

# APPENDIX FOR “CHATSR: CONVERSATIONAL SYMBOLIC REGRESSION”

## A APPENDIX: DETAILED SETTINGS OF HYPERPARAMETERS DURING TRAINING THE SETTRANSFORMER.

Table 3: Hyperparameters of SetTransformer

<b>hyperparameters</b>	<b>Numerical value</b>
<b>N_p</b>	0
<b>activation</b>	‘relu’
<b>bit16</b>	True
<b>dec_layers</b>	5
<b>dec_pf_dim</b>	512
<b>dim_hidden</b>	512
<b>dim_input</b>	3
<b>dropout</b>	0
<b>input_normalization</b>	False
<b>length_eq</b>	60
<b>linear</b>	False
<b>ln</b>	True
<b>lr</b>	0.0001
<b>mean</b>	0.5
<b>n_l_enc</b>	5
<b>norm</b>	True
<b>num_features</b>	20
<b>num_heads</b>	8
<b>num_inds</b>	50
<b>output_dim</b>	60
<b>sinuisodal_embeddings</b>	False
<b>src_pad_idx</b>	0
<b>std</b>	0.5
<b>trg_pad_idx</b>	0

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810    **B APPENDIX: DETAILS OF THE EXPRESSIONS FOR THE VARIOUS PROPERTIES**  
811    **INVOLVED IN THE ZERO-SHOT EXPERIMENT**  
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813    To test ChatSR’s Zero-shot capability, we designed some properties not included in the training dataset  
814    for testing. They include Continuous Monotonic Decreasing, Continuous Globally Monotonically  
815    Increasing, Origin-Centered Symmetric, Continuous Convex and Continuous Concave are the five  
816    properties. For each property, 10 functions satisfying this property are designed. The form of the  
817    function is as follows Table 4,5,6,7,8.  
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Function Index	Expression	Domain
1	$f(x) = -x - \ln(x + 1)$	$x \geq 0$
2	$f(x) = e^{-x} - x^2$	$\mathbb{R}$
3	$f(x) = \frac{1}{x+1} - \sqrt{x}$	$x > 0$
4	$f(x) = 10 - x^2 - \arctan(x)$	$\mathbb{R}$
5	$f(x) = \frac{1}{\sqrt{x+1}} - \ln(x + 2)$	$x \geq 0$
6	$f(x) = e^{-x} \cos(x) + \frac{1}{x+1}$	$x > 0$
7	$f(x) = -\ln(x + 1) + x^{-0.5}$	$x > 0$
8	$f(x) = \sqrt{x+1} - 3 \ln(x + 2)$	$x \geq 0$
9	$f(x) = e^{-x^2} - x$	$\mathbb{R}$
10	$f(x) = -x^{3/2} - \tan^{-1}(x)$	$x \geq 0$

832    Table 4: List of Continuous Monotonic Decreasing Functions  
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Function Index	Expression	Domain
1	$f(x) = x + \ln(x^2 + 1)$	$\mathbb{R}$
2	$f(x) = e^x + x^2$	$\mathbb{R}$
3	$f(x) = x + \arctan(x)$	$\mathbb{R}$
4	$f(x) = x\sqrt{x^2 + 1}$	$\mathbb{R}$
5	$f(x) = x^3 + 3x$	$\mathbb{R}$
6	$f(x) = x + \sqrt{x+2} + \ln(x^2 + 1)$	$x \geq -2$
7	$f(x) = e^x + \ln(x^2 + 1)$	$\mathbb{R}$
8	$f(x) = \sqrt{x^2 + 1} + x^3$	$\mathbb{R}$
9	$f(x) = x + \arcsin(\tanh(x))$	$\mathbb{R}$
10	$f(x) = \ln(x + 2) + e^x$	$x > -2$

