ABSTRACT

When presented with Out-of-Distribution (OOD) examples, deep neural networks yield confident, incorrect predictions. Detecting OOD examples is challenging, and the potential risks are high. In this paper, we propose to detect OOD examples by identifying inconsistencies between activity patterns and class predicted. We find that characterizing activity patterns by feature correlations and identifying anomalies in pairwise feature correlation values can yield high OOD detection rates. We identify anomalies in the pairwise feature correlations by simply comparing each pairwise correlation value with its respective range observed over the training data. Unlike many approaches, this can be used with any pre-trained softmax classifier and does not require access to OOD data for fine-tuning hyperparameters, nor does it require OOD access for inferring parameters. The method is applicable across a variety of architectures and vision datasets and generally performs better than or equal to state-of-the-art OOD detection methods, including those that do assume access to OOD examples.\footnote{The code for this work is available at \url{https://github.com/zeroshot-ood/ood-detection}}

1 INTRODUCTION

Even when deep neural networks (DNNs) achieve impressive accuracy on challenging tasks, they do not always visibly falter on misclassified examples: in those cases they can often make predictions that are both very confident and completely incorrect. Yet, predictive uncertainty is essential in real-world contexts tolerating minimal error margins such as autonomous vehicle control and medical, financial and legal fields.

In this work, we focus on flagging test examples that do not contain any of the classes modeled in the train distribution. Such examples are often referred to as being out-of-distribution (OOD), and while their existence has been well-known for some time, the challenges of identifying them and a baseline method to do so in a variety of tasks such as image classification, text classification, and speech recognition were presented by Hendrycks and Gimpel (2017). Recently, Nalisnick et al. (2019a) identified a similar problem with generative models: they demonstrate that flow-based models, VAEs, and PixelCNNs cannot distinguish images of common objects such as dogs, trucks, and horses (i.e. CIFAR-10) from those of house numbers (i.e. SVHN), assigning a higher likelihood to the latter when the model is trained on the former. They report similar findings across several other pairs of popular image datasets.

While we might expect neural networks to respond differently to OOD examples than to in-distribution (ID) examples, exactly where and how to find these differences in activity patterns is not at all clear. Hendrycks and Gimpel (2017) and others (Nguyen et al., 2015; Yu et al., 2011) showed that looking at the maximal softmax value is insufficient. In Section 2, we describe some other recent approaches to this problem. In this work, we find that characterizing activity patterns by feature correlations—computed with an extension of Gram matrices that we introduce—lets us quantify anomalies to allow state-of-the-art (SOTA) detection rates on OOD examples.

Intuition. We identify out-of-distribution examples by jointly considering the class assigned at the output layer and the activity patterns in the intermediate layers. For example, if an image is predicted to be a dog, yet the intermediate activity patterns are somehow atypical of those seen by...
the network for other dog images during training, then that is a strong indicator of an OOD example. This effectively allows us to detect incongruence between the prediction made by the network and the path by which it arrived at that prediction.

**Strengths.** Unlike those previous works that assume access to OOD examples and train an auxiliary classifier for identifying anomalous activity patterns, our method finds differences in activity patterns without requiring access to any OOD examples, and it works across architectures. We hope this will also help further our understanding of how neural networks respond differently to OOD examples in general, not just how a particular network responds to examples coming from a particular distribution.

**Contributions.** This work includes the following contributions:

1. We extend Gram matrices to compute effective feature correlations.
2. Using the $p^{th}$-order Gram matrices, we present a new technique for computing class-conditional anomalies in activity patterns.
3. We evaluate this technique on OOD detection, testing on
   - competitive architectures: DenseNet, ResNet;
   - benchmark OOD datasets including: CIFAR-10, CIFAR-100, SVHN, TinyImageNet, LSUN and iSUN.
4. Zero-shot: crucially, our method does not require access to OOD samples for tuning hyperparameters or for training auxiliary models.
5. Nevertheless, we report results which are generally better than or equal to the state-of-the-art method that does require access to OOD examples.

