## Appendix

## A. Models Hyperparameter Details

We use SGD as optimizer, as it performs better in the continual learning setups [34], with a momentum value of 0.9. For the IIRC-CIFAR experiments, The learning rate starts with 1.0 and is decayed by a factor of 10 on plateau of the performance of the peri-task validation subset that corresponds to the current task. For the IIRC-ImageNet experiments, the learning rate starts with 0.5 in the case of iCaRL-CNN, iCaRL-norm and BiC, and 0.1 in the case of finetune, ER and LUCIR, and is decayed by a factor of 10 on plateau. The number of training epochs per task is 140 for IIRC-CIFAR and 100 for IIRCImageNet, with the first task always trained for double the number of epochs (due to its larger size). We set the batch size to 128 and the weight decay parameter to $1 e-5$. Moreover, We set the A-GEM memory batch size, which is used to calculate the reference gradient, to 128 . For LUCIR, the margin threshold $m$ is set to 0.5 , and $\lambda_{\text {base }}$ is set to 5 . All the hyperparameters were tuned based on the validation performance in experiments that include only the first four tasks.

During training, data augmentations are applied as follows: for IIRC-ImageNet, a random crop of size $(224 \times 224)$ is sampled from an image, a random horizontal flip is applied, then the pixels are normalized by a pre-calculated per-channel mean and standard deviation. In IIRC-CIFAR, a padding of size 4 is added to each size, then a random crop of size $(32 \times 32)$ is sampled, a random horizontal flip is applied, then the pixels are normalized.

We keep a fixed number of samples per class in the replay buffer ( 20 , except otherwise indicated). Hence, the capacity increases linearly as the model learns more classes. These samples are chosen randomly, except for iCaRL, LUCIR and BiC which use the herding approach. IIRC-CIFAR experiments are averaged over ten task configurations and the each version of IIRC-ImageNet is averaged over 5 task configurations (see 4 for details).

## B. Baselines Details

Following are three well known baselines that we used to evaluate in the IIRC setup along other baselines including finetune, joint and incremental joint, Vanilla Experience Re-play (ER), and Experience Replay with infinite buffer (ERinfinite).
iCaRL: iCaRL [38] was among the first deep learning methods to use exemplar rehearsal in order to alleviate the catastrophic forgetting in the class incremental learning setup. iCaRL model updates the model parameters using the distillation loss, where the outputs of the previous network are used as soft labels for the current network. Moreover, it uses the nearest-mean-of-exemplars classifications (NMC) strategy to classify test samples during inference. Since it is difficult to use NMC when the number of labels is variable (not a single label setup), we use the classification layer used during training during inference as well.

Unified learning via rebalancing (LUCIR): LUCIR [20] is a class incremental method that exploits three components to alleviate the catastrophic forgetting and reduce the negative effect of the imbalance between the old and new classes, since the number of samples in the replay buffer is much less than the current task samples. LUCIR uses the cosine normalization to get balanced magnitudes for classes seen so far. It also uses the less forget constraint, where the distillation loss is applied in the feature space instead of the output space, and a margin ranking loss to ensure interclass separation.

A-GEM: A-GEM [9] is an improved version of GEM that is a constrained optimization method in the Replay-based approach. GEM uses memory to constrain gradients so as to update the model parameters to not interfere with previous tasks. GEM is a very computationally expensive approach that is not applicable to the large-scale setup. Hence, Averaged GEM (A-GEM) provides an efficient version of GEM, where it only requires computing the gradient on a random subset of memory examples, and it does not need as well to solve any quadratic program but just an inner product. Since A-GEM is a very well known constrained optimization method that has reasonable guarantees in terms of average accuracy in comparison to GEM, we selected it as a candidate to evaluate its performance in our more realistic large scale setting.

## C. IIRC Dataset Statistics



Figure A.7. The distribution of the number of subclasses per superclass on IIRC-ImageNet.

|  | with duplicates |  | without duplicates |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| dataset | train | in-task validation | train | in-task validation | post-task validation | test |
| IIRC-CIFAR | 46,160 | 5,770 | 40,000 | 5,000 | 5,000 | 10,000 |
| IIRC-ImageNet-full | $1,215,123$ | 51,873 | $1,131,966$ | 48,802 | 51,095 | 49,900 |

Table 1. The number of samples for each split of the training set. with duplicates represents the number of samples including the dublicates between some superclasses and their subclasses (the samples that the model see two times with two different labels). This doesn't happen for the post-task validation set and test set as they are in the complete information setup

| dataset | superclasses | subclasses (under superclasses) | subclasses (with no superclasses) | total |
| :---: | :---: | :---: | :---: | :---: |
| IIRC-CIFAR | 15 | 77 | 23 | 115 |
| IIRC-ImageNet-full | 85 | 788 | 210 | 1083 |

Table 2. For each dataset, these are the number of superclasses, the number of subclasses that belong to these superclasses, the number of subclasses that don't have a superclass, and the total number of superclasses and subclasses

| dataset | superclass | num of subclasses | superclass size | subclass | subclass size |
| :---: | :---: | :---: | :---: | :---: | :---: |
| IIRC-CIFAR | vehicles | 8 | 1,280 | bus | 320 |
| IIRC-CIFAR | small mammals | 5 | 800 | squirrel | 320 |
| IIRC-CIFAR | - | - | - | mushroom | 400 |
| IIRC-ImageNet | bird | 58 | 3,762 | ostrich | 956 |
| IIRC-ImageNet | big cat | 6 | 2,868 | leopard | 956 |
| IIRC-ImageNet | keyboard instrument | 4 | 1,912 | grand piano | 956 |
| IIRC-ImageNet | - | - | - | wooden spoon | 1,196 |

Table 3. Several examples for classes and the number of samples they have in the training set. The subclass on the right is a subclass that belongs to the superclass on the left. The left side is blank for subclasses that have no superclasses.

