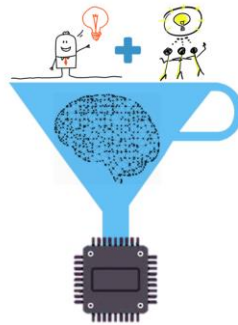


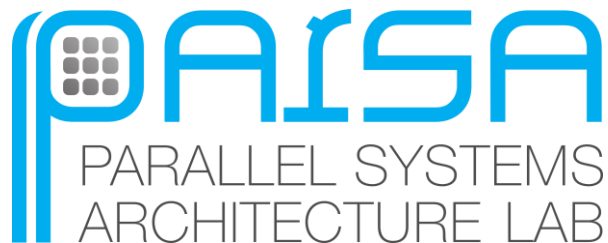
Accuracy Boosters

Epoch-Driven Mixed-Mantissa Block Floating Point for DNN Training

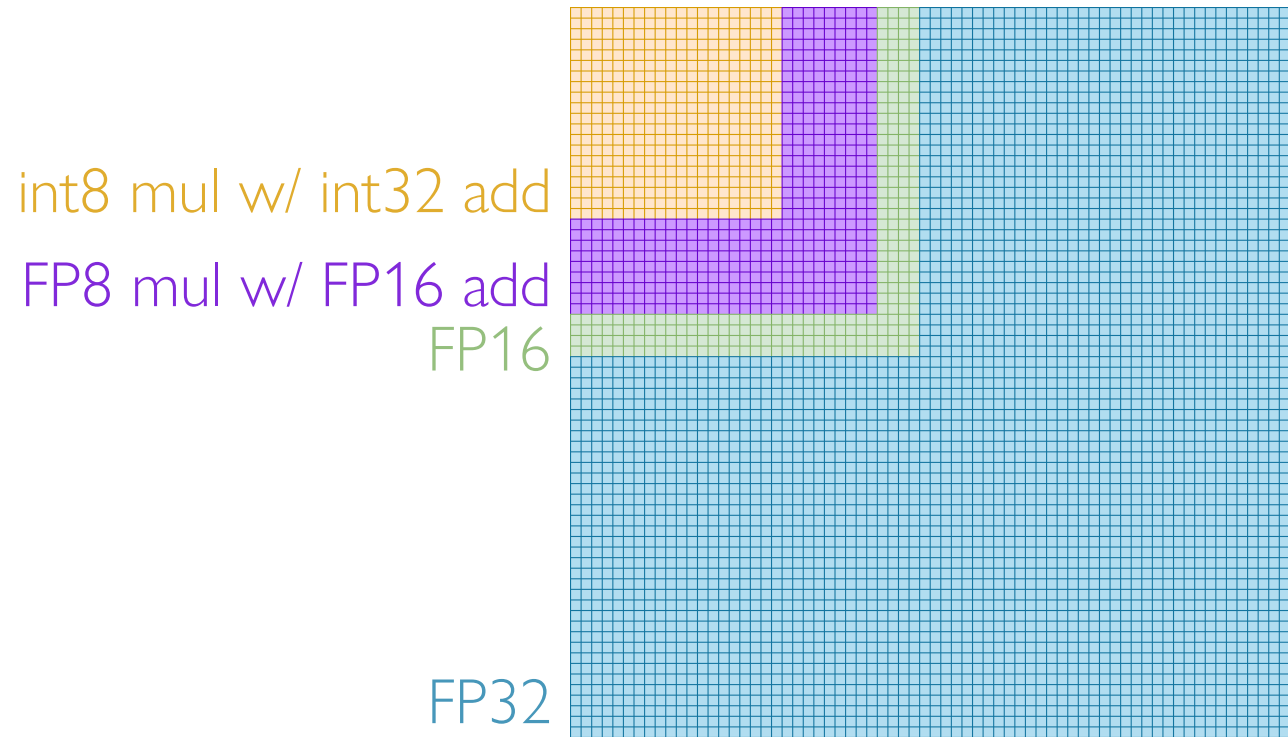
Simla Burcu Harma, Ayan Chakraborty,
Babak Falsafi, Martin Jaggi, Yunho Oh



parsa.epfl.ch/coltrain



Dense and Accurate DNN Training

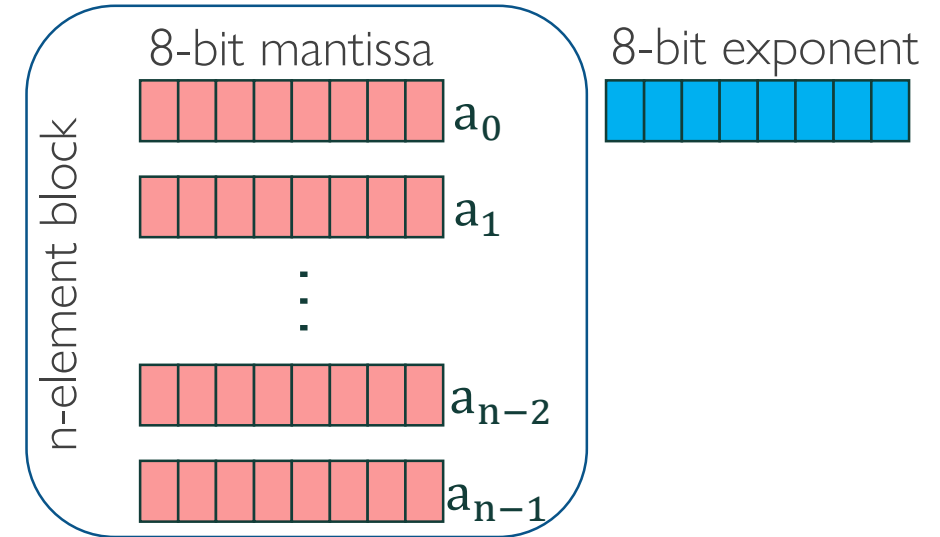


Relative logic area of multiply-and-accumulate (MAC) using different datatypes on the same silicon [Fox et al., ICLR'21]

