Generator Surgery for Compressed Sensing

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Code: https://github.com/nik-sm/generator-surgery

*We show that **cutting initial layers** of a **generative signal prior** at test time **improves image recovery** performance.*

Problem Statement

- We study **compressed sensing of images** under generative priors.
  - Goal: recover images from noisy undersampled measurements.
  - Unique recovery is possible under prior assumptions on image.
  - CS with Generative Models (CSGM): assume images are sampled from a generative model (e.g. GAN, VAE, etc).
- **Procedure**: project noisy measurements onto range of model.
  - Given measurement matrix A, noise η, generator $G(z)$:

$$y = Ax^* + \eta \qquad A_{ij} \sim \mathcal{N}(0, 1/m) \qquad \eta \sim \mathcal{N}(0, \sigma^2)$$

$$\hat{z} = \arg\min_z \|y - AG(z)\|_2^2 \qquad \hat{x} = G(\hat{z})$$
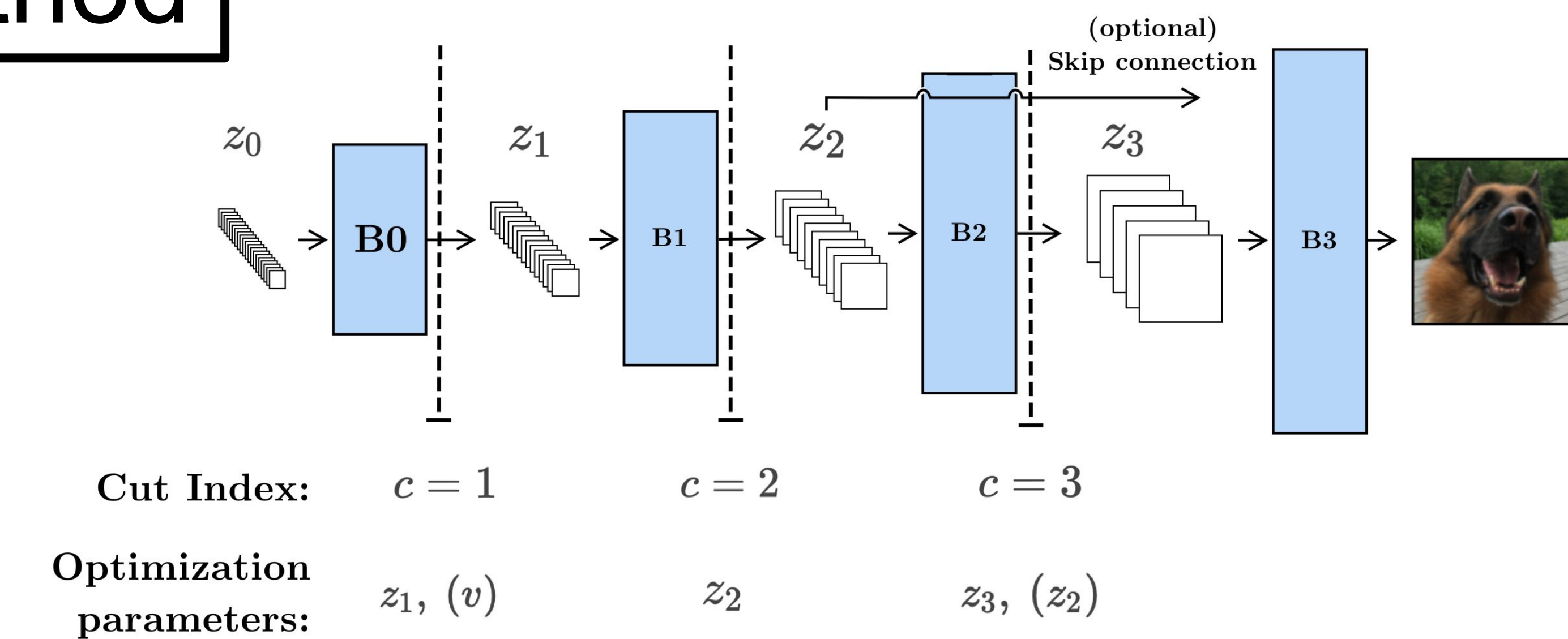
- **Intuition**: of all images consistent with measurements, use a generative model to decide which looks most natural.
- **Key Problem**: typical generative models cannot represent all natural images, inducing **representation error**.

$$\texttt{Rep-Err}(x^*) = \min_z \|x^* - G(z)\|_2^2$$

We introduce **Generator Surgery (GS)**, which mitigates representation error and improves CSGM recovery performance.

