

## A APPENDIX

### A.1 ADDITIONAL FORMULATION: STEERING AND ACCELERATION

We also derive an additional second-order kinematic formulation: steering and acceleration. This formulation is the second-order version of the velocity-heading formulation. Here, we assume acceleration  $a$  to be scalar and directionless, in contrast to Formulation 2, where we consider acceleration to be a vector with lateral and longitudinal components. Similarly to Formulation 2, we also use the linear approximation of  $\tan(\cdot)$  in order to derive approximated position distributions.

Following the Bicycle Model, the update for speed and heading at each timestep is:

$$\begin{bmatrix} s^{t+1} \\ \theta^{t+1} \end{bmatrix} = \begin{bmatrix} s^t + a \cdot \Delta t \\ \theta^t + \frac{s \cdot \tan(\delta)}{L} \cdot \Delta t \end{bmatrix}$$

Where  $L$  is the length of the agent. When we represent this process probabilistically as random Gaussian variables, the formulation becomes:

$$\begin{aligned} \mathcal{N}_{s^{t+1}} &= (\mu_s^t + \sigma_s^t \cdot \epsilon_s) + (\mu_a^t + \sigma_a^t \cdot \epsilon_a) \cdot \Delta t \\ \implies \mu_s^{t+1} &= \mu_s^t + \mu_a^t \cdot \Delta t, \\ \sigma_s^{t+1} &= \sigma_s^t + \sigma_a^t \cdot \Delta t \\ \mathcal{N}_{\theta^{t+1}} &= (\mu_\theta^t + \sigma_\theta^t \cdot \epsilon_\theta) + \frac{1}{L} \cdot T(\mu_\delta^t + \sigma_\delta^t \cdot \epsilon_\delta) \cdot (\mu_s^t + \sigma_s^t \cdot \epsilon_s) \cdot \Delta t \\ &= (\mu_\theta^t + \sigma_\theta^t \cdot \epsilon_\theta) + \frac{1}{L} \cdot \left( \tan(\mu_\delta^t) + \frac{1}{\cos^2(\mu_\delta^t)} \cdot (\sigma_\delta^t \cdot \epsilon_\delta) \right) \cdot (\mu_s^t + \sigma_s^t \cdot \epsilon_s) \cdot \Delta t \\ \implies \mu_\theta^{t+1} &= \mu_\theta^t + \frac{1}{L} \cdot (\mu_s^t \cdot \tan(\mu_\delta^t)) \cdot \Delta t, \\ \sigma_\theta^{t+1} &= \sigma_\theta^t + \frac{1}{L} \cdot \left( \mu_s^t \cdot \sigma_\delta^t \cdot \frac{1}{\cos^2(\mu_\delta^t)} + \sigma_s^t \cdot \tan(\mu_\delta^t) + \frac{1}{\sqrt{2}} \cdot \left( \sigma_s^t \cdot \sigma_\delta^t \cdot \frac{1}{\cos^2(\mu_\delta^t)} \right) \right) \cdot \Delta t \end{aligned}$$

With the terms characterizing  $\mathcal{N}_s^{t+1}$  and  $\mathcal{N}_\theta^{t+1}$ , this formulation then degenerates into Formulation 3 in Section 4.2.3.

## A.2 ADDITIONAL RESULTS BY CLASS

In the paper, we present results on vehicles since we use kinematic models based on vehicles as priors. Here, we present the full results per-class for each experiment in Tables 4, 5, 6, and 7. The results reported in the paper are starred (\*), which are re-iterated below for full context.

Table 4: Per-class results for performance on 100% of the Waymo Dataset.