Goal: Training DNNs using fixed-point arithmetic with FP32 accuracy

A Narrow Bitwidth Format: HBFP

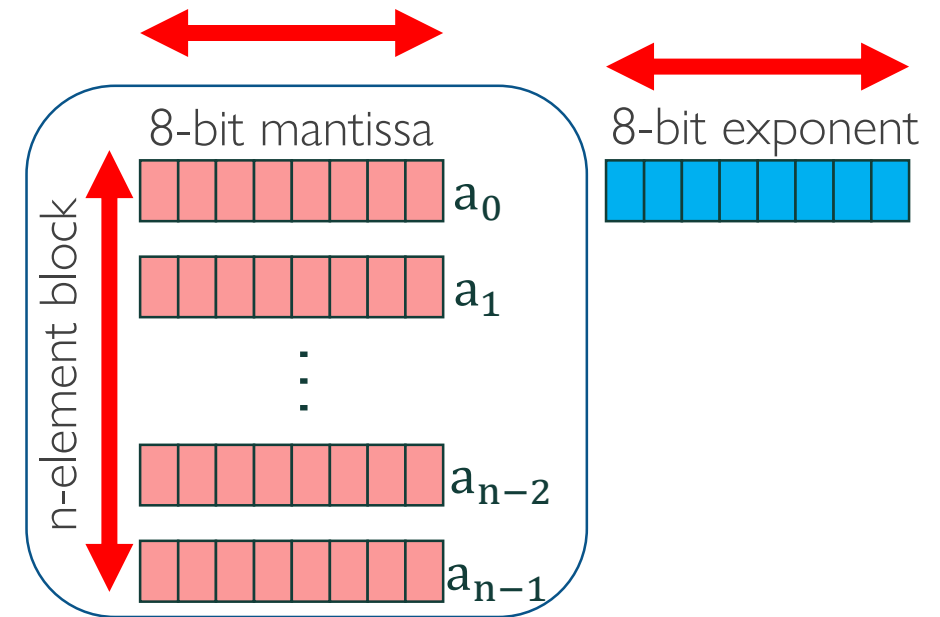
- High accuracy of floating point
- The superior hardware density of fixed point
- Block Floating Point (BFP) for dot products ($> 90\%$ ops)
- Floating Point for activations and other arithmetic



BFP representation with an exponent per tensor

A Narrow Bitwidth Format: HBFP

- Explore the HBFP parameter space
 - Maximizing block size
 - Minimizing mantissa bits
- ⇒ Study the tensor distribution similarities
- ⇒ Analyze the loss landscapes



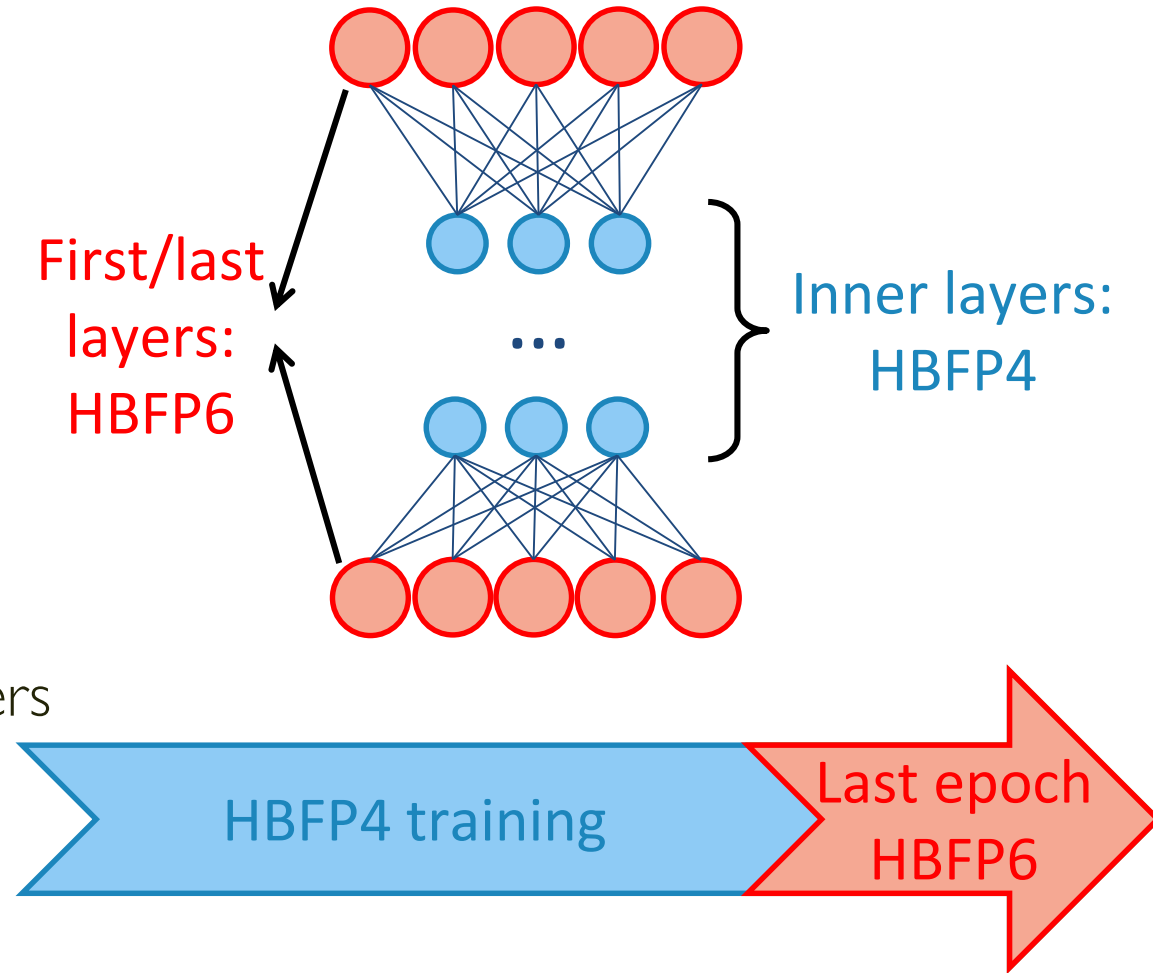
BFP representation with an exponent per tensor

The parameter space of HBFP is yet to be explored!