## D. More Figures

## D.1. Main Paper Figures With The Standard Deviation Reported



Figure A.8. Average performance (Figures 3 and 4) with the standard deviation reported. It was removed from the original figures for more intelligibility


Figure A.9. Per task performance (Figure 5) with the standard deviation reported. It was removed from the original figures for more intelligibility

## D.2. Average Performance Over the Superclasses Only

Figures A. 10 and A. 11 show how much each model is able to predict correctly the superclasses it learned earlier for the samples that come in later tasks (which mostly belong to their subclasses). This is measured by calculating the precision weighted Jaccard similarity solely over the superclasses (only the model predictions that belong to superclasses are taken into account).


Figure A.10. The average performance of IIRC-ImageNet-lite if only the superclasses are taken into account for calculating this performance


Figure A.11. The average performance of IIRC-CIFAR if only the superclasses are taken into account for calculating this performance

## D.3. Average Precision Among Subclass Types

Figures A. 12 and A. 13 show how much each model is confused between the subclasses that belong to superclasses, which is measured by calculating the precision over only these subclasses (only the model predictions that belong to these subclasses are taken into account). As a baseline, the precision over subclasses which have no superclasses are also plotted. We can see that models collectively tend to be less precise with subclasses that have superclasses vs subclasses which have no superclasses, which is the intuitive result given that subclasses that belong to superclasses are more visually similar and easier to confuse, but also these figures help in highlighting which models are more prone to this kind of confusion between similar subclasses.


Figure A.12. The average precision of IIRC-ImageNet-lite over each type of subclasses, excluding other types of classes, to measure how much do the models confuse the subclasses as they encounter more related subclasses)


Figure A.13. The average precision of IIRC-CIFAR over each type of subclasses, excluding other types of classes, to measure how much do the models confuse the subclasses as they encounter more related subclasses)

## D.4. pw-Jaccard Similarity vs Jaccard Similarity



Figure A.14. Average performance on IIRC-CIFAR. (left) the precision-weighted Jaccard Similarity and (right) the Jaccard Similarity.


Figure A.15. Average performance on IIRC-CIFAR. (left) the precision-weighted Jaccard Similarity and (right) the Jaccard Similarity.

## D.5. Performance Per Task



Figure A.16. IIRC-ImageNet-full Performance on four middle tasks throughout the whole training process, to measure their catastrophic forgetting and backward transfer. Note that a degradation in performance is not necessarily caused by catastrophic forgetting, as a new subclass of a previously observed superclass might be introduced and the model would be penalized for not applying that label retroactively. Experiments are averaged on ten different task configurations with the mean reported.


Figure A.17. IIRC-CIFAR Performance on four middle tasks throughout the whole training process, to measure their catastrophic forgetting and backward transfer. Note that a degradation in performance is not necessarily caused by catastrophic forgetting, as a new subclass of a previously observed superclass might be introduced and the model would be penalized for not applying that label retroactively. Experiments are averaged on ten different task configurations with the mean reported.

## D.6. Confusion Matrix Over time



Figure A.18. Ground Truth confusion matrix after introducing tasks $0,1,5,10$ of IIRC-CIFAR respectively. The $y$-axis is the correct label (or one of the correct labels). The x -axis is the model predicted labels. Labels are arranged by their order of introduction. Only 25 labels are shown for better visibility.


Figure A.19. ER confusion matrix after introducing tasks $0,1,5,10$ of IIRC-CIFAR respectively. The $y$-axis is the correct label (or one of the correct labels). The x -axis is the model predicted labels. Labels are arranged by their order of introduction. Only 25 labels are shown for better visibility.


Figure A.20. iCaRL-CNN confusion matrix after introducing tasks $0,1,5,10$ of IIRC-CIFAR respectively. The y-axis is the correct label (or one of the correct labels). The x -axis is the model predicted labels. Labels are arranged by their order of introduction. Only 25 labels are shown for better visibility.


Figure A.21. iCaRL-norm confusion matrix after introducing tasks $0,1,5,10$ of IIRC-CIFAR respectively. The $y$-axis is the correct label (or one of the correct labels). The x -axis is the model predicted labels. Labels are arranged by their order of introduction. Only 25 labels are shown for better visibility.


Figure A.22. LUCIR confusion matrix after introducing tasks $0,1,5,10$ of IIRC-CIFAR respectively. The $y$-axis is the correct label (or one of the correct labels). The $x$-axis is the model predicted labels. Labels are arranged by their order of introduction. Only 25 labels are shown for better visibility.

## D.7. Full Resolution Confusion Matrix



Figure A.23. Confusion matrix (ground truth) after training on task 10 of IIRC-CIFAR. the y-axis is the correct label (or one of the correct labels), the x -axis is the model predicted labels, The classes are arranged by their order of introduction. Only 25 classes are shown for better visibility. The y -axis represents the true label (or one of the true labels), while the x -axis represents the model predictions.


Figure A.24. Confusion matrix (ER) after training on task 10 of IIRC-CIFAR. the $y$-axis is the correct label (or one of the correct labels), the x -axis is the model predicted labels, The classes are arranged by their order of introduction. Only 25 classes are shown for better visibility. The $y$-axis represents the true label (or one of the true labels), while the $x$-axis represents the model predictions.


Figure A.25. Confusion matrix (iCaRL-norm) after training on task 10 of IIRC-CIFAR. The x -axis is the model predicted labels, The classes are arranged by their order of introduction. Only 25 classes are shown for better visibility. The y-axis represents the true label (or one of the true labels), while the x -axis represents the model predictions.


Figure A.26. Confusion matrix (LUCIR) after training on task 10 of IIRC-CIFAR. The x -axis is the model predicted labels, The classes are arranged by their order of introduction. Only 25 classes are shown for better visibility. The $y$-axis represents the true label (or one of the true labels), while the x -axis represents the model predictions.

