# **Supplementary Material**



Figure 1: Infrastructure-side projection model. The left side is a zoom-in of the right side. As can be seen on the right side, O in the figure is the optical center of the camera, the ray OZ denotes the optical axis (z-axis), point C represents the center point of the obstacle, P represents the intersection point between the vertical line from the center point C to the ground and the ground plane, H denotes the 3D distance of PC, and h is the pixel distance from the center point C to the ground in the imaging plane,  $\theta$  is the pitch angle of the camera, z denotes the depth of center point C, f represents the focal length and  $\delta$  is the included angle between the line connecting the point P to the optical center O and OZ.

### 1 Detailed calculation process of the normalized depth

Our aim is to work out how to express the depth z and further derive the normalized depth. First, since the image plane is parallel to the AB (AB is the virtual auxiliary plane set by us), we can get:

$$\frac{H'}{h} = \frac{z}{f} \tag{1}$$

where H' = AC. Here, f is a known quantity and h is easily obtained from visual features, so we only need to obtain H'. From point P to straight line AB draw an auxiliary vertical line and intersect AB at point E, that is, PE is perpendicular to AB. We can get:

$$H' = AC = CE - AE \tag{2}$$

Since:

$$CE = PC * \cos \angle ACP \tag{3}$$

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$$AE = PE * \tan \angle APE = PC * \sin \angle ACP * \tan \angle APE$$
(4)

$$H = PC \tag{5}$$

We have:

$$H' = H \cos \angle ACP - H \sin \angle ACP * \tan \angle APE$$
(6)

According to the parallel relationship, we can get:  $\angle ACP = \theta$ ,  $\angle APE = \delta$ . Thus:

$$H' = H\cos\theta - H\sin\theta * \tan\delta = H * (\cos\theta - \sin\theta * \tan\delta)$$
(7)

Substitute it into equation (1) and we get:

$$z = \frac{H}{h} * (\cos\theta - \sin\theta * \tan\delta) * f$$
(8)

#### 2 More detailed results on three benchmarks

#### 2.1 Detailed results on KITTI

Method	Reference	Extra Data	$AP_{3D}(IOU = 0.7 R_{40})$			$AP_{BEV}(IOU = 0.7 R_{40})$		
Wiethou	Kelelelice	Extra Data	Easy Mod. Ha		Hard	Easy	Mod.	Hard
MonoPSR [7]	CVPR 2019	LIDAR	10.76	7.25	5.85	18.33	12.58	9.91
PatchNet [14]	ECCV 2020	Depth	15.68	11.12	10.17	22.97	16.86	14.97
D4LCN[5]	CVPR 2020	Depth	16.65	11.72	9.51	22.51	16.02	12.55
MonoRUn [3]	CVPR 2021	LIDAR	19.65	12.30	10.58	27.94	17.34	15.24
CaDDN [18]	CVPR 2021	LIDAR	19.17	13.41	11.46	27.94	18.91	17.19
DFR-Net [29]	ICCV 2021	Depth	19.40	13.63	10.35	28.17	19.17	14.84
AutoShape [12]	ICCV 2021	CAD	22.47	14.17	11.36	30.66	20.08	15.59
DID-M3D [17]	ECCV 2022	Depth	24.40	16.29	13.75	32.95	22.76	19.83
DD3D [16]	ICCV 2021	Depth	23.22	16.34	14.20	30.98	22.56	20.03
MoGDE [27]	NeurIPS 2022	Odometry	27.07	17.88	15.66	38.38	25.60	22.91
M3D-RPN [1]	ICCV 2019	None	14.76	9.71	7.42	21.02	13.67	10.23
SMOKE [11]	CVPR 2020	None	14.03	9.76	7.84	20.83	14.49	12.75
MonoPair [4]	CVPR2020	None	13.04	9.99	8.65	19.28	14.83	12.89
MonoDLE [15]	CVPR2021	None	17.23	12.26	10.29	24.79	18.89	16.00
PCT [21]	NeurIPS 2021	None	21.00	13.37	11.31	29.65	19.03	15.92
MonoFlex [26]	CVPR 2021	None	19.94	13.89	12.07	28.23	19.75	16.89
MonoEdge [28]	WACV 2023	None	21.08	14.47	12.73	28.80	20.35	17.57
GUPNet [13]	ICCV 2021	None	22.26	15.02	13.12	30.29	21.19	18.20
MonoDTR [6]	CVPR 2022	None	21.99	15.39	12.73	28.59	20.38	17.14
MonoCon [22]	AAAI 2022	None	22.50	16.46	13.95	31.12	22.10	19.00
MonoUNI(Ours)	-	None	24.75	16.73	13.49	33.28	23.05	19.39

Table 1: Monocular 3D detection performance of Car category on KITTI *test* set. All results are evaluated on KITTI testing server. Same as KITTI leaderboard, methods are ranked under the moderate difficulty level. For the extra data: 1) LIDAR denotes methods use extra LIDAR cloud points in training process. 2) Depth means utilizing depth maps or models pre-trained under another depth estimation dataset. 3) CAD denotes using dense shape annotations provided by CAD models. 4) Odometry means utilizing extra odometry poses, images, or a well-trained network. 5) None means no extra data is used.

Table 1 lists the results of the vehicle-side 3D detection methods on the KITTI dataset in recent years. Our method ranks first among methods that do not use any additional data, which is improved (2.25%/0.27%/-0.46%) in  $AP_{3D}$  and (2.16%/0.95%/0.39%) in  $AP_{BEV}$  compared to MonoCon [22].

#### 2.2 Detailed results on Rope3D

Table 2 shows the comparison of the results of methods on the Rope3D dataset in recent years.
Compared with other methods, our method has greatly improved AP and Rope <sub>score</sub> which ranks
first.