Contributions

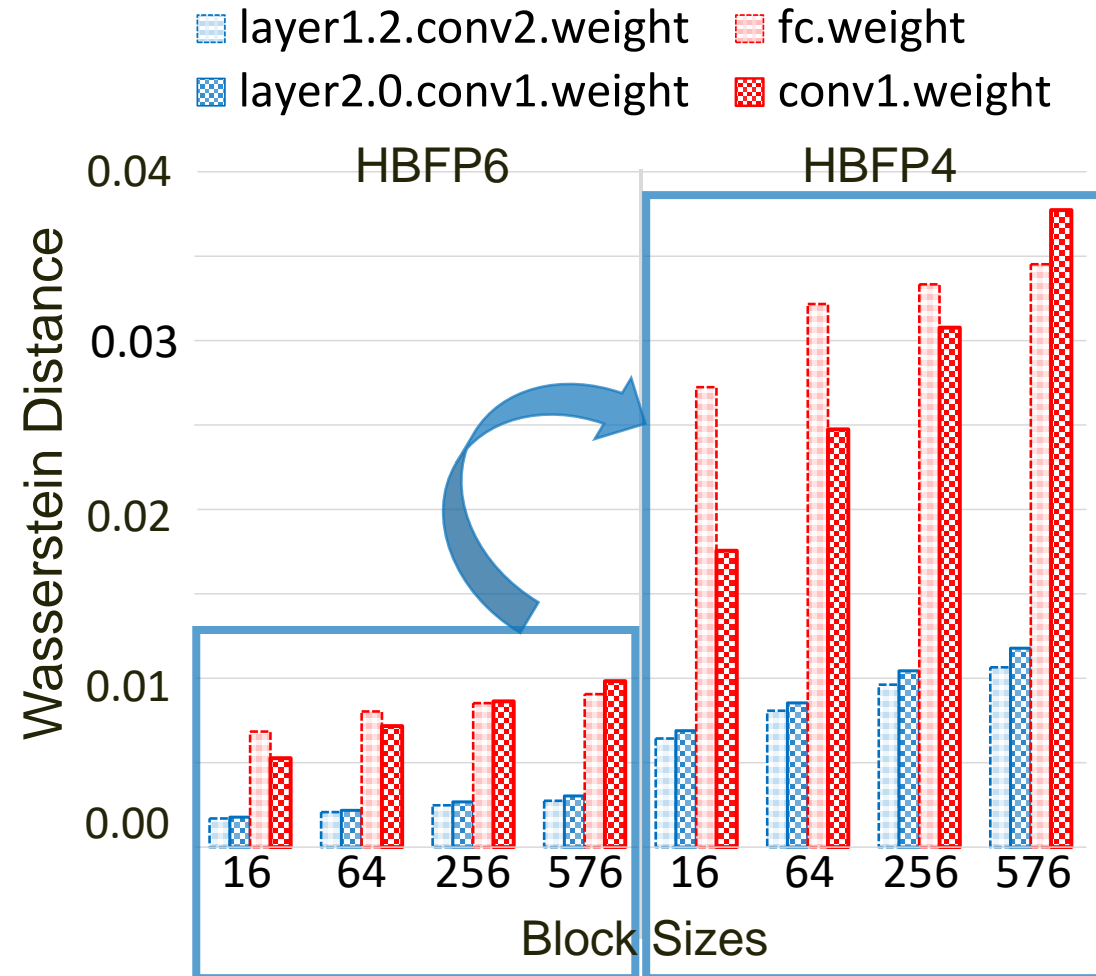
- Explore the HBFP parameter space
 - Maximizing block size
 - Minimizing mantissa bits
 - ⇒ Study the tensor distribution similarities
 - ⇒ Analyze the loss landscapes

- Accuracy Boosters
 - HBFP6 only in the last epoch and first/last layers
 - HBFP4 for the rest (99.7% of ops)



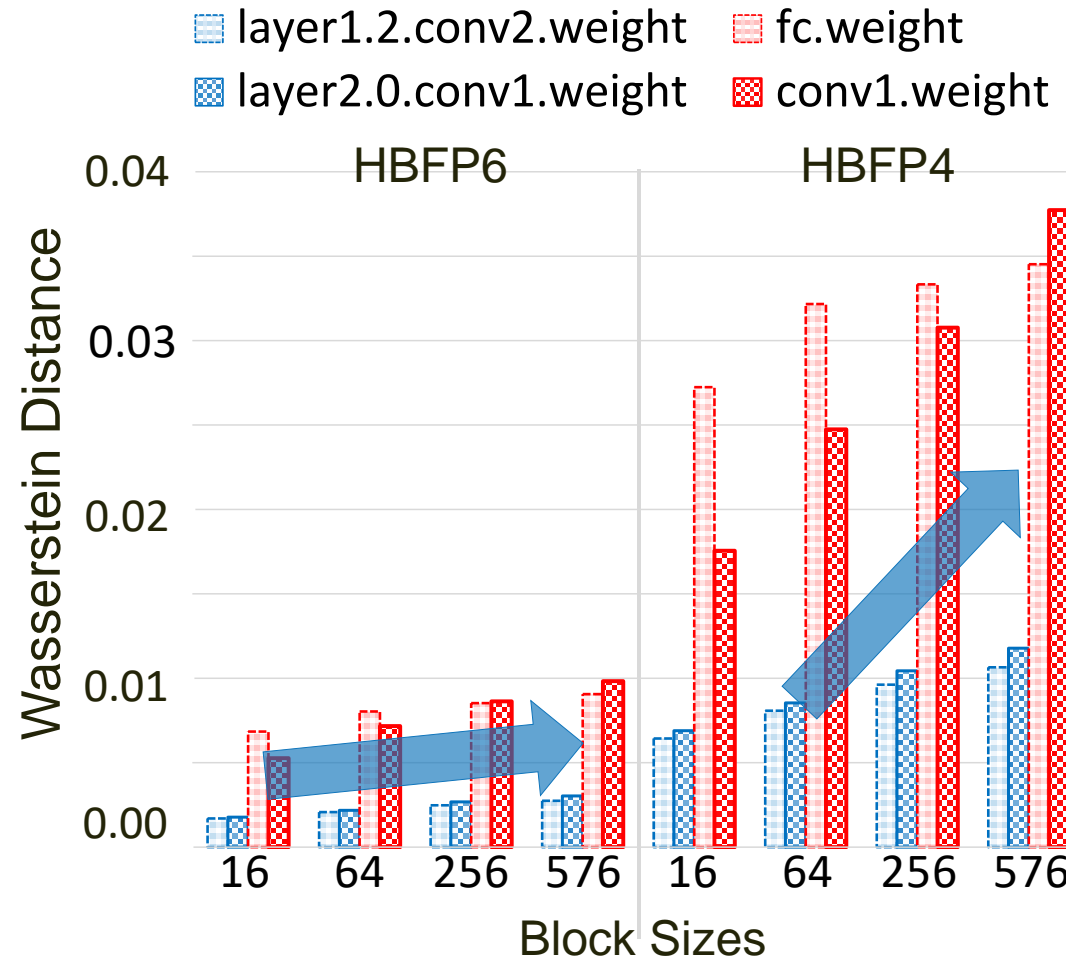
We can get the HW benefits of HBFP4 while maintaining FP32 accuracies