Class	Method	( $\Delta\%$ ) mAP $\uparrow$	( $\Delta\%$ ) minADE $\downarrow$	( $\Delta\%$ ) minFDE $\downarrow$	( $\Delta\%$ ) MissRate $\downarrow$
Average	Baseline	0	0	0	0
	Ours + Formulation 1	<b>1.7492</b>	-0.4455	<b>-2.3882</b>	<b>-1.1098</b>
	Ours + Formulation 2	-2.2235	0.1337	-1.0881	-0.7009
	Ours + Formulation 3	-0.9487	<b>-0.4604</b>	-0.7560	1.2850
	Ours + Formulation 1 + Interpolation	-0.5336	1.4553	-1.6534	0.0000
Vehicle*	Baseline	0	0	0	0
	Ours + Formulation 1	<b>2.376</b>	<b>-0.3444</b>	<b>-0.9102</b>	-0.3853
	Ours + Formulation 2	-0.2066	1.1069	0.1138	-0.1651
	Ours + Formulation 3	-1.7045	0.246	1.0838	3.1921
	Ours + Formulation 1 + Interpolation	0.9039	2.2260	-0.7365	<b>-0.4403</b>
Pedestrian	Baseline	0	<b>0</b>	0	0
	Ours + Formulation 1	<b>0.4657</b>	0.2343	<b>-0.7773</b>	-2.7692
	Ours + Formulation 2	-1.2806	0.885	-0.2065	<b>-3.8974</b>
	Ours + Formulation 3	0.0873	0.9630	0.6072	-1.9487
	Ours + Formulation 1 + Interpolation	0.3492	4.1385	1.4574	0.8205
Cyclist	Baseline	0	0	0	0
	Ours + Formulation 1	<b>2.4911</b>	-0.8991	<b>-4.5646</b>	<b>-1.0656</b>
	Ours + Formulation 2	-6.0854	-1.1786	-2.6418	0.1279
	Ours + Formulation 3	-1.2100	<b>-1.8348</b>	-3.1439	1.0230
	Ours + Formulation 1 + Interpolation	-3.5943	-0.5832	-3.9884	0.0000

Table 5: Per-class results for performance on 1% of the Waymo Dataset.

Class	Method	( $\Delta\%$ ) mAP $\uparrow$	( $\Delta\%$ ) minADE $\downarrow$	( $\Delta\%$ ) minFDE $\downarrow$	( $\Delta\%$ ) MissRate $\downarrow$
Average	Baseline	0	0	0	0
	Ours + Formulation 1	-1.6418	<b>-6.3763</b>	<b>-14.9755</b>	<b>-5.173</b>
	Ours + Formulation 2	<b>0.7463</b>	-0.7756	-14.5275	-2.9916
	Ours + Formulation 3	-6.1692	16.0354	-11.2498	-0.2493
	Ours + Formulation 1 + Interpolation	-1.2438	-2.1014	-12.2530	-0.0312
Vehicle*	Baseline	0	0	0	0
	Ours + Formulation 1	<b>11.8444</b>	<b>-12.5280</b>	-27.1767	<b>-8.3266</b>
	Ours + Formulation 2	6.7767	-5.8432	<b>-27.7645</b>	-7.2791
	Ours + Formulation 3	-5.3035	30.6413	-20.5494	-0.8327
	Ours + Formulation 1 + Interpolation	4.1839	-7.3498	-23.8817	-4.8080
Pedestrian	Baseline	<b>0</b>	0	0	0
	Ours + Formulation 1	-7.8373	<b>-1.1325</b>	-1.2123	3.2820
	Ours + Formulation 2	-11.1275	1.7743	-0.9999	6.2960
	Ours + Formulation 3	-3.2902	-0.6795	<b>-3.0440</b>	0.1340
	Ours + Formulation 1 + Interpolation	-8.0961	3.7750	1.3716	11.2525
Cyclist	Baseline	0	0	0	0
	Ours + Formulation 1	-5.5283	<b>-1.6251</b>	<b>-4.6731</b>	<b>-5.3754</b>
	Ours + Formulation 2	<b>14.2506</b>	3.8549	-2.8120	-2.4949
	Ours + Formulation 3	-11.9165	6.4701	-2.5166	0.1588
	Ours + Formulation 1 + Interpolation	4.4840	1.3908	-2.6320	0.2041

Table 6: Per-class performance degradation results with perturbed evaluation for models trained on 100% of the Waymo Dataset.