## 2 RELATED WORK

Previous work which aims to improve OOD detection can be roughly grouped by several themes:

**Bayesian Neural Networks.** A nice early Bayesian approach (Gal and Ghahramani, 2016) estimates predictive uncertainty by using an ensemble of sub-networks instantiated by applying dropout at test time. As opposed to implicitly learning a distribution over the predictions by learning a distribution over the weights, Chen et al. (2019) and Malinin and Gales (2018) explicitly parameterize a Dirichlet distribution over the output class distributions using DNNs in order to obtain a better estimate of predictive uncertainty; the main differences between these methods is that Chen et al. (2019) use ELBO, which only requires the in-distribution dataset for training whereas Malinin and Gales (2018) use a contrastive loss which requires access to (optionally synthetic) OOD examples.

Using any pre-trained softmax deep neural network with OOD examples. Lee et al. (2018b)—to the best of our knowledge, the current SOTA technique by a significant margin—compute the Mahalanobis distance between the test sample’s feature representations and the class-conditional gaussian distribution at each layer; they then represent each sample as a vector of the Mahalanobis distances, and finally train a logistic regression detector on these representations to identify OOD examples. Another technique in this category is ODIN (Liang et al., 2018): they use a mix of temperature scaling at the softmax layer and input perturbations to achieve better results. In fact, both Lee et al. (2018b) and Liang et al. (2018) add small input perturbations to achieve better results; the former do so to increase the confidence score, while the latter do so to increase the softmax score. Recently, Quintanilha et al. (2019) achieve results comparable to that of Lee et al. (2018b) by training a logistic regression detector that looks at the means and standard deviations of various channels activations. Unlike the previous two techniques, Quintanilha et al. (2019) achieves comparable results even without the use of input perturbations, which allows it to be applicable to non-continuous domains. Our work, too, does not involve input perturbations.

All of these techniques depend on OOD examples for fine-tuning hyperparameters (Liang et al., 2018) or for training auxiliary OOD classifiers (Lee et al., 2018b; Quintanilha et al., 2019). Furthermore, these classifiers neither transfer between one non-training distribution and another, nor do they transfer between networks, so separate classifiers must be trained for each (In-Distribution, OOD, Architecture) triplet. In many real-world applications, this is infeasible: we cannot assume advance access to all possible OOD distributions. Our work does not require access to OOD samples.
Alternative Training Strategies. [Lee et al. (2018a)] jointly train a classifier, a generator and an adversarial discriminator such that the classifier produces a more uniform distribution on the boundary examples generated by the generator; they use OOD examples to fine-tune hyperparameters. [DeVries and Taylor (2018)] train neural networks with a multi-task loss for jointly learning to classify and estimate confidence. [Shalev et al. (2018)] use multiple semantic dense representations as the target instead of sparse one-hot vectors and use a cosine-similarity based measure for detecting OODs. Building on the idea proposed by [Lee et al. (2018a)], [Hendrycks et al. (2019)] propose an Outlier Exposure (OE) technique. They regularize a softmax classifier to predict uniform distribution on (any) OOD distribution and show the resulting model can identify examples from unseen OOD distributions; this differs significantly from previous works which used the same OOD distributions for both training and testing. Unlike other methods, they retain the architecture of the classifier and introduce just one additional hyperparameter—the regularization rate—and also demonstrate that their model is quite robust to the choice of OOD examples chosen for the regularization. However, while the OE method is able to generalize across different non-training distributions, it does not achieve the SOTA rates of [Lee et al. (2018b)] on most cases.

Generative Models. [Ren et al. (2019)] hypothesize that stylistic factors might impact the likelihood assignment and propose to detect OOD examples by computing a likelihood ratio which depends on the semantic factors that remain after the dominant stylistic factors are cancelled out. On the other hand, [Nalisnick et al. (2019b)] argue that samples generated by a generative model reside in the typical set, which might not necessarily coincide with areas of high density. They demonstrate empirically that OOD examples can be identified by checking if an input resides in the typical set of the generative model. Unlike the standard experimental setting, they aim to identify distributional shift, which predicts if a batch of examples are OOD.

3 Extending Gram Matrices for Out-of-Distribution Detection

Overview In light of the above considerations, we are interested in proposing a method that does not require access to any OOD examples, that does not introduce hyperparameters that need tuning, and that works across architectures. Gram matrices can be used to compute pairwise feature correlations, and are often used in DNNs to encode stylistic attributes like textures and patterns [Gatys et al. (2016)]. We extend these matrices as will be described below, and then use them to compute class-conditional bounds of pairwise feature correlations at multiple layers of the network. Starting with a pre-trained network, we compute these bounds over only the training set, and can then use them to effectively discriminate between in-distribution samples and out-of-distribution samples at test time. Unlike other SOTA algorithms, we do not need to “look” at any out-of-distribution samples to tune any parameters; the only tuning required is that of a normalizing factor, which we compute using a randomly-selected validation partition of the (in-distribution) test set.