Tensor Distributions: HBFP4 vs. HBFP6



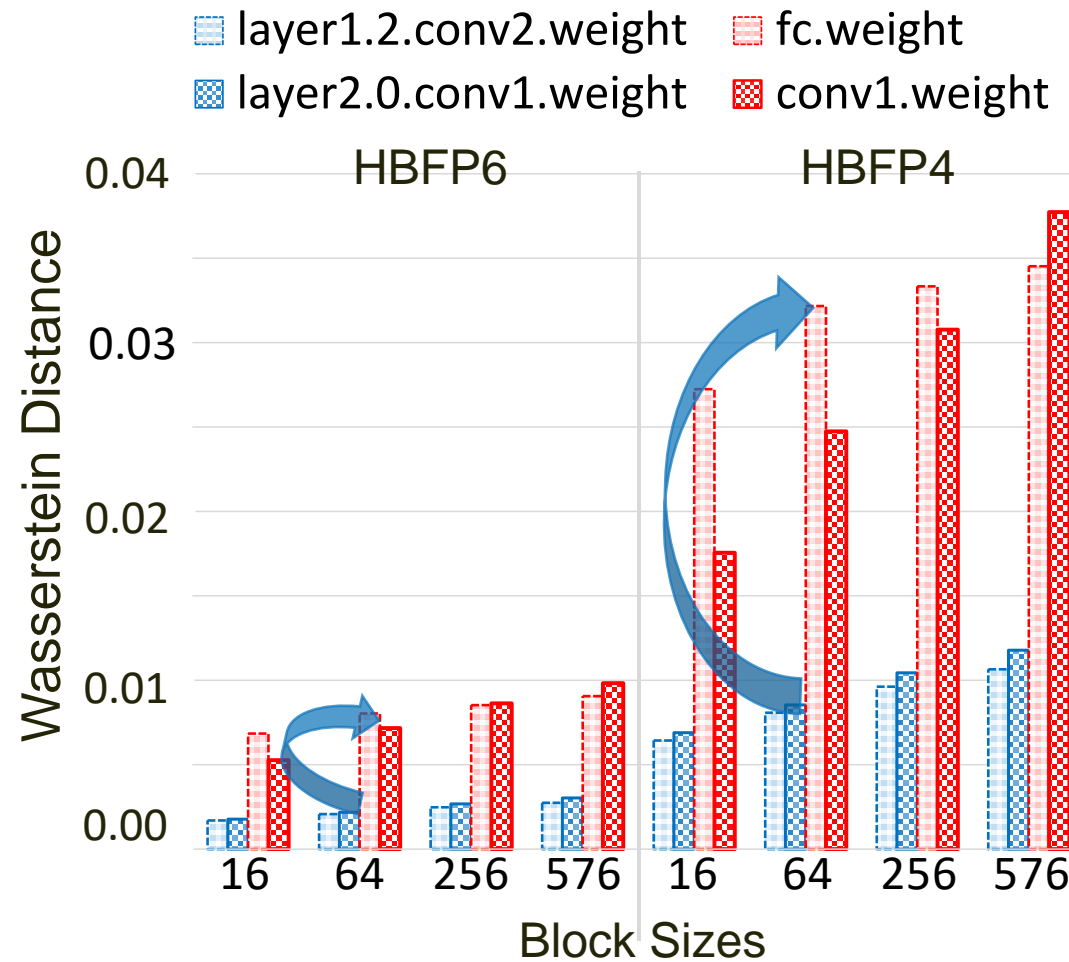
Tensor distributions are much more distorted for HBFP4 compared to HBFP6

Tensor Distributions: Block Sizes



HBFP6 is not sensitive to the block size, while HBFP4 is sensitive

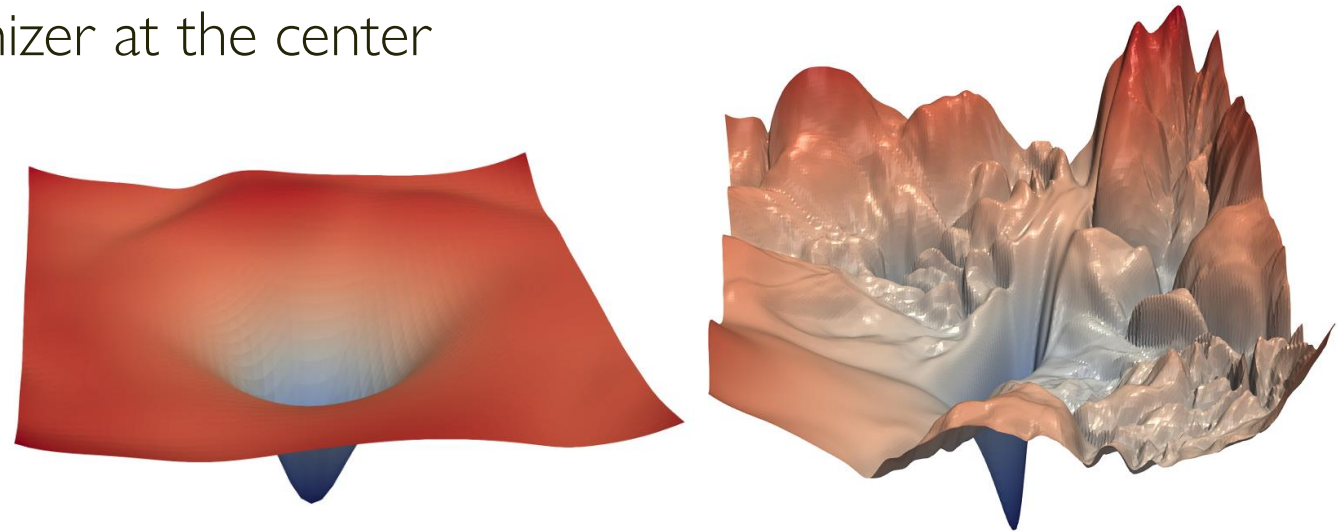
Tensor Distributions: First/Last Layers



Wasserstein distance of first/last layers is higher than the other layers

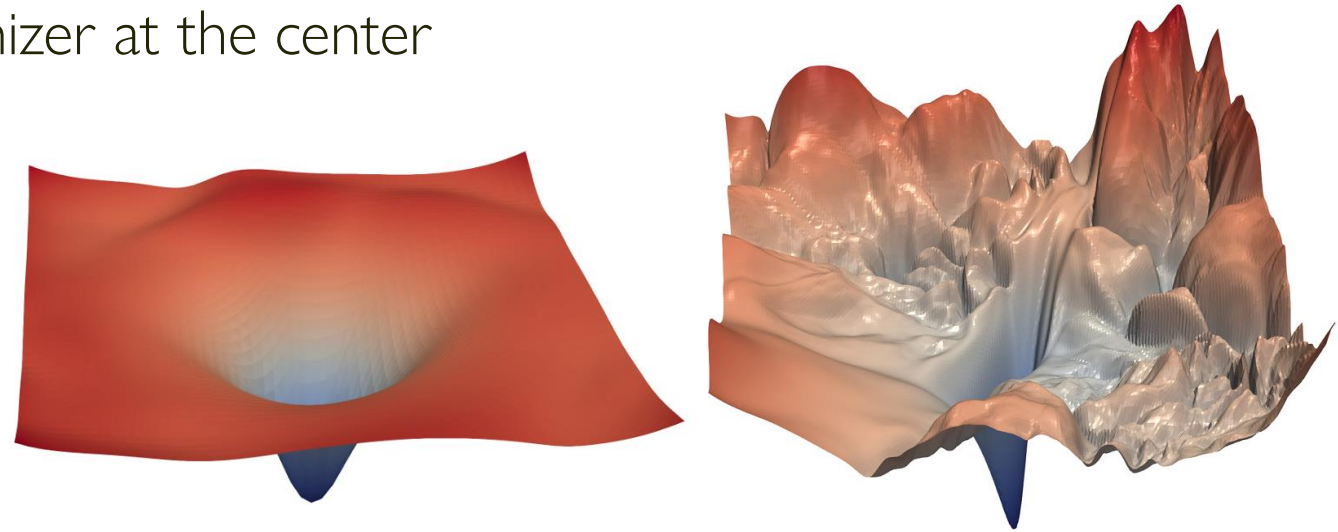
Analyzing the Loss Landscapes

- Plot the landscape around the current position of the minimizer
- Dimensionality reduction
 - Pick two random directions and form a plane
 - Add a third dimension → will be the loss value calculated at each point within that plane
 - Position the current state of the minimizer at the center