Method

Cut Index: $c = 1$ $\quad c = 2$ $\quad c = 3$

Optimization parameters: $z_1, (v)$ $\quad z_2$ $\quad z_3, (z_2)$
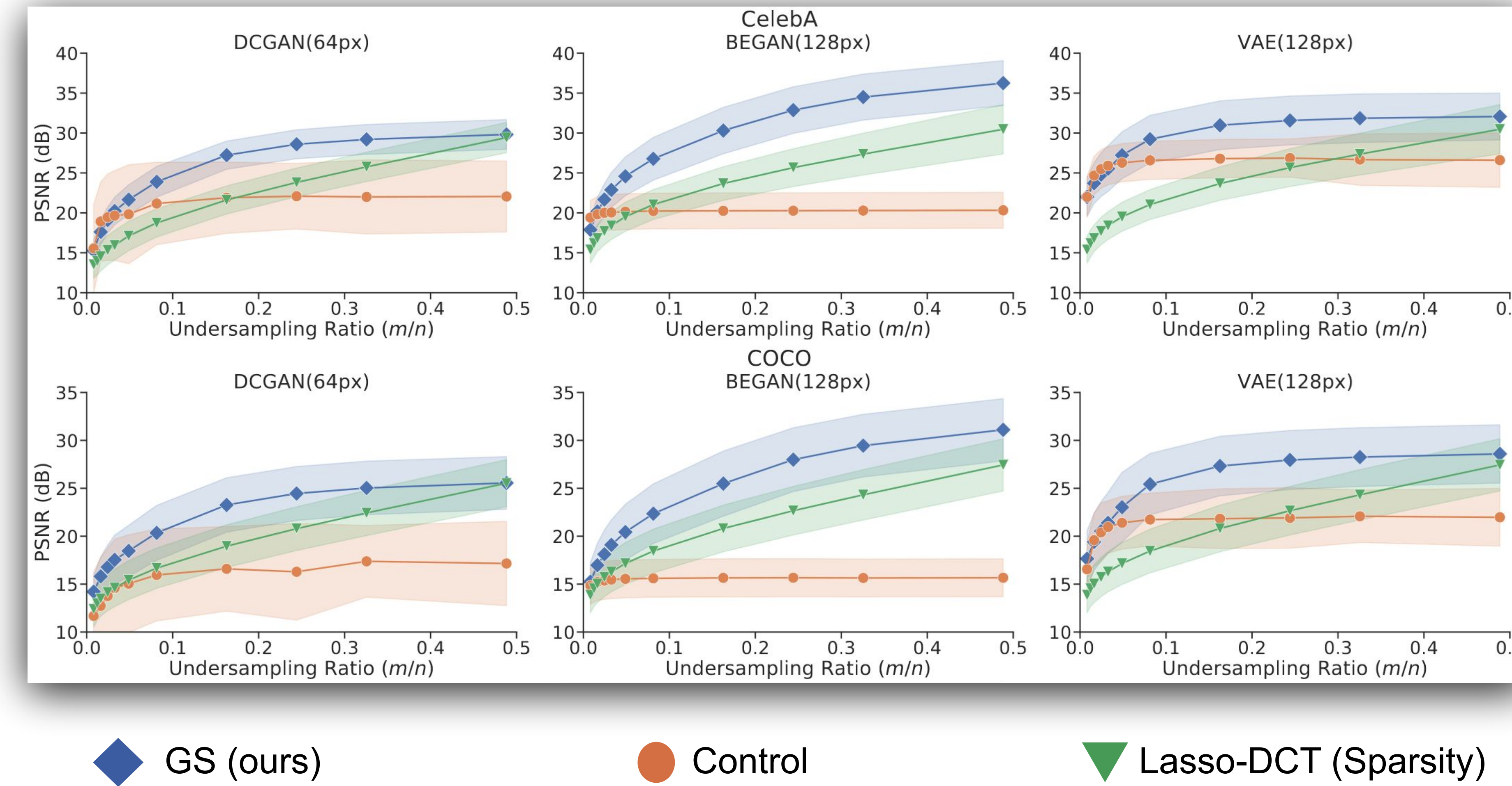
- Consider the generator as a composition of blocks. Each block may contain convolutions, upsample, batch norm, etc.