837    Table 5: List of Continuous Globally Monotonically Increasing Functions  
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Function Index	Expressions	Domain
1	$f(x) = x \sin(x)$	$x \in \mathbb{R}$
2	$f(x) = 3x^3 - 2x$	$x \in \mathbb{R}$
3	$f(x) = \log(1 + x) - \log(1 - x)$	$x \in (-1, 1)$
4	$f(x) = e^x - e^{-x}$	$x \in \mathbb{R}$
5	$f(x) = \arctan(x) - \arctan(-x)$	$x \in \mathbb{R}$
6	$f(x) = x(x^2 + 3)$	$x \in \mathbb{R}$
7	$f(x) = x^5 - 10x^3 + 9x$	$x \in \mathbb{R}$
8	$f(x) = \sinh(x) = \frac{e^x - e^{-x}}{2}$	$x \in \mathbb{R}$
9	$f(x) = 7x - x^7$	$x \in \mathbb{R}$
10	$f(x) = x \cos(x) + \sin(x)$	$x \in \mathbb{R}$

Table 6: Expressions that are Origin-Centered Symmetric (Odd Functions)

Function Index	Expression	Domain
1	$f(x) = x^4 + 2x^2 + 1$	$x \in \mathbb{R}$
2	$f(x) = e^x + x^2$	$\mathbb{R}$
3	$f(x) = x^2 + \log(1 + e^x)$	$x \in \mathbb{R}$
4	$f(x) = x \sinh(x) + \cosh(x)$	$x \in \mathbb{R}$
5	$f(x) = x^2 + \sqrt{x^2 + 1}$	$x \in \mathbb{R}$
6	$f(x) = e^{x^2} - x$	$x \in \mathbb{R}$
7	$f(x) = x^2 + \arctan(x)$	$x \in \mathbb{R}$
8	$f(x) = \sqrt{1 + e^x}$	$x \in \mathbb{R}$
9	$f(x) = x + \log(1 + x^2)$	$x \in \mathbb{R}$
10	$f(x) = x^6 + x^4 - x^3 + x + e^{-x}$	$x \in \mathbb{R}$

Table 7: List of Continuous Convex Functions

Function Index	Expression	Domain
1	$f(x) = -x^4 + 2x^2 + 1$	$x \in \mathbb{R}$
2	$f(x) = -e^x + 3x - 2$	$x \in \mathbb{R}$
3	$f(x) = -x^2 + \log(1 + x^2)$	$x \in \mathbb{R}$
4	$f(x) = -\cosh(x)$	$x \in \mathbb{R}$
5	$f(x) = -x^2 - \sqrt{x^2 + 1}$	$x \in \mathbb{R}$
6	$f(x) = -e^{x/2} - x^2$	$x \in \mathbb{R}$
7	$f(x) = \log(1 + e^{-x})$	$x \in \mathbb{R}$
8	$f(x) = -\sqrt{1 + x^2}$	$x \in \mathbb{R}$
9	$f(x) = -\log(x^2 + 1)$	$x \in \mathbb{R}$
10	$f(x) = -x^6 - x^4 + x^3 - x + e^{-x^2}$	$x \in \mathbb{R}$

Table 8: List of Continuous Concave Functions

## C APPENDIX: TEST DATASET IN DETAIL

Table 9,10,11 shows in detail the expression forms of the data set used in the experiment, as well as the sampling range and sampling number. Some specific presentation rules are described below

- The variables contained in the regression task are represented as  $[x_1, x_2, \dots, x_n]$ .

- 918     •  $U(a, b, c)$  signifies  $c$  random points uniformly sampled between  $a$  and  $b$  for each input  
 919       variable. Different random seeds are used for training and testing datasets.  
 920     •  $E(a, b, c)$  indicates  $c$  points evenly spaced between  $a$  and  $b$  for each input variable.