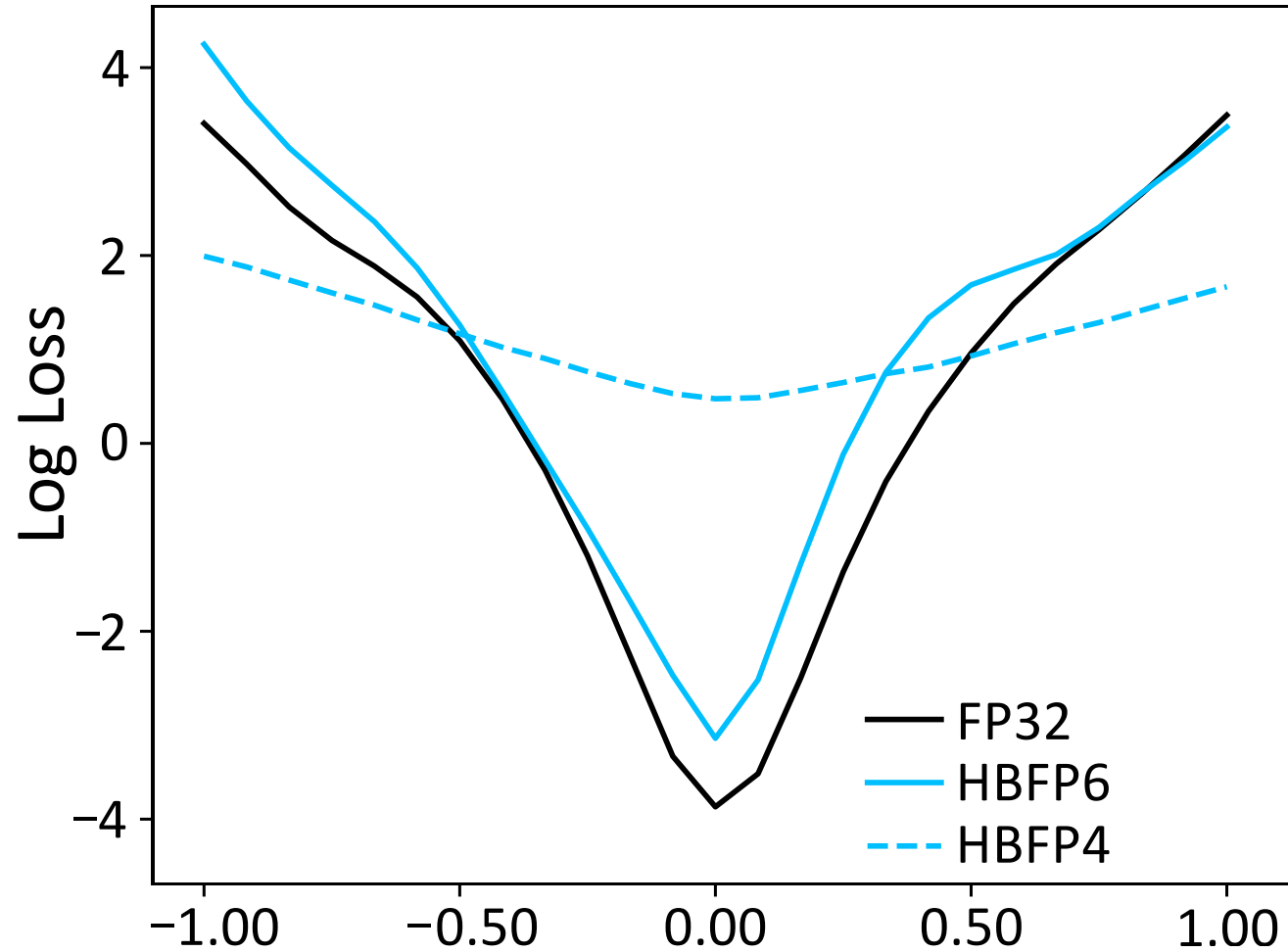
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 - Pick two random directions and form a plane
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 - Position the current state of the minimizer at the center
- Loss value → Optimization
- Flatness → Generalization



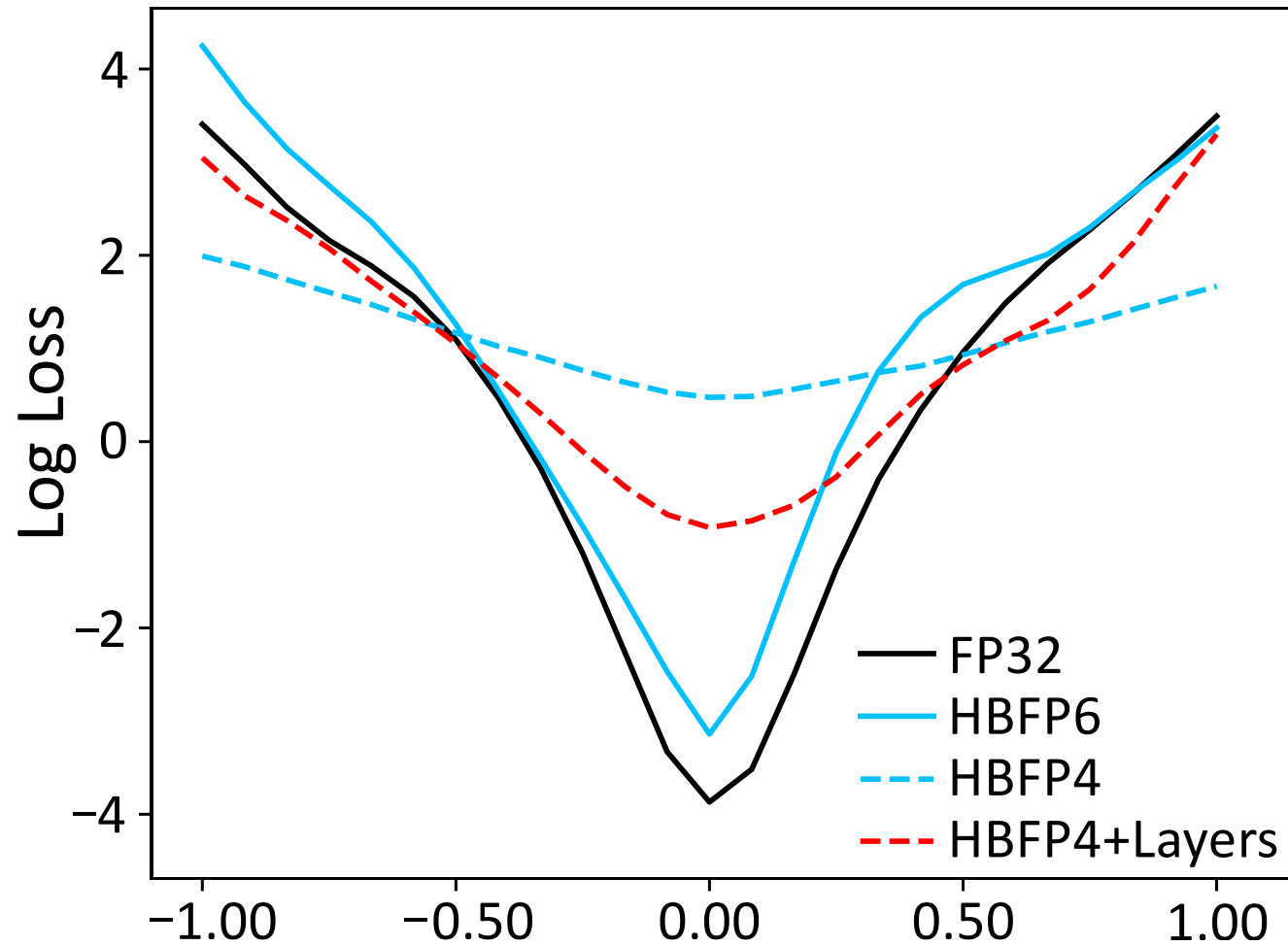
Loss landscapes provides information for the interplay between generalization & optimization