$$G_0(z_0) = [B_{d-1} \circ \ldots \circ B_1 \circ B_0](z_0)$$

- **Generator Surgery (GS)**: Remove the first c blocks of the generator. Recover images by projection onto range of the new model.
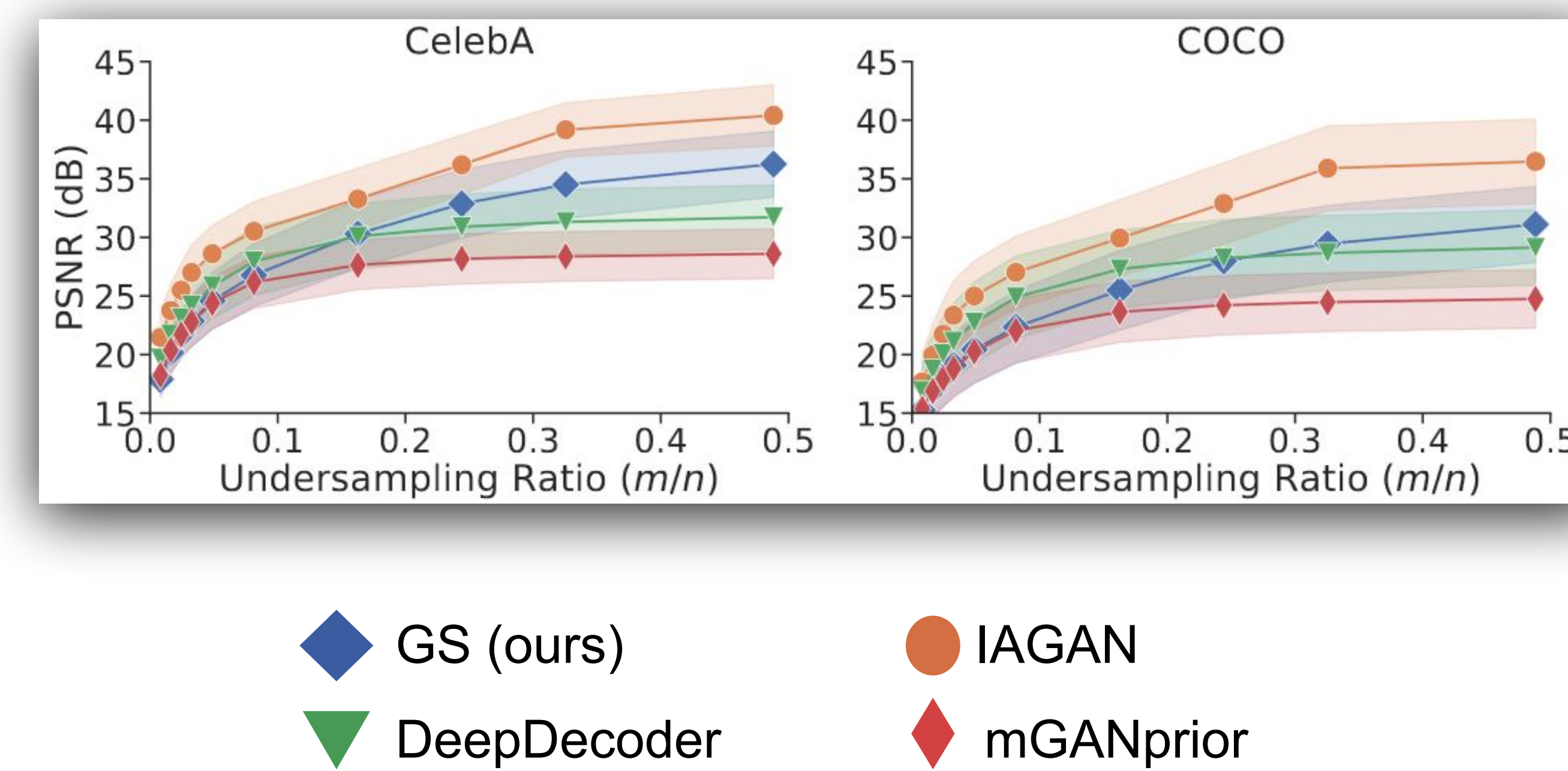
$$G_c(z_c) = [B_{d-1} \circ \ldots \circ B_c](z_c)$$