Name	Expression	Dataset
Nguyen-1	$x_1^3 + x_1^2 + x_1$	$U(-1, 1, 20)$
Nguyen-2	$x_1^4 + x_1^3 + x_1^2 + x_1$	$U(-1, 1, 20)$
Nguyen-3	$x_1^5 + x_1^4 + x_1^3 + x_1^2 + x_1$	$U(-1, 1, 20)$
Nguyen-4	$x_1^6 + x_1^5 + x_1^4 + x_1^3 + x_1^2 + x_1$	$U(-1, 1, 20)$
Nguyen-5	$\sin(x_1^2) \cos(x_1) - 1$	$U(-1, 1, 20)$
Nguyen-6	$\sin(x_1) + \sin(x_1 + x_2^2)$	$U(-1, 1, 20)$
Nguyen-7	$\log(x_1 + 1) + \log(x_1^2 + 1)$	$U(0, 2, 20)$
Nguyen-8	$\sqrt{x_1}$	$U(0, 4, 20)$
Nguyen-9	$\sin(x_1) + \sin(x_2^2)$	$U(0, 1, 20)$
Nguyen-10	$2 \sin(x_1) \cos(x_2)$	$U(0, 1, 20)$
Nguyen-11	$x_1^{x_2}$	$U(0, 1, 20)$
Nguyen-12	$x_1^4 - x_1^3 + \frac{1}{2}x_2^2 - x_2$	$U(0, 1, 20)$
Nguyen-2'	$4x_1^4 + 3x_1^3 + 2x_1^2 + x_1$	$U(-1, 1, 20)$
Nguyen-5'	$\sin(x_1^2) \cos(x_1) - 2$	$U(-1, 1, 20)$
Nguyen-8'	$\sqrt[3]{x_1}$	$U(0, 4, 20)$
Nguyen-8''	$\sqrt[3]{x_1^2}$	$U(0, 4, 20)$
Nguyen-1 <sup>c</sup>	$3.39x_1^3 + 2.12x_1^2 + 1.78x_1$	$U(-1, 1, 20)$
Nguyen-5 <sup>c</sup>	$\sin(x_1^2) \cos(x_1) - 0.75$	$U(-1, 1, 20)$
Nguyen-7 <sup>c</sup>	$\log(x_1 + 1.4) + \log(x_1^2 + 1.3)$	$U(0, 2, 20)$
Nguyen-8 <sup>c</sup>	$\sqrt{1.23x_1}$	$U(0, 4, 20)$
Nguyen-10 <sup>c</sup>	$\sin(1.5x_1) \cos(0.5x_2)$	$U(0, 1, 20)$
Korns-1	$1.57 + 24.3 * x_1^4$	$U(-1, 1, 20)$
Korns-2	$0.23 + 14.2 \frac{(x_4+x_1)}{(3x_2)}$	$U(-1, 1, 20)$
Korns-3	$4.9 \frac{(x_2-x_1+x_1)}{(3x_2)} - 5.41$	$U(-1, 1, 20)$
Korns-4	$0.13\sin(x_1) - 2.3$	$U(-1, 1, 20)$
Korns-5	$3 + 2.13\log( x_5 )$	$U(-1, 1, 20)$
Korns-6	$1.3 + 0.13\sqrt{ x_1 }$	$U(-1, 1, 20)$
Korns-7	$2.1(1 - e^{-0.55x_1})$	$U(-1, 1, 20)$
Korns-8	$6.87 + 11\sqrt{ 7.23x_1x_4x_5 }$	$U(-1, 1, 20)$
Korns-9	$12\sqrt{ 4.2x_1x_2x_2 }$	$U(-1, 1, 20)$
Korns-10	$0.81 + 24.3 \frac{2x_1+3x_2}{4x_3^3+5x_4^4}$	$U(-1, 1, 20)$
Korns-11	$6.87 + 11\cos(7.23x_1^3)$	$U(-1, 1, 20)$
Korns-12	$2 - 2.1\cos(9.8x_1^3)\sin(1.3x_5)$	$U(-1, 1, 20)$
Korns-13	$32.0 - 3.0 \frac{\tan(x_1)}{\tan(x_2)} \frac{\tan(x_3)}{\tan(x_4)}$	$U(-1, 1, 20)$
Korns-14	$22.0 - (4.2\cos(x_1) - \tan(x_2)) \frac{\tanh(x_3)}{\sin(x_4)}$	$U(-1, 1, 20)$
Korns-15	$12.0 - \frac{6.0\tan(x_1)}{e^{x_2}} (\log(x_3) - \tan(x_4)))$	$U(-1, 1, 20)$
Jin-1	$2.5x_1^4 - 1.3x_1^3 + 0.5x_2^2 - 1.7x_2$	$U(-3, 3, 100)$
Jin-2	$8.0x_1^2 + 8.0x_2^3 - 15.0$	$U(-3, 3, 100)$
Jin-3	$0.2x_1^3 + 0.5x_2^3 - 1.2x_2 - 0.5x_1$	$U(-3, 3, 100)$
Jin-4	$1.5 \exp x + 5.0\cos(x_2)$	$U(-3, 3, 100)$
Jin-5	$6.0\sin(x_1)\cos(x_2)$	$U(-3, 3, 100)$
Jin-6	$1.35x_1x_2 + 5.5\sin((x_1 - 1.0)(x_2 - 1.0))$	$U(-3, 3, 100)$

Table 9: Specific formula form and value range of the three data sets Nguyen, Korns, and Jin.