Notation If the considered deep convolutional network has $L$ layers and the $t^{th}$ layer has $n_l$ channels, we consider feature co-occurrences between the $\sum_{1 < i < L}^{n_l \times (n_l + 1)}$ pairs of feature-maps. (Note that by “layer” we refer to any set of values obtained immediately after applying convolution or activation functions.) We use the following notation:

\[
F_l(D) \quad \text{The feature map at the } l^{th} \text{ layer for input image } D; \text{ when referring to an arbitrary image } D, \text{ we just write } F_l. \text{ It can be stored in a matrix of dimensions } n_l \times p_l, \text{ where } p_l \text{ is the number of channels at the } l^{th} \text{ layer and } p_l, \text{ the number of pixels per channel, is the height times the width of the feature map.}
\]

\[
D_{\text{Train}}(D) \quad \text{The predicted class for input image } D
\]

\[
\text{Va} \quad \text{The set of all validation examples. 10\% of the examples not used in training are randomly chosen as validation examples.}
\]

\[
\text{Te} \quad \text{The set of all test examples, disjoint as usual from the training and validation sets. We assume that only the test set may contain out-of-distribution examples.}
\]

Gram Matrices and Higher order Gram Matrices We compute pairwise feature correlations between channels of the $l^{th}$ layer using the Gram matrix:

\[
G_l = F_l F_l^T
\]
where $F_l$ is an $n_l \times p_l$ matrix as defined above.

In order to compute feature correlations with more prominent activations of the feature maps, we define a higher-order gram matrix, which we write $G_l^p$, to be a matrix computed identically to the regular Gram matrix, but where, instead of using a raw channel activation $a$, we use $a^p$, the $p^{th}$ power of each activation. $G_l^p$ is therefore computed using $F_l^p$, where the power of $F_l$ is computed element-wise; in an effort to retain uniform scale across all orders of Gram matrices for a given layer, we compute the (element-wise) $p$-th root. The $p$-th order gram matrix is thus computed as:

$$G_l^p = \left( F_l^p F_l^{p\top} \right)^{\frac{1}{p}}$$  \hfill (2)

We show in Section 5 that higher $p$ values help significantly in improving the OOD detectability. In our experiments, we limit the value of $p$ to 10, as exponents beyond 10 are not worth the extra computation that is needed to avoid overflow errors.

The flattened upper (or lower) triangular matrix along with the diagonal entries is denoted as $\bar{G}_l^p$. The set of all orders of gram matrices (in our case \{1, …, 10\}) are 6.5 and 6.3 on train and test partitions.

**Computing Layerwise Deviations**  Given the class-specific minimum and maximum values of the $N_S$ feature correlations, we can compute the deviation of the test sample from the images seen at train time with respect to each of the layers. In order to account for the scale of values, we compute the deviation as the percentage change with respect to the maximum or minimum values of feature correlations for any image $D$. The preprocessing involves computing the class-specific minimum and maximum values of the features over all training examples $D$. We keep track of the minimum and maximum values of the $N_S$ correlations for all the classes in 4-D arrays $Mins$ and $Maxs$, each of the order $C \times L \times |P| \times \max_{1 \leq l \leq L} \frac{n_l(n_l+1)}{2}$.

Since each layer has different number of channels, the 4-th dimension has been large enough to accommodate the layer with the highest number of channels.

**Algorithm 1**  Compute the minimum and maximum values of feature co-occurrences for each class, layer and order

**Input:**
- $C$: Number of output classes
- $L$: Number of Layers in entire network
- $P$: Set of all orders of Gram Matrix to consider
- $Train$: The train data