Main Results
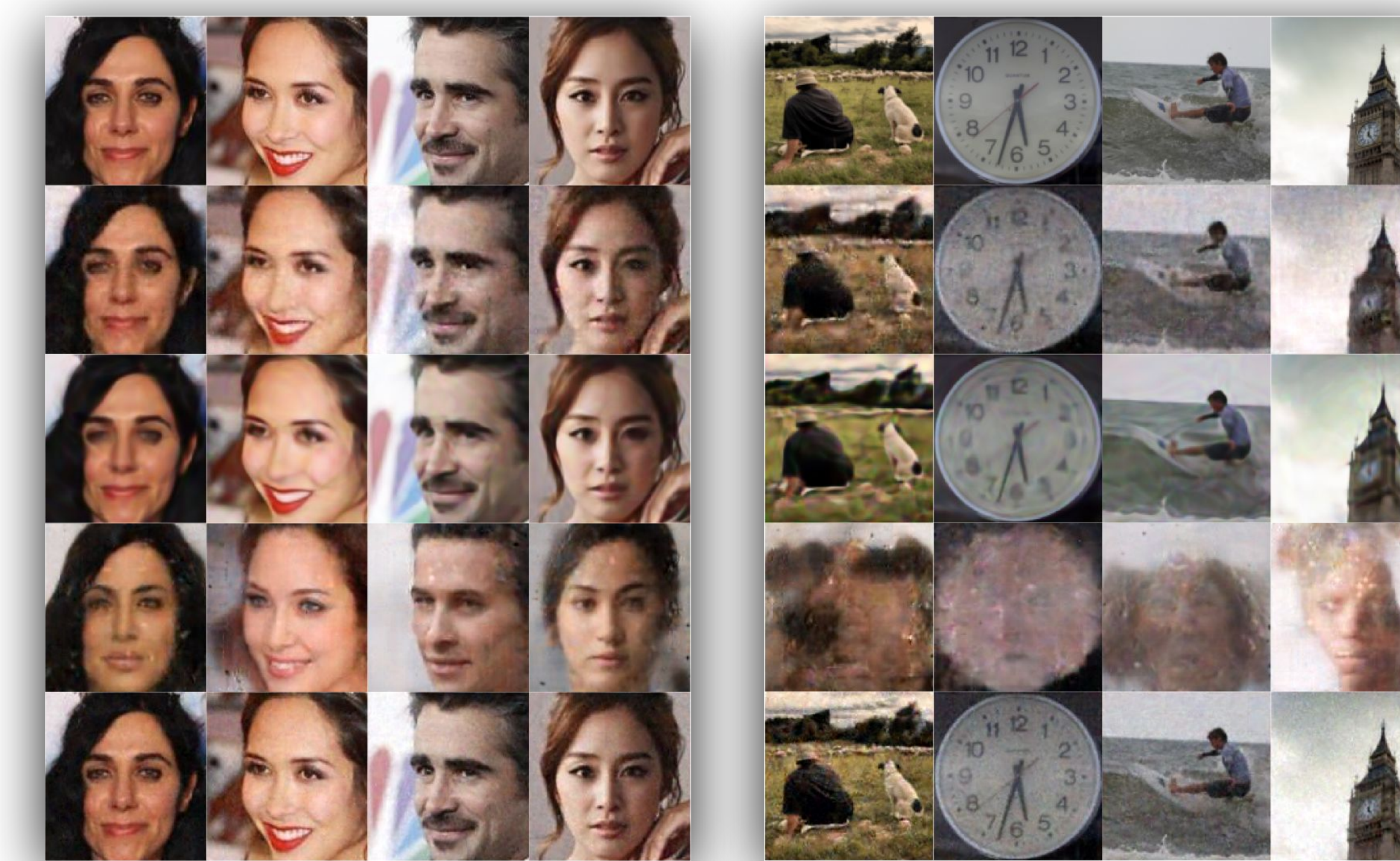
- CelebA (in-training-distribution): GS substantially improves recovery performance for all considered architectures (DCGAN, BEGAN, and VAE).