## E. Effect of Buffer



Figure A.27. ImageNet average performance using different buffer sizes, The number next to ER indicates the number of samples per class used for the replay buffer


Figure A.28. CIFAR average performance using different buffer sizes, The number next to ER indicates the number of samples per class used for the replay buffer

## F. Pseudo Codes

```
Algorithm 1: IncrementalTrain
    Require: tasks // A list of the classes to-be-introduced at each task
    trainSet, validSet inTask , validSet postTask , testSet \(\leftarrow\) LoadDatasets()
    model \(\leftarrow\) CreateModel()
    /* create an empty buffer */
    buffer \(\leftarrow\) CreateBuffer()
    for task in tasks do
        model \(\leftarrow\) TrainOnTask(model, buffer, trainingSet, validSet inTask )
        /* add randomly selected samples to buffer */
        buffer \(\leftarrow\) AddToBuffer (buffer, trainingSet)
        PostTaskEvaluate( model, validSet postTask , testSet)
    end
```

```
Algorithm 2: LoadDatasets
    input : rawData \(_{\text {train }} \quad / /\) The default single-label full dataset (train)
    input : rawData test \(_{\text {t }}\) // The default single-label full dataset (test)
    input : classHierarchy // A dictionary that maps each superclass to its constituent subclasses
    multilabeledData \(_{\text {train }} \leftarrow\) AddSuperclassLabels(rawData train , classHierarchy)
    multilabeledData \(_{\text {test }} \leftarrow\) AddSuperclassLabels \(\left(\right.\) rawData \(_{\text {test }}\), classHierarchy)
```



```
        SplitData(multilabeledData train )
    trainSet \(\leftarrow\) IncompleteInfoIncrementalDataset \(\left(\right.\) multilabeledData \(_{\text {train }}\) )
    validSet \(_{\text {inTask }} \leftarrow\) IncompleteInfoIncrementalDataset \(^{\left(\text {multilabeledData }_{\text {valid }_{\text {inTask }}} \text { ) }\right.}\)
    validSet \(_{\text {postTask }} \leftarrow\) CompleteInfoIncrementalTestDataset \(\left(\right.\) multilabeledData \(_{\text {valid }_{\text {postTask }}}\) )
    testSet \(\leftarrow\) CompleteInfoIncrementalTestDataset \(\left(\right.\) multilabeledData \(_{\text {test }}\) )
    output : trainSet // The incomplete information incremental learning training set
    output : validSet inTask \(^{\text {// The incomplete information incremental learning validation set (for in-task }}\)
                performance)
    output : validSet postTask \(^{\text {// The complete information incremental learning validation set (for post-task }}\)
                performance)
    output : testSet // The complete information incremental learning test set
```

```
Algorithm 3: IncompleteInfoIncrementalDataset
    input : multilabelData // A list of samples with each sample in the form of (image,
                (superclassLabel, subclassLabel)) or (image, (subclassLabel)))
    input : superclassToSubclass // a mapping that maps superclasses to their constituent subclasses
    input : tasks // The classes to-be-introduced at each task
    Require: subclasses // All refined subclasses (those who have a superclass as well as those who don't)
    output : a dataset object with the data changing along the tasks
    Initialization:
    classToDataIndices \(\leftarrow\) EmptyDictionary
    currentTaskId \(\leftarrow 0\)
    dataIndices \(_{\text {task }} \leftarrow[]\)
    for subclass in subclasses do
        /* get the indices of the samples which correspond to this subclass */
```



```
        if subclass has superclass then
            dataSubsetLength \(_{\text {superclass } \leftarrow 0.4 * \text { Length } \text { dataIndices }_{\text {subclass }} \text { ) }}\)
            dataSubsetLength subclass \(^{\left.\leftarrow 0.8 * \text { Length }^{\text {(dataIndices }}{ }_{\text {subclass }}\right) ~}\)
            dataIndices \(_{\text {subclass }} \leftarrow\) Shuffle(dataIndices subclass )
```




```
            classToDataIndices[subclass] \(\leftarrow\) dataIndices \(_{\text {subclass }}\)
```



```
        end
        else if subclass has no superclass then
            classToDataIndices[subclass] \(\leftarrow\) dataIndices subclass
        end
    end
    IncrementTask:
    currentTaskId \(\leftarrow\) currentTaskId +1
    dataIndices \(_{\text {task }} \leftarrow[]\)
    for class in tasks[currentTaskId] do
        dataIndices \(_{\text {task }} \leftarrow\) dataIndices \(_{\text {task }} \cup\) classToDataIndices[class] \(^{\text {a }}\)
    end
    GetItem:
    Require: classes \(_{\text {task }}\) // The classes present in the current task
    input : index // an index in the range of length of dataIndices \({ }_{\text {task }}\)
    image, labels \(\leftarrow\) multilabelData[dataIndices task [index]]
    label \(\leftarrow\) labels \(\cap\) classes \(_{\text {task }}\)
    output : image // The sample image
    output : label // The label corresponding to this image that exists in the current task
```

```
Algorithm 4: CompleteInfoIncrementalTestDataset
    input :multilabelData // A list of samples with each sample in the form of (image,
                (superclassLabel, subclassLabel)) or (image,(subclassLabel)))
    input : superclassToSubclass // a mapping that maps superclasses to their constituent subclasses
    input :tasks // The classes available at each task
    Require: subclasses // All refined subclasses (those who have a superclass as well as those who don't)
    output : a test dataset object which keeps collecting data along the tasks
    Initialization:
    classToDataIndices }\leftarrow\mathrm{ empty_dictionary
    classes observed}\leftarrow[
    dataIndices accessible }\leftarrow [
    for subclass in subclasses do
        /* get the indices of the samples which correspond to this subclass */
        dataIndices subclass}*\leftarrowGetSamplesIndices(multilabelData, subclass
        classToDataIndices[subclass]}\leftarrow\mp@subsup{\mathrm{ dataIndices subclass}}{}{\mathrm{ sin}
        if subclass has superclass then
            classToDataIndices[superclass]}\leftarrowclassToDataIndices[superclass]\cup
                classToDataIndices[subclass]
        end
    end
    LoadTask
    input : taskId // The index of the task to load
    dataIndices accessible }\leftarrow[
    classes}\mp@subsup{}{\mathrm{ observed }}{}\leftarrow\mp@subsup{\mathrm{ classes observed }}{\cup}{
    for class in tasks[taskId] do
        dataIndices accessible }\leftarrow\mp@subsup{\mathrm{ dataIndices }}{\mathrm{ accessible }}{}\cup\mp@subsup{\mathrm{ classToDataIndices[class]}}{}{\mathrm{ a/a}
    end
    LoadAllObservedData
    Require: classes observed // All classes observed till now in all previous tasks
    dataIndicesaccessible }\leftarrow [
    for class in classes observed do
        dataIndices accessible }\leftarrow\mathrm{ dataIndices accessible }\cup\mp@subsup{\mathrm{ classToDataIndices[class]}}{}{\mathrm{ and}
    end
    dataIndices accessible }\leftarrow\mathrm{ RemoveDuplicates(dataIndicesaccessible)
    GetItem
    Require: classes observed // All classes observed till now in all previous tasks
    input :index // an index in the range of task_data_indices
    image, labels }\leftarrow\mathrm{ multilabelData[dataIndicesaccessible [index]]
    labels }\leftarrow\mathrm{ labels }\cap\mp@subsup{\mathrm{ classes}}{\mathrm{ observed}}{
    output : image // The sample image
    output :labels // The labels corresponding to this image that exist in the classes observed
```


