

Sample Efficient Offline RL via T-symmetry Enforced Latent State-Stitching

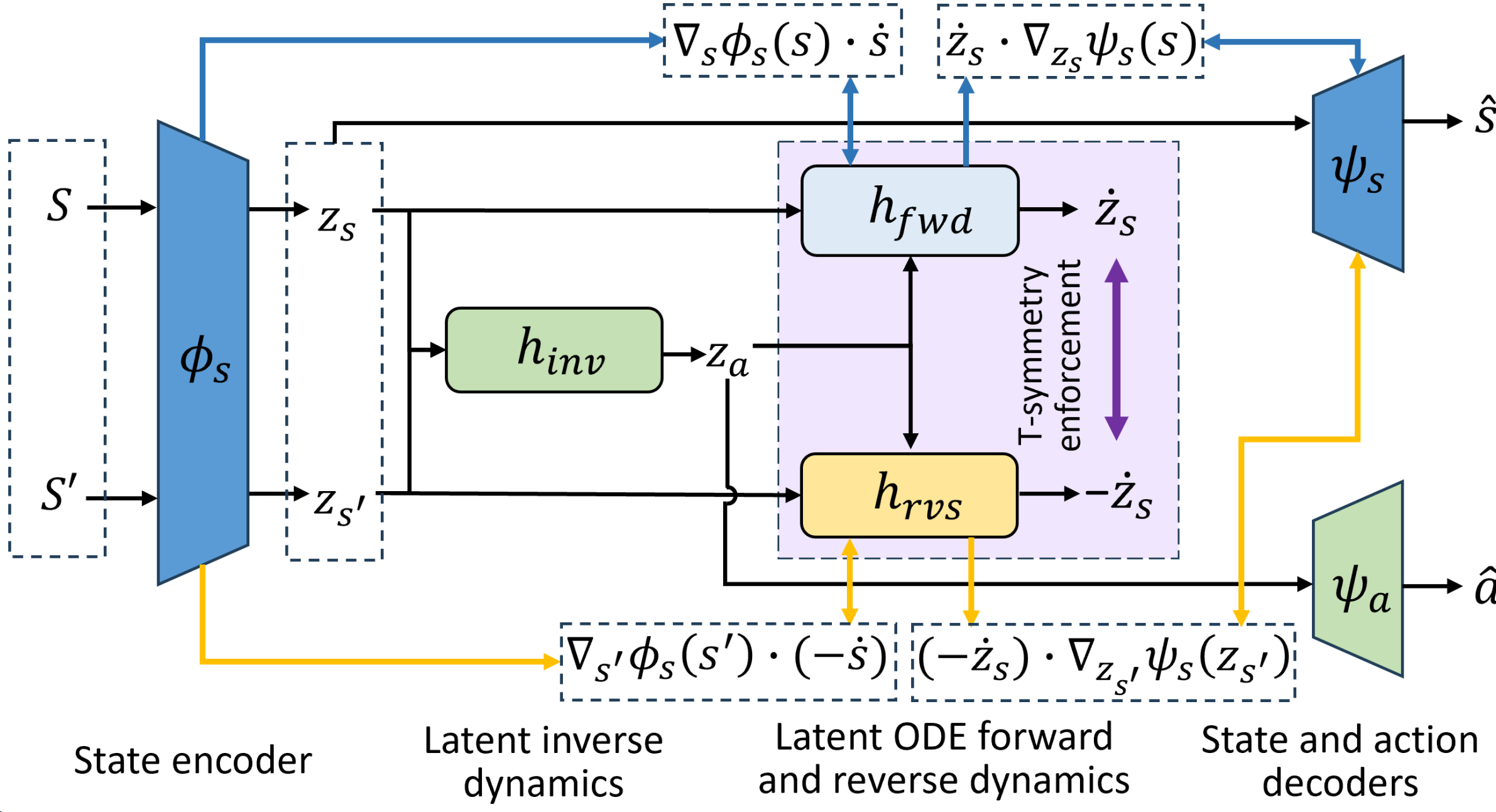
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Introduction