**Output:**
- $Mins$, $Maxs$

1: $Mins[C][L][P]\left[ \max_{1 \leq l \leq L} \frac{n_l(n_l+1)}{2} \right] \leftarrow \infty$  \hfill $\triangleright$ Stores the Mins for each class, layer and order
2: $Maxs[C][L][P]\left[ \max_{1 \leq l \leq L} \frac{n_l(n_l+1)}{2} \right] \leftarrow -\infty$  \hfill $\triangleright$ Stores the Maxs for each class, layer and order
3: for $c \in [1, C]$ do
4:     $Train_c = \{D | D \in Train \ s.t. f(D) = c\}$  \hfill $\triangleright$ All the training examples predicted as $c$
5:     for $D \in Train_c$ do
6:         for $l$ in $[1, L]$ do
7:                     for $p$ in $P$ do
8:                         $stat = \bar{G}_l^p(D)$  \hfill $\triangleright$ The flattened upper triangular matrix
9:                             for $i$ in $[1, \frac{n_l(n_l+1)}{2}]$ do
10:                                $Mins[c][l][p][i] = \min(Mins[c][l][p][i], stat[i])$
11:                                $Maxs[c][l][p][i] = \max(Maxs[c][l][p][i], stat[i])$
12: return $Mins$, $Maxs$
We benchmark our algorithm with the works listed in Table 1 using the following metrics: we found that computing the anomalies this way yields differences of less than 0.5%.

In order to reduce computational time, we can in fact compute deviations based on row-wise sums rather than individual elements. This would mean that the variable \( \text{stat} \), defined in line 8 of Algorithm 1, would now contain row-wise sums of \( G^p_l \) instead of the flattened upper triangular matrix; the inner loop of Eq. 4 would loop over \( n_l \) elements instead of \( \frac{1}{2} n_l (n_l + 1) \) elements while also reducing the storage required for Mins and Maxs. In practise, we found that computing the anomalies this way yields differences of less than 0.5%, and usually imperceptible, so the results described in the next section were computed in this way.

### 4 Experiments - Detecting OOD

In this section, we demonstrate the effectiveness of the proposed metric using competitive deep convolutional neural network architectures such as DenseNet and ResNet on various computer vision benchmark datasets such as: CIFAR-10, CIFAR-100, SVHN, TinyImageNet, LSUN and iSUN.

For fair comparison and to aid reproducibility, we use the pretrained ResNet [He et al. 2016] and DenseNet [Huang et al. 2017] models open-sourced by Lee et al. [2018b], i.e. ResNet34 and DenseNet3 models trained on CIFAR-10, CIFAR-100 and SVHN datasets. For each of these models, we considered the corresponding test partitions as the in-distribution (positive) examples. For CIFAR-10 and CIFAR-100, we considered the out-of-distribution datasets used by Lee et al. [2018b]: TinyImageNet, LSUN and SVHN. Additionally, we also considered the iSUN dataset. For ResNet and DenseNet models trained on SVHN, we used considered CIFAR-10 dataset as the third OOD dataset. Details on these datasets are available in Appendix B.

We benchmark our algorithm with the works listed in Table 1 using the following metrics:

1. **TNR@95TPR** is the probability that an OOD (negative) example is correctly identified when the true positive rate (TPR) is as high as 95%. TPR can be computed as \( TPR = \frac{TP}{TP + FN} \), where TP and FN denote True Positive and False Negative respectively.
Can work with pre-trained Net? | Can work without access to OOD validation examples?
---|---
DPN (Malinin and Gales, 2018) | ✗ | ✓
Semantic (Shalev et al., 2018) | ✗ | ✓
Variational Dirichlet (Chen et al., 2019) | ✗ | ✓
Mahalanobis (Lee et al., 2018b) | ✓ | ✗
ODIN (Liang et al., 2018) | ✓ | ✗
OE (Hendrycks et al., 2019) | ✗ | ✗
Baseline (Hendrycks and Gimpel, 2017) | ✓ | ✓
Ours | ✓ | ✓

Table 1: List of closely related methods

2. **Detection Accuracy** measures the maximum possible classification accuracy over all possible thresholds in discriminating between in-distribution and out-of-distribution examples. For those methods which assign a higher-score to the in-distribution examples, it can be calculated as \( \max_\tau \{0.5P_{\text{in}}(f(x) \geq \tau) + 0.5P_{\text{out}}(f(x) < \tau)\} \); for those methods which assign a lower score to in-distribution examples, it can be calculated as \( \max_\tau \{0.5P_{\text{in}}(f(x) \leq \tau) + 0.5P_{\text{out}}(f(x) > \tau)\} \).

3. **AUROC** is the measure of the area under the plot of TPR vs FPR. For example, for those methods which assign a higher score to the in-distribution examples, this measures the probability that an OOD example is assigned a lower score than an in-distribution example.

