AR: lower tail coverage for $\theta^*$