- Current offline RL methods require a large amount of training data to achieve reasonable performance and offer limited generalizability in out-of-distribution (OOD) regions due to conservative data-related regularizations.
- We propose a **highly sample-efficient offline RL algorithm (TELS)** that learns optimized policy within the latent space regulated by the fundamental T-symmetry in the dynamical systems.
- Our approach achieves amazing sample efficiency and OOD generalizability, significantly outperforming existing offline RL methods in various small-sample tasks, even **using as few as 1% of the data samples** in D4RL datasets.

T-symmetry Enforced Latent State-Stitching (TELS)

T-symmetry enforced inverse dynamic model (TS-IDM)



1 Latent state-value function learning

$$\min_{\psi} \mathbb{E}_{(s,r,s') \sim \mathcal{D}} \left[L_2^r \left(r + \gamma \bar{V}(\phi_s(s')) - V(\phi_s(s)) \right) \right]$$

Learning in the latent space

2 T-symmetry regularized guide-policy optimization

$$\max_{\pi_g} \mathbb{E}_{(s,s') \sim \mathcal{D}} \left[\lambda_{\alpha} V(\pi_g(z_s)) - \eta \left\| \psi_s(\pi_g(z_s)) - s' \right\|_2^2 - \ell_{T-sym}(z_s, h_{inv}(z_s, \pi_g(z_s))) \right]$$

Or

$$\max_{\pi_g} \mathbb{E}_{(s,s') \sim \mathcal{D}} \left[\exp(\alpha \cdot A(z_s, z_{s'})) \log \pi_g(z_{s'} | z_s) - \ell_{T-sym}(z_s, h_{inv}(z_s, \pi_g(\cdot | z_s))) \right]$$

T-symmetry regularization

3 Action inference

$$a^* = \psi_a \left(h_{inv}(z_s, \pi_g(z_s)) \right)$$

Extract optimized action using latent inverse dynamics

- TS-IDM:** Learns well-behaved latent representations that address OOD generalization challenges and enhance action inference efficiency.
- Latent Space Offline Policy Optimization:** Learns a latent state-value function and T-symmetry-regularized guide-policy to generate valuable and reliable next latent states, enabling TS-IDM's inverse dynamics to infer optimal actions.

Main Results

Table 1: Average normalized scores on reduced-size D4RL datasets. The scores are taken over the final 10 evaluations with 5 seeds.