Loss Landscapes: FP32 vs Standalone HBFP



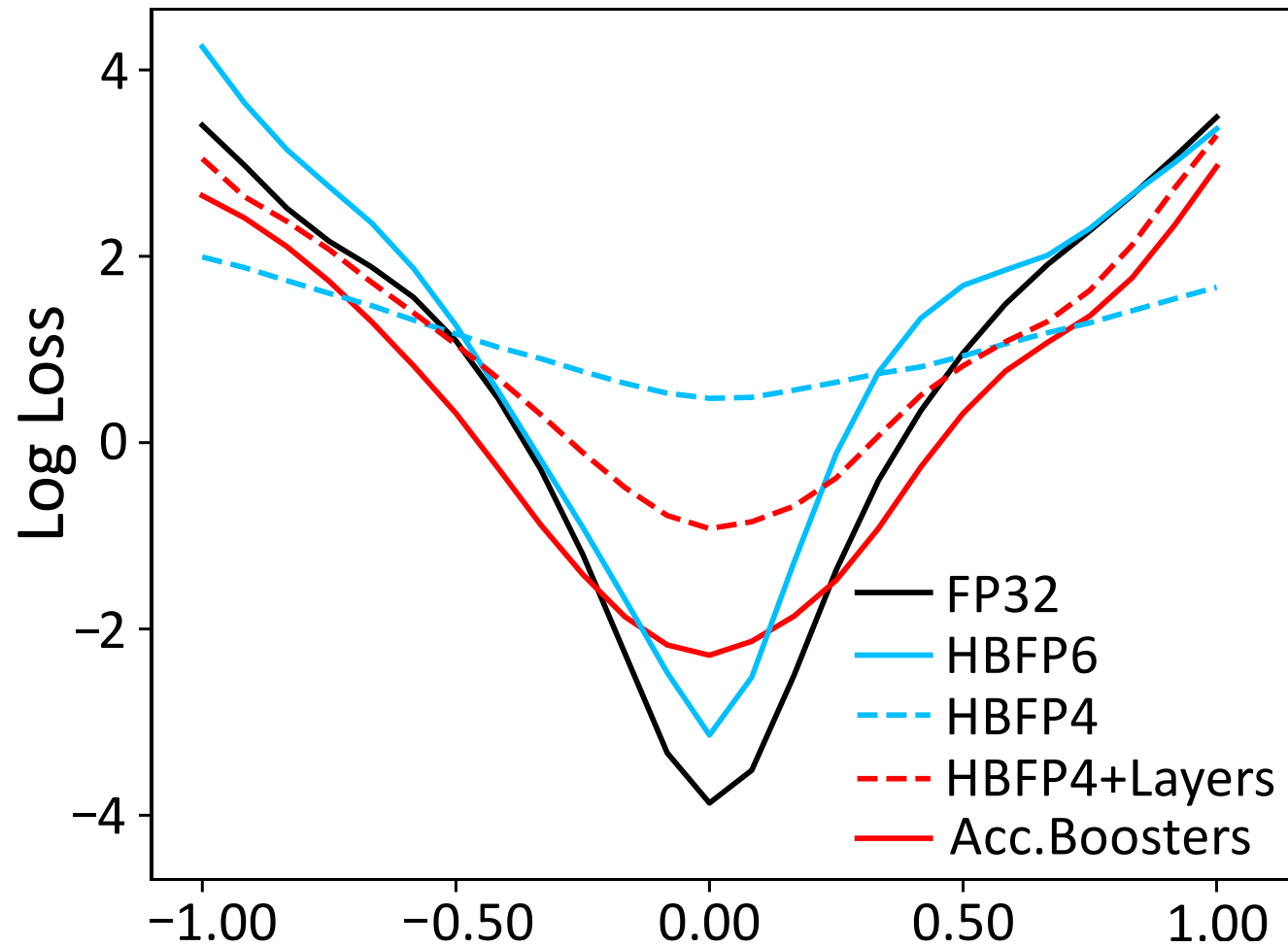
HBFP4 fails to converge to good minimum in contrast to HBFP6

Loss Landscapes: HBFP4+Layers



Increase in accuracy but there is still imbalance btw. optimization and generalization