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Name	Expression	Dataset
Neat-1	$x_1^4 + x_1^3 + x_1^2 + x$	U(-1, 1, 20)
Neat-2	$x_1^5 + x_1^4 + x_1^3 + x_1^2 + x$	U(-1, 1, 20)
Neat-3	$\sin(x_1^2) \cos(x) - 1$	U(-1, 1, 20)
Neat-4	$\log(x+1) + \log(x_1^2 + 1)$	U(0, 2, 20)
Neat-5	$2 \sin(x) \cos(x_2)$	U(-1, 1, 100)
Neat-6	$\sum_{k=1}^x \frac{1}{k}$	E(1, 50, 50)
Neat-7	$2 - 2.1 \cos(9.8x_1) \sin(1.3x_2)$	E(-50, 50, 10 <sup>5</sup> )
Neat-8	$\frac{e^{-(x_1)^2}}{1.2 + (x_2 - 2.5)^2}$	U(0.3, 4, 100)
Neat-9	$\frac{1}{1+x_1^{-4}} + \frac{1}{1+x_2^{-4}}$	E(-5, 5, 21)
Keijzer-1	$0.3x_1 \sin(2\pi x_1)$	U(-1, 1, 20)
Keijzer-2	$2.0x_1 \sin(0.5\pi x_1)$	U(-1, 1, 20)
Keijzer-3	$0.92x_1 \sin(2.41\pi x_1)$	U(-1, 1, 20)
Keijzer-4	$x_1^3 e^{-x_1} \cos(x_1) \sin(x_1) \sin(x_1)^2 \cos(x_1) - 1$	U(-1, 1, 20)
Keijzer-5	$3 + 2.13 \log( x_5 )$	U(-1, 1, 20)
Keijzer-6	$\frac{x_1(x_1+1)}{2}$	U(-1, 1, 20)
Keijzer-7	$\log(x_1)$	U(0, 1, 20)
Keijzer-8	$\sqrt{(x_1)}$	U(0, 1, 20)
Keijzer-9	$\log(x_1 + \sqrt{x_1^2 + 1})$	U(-1, 1, 20)
Keijzer-10	$x_1^{x_2}$	U(-1, 1, 20)
Keijzer-11	$x_1 x_2 + \sin((x_1 - 1)(x_2 - 1))$	U(-1, 1, 20)
Keijzer-12	$x_1^4 - x_1^3 + \frac{x_2^2}{2} - x_2$	U(-1, 1, 20)
Keijzer-13	$6 \sin(x_1) \cos(x_2)$	U(-1, 1, 20)
Keijzer-14	$\frac{8}{2+x_1^2+x_2^2}$	U(-1, 1, 20)
Keijzer-15	$\frac{x_1^3}{5} + \frac{x_2^3}{2} - x_2 - x_1$	U(-1, 1, 20)
Livermore-1	$\frac{1}{3} + x_1 + \sin(x_1^2)$	U(-3, 3, 100)
Livermore-2	$\sin(x_1^2) * \cos(x_1) - 2$	U(-3, 3, 100)
Livermore-3	$\sin(x_1^3) * \cos(x_1^2) - 1$	U(-3, 3, 100)
Livermore-4	$\log(x_1 + 1) + \log(x_1^2 + 1) + \log(x_1)$	U(-3, 3, 100)
Livermore-5	$x_1^4 - x_1^3 + x_2^2 - x_2$	U(-3, 3, 100)
Livermore-6	$4x_1^4 + 3x_1^3 + 2x_1^2 + x_1$	U(-3, 3, 100)
Livermore-7	$\frac{(\exp(x_1) - \exp(-x_1))}{2}$	U(-1, 1, 100)
Livermore-8	$\frac{(\exp(x_1) + \exp(-x_1))}{3}$	U(-3, 3, 100)
Livermore-9	$x_1^9 + x_1^8 + x_1^7 + x_1^6 + x_1^5 + x_1^4 + x_1^3 + x_1^2 + x_1$	U(-1, 1, 100)
Livermore-10	$6 * \sin(x_1) \cos(x_2)$	U(-3, 3, 100)
Livermore-11	$\frac{x_1^2 x_2^2}{(x_1 + x_2)}$	U(-3, 3, 100)
Livermore-12	$\frac{x_1^5}{x_2^3}$	U(-3, 3, 100)
Livermore-13	$x_1^{\frac{1}{3}}$	U(-3, 3, 100)
Livermore-14	$x_1^3 + x_1^2 + x_1 + \sin(x_1) + \sin(x_2^2)$	U(-1, 1, 100)
Livermore-15	$x_1^{\frac{1}{5}}$	U(-3, 3, 100)
Livermore-16	$x_1^{\frac{2}{3}}$	U(-3, 3, 100)
Livermore-17	$4 \sin(x_1) \cos(x_2)$	U(-3, 3, 100)
Livermore-18	$\sin(x_1^2) * \cos(x_1) - 5$	U(-3, 3, 100)
Livermore-19	$x_1^5 + x_1^4 + x_1^2 + x_1$	U(-3, 3, 100)
Livermore-20	$e^{(-x_1^2)}$	U(-3, 3, 100)
Livermore-21	$x_1^8 + x_1^7 + x_1^6 + x_1^5 + x_1^4 + x_1^3 + x_1^2 + x_1$	U(-1, 1, 20)
Livermore-22	$e^{(-0.5x_1^2)}$	U(-3, 3, 100)