- COCO (out-of-training-distribution): performance increase over no surgery is similar to CelebA images.

- Baselines: IAGAN, mGANprior, Deep Decoder (with similar number of optimized parameters).

- GS generally beats mGANprior and performs similarly to DD. IAGAN is highly overparameterized.
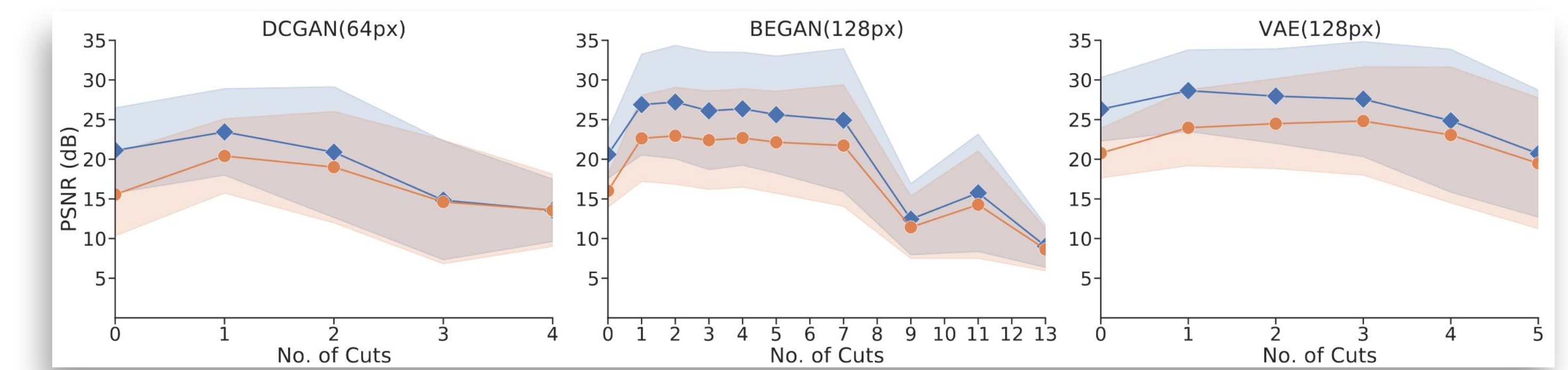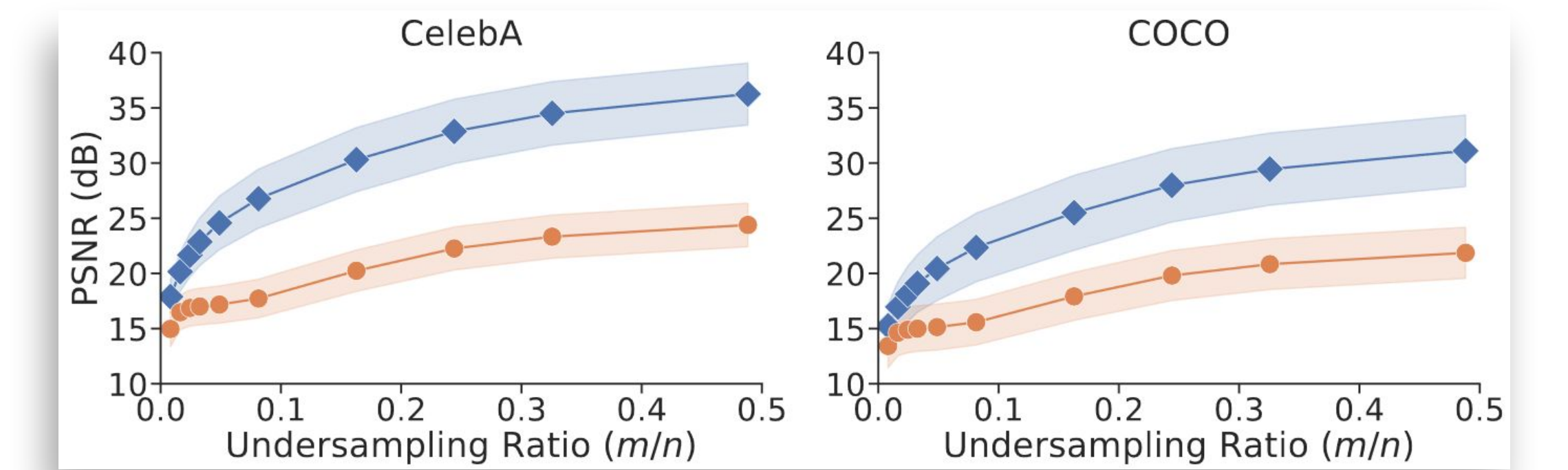
- Qualitative comparison of GS to other baseline methods.
- Note: all models trained on CelebA.