## G. IIRC Datasets Hierarchies

## G.1. IIRC-CIFAR Hierarchy

| superclass | subclasses |
| :---: | :---: |
| aquatic mammals | beaver, dolphin, otter, seal, whale |
| fish | aquarium fish, flatfish, ray, shark, trout |
| flowers | orchid, poppy, rose, sunflower, tulip |
| food containers | bottle, bowl, can, cup, plate |
| fruit and vegetables | apple, orange, pear, sweet pepper |
| household furniture | bed, chair, couch, table, wardrobe |
| insects | bee, beetle, butterfly, caterpillar, cockroach |
| large carnivores | leopard, lion, tiger, wolf |
| bear, camel, cattle, chimpanzee, elephant, kangaroo |  |
| medium sized mammals | fox, porcupine, possum, raccoon, skunk |
| people | baby, boy, girl, man, woman |
| reptiles | crocodile, dinosaur, lizard, snake, turtle |
| small mammals | hamster, mouse, rabbit, shrew, squirrel |
| trees | maple tree, oak tree, palm tree, pine tree, willow tree |
| vehicles | mushroom, clock, keyboard, lamp, telephone, television, bridge, castle, house, road, <br> skyscraper, cloud, forest, mountain, plain, sea, crab, lobster, snail, spider, worm, lawn <br> mower, rocket |
| - |  |

## G.2. IIRC-ImageNet Hierarchy

| superclass | subclasses |
| :---: | :---: |
| dog | dalmatian, basenji, pug, Leonberg, Newfoundland, Great Pyrenees, Mexican hairless, Brabancon griffon, Pembroke, Cardigan, Chihuahua, Japanese spaniel, Maltese dog, Pekinese, Shih-Tzu, toy terrier, papillon, Blenheim spaniel, Rhodesian ridgeback, boxer, bull mastiff, Great Dane, Saint Bernard, Eskimo dog, Tibetan mastiff, French bulldog, malamute, Siberian husky, Samoyed, Pomeranian, chow, keeshond, toy poodle, miniature poodle, standard poodle, Afghan hound, basset, beagle, bloodhound, bluetick, redbone, Ibizan hound, Norwegian elkhound, otterhound, Saluki, Scottish deerhound, Weimaraner, black-and-tan coonhound, Walker hound, English foxhound, borzoi, Irish wolfhound, Italian greyhound, whippet, Bedlington terrier, Border terrier, Kerry blue terrier, Irish terrier, Norfolk terrier, Norwich terrier, Yorkshire terrier, Airedale, cairn, Australian terrier, Dandie Dinmont, Boston bull, Scotch terrier, Tibetan terrier, silky terrier, soft-coated wheaten terrier, West Highland white terrier, Lhasa, Staffordshire bullterrier, American Staffordshire terrier, wire-haired fox terrier, Lakeland terrier, Sealyham terrier, German short-haired pointer, vizsla, kuvasz, schipperke, Doberman, miniature pinscher, affenpinscher, Brittany spaniel, clumber, cocker spaniel, Sussex spaniel, English springer, Welsh springer spaniel, Irish water spaniel, English setter, Irish setter, Gordon setter, flat-coated retriever, curly-coated retriever, golden retriever, Labrador retriever, Chesapeake Bay retriever, miniature schnauzer, giant schnauzer, standard schnauzer, Greater Swiss Mountain dog, Bernese mountain dog, Appenzeller, EntleBucher, briard, kelpie, komondor, Old English sheepdog, Shetland sheepdog, collie, Border collie, Bouvier des Flandres, Rottweiler, German shepherd, groenendael, malinois |
| bird | cock, hen, ostrich, bee eater, hornbill, hummingbird, jacamar, toucan, coucal, quail, partridge, peacock, black grouse, ptarmigan, ruffed grouse, prairie chicken, water ouzel, robin, bulbul, jay, magpie, chickadee, brambling, goldfinch, house finch, junco, indigo bunting, black swan, European gallinule, goose, drake, red-breasted merganser, pelican, albatross, king penguin, spoonbill, flamingo, limpkin, bustard, white stork, black stork, American coot, oystercatcher, red-backed sandpiper, redshank, dowitcher, ruddy turnstone, little blue heron, bittern, American egret, African grey, macaw, sulphur-crested cockatoo, lorikeet, vulture, kite, bald eagle, great grey owl |
| garment | suit, abaya, kimono, cardigan, feather boa, stole, jersey, sweatshirt, poncho, brassiere, jean, gown, military uniform, pajama, apron, academic gown, vestment, bow tie, Windsor tie, fur coat, lab coat, trench coat, hoopskirt, miniskirt, overskirt, sarong, cloak |
| beverage | espresso, red wine, cup, eggnog |
| aircraft | airship, balloon, airliner, warplane, wing, space shuttle |
| bear | brown bear, American black bear, ice bear, sloth bear |
| fox | red fox, kit fox, Arctic fox, grey fox |
| wolf | timber wolf, white wolf, red wolf, coyote |
| bag | backpack, mailbag, plastic bag, purse, sleeping bag |
| footwear | clog, cowboy boot, Loafer, running shoe, sandal |
| toiletry | hair spray, lotion, perfume, face powder, sunscreen, lipstick |
| box | carton, chest, crate, mailbox, pencil box, safe |
| rodent | hamster, porcupine, marmot, beaver, guinea pig, fox squirrel |
| bottle | beer bottle, pill bottle, pop bottle, water bottle, wine bottle, water jug, whiskey jug |
| fabric | velvet, wool, bib, dishrag, handkerchief, bath towel, paper towel |