Task	Size (ratio)	BC	TD3+BC	CQL	IQL	DOGE	IDQL	POR	TSRL	TELS
Hopper-m	10k (1%)	29.7±11.7	40.1±18.6	43.1±24.6	46.7±6.5	44.2±10.2	44.2±12.1	46.4±1.7	62.0±3.7	77.3±10.7
Hopper-mr	10k (2.5%)	12.1±5.3	7.3±6.1	2.3±1.9	13.4±3.1	17.9±4.5	21.7±7.0	17.4±6.2	21.8±8.2	43.2±3.5
Hopper-me	10k (0.5%)	27.8±10.7	17.8±7.9	29.9±4.5	34.3±8.7	50.5±25.2	43.2±4.4	37.9±6.1	50.9±8.6	100.9±6.8
Halfcheetah-m	10k (1%)	26.4±7.3	16.4±10.2	35.8±3.8	29.9±0.12	36.2±3.4	36.4±1.5	33.3±3.2	38.4±3.1	40.8±0.6
Halfcheetah-mr	10k (5%)	14.3±7.8	17.9±9.5	8.1±9.4	22.7±6.4	23.4±3.6	26.7±1.0	27.5±3.6	28.1±3.5	33.2±1.0
Halfcheetah-me	10k (0.5%)	19.1±9.4	15.4±10.7	26.5±10.8	10.5±8.8	26.7±6.6	38.8±1.9	34.7±2.6	39.9±21.1	40.7±1.2
Walker2d-m	10k (1%)	15.8±14.1	7.4±13.1	18.8±18.8	22.5±3.8	45.1±10.2	31.7±14.2	22.2±3.6	49.7±10.6	62.4±5.3
Walker2d-mr	10k (3.3%)	1.4±1.9	5.7±5.8	8.5±2.19	10.7±11.9	13.5±8.4	12.2±10.5	14.8±4.2	26.0±11.3	54.8±6.0
Walker2d-me	10k (0.5%)	21.7±8.2	7.9±9.1	19.1±14.4	26.5±8.6	35.3±11.6	21.8±14.5	20.1±8.6	46.4±17.4	87.4±13.3
Antmaze-u	10k (1%)	44.7±42.1	0.7±1.2	0.1±0.0	65.1±19.4	56.3±24.4	67.5±12.4	6.1±7.3	76.1±15.6	88.7±7.7
Antmaze-u-d	10k (1%)	24.1±22.2	16.27±16.4	0.5±0.1	34.6±18.5	41.7±18.9	55.1±36.8	42.1±14.2	52.2±22.1	60.9±16.9
Antmaze-m-d	100k (10%)	0.0	0.0	0.0	4.8±5.9	0.0	9.0±3.4	0.0	0.0	47.2±17.3
Antmaze-m-p	100k (10%)	0.0	0.0	0.0	12.5±5.4	0.0	9.4±14.7	0.0	0.0	62.9±17.8
Antmaze-l-d	100k (10%)	0.0	0.0	0.0	3.6±4.1	0.0	16.1±8.4	0.0	0.0	39.8±14.1
Antmaze-l-p	100k (10%)	0.0	0.0	0.0	3.5±4.1	0.0	9.7±8.5	0.0	0.0	47.3±13.1

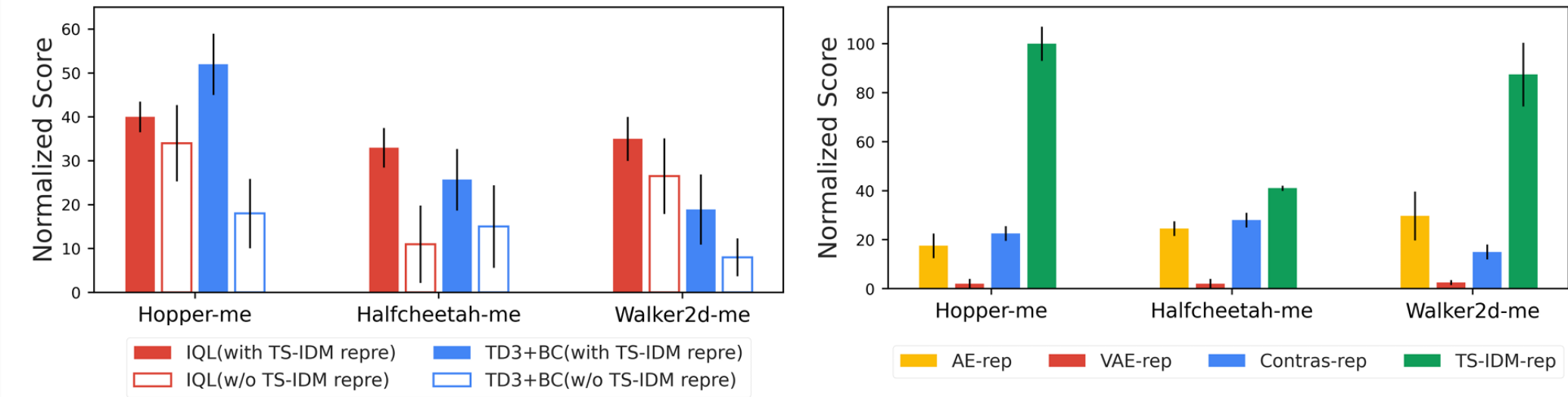


Figure 4: **Left:** The performance of IQL and TD3+BC on 10k datasets with or without using the representation from TS-IDM. **Right:** Performance of TELS with different representation models on 10k datasets, error bars indicate the normalized scores over 5 random seeds.