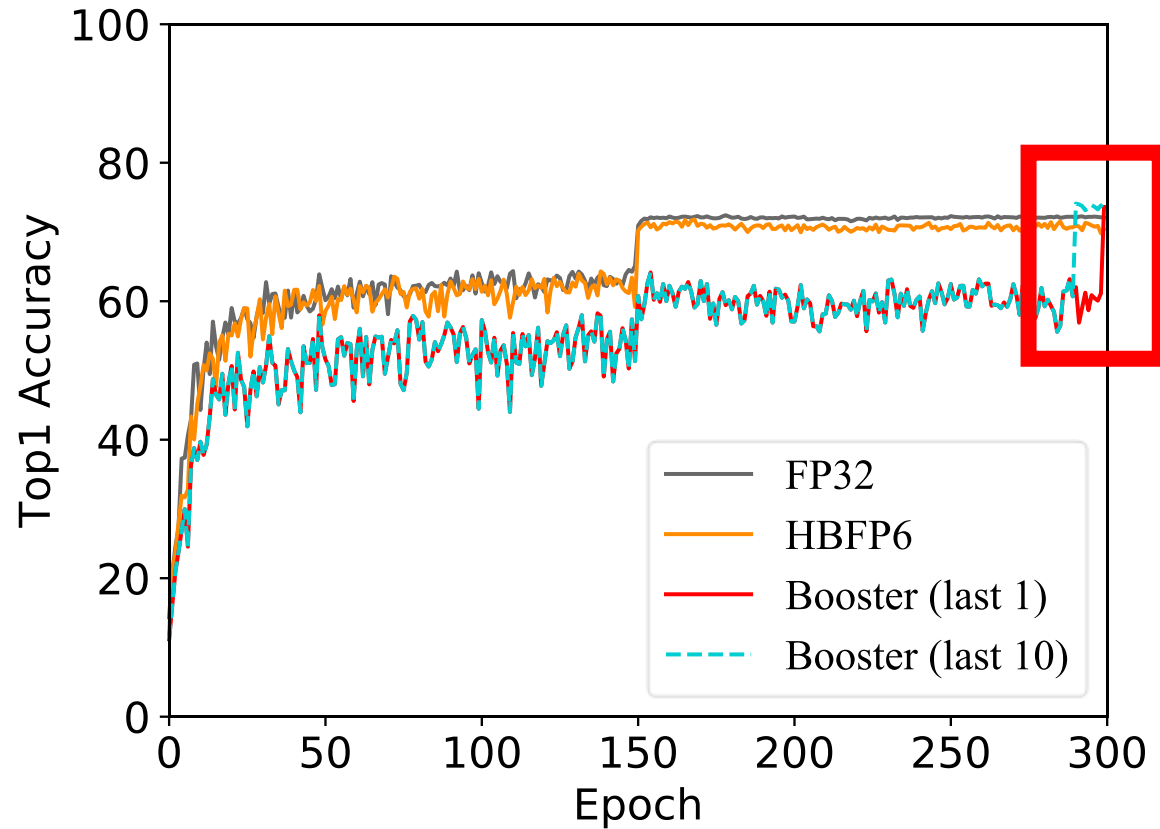
Loss Landscapes: Accuracy Boosters



Accuracy Boosters is the recipe to reach the sweet spot between generalization & optimization

Accuracy Boosters: Model Accuracies

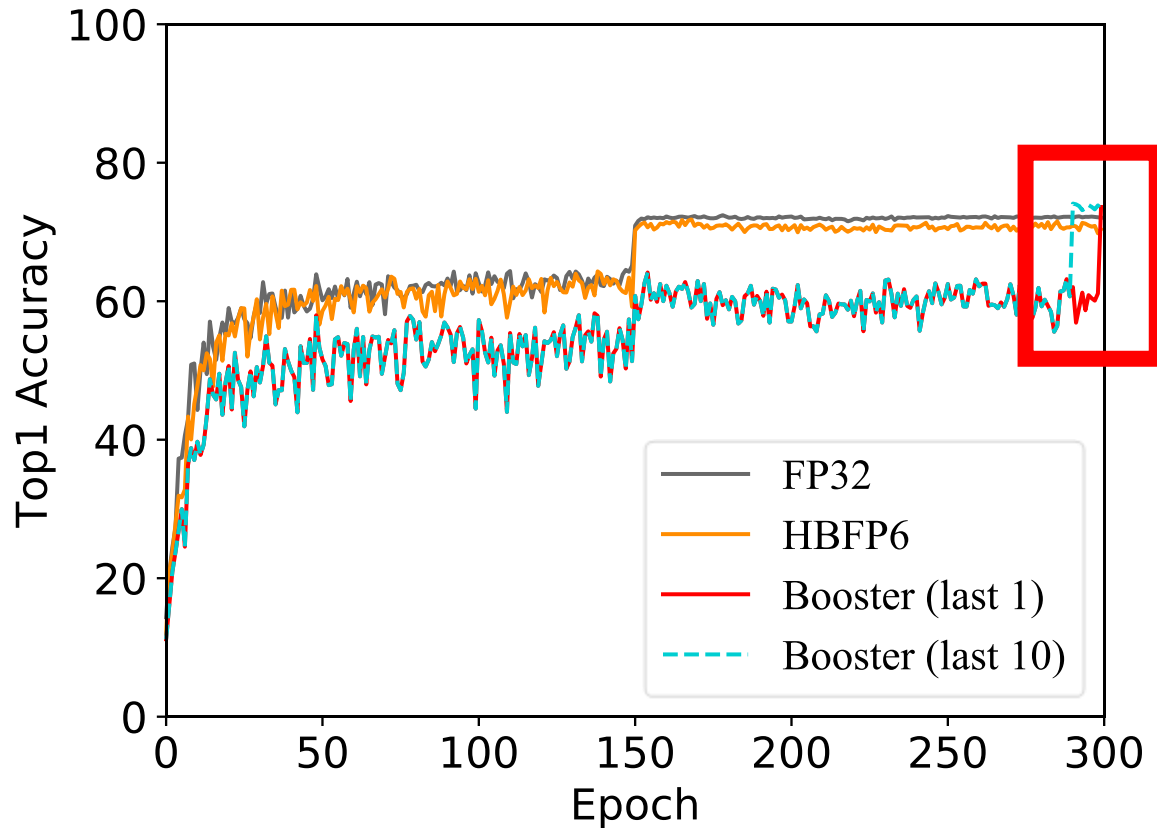
DenseNet40 on CIFAR100



FP32 level accuracy while using HBFP4 for majority of operations with 21.3x higher density