| cup | beer glass, goblet, cocktail shaker, measuring cup, pitcher, beaker, coffee mug |
| :---: | :---: |
| fungus | coral fungus, gyromitra, stinkhorn, earthstar, hen-of-the-woods, bolete, agaric |
| musteline | weasel, mink, polecat, black-footed ferret, otter, skunk, badger |
| truck | fire engine, garbage truck, pickup, tow truck, trailer truck, moving van, police van, recreational vehicle, forklift, harvester, snowplow, tractor |
| headdress | crash helmet, football helmet, bearskin, bonnet, cowboy hat, sombrero, bathing cap, mortarboard, shower cap, pickelhaube |
| ball | baseball, basketball, croquet ball, golf ball, ping-pong ball, punching bag, rugby ball, soccer ball, tennis ball, volleyball |
| car | ambulance, beach wagon, cab, convertible, jeep, limousine, Model T, racer, sports car, minivan, grille, golfcart |
| measuring instrument | barometer, scale, odometer, rule, sundial, digital watch, hourglass, parking meter, stopwatch, analog clock, digital clock, wall clock |
| tool | hammer, plunger, screwdriver, shovel, cleaver, letter opener, can opener, corkscrew, hatchet, chain saw, plane, scabbard, power drill, carpenter's kit |
| watercraft | schooner, catamaran, trimaran, fireboat, gondola, canoe, yawl, lifeboat, speedboat, pirate, wreck, container ship, liner, aircraft carrier, submarine, amphibian, paddle |
| dish | Petri dish, mixing bowl, soup bowl, tray |
| bus | minibus, school bus, trolleybus |
| cart | horse cart, jinrikisha, oxcart |
| tracked vehicle | snowmobile, half track, tank |
| lamp | candle, spotlight, jack-o'-lantern, lampshade, table lamp |
| optical instrument | binoculars, projector, sunglasses, lens cap, loupe, Polaroid camera, reflex camera |
| gymnastic apparatus | balance beam, horizontal bar, parallel bars |
| swine | hog, wild boar, warthog |
| rabbits | hare, wood rabbit, Angora |
| echinoderm | starfish, sea urchin, sea cucumber |
| wild dog | dingo, dhole, African hunting dog |
| pouched mammal | wombat, wallaby, koala |
| aquatic mammal | dugong, grey whale, killer whale, sea lion |
| person | ballplayer, scuba diver, groom |
| mollusk | chiton, chambered nautilus, conch, snail, slug, sea slug |
| weapon | bow, projectile, cannon, missile, rifle, revolver, assault rifle, holster |
| bovid | bison, water buffalo, ram, ox, bighorn, ibex, hartebeest, impala, gazelle |
| salamander | European fire salamander, common newt, eft, spotted salamander, axolotl |
| frog | tree frog, tailed frog, bullfrog |
| big cat | leopard, snow leopard, jaguar, lion, tiger, cheetah |
| domestic cat | tabby, tiger cat, Persian cat, Siamese cat, Egyptian cat |
| cooking utensil | spatula, frying pan, wok, Crock Pot, Dutch oven, caldron, coffeepot, teapot |
| primate | Madagascar cat, indri, gibbon, siamang, orangutan, gorilla, chimpanzee, marmoset, capuchin, howler monkey, titi, spider monkey, squirrel monkey, guenon, patas, baboon, macaque, langur, colobus, proboscis monkey |
| fish | barracouta, electric ray, stingray, hammerhead, great white shark, tiger shark, sturgeon, gar, puffer, rock beauty, anemone fish, lionfish, eel, tench, goldfish, coho |
| lizard | banded gecko, common iguana, American chameleon, whiptail, agama, frilled lizard, alligator lizard, Gila monster, green lizard, African chameleon, Komodo dragon |