Table 10: Specific formula form and value range of the three data sets neat, Keijzer, and Livermore.

	Name	Expression	Dataset
1026	Vladislavleva-1	$\frac{(e^{-(x_1-1)^2})}{(1.2+(x_2-2.5)^2))}$	U(-1, 1, 20)
1027	Vladislavleva-2	$e^{-x_1} x_1^3 \cos(x_1) \sin(x_1) (\cos(x_1) \sin(x_1)^2 - 1)$	U(-1, 1, 20)
1028	Vladislavleva-3	$e^{-x_1} x_1^3 \cos(x_1) \sin(x_1) (\cos(x_1) \sin(x_1)^2 - 1) (x_2 - 5)$	U(-1, 1, 20)
1029	Vladislavleva-4	$\frac{10}{5+(x_1-3)^2+(x_2-3)^2+(x_3-3)^2+(x_4-3)^2+(x_5-3)^2}$	U(0, 2, 20)
1030	Vladislavleva-5	$30(x_1 - 1) \frac{x_3 - 1}{(x_1 - 10)} x_2^2$	U(-1, 1, 100)
1031	Vladislavleva-6	$6 \sin(x_1) \cos(x_2)$	E(1, 50, 50)
1032	Vladislavleva-7	$2 - 2.1 \cos(9.8x) \sin(1.3x_2)$	E(-50, 50, 10 <sup>5</sup> )
1033	Vladislavleva-8	$\frac{e^{-(x-1)^2}}{1.2+(x_2-2.5)^2}$	U(0.3, 4, 100)
1034	Test-2	$3.14x_1^2$	U(-1, 1, 20)
1035	Const-Test-1	$5x_1^2$	U(-1, 1, 20)
1036	GrammarVAE-1	$1/3 + x_1 + \sin(x_1^2))$	U(-1, 1, 20)
1037	Sine	$\sin(x_1) + \sin(x_1 + x_1^2))$	U(-1, 1, 20)
1038	Nonic	$x_1^9 + x_1^8 + x_1^7 + x_1^6 + x_1^5 + x_1^4 + x_1^3 + x_1^2 + x_1$	U(-1, 1, 100)
1039	Pagie-1	$\frac{1}{1+x_1^{-4}+\frac{1}{1+x_2-4}}$	E(1, 50, 50)
1040	Meier-3	$\frac{x_1^2 x_2^2}{(x_1+x_2)}$	E(-50, 50, 10 <sup>5</sup> )
1041	Meier-4	$\frac{x_1^5}{x_2^3}$	U(0.3, 4, 100)
1042	Poly-10	$x_1 x_2 + x_3 x_4 + x_5 x_6 + x_1 x_7 x_9 + x_3 x_6 x_{10}$	E(-1, 1, 100)
1043	Constant-1	$3.39 * x_1^3 + 2.12 * x_1^2 + 1.78 * x_1$	U(-4, 4, 100)
1044	Constant-2	$\sin(x_1^2) * \cos(x_1) - 0.75$	U(-4, 4, 100)
1045	Constant-3	$\sin(1.5 * x_1) * \cos(0.5 * x_2)$	U(0.1, 4, 100)
1046	Constant-4	$2.7 * x_1^{x_2}$	U(0.3, 4, 100)
1047	Constant-5	$\sqrt{1.23 * x_1}$	U(0.1, 4, 100)
1048	Constant-6	$x_1^{0.426}$	U(0.0, 4, 100)
1049	Constant-7	$2 * \sin(1.3 * x_1) * \cos(x_2)$	U(-4, 4, 100)
1050	Constant-8	$\log(x_1 + 1.4) + \log(x_1, 2 + 1.3)$	U(-4, 4, 100)
1051	R1	$\frac{(x_1+1)^3}{x_2^2-x_1+1)}$	U(-5, 5, 100)
1052	R2	$\frac{(x_1^2-3*x_1^2+1)}{x_2^2+1)}$	U(-4, 4, 100)
1053	R3	$\frac{x_1^6+x_1^5}{(x_1^4+x_1^3+x_1^2+x_1+1)}$	U(-4, 4, 100)