Table 2: Ablation results on the design components of TS-IDM.

	$\phi/\psi + h_{inv}$	$+ h_{fwd}, h_{rvs} \uparrow$	$+ \ell_{ode} \uparrow$	$+ \ell_{T-sym} \uparrow$
Hopper-me	17.2 ± 7.0	35.5 ± 7.3	61.4 ± 23.7	100.9 ± 6.8
Halfcheetah-me	29.7 ± 3.6	31.3 ± 1.1	31.2 ± 1.2	40.7 ± 1.2
Walker2d-me	24.5 ± 10.1	33.6 ± 9.2	58.5 ± 18.1	87.4 ± 13.3

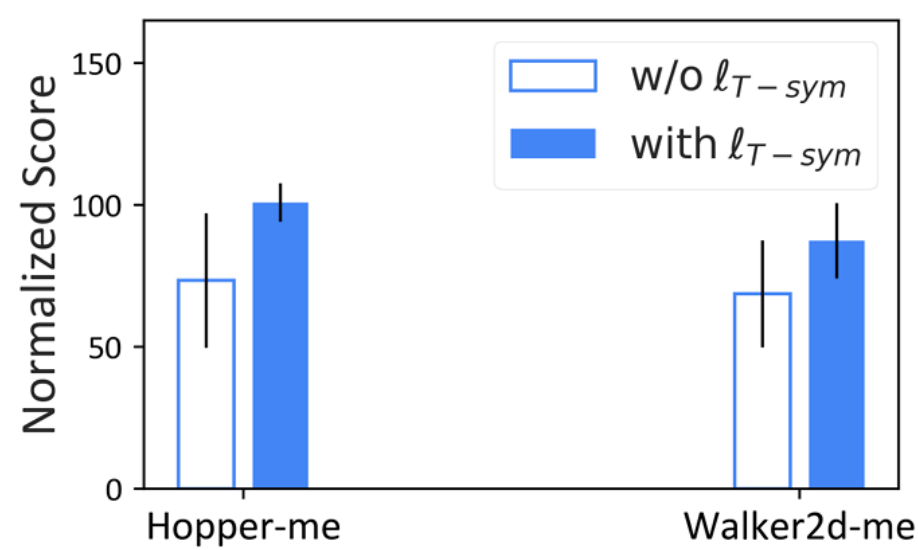


Figure 5: Impact of ℓ_{T-sym} on policy optimization

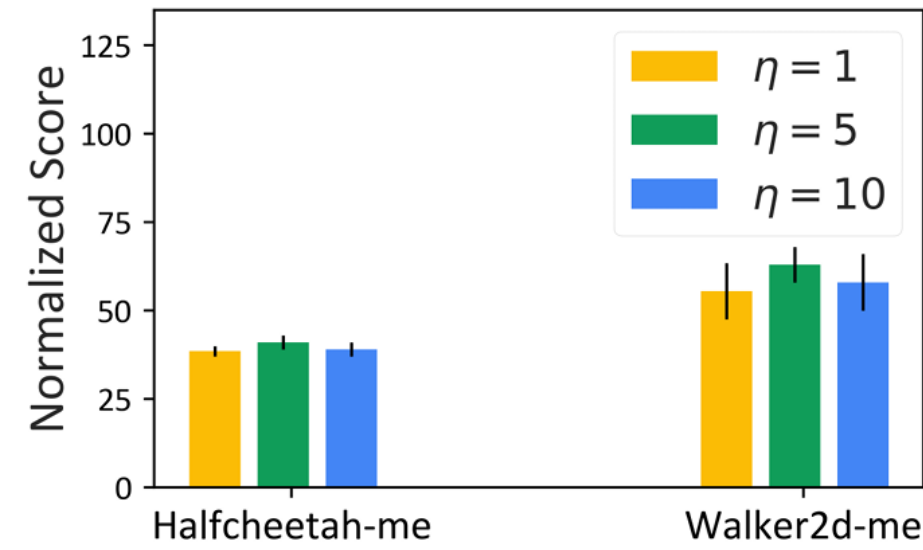


Figure 6: Performance of TELS with different η