| turtle | mud turtle, terrapin, box turtle, loggerhead, leatherback turtle |
| :---: | :---: |
| spider | black and gold garden spider, barn spider, garden spider, black widow, tarantula, wolf spider, spider web |
| insect | ringlet, sulphur butterfly, lycaenid, cabbage butterfly, monarch, admiral, dragonfly, damselfly, lacewing, cicada, leafhopper, cockroach, mantis, walking stick, grasshopper, cricket, bee, ant, fly, tiger beetle, ladybug, ground beetle, long-horned beetle, leaf beetle, weevil, dung beetle, rhinoceros beetle |
| green groceries | acorn, hip, ear, fig, pineapple, banana, jackfruit, custard apple, pomegranate, strawberry, orange, lemon, Granny Smith, buckeye, rapeseed, corn, cucumber, artichoke, cardoon, mushroom, bell pepper, mashed potato, zucchini, spaghetti squash, acorn squash, butternut squash, broccoli, cauliflower, head cabbage |
| keyboard instrument | accordion, organ, grand piano, upright |
| percussion instrument | chime, drum, gong, maraca, marimba, steel drum |
| stringed instrument | banjo, acoustic guitar, electric guitar, cello, violin, harp |
| wind instrument | ocarina, harmonica, flute, panpipe, bassoon, oboe, sax, cornet, French horn, trombone |
| crustacean | isopod, crayfish, hermit crab, spiny lobster, American lobster, Dungeness crab, rock crab, fiddler crab, king crab |
| pen | ballpoint, fountain pen, quill |
| display | desktop computer, laptop, notebook, screen, television, monitor |
| electronic equipement | cassette player, CD player, modem, oscilloscope, tape player, iPod, printer, joystick, dial telephone, pay-phone, cellular telephone, mouse, hand-held computer |
| snake | sea snake, horned viper, boa constrictor, rock python, Indian cobra, green mamba, diamondback, sidewinder, thunder snake, ringneck snake, hognose snake, green snake, king snake, garter snake, water snake, vine snake, night snake |
| geological formation | cliff, geyser, lakeside, seashore, valley, promontory, alp, volcano, coral reef, sandbar |
| food | dough, guacamole, chocolate sauce, carbonara, French loaf, bagel, pretzel, plate, trifle, ice cream, ice lolly, pizza, potpie, burrito, consomme, hot pot, hotdog, cheeseburger, meat loaf |
| white home appliances | dishwasher, refrigerator, washer, stove |
| kitchen appliances | microwave, toaster, waffle iron, espresso maker |
| wheel | car wheel, paddlewheel, pinwheel, potter's wheel, reel, disk brake |
| seat | toilet seat, studio couch, park bench, barber chair, folding chair, rocking chair, throne |
| baby bed | bassinet, cradle, crib |
| cabinet | medicine chest, wardrobe, china cabinet, bookcase, chiffonier, file, entertainment center, plate rack |
| table | desk, pool table, dining table |
| bridges | steel arch bridge, suspension bridge, viaduct |
| fence | chainlink fence, picket fence, stone wall, worm fence |
| long structures | beacon, obelisk, totem pole |
| movable homes | mountain tent, mobile home, yurt |
| building | planetarium, barn, cinema, boathouse, palace, monastery, castle, dome, church, mosque, stupa, bell cote, thatch, tile roof, triumphal arch |
| body armor | chain mail, cuirass, bulletproof vest, breastplate |
| mask | mask, oxygen mask, gasmask, ski mask |
| curtain-screen | window shade, shower curtain, theater curtain |
| bike | moped, bicycle-built-for-two, tricycle, unicycle, mountain bike, motor scooter |


| train | passenger car, freight car, electric locomotive, bullet train, streetcar, steam locomotive |
| :---: | :---: |
| swimsuit | bikini, maillot, swimming trunks |
| socks mittens | Christmas stocking, mitten, sock |
| keyboard | computer keyboard, space bar, typewriter keyboard |
| - | African crocodile, American alligator, triceratops, trilobite, harvestman, scorpion, tick, centipede, tusker, echidna, platypus, jellyfish, sea anemone, brain coral, flatworm, nematode, crane, hyena, cougar, lynx, mongoose, meerkat, sorrel, zebra, hippopotamus, Arabian camel, llama, armadillo, three-toed sloth, Indian elephant, African elephant, lesser panda, giant panda, abacus, altar, apiary, ashcan, bakery, Band Aid, bannister, barbell, barbershop, barrel, barrow, bathtub, binder, birdhouse, bobsled, bolo tie, bookshop, bottlecap, brass, breakwater, broom, bucket, buckle, butcher shop, car mirror, carousel, cash machine, cassette, chain, cliff dwelling, coil, combination lock, confectionery, crutch, dam, diaper, dock, dogsled, doormat, drilling platform, drumstick, dumbbell, electric fan, envelope, fire screen, flagpole, fountain, four-poster, gas pump, go-kart, greenhouse, grocery store, guillotine, hair slide, hamper, hand blower, hard disc, home theater, honeycomb, hook, iron, jigsaw puzzle, knee pad, knot, ladle, lawn mower, library, lighter, loudspeaker, lumbermill, magnetic compass, manhole cover, matchstick, maypole, maze, megalith, microphone, milk can, mortar, mosquito net, mousetrap, muzzle, nail, neck brace, necklace, nipple, oil filter, packet, padlock, paintbrush, parachute, patio, pedestal, pencil sharpener, photocopier, pick, pier, piggy bank, pillow, plow, pole, pot, prayer rug, prison, puck, quilt, racket, radiator, radio, radio telescope, rain barrel, remote control, restaurant, rotisserie, rubber eraser, safety pin, saltshaker, scoreboard, screw, seat belt, sewing machine, shield, shoe shop, shoji, shopping basket, shopping cart, ski, slide rule, sliding door, slot, snorkel, soap dispenser, solar dish, space heater, spindle, stage, stethoscope, strainer, stretcher, sunglass, swab, swing, switch, syringe, teddy, thimble, thresher, tobacco shop, torch, toyshop, tripod, tub, turnstile, umbrella, vacuum, vase, vault, vending machine, wallet, washbasin, water tower, whistle, wig, window screen, wooden spoon, web site, comic book, crossword puzzle, street sign, traffic light, book jacket, menu, hay, bubble, daisy, yellow lady's slipper, toilet tissue |