Supplemental Results
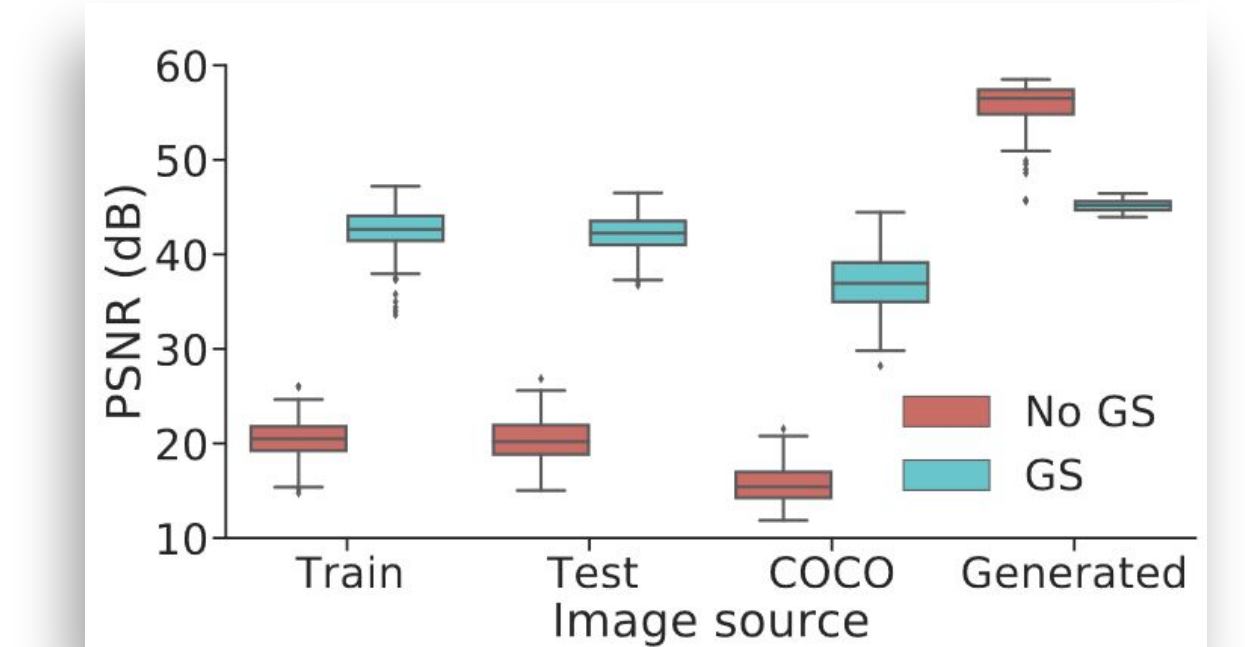
- We select the cut index c based on 100 CelebA validation images. Recovery quality is roughly a concave function of c.

- The generator's trained weights contribute to recovery quality: reinitializing weights after surgery is harmful to performance.

- Samples from the uncut generator have zero representation error. Gradient descent converges with negligible error in this case.

Discussion

- We find promising results using test-time modifications for image recovery.
- Surprisingly, GS allows models trained on CelebA to recover images from COCO with high quality.
- Our method trades the model's generative sampling procedure for increased recovery quality.