0.97	1.01	0.99	0.04	0.98	0.51	3.48
CF-k	-	-	-	-	-	-	-	-	-	-
CFW	0.99	0.94	0.92	0.99	1.01	1.00	0.02	0.99	0.51	5.40
CT	0.98	0.92	0.91	0.98	0.99	0.99	0.04	0.99	0.50	6.00
EU-k	0.95	0.94	0.91	0.95	1.01	0.99	0.07	0.97	0.51	5.34
FCS	0.98	0.93	0.91	0.98	1.01	0.99	0.04	0.98	0.51	4.58
FF	-	-	-	-	-	-	-	-	-	-
FT	0.99	0.94	0.92	1.00	1.01	1.00	0.02	0.98	0.51	5.12
GA	0.92	0.91	0.85	0.92	0.99	0.93	0.17	0.93	0.53	50.72
IU	-	-	-	-	-	-	-	-	-	-
KDE	1.00	0.94	0.92	1.00	1.02	1.00	0.02	0.98	0.51	3.38
MSG	0.96	0.92	0.91	0.96	1.00	0.99	0.05	0.99	0.51	8.21
NG+	0.97	0.92	0.91	0.97	1.00	0.99	0.05	0.98	0.51	13.65
0	1.00	1.00	0.92	1.00	1.08	1.00	0.08	0.89	0.56	0.97
PRMQ	0.98	0.94	0.91	0.98	1.01	0.99	0.04	0.98	0.51	4.67
R	1.00	0.93	0.92	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	0.97	0.94	0.91	0.97	1.01	0.99	0.05	0.97	0.51	5.00
SCRUB	0.96	0.95	0.91	0.96	1.03	0.99	0.08	0.96	0.52	9.56
SRL	0.98	0.94	0.91	0.98	1.01	0.99	0.04	1.00	0.50	9.41
SalUN	0.97	0.94	0.91	0.97	1.01	0.99	0.05	0.99	0.51	6.53

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	0.91	0.91	0.85	0.91	1.02	0.97	0.14	0.99	0.50	4.13
CF-k	0.99	0.89	0.84	0.99	1.00	0.95	0.06	0.96	0.52	5.18
CFW	0.98	0.87	0.84	0.99	0.98	0.96	0.07	0.98	0.51	28.85
CT	0.98	0.82	0.81	0.98	0.93	0.92	0.17	1.00	0.50	23.48
EU-k	0.90	0.90	0.84	0.90	1.02	0.95	0.16	0.97	0.52	43.25
FCS	0.98	0.84	0.83	0.98	0.95	0.94	0.13	0.99	0.49	5.15
FF	-	-	-	-	-	-	-	-	-	-
FT	1.00	0.87	0.84	1.00	0.98	0.95	0.07	0.98	0.51	5.85
GA	0.85	0.85	0.80	0.85	0.96	0.91	0.29	0.97	0.52	514.77
IU	-	-	-	-	-	-	-	-	-	-
KDE	0.97	0.86	0.84	0.97	0.97	0.96	0.11	0.99	0.50	5.27
MSG	1.00	0.85	0.83	1.00	0.96	0.94	0.10	0.99	0.51	7.38
NG+	0.93	0.86	0.85	0.93	0.97	0.96	0.14	0.99	0.50	4.10
0	0.92	0.92	0.86	0.92	1.04	0.97	0.15	0.95	0.53	0.97
PRMQ	1.00	0.87	0.84	1.00	0.98	0.95	0.07	0.99	0.51	4.00
R	1.00	0.89	0.88	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	0.97	0.84	0.81	0.98	0.95	0.92	0.15	0.98	0.51	6.50
SCRUB	1.00	0.84	0.84	1.00	0.95	0.95	0.10	0.99	0.50	-
SRL	0.97	0.88	0.84	0.97	0.99	0.96	0.08	0.99	0.49	8.52
SalUN	0.96	0.89	0.85	0.96	1.00	0.96	0.08	0.99	0.50	8.30

Table 11: CIFAR-10 - TinyViT

Table 12: CIFAR-100 - TinyViT

	RA	FA	TA	RR	FR	TR	RetDev	Indisc	T-MIA	RTE
Unlearner										
BT	0.82	0.66	0.57	0.82	1.11	0.96	0.33	0.94	0.53	31.63
CF-k	0.24	0.18	0.18	0.24	0.31	0.30	2.15	0.98	0.51	5.97
CFW	0.98	0.58	0.56	0.98	0.97	0.95	0.10	0.99	0.51	9.18
СТ	0.97	0.55	0.55	0.98	0.93	0.93	0.17	0.99	0.49	9.80
EU-k	0.61	0.60	0.49	0.61	1.01	0.81	0.59	0.90	0.55	19.29
FCS	0.89	0.60	0.58	0.89	1.01	0.98	0.13	0.97	0.48	7.05
FF	-	-	-	-	-	-	-	-	-	-
FT	1.00	0.56	0.55	1.00	0.94	0.91	0.15	1.00	0.50	5.90
GA	0.60	0.58	0.46	0.60	0.97	0.77	0.66	0.87	0.56	91.91
IU	-	-	-	-	-	-	-	-	-	-
KDE	0.93	0.58	0.57	0.94	0.98	0.96	0.13	0.99	0.50	4.03
MSG	0.97	0.57	0.56	0.97	0.95	0.93	0.15	1.00	0.50	5.89
NG+	0.84	0.57	0.55	0.84	0.95	0.92	0.29	0.96	0.52	3.01
0	0.87	0.87	0.61	0.87	1.46	1.02	0.61	0.74	0.63	0.98
PRMQ	0.95	0.62	0.57	0.95	1.03	0.96	0.13	0.95	0.52	5.58
R	1.00	0.60	0.60	1.00	1.00	1.00	0.00	1.00	0.50	1.00
RNI	0.85	0.52	0.51	0.85	0.87	0.85	0.42	0.99	0.50	5.38
SCRUB	0.77	0.64	0.57	0.77	1.08	0.96	0.35	0.93	0.53	6.17
SRL	0.98	0.57	0.57	0.98	0.96	0.96	0.11	0.97	0.49	5.92
SalUN	0.97	0.58	0.57	0.97	0.97	0.96	0.10	0.98	0.49	7.03