## H. Results in Tables

| task | model |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ER | iCaRL-CNN | iCaRL-norm | LUCIR | AGEM | incremental joint | ER-infinite |
| task 0 | $0.72(0.039)$ | $0.71(0.042)$ | $0.75(0.037)$ | $0.74(0.036)$ | $0.72(0.032)$ | $0.71(0.032)$ | $0.72(0.033)$ |
| task 1 | $0.31(0.046)$ | $0.47(0.032)$ | $0.5(0.035)$ | $0.5(0.101)$ | $0.15(0.024)$ | $0.7(0.035)$ | $0.64(0.067)$ |
| task 2 | $0.23(0.054)$ | $0.36(0.017)$ | $0.39(0.024)$ | $0.35(0.178)$ | $0.1(0.023)$ | $0.67(0.029)$ | $0.63(0.029)$ |
| task 3 | $0.2(0.027)$ | $0.3(0.022)$ | $0.32(0.026)$ | $0.3(0.162)$ | $0.07(0.028)$ | $0.66(0.021)$ | $0.58(0.054)$ |
| task 4 | $0.17(0.024)$ | $0.26(0.022)$ | $0.27(0.024)$ | $0.27(0.148)$ | $0.05(0.01)$ | $0.66(0.02)$ | $0.55(0.04)$ |
| task 5 | $0.18(0.024)$ | $0.23(0.017)$ | $0.24(0.027)$ | $0.25(0.13)$ | $0.07(0.034)$ | $0.65(0.019)$ | $0.55(0.027)$ |
| task 6 | $0.19(0.03)$ | $0.21(0.022)$ | $0.21(0.028)$ | $0.23(0.133)$ | $0.07(0.031)$ | $0.64(0.02)$ | $0.52(0.02)$ |
| task 7 | $0.17(0.035)$ | $0.19(0.021)$ | $0.19(0.027)$ | $0.19(0.141)$ | $0.06(0.045)$ | $0.63(0.029)$ | $0.51(0.019)$ |
| task 8 | $0.16(0.02)$ | $0.18(0.02)$ | $0.18(0.026)$ | $0.18(0.135)$ | $0.04(0.014)$ | $0.63(0.022)$ | $0.49(0.026)$ |
| task 9 | $0.15(0.021)$ | $0.17(0.018)$ | $0.18(0.022)$ | $0.15(0.134)$ | $0.04(0.018)$ | $0.63(0.021)$ | $0.47(0.033)$ |
| task 10 | $0.17(0.035)$ | $0.16(0.017)$ | $0.17(0.017)$ | $0.14(0.118)$ | $0.06(0.039)$ | $0.62(0.019)$ | $0.45(0.036)$ |
| task 11 | $0.15(0.018)$ | $0.16(0.017)$ | $0.16(0.018)$ | $0.13(0.117)$ | $0.04(0.019)$ | $0.62(0.023)$ | $0.44(0.043)$ |
| task 12 | $0.15(0.03)$ | $0.16(0.017)$ | $0.16(0.015)$ | $0.12(0.109)$ | $0.05(0.033)$ | $0.62(0.022)$ | $0.43(0.035)$ |
| task 13 | $0.15(0.025)$ | $0.15(0.016)$ | $0.16(0.016)$ | $0.13(0.094)$ | $0.05(0.025)$ | $0.62(0.016)$ | $0.43(0.02)$ |
| task 14 | $0.14(0.017)$ | $0.15(0.011)$ | $0.15(0.014)$ | $0.11(0.096)$ | $0.04(0.022)$ | $0.62(0.014)$ | $0.42(0.028)$ |
| task 15 | $0.13(0.012)$ | $0.15(0.01)$ | $0.15(0.014)$ | $0.11(0.094)$ | $0.03(0.012)$ | $0.62(0.012)$ | $0.4(0.02)$ |
| task 16 | $0.14(0.011)$ | $0.15(0.013)$ | $0.15(0.015)$ | $0.09(0.094)$ | $0.03(0.005)$ | $0.63(0.013)$ | $0.39(0.037)$ |
| task 17 | $0.14(0.019)$ | $0.15(0.013)$ | $0.15(0.013)$ | $0.07(0.084)$ | $0.04(0.021)$ | $0.63(0.017)$ | $0.39(0.011)$ |
| task 18 | $0.14(0.012)$ | $0.15(0.012)$ | $0.15(0.012)$ | $0.06(0.081)$ | $0.03(0.014)$ | $0.63(0.013)$ | $0.37(0.01)$ |
| task 19 | $0.14(0.019)$ | $0.15(0.009)$ | $0.14(0.012)$ | $0.06(0.075)$ | $0.03(0.012)$ | $0.63(0.007)$ | $0.36(0.009)$ |
| task 20 | $0.13(0.011)$ | $0.15(0.01)$ | $0.14(0.011)$ | $0.06(0.072)$ | $0.03(0.015)$ | $0.63(0.007)$ | $0.35(0.011)$ |
| task 21 | $0.13(0.005)$ | $0.15(0.01)$ | $0.15(0.01)$ | $0.06(0.071)$ | $0.02(0.003)$ | $0.63(0.008)$ | $0.35(0.012)$ |

Table 5. The average performance on IIRC-CIFAR after each task using the precision-weighted Jaccard Similarity. This table represents the same results as in Figure 4 with the standard deviation between brackets

| task | model |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ER | iCaRL-CNN | iCaRL-norm | LUCIR | incremental joint |
| task 0 | $0.7(0.027)$ | $0.78(0.018)$ | $0.8(0.019)$ | $0.76(0.025)$ | $0.73(0.02)$ |
| task 1 | $0.13(0.022)$ | $0.46(0.039)$ | $0.49(0.034)$ | $0.17(0.044)$ | $0.73(0.026)$ |
| task 2 | $0.12(0.071)$ | $0.34(0.047)$ | $0.38(0.041)$ | $0.15(0.048)$ | $0.73(0.019)$ |
| task 3 | $0.08(0.01)$ | $0.27(0.035)$ | $0.31(0.024)$ | $0.14(0.045)$ | $0.73(0.012)$ |
| task 4 | $0.08(0.01)$ | $0.23(0.022)$ | $0.27(0.015)$ | $0.1(0.068)$ | $0.73(0.015)$ |
| task 5 | $0.07(0.012)$ | $0.2(0.018)$ | $0.25(0.014)$ | $0.1(0.063)$ | $0.73(0.01)$ |
| task 6 | $0.07(0.017)$ | $0.18(0.018)$ | $0.23(0.017)$ | $0.06(0.062)$ | $0.73(0.01)$ |
| task 7 | $0.06(0.004)$ | $0.17(0.013)$ | $0.22(0.013)$ | $0.04(0.057)$ | $0.73(0.013)$ |
| task 8 | $0.07(0.013)$ | $0.16(0.01)$ | $0.21(0.01)$ | $0.03(0.056)$ | $0.72(0.015)$ |
| task 9 | $0.06(0.002)$ | $0.16(0.011)$ | $0.2(0.01)$ | $0.03(0.053)$ | $0.72(0.017)$ |