		IOU = 0.5					IOU = 0.7		
Method	Extra Data	C	ar	Big V	ehicle	C	ar	Big V	ehicle
		AP	Rope	AP	Rope	AP	Rope	AP	Rope
M3D-RPN [1]	Ground	54.19	62.65	33.05	44.94	16.75	32.90	6.86	24.19
M3D-RPN [1]	Depth	67.17	73.14	39.06	49.95	33.94	46.45	11.28	28.12
Kinematic3D [2]	Ground	50.57	58.86	37.60	48.08	17.74	32.99	6.10	22.88
MonoDLE [15]	Ground	51.70	60.36	40.34	50.07	13.58	29.46	9.63	25.80
MonoDLE [15]	Depth	77.50	80.84	49.07	57.22	54.53	62.48	17.25	32.00
MonoFlex [26]	Ground	60.33	66.86	37.33	47.96	33.78	46.12	10.08	26.16
MonoFlex [26]	Depth	59.78	66.66	59.81	66.07	35.64	47.43	24.61	38.01
BEVFormer [10]	None	50.62	58.78	34.58	45.16	24.64	38.71	10.05	25.56
BEVDepth [9]	None	69.63	74.70	45.02	54.64	42.56	53.05	21.47	35.82
BEVHeight [24]	None	74.60	78.72	48.93	57.70	45.73	55.62	23.07	37.04
MonoUNI(Ours)	None	92.45	92.63	76.30	79.20	74.50	78.26	43.04	52.63

AP and Rope denote  $AP_{3D|R40}$  and  $Rope_{score}$  respectively.

 Table 2: Monocular 3D detection performance of Car and Big Vehicle categories on Rope3D val set.

Method	М	Vel	n.(IOU=	0.5)	Ped	L(IOU=0.25) $Cyc.(IO)$				0.25)
	141	Easy	Mod.	Hard	Easy	Mod.	Hard	Easy	Mod.	Hard
PointPillars [8]	L	63.07	54.00	54.01	38.53	37.20	37.28	38.46	22.60	22.49
SECOND [23]	L	71.47	53.99	54.00	55.16	52.49	52.52	54.68	31.05	31.19
MVXNet [20]	LC	71.04	53.71	53.76	55.83	54.45	54.40	54.05	30.79	31.06
ImvoxelNet [19]	C	44.78	37.58	37.55	6.81	6.746	6.73	21.06	13.57	13.17
BEVFormer [10]	C	61.37	50.73	50.73	16.89	15.82	15.95	22.16	22.13	22.06
BEVDepth [9]	C	75.50	63.58	63.67	34.95	33.42	33.27	55.67	55.47	55.34
BEVHeight [24]	C	77.78	65.77	65.85	41.22	39.29	39.46	60.23	60.08	60.54
MonoUNI(Ours)	C	90.92	87.24	87.20	51.78	49.10	48.02	69.05	69.80	69.64

#### 2.3 Detailed results on DAIR-V2X-I

M, L, C denotes modality, LiDAR, camera respectively.

Table 3: Monocular 3D detection performance of Car category on DAIR-V2X-I val set.

## **3** Repartitioning of the Rope3D dataset

To investigate the influence of focal length diversity on model performance, we partitioned the Rope3D [25] dataset according to the focal length of each image. We observed that the focal lengths of the Rope3D dataset predominantly fell within two focal length ranges: 2150-2200 and 2749-2780. Based on the provided training-test distribution from the official website and taking into account the focal length of each image, we reorganized the Rope3D dataset as follows:

Table 4: The number of images in each subset of the Rope3D dataset.

numbers	2100	2700	all
Train	20247	20086	40333
Val	3149	1527	4676

We conducted training and evaluation on three distinct sets using the widely adopted two-stage approach GUPNet [13], the single-stage approach SMOKE [11], and our proposed method MonoUNI, respectively.

Method	Train sat	$AP_{3D}(IOU = 0.5 R_{40})$				
Method	Train_set	val_2100	val_2700	val_all		
GUPNet [13]	train_2100	13.20	0.03	7.42		
GUPNet [13]	train_2700	0.17	21.65	3.07		
GUPNet [13]	train_all	10.82	5.85	9.38		
SMOKE [11]	train_2100	9.77	0.13	6.19		
SMOKE [11]	train_2700	0.04	23.20	3.64		
SMOKE [11]	train_all	6.04	18.01	8.48		
MonoUNI	train_2100	25.78	21.30	24.47		
MonoUNI	train_2700	5.77	23.42	9.25		
MonoUNI	train_all	26.63	38.10	28.91		

Table 5: Analysis for different focal lengths on Rope3D dataset with new train/val division.

As shown in Table 5, due to the presence of ambiguity issues arising from focal length and mounting angles, the ordinary vehicle-side 3D detection methods exhibited lower AP on individual focal length testing subsets when trained on the entire dataset, compared to training them separately on the corresponding focal length training subsets. MonoUNI introduces the concept of normalized depth to address the ambiguity issue, effectively mitigating the mutual interference problem between two different focal length training subsets. By employing this approach, MonoUNI achieves state-of-the-art average precision (AP) performance across all testing subsets. Interestingly, when training solely on the  $train_2100$  subset, the model achieved a level of accuracy on the  $val_2700$  subset that was comparable to models trained exclusively on the  $train_2700$  subset. This further highlights the effectiveness of our method.



Figure 2: **Qualitative Results on Rope3D.** The 3D green boxes are produced by MonoUNI and the red boxes are the ground truths.

## 4 More Qualitative Results

We provide more qualitative results in Figure 2 and Figure 3.



Figure 3: **Qualitative Results on KITTI.** The 3D green boxes are produced by MonoUNI and the red boxes are the ground truths.

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