**Experimental setup:** We use a pre-trained network to extract class-specific minimum and maximum correlation values for all pairs of features across all orders of gram matrices. Subsequently, the total deviation is computed for each example following Eq. 5. Since the total deviation values depend on the randomly selected validation examples, we repeat the experiment 10 times to get a reliable estimate of the performance. The OOD detection performance for several combinations of model architecture, in-distribution dataset and out-of-distribution dataset are shown in Table 2. The results for Outlier Exposure (OE) are available in Table 3, some more results for OE and the results for DPN, Variational Dirichlet and Semantic are available in Appendix C.1 and Appendix C.2 respectively.

The results of Table 2 show that at a glance, over a total of 24 combinations of model architecture/in-distribution-dataset/out-of-distribution-datasets, the proposed method outperforms the previous competing methods in 15 of them, is on par in 6 of them, and gives second highest results on 3 of them.

Furthermore, it does so without requiring access to samples from the OOD dataset. If the hyperparameters and/or parameters of Mahalanobis and ODIN algorithms are fine-tuned using FGSM adversarial examples instead of the real OOD examples, their performance decreases. We also observe that our performance is similar for both architectures.

We also performed experiments with fully-connected networks by using three different MLP architectures trained on MNIST; Fashion-MNIST (Xiao et al., 2017) and KMNIST (Clanuwat et al., 2018) were considered as the out-of-distribution datasets (Results are provided in Appendix C.3).

```
<table>
<thead>
<tr>
<th>In-dist</th>
<th>Mean TNR @ TPR95</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>OE (Base)</td>
</tr>
<tr>
<td>CIFAR-10</td>
<td>65.1</td>
</tr>
<tr>
<td>CIFAR-100</td>
<td>37.3</td>
</tr>
<tr>
<td>SVHN</td>
<td>93.7</td>
</tr>
</tbody>
</table>
```

Table 3: Comparison of results with OE (Hendrycks et al., 2019). Since OE uses a different model from ours, we also report the corresponding baseline accuracy. We extract the mean TNR @ TPR95 for our technique by considering both ResNet and DenseNet models. Some more results are available in Appendix C.1.

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3 This is based on the TNR at TPR 95% value; AUROC and Detection Accuracy results are comparable.
Table 2: Comparison of OOD Detection Performance for all combinations of model architecture and training dataset are shown. The hyperparameters of ODIN and the hyperparameters and parameters of Mahalanobis are tuned using a random sample of the OOD dataset.

5 DISCUSSION AND CONCLUSION

Beyond explicit OOD detection, this line of work may ultimately help better interpret neural networks’ responses to OOD examples. With this goal in mind, and at the same time to clarify the internal mechanism of our method, we perform tests to address the following two questions:

1. Which representations are most useful? In order to examine the role of the depth at which we compute $G$ in detecting OODs, we construct detectors which make use of correlations derived from just one residual or dense block at a time: however, all orders of gram matrices are considered. Representative results are shown in Figure[1]. For all combinations of model/in-distribution/out-of-distribution-dataset, we find that the lower level representations are much more informative in discriminating between in-distribution and out-of-distribution datasets. However, the difference in detective power depends on the in-distribution dataset considered: for example, the difference in detective power between higher-level representations and lower-level representations is bigger for Cifar-10 than for Cifar-100.

2. Which orders of gram matrices are most useful? In order to understand which orders of gram matrices are most helpful in detecting OODs, we construct detectors which make use of only one order of gram matrix at a time: however, correlations are derived from the representations of all residual and dense blocks. Representative results are shown in Figure[2]. For all combinations of model/in-distribution/out-of-distribution-dataset, we find that the higher order gram matrices are much more informative in discriminating between in-distribution and out-of-distribution datasets. Ignoring the variations at orders greater than 4, we find that the TNR @ 95TPR increases with higher orders and finally saturates.

Conclusion. Out-of-distribution detection is a challenging and important problem. We have proposed and reported on a relatively simple OOD detection method based on pairwise feature correlations that gives new state of the art detection results without requiring access to anything other than the training data itself.
Figure 1: Significance of depth: The TNR@TPR95 is computed by constructing detectors which make use of all the gram matrices but consider only one residual or dense block at a time. ResNet32 has 4 residual blocks and DenseNet3 has 3 dense blocks.

Figure 2: The importance of higher order gram matrices: The TNR@TPR95 is computed by constructing detectors which make use of only one of the gram matrices but consider all layers.