Class	Method	( $\Delta\%$ ) mAP $\uparrow$	( $\Delta\%$ ) minADE $\downarrow$	( $\Delta\%$ ) minFDE $\downarrow$	( $\Delta\%$ ) MissRate $\downarrow$
Average	Baseline	<b>-2.5793</b>	2.5097	0.7066	1.6939
	Ours + Formulation 1	-2.9138	1.5662	<b>0.3547</b>	<b>-0.6497</b>
	Ours + Formulation 2	-3.2141	<b>1.4385</b>	0.9715	1.8824
	Ours + Formulation 3	-3.5917	1.7306	0.7760	0.6344
Vehicle*	Baseline	-4.9587	4.7965	1.6527	3.5223
	Ours + Formulation 1	<b>-4.9445</b>	<b>3.5542</b>	<b>1.4322</b>	<b>2.7072</b>
	Ours + Formulation 2	-3.9596	2.4693	1.2800	2.7012
	Ours + Formulation 3	-4.7294	3.3984	1.3447	2.5600
Pedestrian	Baseline	<b>-1.1932</b>	0.8329	0.0243	3.3846
	Ours + Formulation 1	-1.5933	<b>-0.2077</b>	<b>-0.7344</b>	<b>-1.0549</b>
	Ours + Formulation 2	-3.066	0.4902	0.1582	2.7748
	Ours + Formulation 3	-2.0646	0.4383	0.4587	2.7197
Cyclist	Baseline	<b>-0.9253</b>	1.0207	0.1255	-0.5541
	Ours + Formulation 1	-1.6667	<b>0.4537</b>	<b>-0.1614</b>	<b>-3.0590</b>
	Ours + Formulation 2	-2.3494	0.8361	1.0608	0.9366
	Ours + Formulation 3	-3.8905	0.6560	0.3594	-1.7300

Table 7: Per-class performance degradation results with perturbed evaluation for models trained on 1% of the Waymo Dataset.

Class	Method	( $\Delta\%$ ) mAP $\uparrow$	( $\Delta\%$ ) minADE $\downarrow$	( $\Delta\%$ ) minFDE $\downarrow$	( $\Delta\%$ ) MissRate $\downarrow$
Average	Baseline	-3.4328	0.5411	0.1187	<b>0.1246</b>
	Ours + Formulation 1	-6.2721	<b>0.1349</b>	<b>-0.1171</b>	0.6901
	Ours + Formulation 2	<b>-3.3086</b>	0.7635	0.3181	1.574
	Ours + Formulation 3	-4.0297	0.3420	0.8672	2.2805
Vehicle	Baseline	-6.0695	1.1266	<b>0.2207</b>	0.9132
	Ours + Formulation 1	<b>-4.4784</b>	1.0241	0.8180	1.2892
	Ours + Formulation 2	-5.6843	1.8236	1.3033	1.5933
	Ours + Formulation 3	-5.6005	<b>-0.3117</b>	0.4686	<b>0.4605</b>
Pedestrian	Baseline	<b>-0.2957</b>	<b>-1.1136</b>	<b>-0.9734</b>	<b>-2.6122</b>
	Ours + Formulation 1	-4.4124	-0.3627	-0.8599	-0.0649
	Ours + Formulation 2	-3.0782	-0.2411	-0.3396	2.8355
	Ours + Formulation 3	-4.8930	-0.3421	-0.2008	2.9431
Cyclist	Baseline	-5.8354	0.5518	0.4041	<b>0.4083</b>
	Ours + Formulation 1	-11.3134	<b>-0.5455</b>	<b>-0.7410</b>	0.5273
	Ours + Formulation 2	-1.3978	0.1019	-0.3669	1.1398
	Ours + Formulation 3	<b>-0.6276</b>	1.4908	1.6792	3.5779

## A.3 EXPERIMENT HYPERPARAMETERS

Table 8: **Model Architecture Hyperparameters**

Component	Hyperparameter	Value
Encoder	# Hidden Features	128
	# Attention Layers	2
	# Attention Heads	2
	Local Attention	True
Decoder	Hidden Features	128
	# Decoder Layers	2
	# Attention Heads	2
	# Hidden Map Features	64