		Rete	ntion	Devia	tion			In	discer	nibilit	у		
Rank	Method	G1	G2	G3	F	Rank	Method	G1	G2	G3	F		
1	FT	5	0	0	0	1	CFW	5	0	0	0		
2	FCS	4	1	0	0	1	CT	5	0	0	0		
2	MSG	4	1	0	0	1	MSG	5	0	0	0		
3	CT	4	0	1	0	1	RNI	5	0	0	0		
3	KDE	4	0	1	0	2	FT	4	1	0	0		
4	NG+	3 2 0 0		2	KDE	4	1	0	0				
4	PRMQ	3	2	0	0	2	NG+	4	1	0	0		
4	SalUN	3	2	0	0	2	PRMQ	4	1	0	0		
5	CFW	3	1	1	0	3	FCS	3	2	0	0		
6	SCRUB	3	0	1	1	3	SRL	3	2	0	0		
7	SRL	2	3	0	0	3	SalUN	3	2	0	0		
8	BT	1	4	0	0	4	SCRUB	3	1	0	1		
8	RNI	1	4	0	0	5	BT	2	3	0	0		
9	CF-k	1	2	1	1	6	6	1 6	EU-k	1	0	0	4
10	IU	1	0	2	2	7	GA	0	3	1	1		
11	EU-k	0	1	0	4	8	CF-k	0	1	3	1		
12	GA	0	0	4	1	9	IU	0	0	3	2		
13	FF	0	0	0	5	10	FF	0	0	0	5		

Table 13: Ranking on ResNet

Table 14: Ranking of ViT

		Retention Deviation						Indiscernibility			
Rank	Method	G1	G2	G3	F	Rank	Method	G1	G2	G3	F
1	CFW	4	0	0	0	1	СТ	4	0	0	0
1	MSG	4	0	0	0	1	MSG	4	0	0	0
1	PRMQ	4	0	0	0	2	KDE	3	1	0	0
2	CT	3	1	0	0	2	SalUN	3	1	0	0
2	FT	3	1	0	0	3	SRL	3	0	1	0
2	KDE	3	1	0	0	4	BT	2	2	0	0
2	SRL	3	1	0	0	4	CFW	2	2	0	0
2	SalUN	3	1	0	0	4	FCS	2	2	0	0
3	FCS	2	2	0	0	4	FT	2	2	0	0
3	NG+	2	2	0	0	4	PRMQ	2	2	0	0
4	BT	1	3	0	0	4	RNI	2	2	0	0
4	RNI	1	3	0	0	4	SCRUB	2	2	0	0
4	SCRUB	1	3	0	0	5	NG+	1	3	0	0
5	CF-k	1	1	1	1	6	CF-k	1	1	1	1
6	EU-k	0	4	0	0	7	EU-k	0	2	2	0
7	GA	0	1	3	0	8	GA	0	1	3	0
8	FF	0	0	0	4	9	FF	0	0	0	4
8	IU	0	0	0	4	9	IU	0	0	0	4

705 G L2 Distances between model weights.

The distance between the Unlearned and Retrained models has also been considered in the literature to evaluate MU. Nevertheless, we observe that models end up at a similar distance to the Retrained model, with significant differences in performance. We further note that one challenging aspect of the L2 distance comparison is the different factors of Weight Decay used by the MU method. The hyper-parameter searches determine these Weight Decay factors, which can significantly vary from one unlearning method to another, making it challenging to compare methods. Furthermore, the best-performing method, MSG, is usually at the same distance as both the Original and Retrained model. For each method, for each initialization seed, we computed the L2 distance between the unlearned model f_U and the retrained model f_R , as well as between the f_U and f_O (Figure 2).

 $f_{\rm R}$ and $f_{\rm R}$ and $f_{\rm R}$ and $f_{\rm R}$ and $f_{\rm R}$ as well as between the $f_{\rm R}$ and $f_{\rm R}$ (1) for 2).

Although having the same weight as the Retrained model would indicate that the unlearned model has unlearned D_F , our evaluations show that distance to the Retrained model might not be an adequate evaluation metric for MU.



Figure 2: L2 Distance between the Unlearned ResNet18 models, the Original and Retrained models. None of the unlearned models gets close to the Retrained model's weights; most unlearned Models are closer to the Original model than the Retrained model.

718 H Requirements

We ran the experiments on compute clusters with different capacities. Nonetheless, each method was tested on devices with the same specifications when recording run times: 1 NVIDIA L4 24GB GPU

and 4 Intel(R) Xeon(R) CPU @ 2.20GHz.