REFERENCES


A Schematic Diagram

![Schematic Diagram](image)

Figure 3: The Schematic Diagram demonstrating the proposed algorithm

B Description of OOD Datasets

The following includes the description of the out-of-distribution datasets:

1. **TinyImaginet**, a subset of ImageNet [Russakovsky et al., 2015] images, contains 10,000 test images from 200 different classes. Each image is downsized to size 32 x 32 and all 10,000 images are used, as given in the opensourced version by Liang et al. [2018].

2. **LSUN**, the Large-scale Scene UNderstanding dataset [Yu et al., 2015] has 10,000 test images from 10 different scenes. Each image is downsized to size 32 x 32 and all 10,000 images are used, as given in the opensourced version by Liang et al. [2018].

3. **iSUN**, a subset of SUN images [Xiao et al., 2010], consists of 8925 images. Each image is downsized to size 32 x 32 and used; the downsized version of the dataset has been opensourced by Liang et al. [2018].

4. **SVHN**, the Street View House Numbers dataset [Netzer et al., 2011], involves recognizing digits 0-9 in natural scene images. The test partition consisting of 26,032 images is used.
C Few more OOD results

C.1 Comparing with OE

<table>
<thead>
<tr>
<th>In-distribution</th>
<th>OOD</th>
<th>OE (Base)</th>
<th>OE Ours (Base)</th>
<th>Ours</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIFAR-10</td>
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<td>85.6</td>
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<td></td>
<td>Rademacher</td>
<td>52.4</td>
<td><strong>99.5</strong></td>
<td>48.3</td>
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<td>Blob</td>
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<td><strong>99.4</strong></td>
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<td>Texture</td>
<td>57.2</td>
<td><strong>87.8</strong></td>
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<td>SVHN</td>
<td>71.2</td>
<td>95.2</td>
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<td>LSUN</td>
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<td>CIFAR-100</td>
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<td>87.9</td>
<td>18.2</td>
</tr>
<tr>
<td></td>
<td>Rademacher</td>
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<td>15.6</td>
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<td></td>
<td>Blob</td>
<td>62.0</td>
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<tr>
<td></td>
<td>Texture</td>
<td>28.5</td>
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</tr>
<tr>
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<td>SVHN</td>
<td>30.7</td>
<td>57.1</td>
<td>23.5</td>
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<td>18.2</td>
</tr>
<tr>
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<td>Gaussian</td>
<td>94.6</td>
<td><strong>100.</strong></td>
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<td></td>
<td>Bernoulli</td>
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<td>Texture</td>
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<td>LSUN</td>
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<td><strong>99.9</strong></td>
<td>75.7</td>
</tr>
</tbody>
</table>

Table 4: Comparison of Mean TNR@TPR95 values.

Following [Hendrycks et al. (2019)], we created the gaussian, rademacher, blob and bernoulli synthetic datasets. Their descriptions are as follows: Gaussian anomalies have each dimension i.i.d. sampled from an isotropic Gaussian distribution. Rademacher anomalies are images where each dimension is 1 or 1 with equal probability, so each dimension is sampled from a symmetric Rademacher distribution. Bernoulli images have each pixel sampled from a Bernoulli distribution if the input range is [0, 1]. Blobs data consist of algorithmically generated amorphous shapes with definite edges. Textures is a dataset of describable textural images (Cimpoi et al., 2014).

C.2 Comparing with DPN, VD and Semantic.

<table>
<thead>
<tr>
<th>OOD</th>
<th>Method</th>
<th>TNR  @ TPR95</th>
<th>AUROC</th>
<th>Detection Accuracy</th>
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</thead>
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<tr>
<td>LSUN</td>
<td>DPN</td>
<td>42.60</td>
<td>90.20</td>
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<td></td>
<td>VD</td>
<td>92.30</td>
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<tr>
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<td>ODIN</td>
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<td>Mahalanobis</td>
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<td></td>
<td>Ours</td>
<td><strong>99.85</strong></td>
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Table 5: We compare our method with DPN, VD and Semantic by reporting results where available.
## C.3 Results for Fully-connected Networks

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<th>Architecture</th>
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<th>AUROC</th>
<th>Detection Accuracy</th>
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Table 6: The method even works quite well with a fully-connected neural network trained on MNIST. The results are shown for 300-unit single layer MLP, 300-150 two-layer MLP and 300-150-50 MLP.