Out-of-Distribution Generalizability of TELS

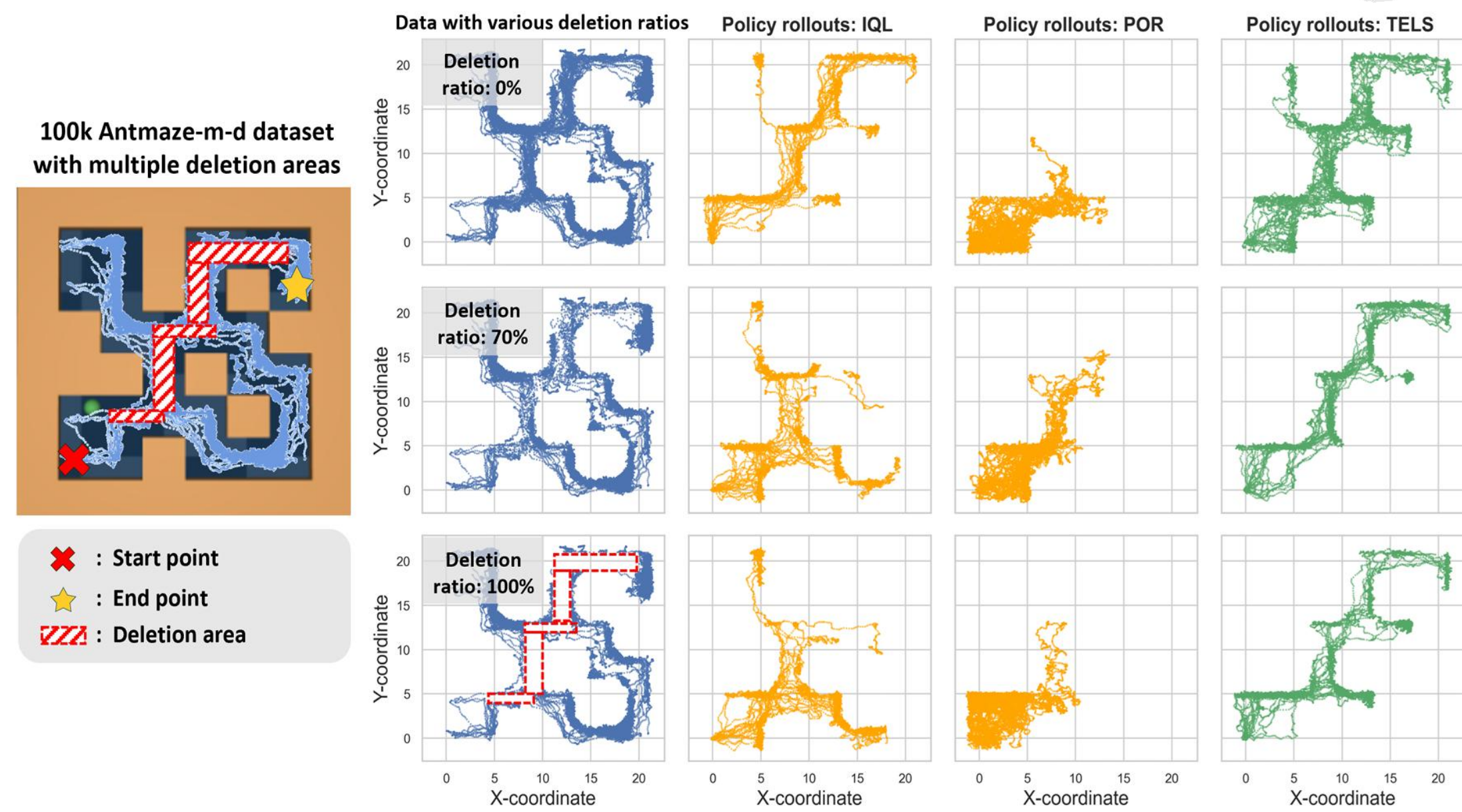
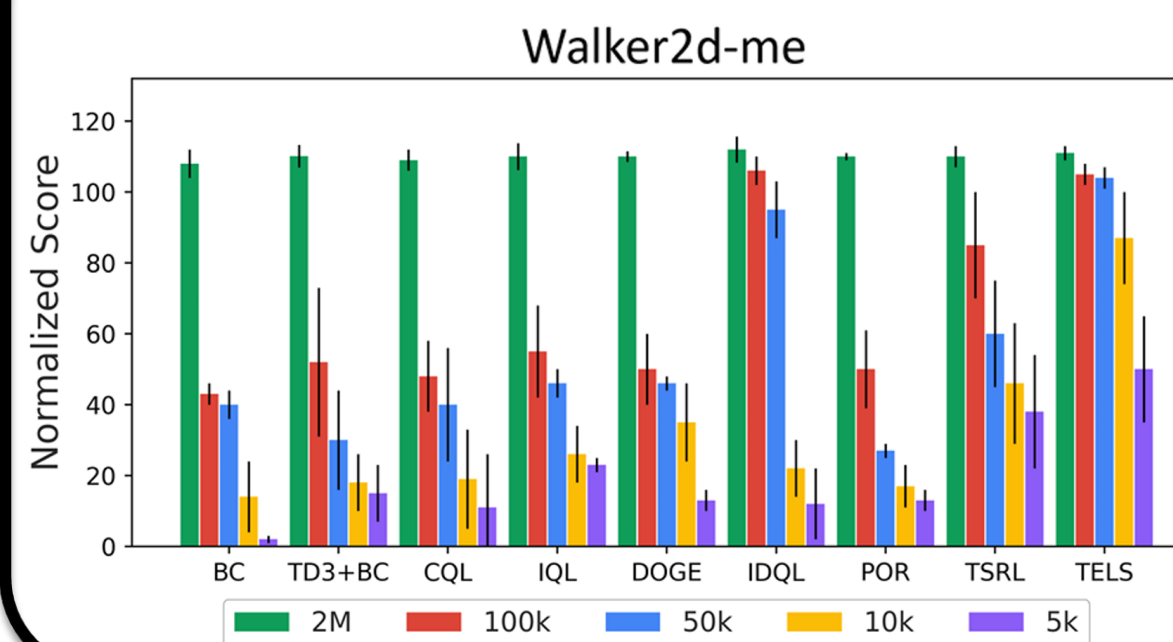


Figure 3: **Left:** Illustration of the 100k Antmaze-m-d task with multiple deletion areas, where the red cross denotes the start point, the yellow star denotes the goal locations, and the red shaded areas denote the data deletion regions. **Right:** Visualization of the training dataset and policy rollout trajectories generated by trained policies from various algorithms under varying deletion ratios.

- We randomly remove samples within 5 critical regions along the critical paths from the start to the goal locations.
- Only TELS** consistently learns optimal policy even with **70% and 100% deletion rates**.
- These highlight the OOD generalization capability of TELS in extremely challenging low-data regimes.

Offline RL under Various Data Size



Performance of offline RL methods and TELS on the D4RL MuJoCo Walker2d-medium-expert-v2 datasets when reducing the number of samples from 2M (full dataset) to 5k (0.5%).