Accuracy Boosters: Model Accuracies

DenseNet40 on CIFAR100



Transformer-Base trained on
IWSLT'14 De→En

Configuration	BLEU Score
FP32	34.77
HBFP6	34.47
HBFP4	32.64
Booster	36.08

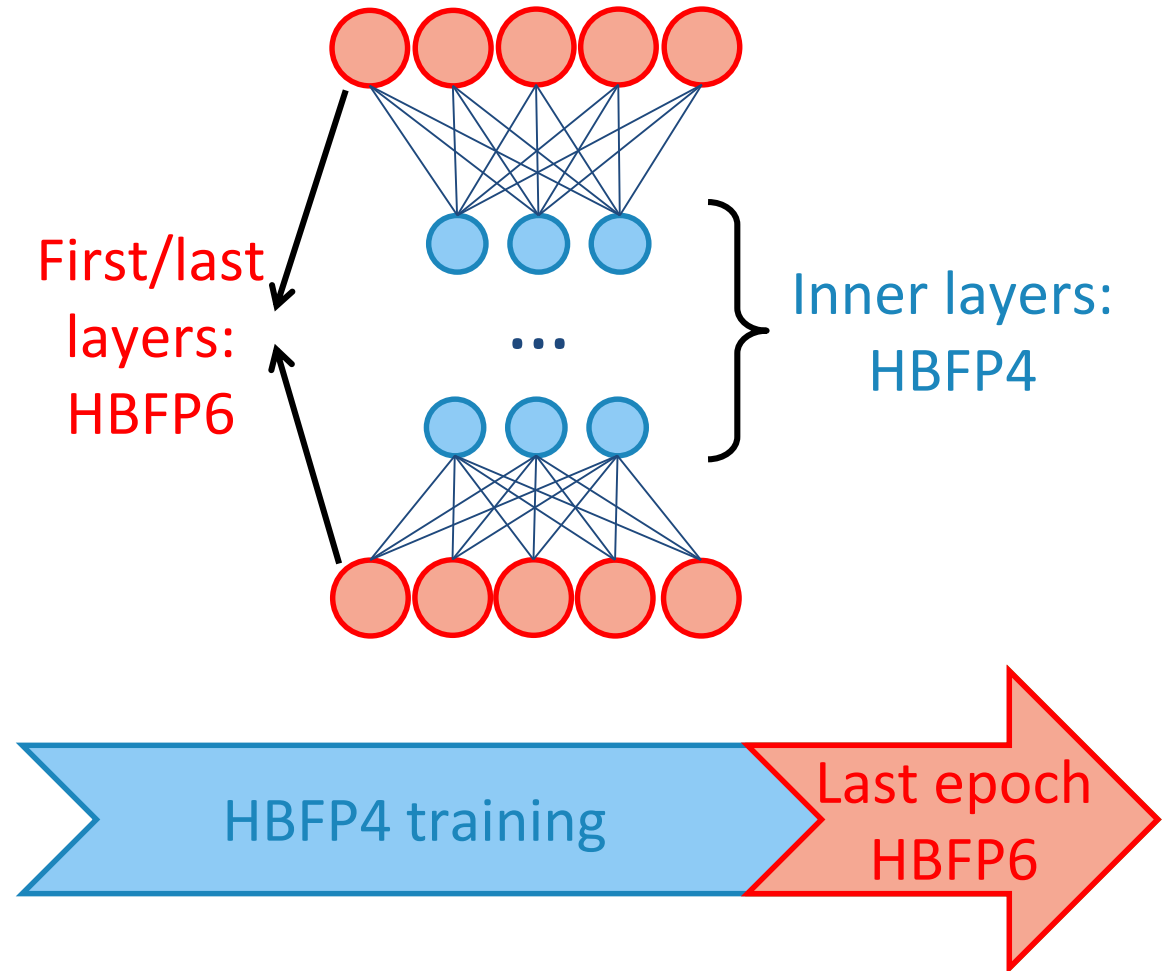
FP32 level accuracy while using HBFP4 for majority of operations with 21.3x higher density

Summary

- HBFP has a rich parameter space → Opportunities to increase arithmetic density
- Explore HBFP parameters
 - Block size ⇒ Tensor distribution similarities
 - Mantissa bitwidth ⇒ Loss landscapes
- Accuracy Boosters: Mixed-mantissa BFP across layers and epochs
- Accuracy Boosters employs HBFP4 for the 99.7% of total operations
 - FP32-level accuracies
 - Up to 21.3× higher arithmetic density over FP32

Thank You!

For more information please visit
us at parsa.epfl.ch
or contact me via
simla.harma@epfl.ch



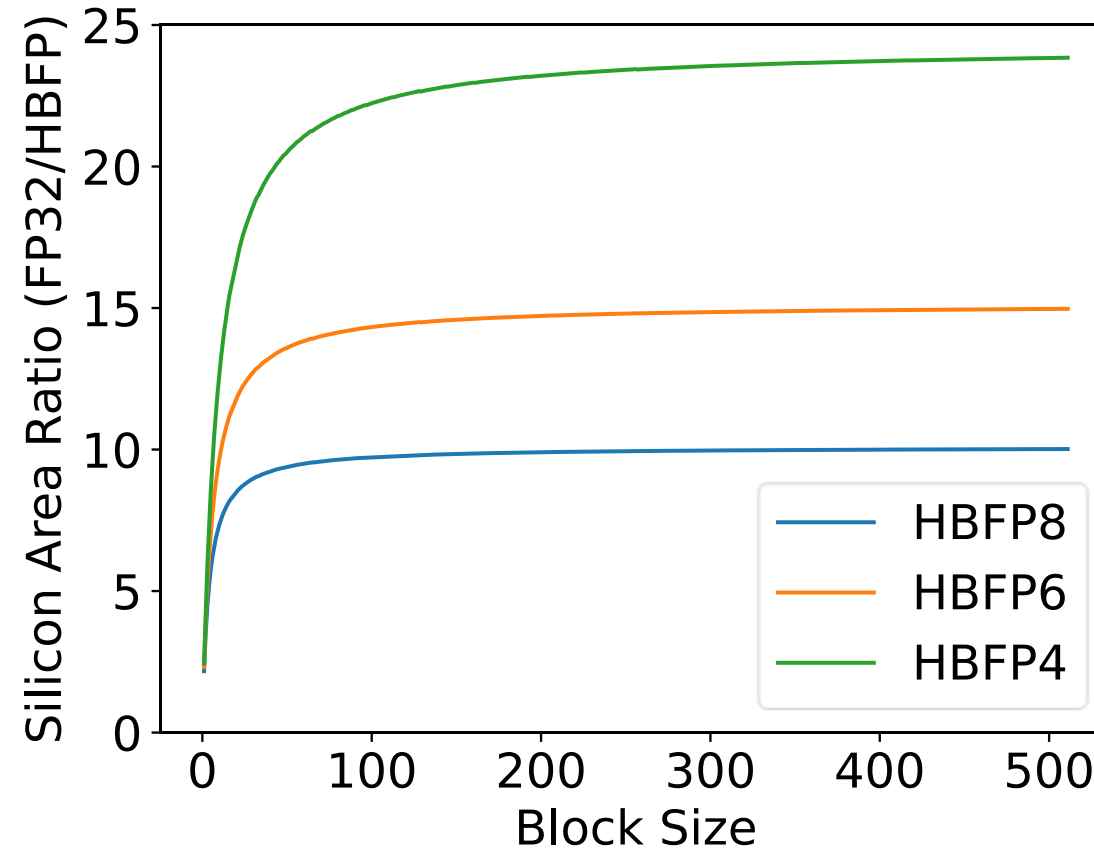
Wasserstein Distance

$$W(P, Q) = \inf_{\gamma \in \Pi(P, Q)} \mathbb{E}_{(x, y) \sim \gamma} [\|x - y\|],$$

where $\Pi(P, Q)$ is the set of all joint distributions $\gamma(x, y)$ whose marginal distributions are equal to P and Q

- $\gamma(x, y)$ can be interpreted as the amount of mass that must be transported from x to y to transform P to Q

HBFP Parameter Space: Why Minimize?



Considerable power and area savings!

Hardware Support

- HBFP4 hardware can support HBFP6 operations in 4 steps

- Lower HBFP6 operations into HBFP4:

$$A \times B = (2^4 \cdot A_{\text{HI}} + A_{\text{LO}}) \times (2^4 \cdot B_{\text{HI}} + B_{\text{LO}})$$

$$A \times B = 2^8 \cdot A_{\text{HI}} \times B_{\text{HI}} + 2^4 \cdot (A_{\text{HI}} \times B_{\text{LO}} + A_{\text{LO}} \times B_{\text{HI}}) + A_{\text{LO}} \times B_{\text{LO}}$$

- Support 2^4 and 2^8 by modifying the BFloat16 accumulators
 - Offset the exponent by 4 or 8
 - With little hardware can achieve lower HBFP6 throughput