Table 6. The average performance on IIRC-ImageNet-lite after each task using the precision-weighted Jaccard Similarity. This table represents the same results as in Figure 3 with the standard deviation between brackets

| task | model |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ER | iCaRL-CNN | iCaRL-norm | LUCIR | joint |
| task 0 | $0.7(0.024)$ | $0.78(0.009)$ | $0.8(0.009)$ | $0.75(0.017)$ | - |
| task 1 | $0.13(0.023)$ | $0.47(0.016)$ | $0.51(0.014)$ | $0.15(0.044)$ | - |
| task 2 | $0.1(0.024)$ | $0.34(0.026)$ | $0.39(0.02)$ | $0.14(0.046)$ | - |
| task 3 | $0.08(0.008)$ | $0.27(0.02)$ | $0.32(0.014)$ | $0.13(0.044)$ | - |
| task 4 | $0.08(0.021)$ | $0.23(0.014)$ | $0.28(0.008)$ | $0.12(0.061)$ | - |
| task 5 | $0.1(0.064)$ | $0.21(0.025)$ | $0.26(0.011)$ | $0.11(0.06)$ | - |
| task 6 | $0.07(0.008)$ | $0.19(0.015)$ | $0.23(0.011)$ | $0.1(0.056)$ | - |
| task 7 | $0.06(0.007)$ | $0.17(0.017)$ | $0.22(0.013)$ | $0.11(0.051)$ | - |
| task 8 | $0.06(0.006)$ | $0.16(0.016)$ | $0.21(0.011)$ | $0.1(0.045)$ | - |
| task 9 | $0.06(0.005)$ | $0.15(0.015)$ | $0.2(0.009)$ | $0.09(0.06)$ | - |
| task 10 | $0.06(0.015)$ | $0.15(0.019)$ | $0.19(0.014)$ | $0.08(0.054)$ | - |
| task 11 | $0.06(0.005)$ | $0.14(0.017)$ | $0.19(0.012)$ | $0.08(0.05)$ | - |
| task 12 | $0.06(0.011)$ | $0.14(0.012)$ | $0.19(0.008)$ | $0.08(0.047)$ | - |
| task 13 | $0.06(0.006)$ | $0.13(0.013)$ | $0.19(0.005)$ | $0.07(0.045)$ | - |
| task 14 | $0.06(0.007)$ | $0.13(0.011)$ | $0.18(0.006)$ | $0.07(0.042)$ | - |
| task 15 | $0.05(0.001)$ | $0.13(0.015)$ | $0.18(0.005)$ | $0.07(0.04)$ | - |
| task 16 | $0.05(0.003)$ | $0.12(0.018)$ | $0.18(0.007)$ | $0.06(0.036)$ | - |
| task 17 | $0.05(0.008)$ | $0.12(0.017)$ | $0.17(0.005)$ | $0.06(0.034)$ | - |
| task 18 | $0.05(0.01)$ | $0.12(0.019)$ | $0.17(0.008)$ | $0.05(0.031)$ | - |
| task 19 | $0.05(0.003)$ | $0.11(0.021)$ | $0.17(0.009)$ | $0.05(0.03)$ | - |
| task 20 | $0.05(0.004)$ | $0.11(0.022)$ | $0.16(0.009)$ | $0.05(0.028)$ | - |
| task 21 | $0.04(0.004)$ | $0.11(0.024)$ | $0.16(0.01)$ | $0.04(0.025)$ | - |
| task 22 | $0.04(0.004)$ | $0.1(0.023)$ | $0.16(0.009)$ | $0.04(0.024)$ | - |
| task 23 | $0.04(0.008)$ | $0.1(0.019)$ | $0.15(0.008)$ | $0.04(0.022)$ | - |
| task 24 | $0.04(0.001)$ | $0.1(0.018)$ | $0.15(0.007)$ | $0.03(0.023)$ | - |
| task 25 | $0.03(0.003)$ | $0.1(0.017)$ | $0.14(0.007)$ | $0.02(0.022)$ | - |
| task 26 | $0.04(0.004)$ | $0.09(0.018)$ | $0.13(0.007)$ | $0.02(0.021)$ | - |
| task 27 | $0.03(0.002)$ | $0.09(0.018)$ | $0.12(0.004)$ | $0.02(0.019)$ | - |
| task 28 | $0.03(0.002)$ | $0.08(0.016)$ | $0.12(0.003)$ | $0.02(0.018)$ | - |
| task 29 | $0.03(0.002)$ | $0.08(0.016)$ | $0.11(0.003)$ | $0.02(0.017)$ | - |
| task 30 | $0.03(0.005)$ | $0.08(0.014)$ | $0.11(0.003)$ | $0.02(0.016)$ | - |
| task 31 | $0.02(0.006)$ | $0.08(0.015)$ | $0.1(0.01)$ | $0.02(0.015)$ | - |
| task 32 | $0.02(0.01)$ | $0.08(0.016)$ | $0.09(0.007)$ | $0.02(0.014)$ | - |
| task 33 | $0.02(0.005)$ | $0.08(0.017)$ | $0.09(0.011)$ | $0.02(0.012)$ | - |
| task 34 | $0.01(0.001)$ | $0.07(0.016)$ | $0.08(0.01)$ | $0.01(0.015)$ | $0.42(0.018)$ |

Table 7. The average performance on IIRC-ImageNet-full after each task using the precision-weighted Jaccard Similarity. This table represents the same results as in Figure 3 with the standard deviation between brackets