Table 11: Specific formula form and value range of the three data sets Vladislavleva and others.

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**D APPENDIX: CHATSR TESTS ON AIFEYNMAN DATASET.**

In our study, we conducted an evaluation of our novel symbol regression algorithm, termed ChatSR, leveraging the AI Feynman dataset, which comprises a diverse array of problems spanning various subfields of physics and mathematics, including mechanics, thermodynamics, and electromagnetism. Originally, the dataset contained 100,000 data points; however, for a more rigorous assessment of ChatSR’s efficacy, our analysis was deliberately confined to a subset of 100 data points. Through the application of ChatSR for symbol regression on these selected data points, we meticulously calculated the  $R^2$  values to compare the algorithm’s predictions against the true solutions.

The empirical results from our investigation unequivocally affirm that ChatSR possesses an exceptional ability to discern the underlying mathematical expressions from a constrained sample size. Notably, the  $R^2$  values achieved were above 0.99 for a predominant portion of the equations, underscoring the algorithm’s remarkable accuracy in fitting these expressions. These findings decisively position ChatSR as a potent tool for addressing complex problems within the domains of physics and mathematics. The broader implications of our study suggest that ChatSR holds considerable promise for a wide range of applications across different fields. Detailed experimental results are presented in Table 12 and Table 13.

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1134	Feynman	Equation	$R^2$
1135	I.6.20a	$f = e^{-\theta^2/2}/\sqrt{2\pi}$	0.9989
1136	I.6.20	$f = e^{-\frac{\theta^2}{2\sigma^2}}/\sqrt{2\pi\sigma^2}$	0.9973
1137	I.6.20b	$f = e^{-\frac{(\theta-\theta_1)^2}{2\sigma^2}}/\sqrt{2\pi\sigma^2}$	0.9421
1138	I.8.14	$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$	0.9413
1139	I.9.18	$F = \frac{Gm_1 m_2}{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$	0.9835
1140	I.10.7	$F = \frac{Gm_1 m_2}{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$	0.9724
1141	I.11.19	$A = x_1 y_1 + x_2 y_2 + x_3 y_3$	0.9891
1142	I.12.1	$F = \mu N_n$	0.9956
1143	I.12.2	$F = \frac{q_1 q_2}{4\pi\epsilon r^2}$	0.9999
1144	I.12.4	$E_f = \frac{q_1}{4\pi\epsilon r^2}$	0.9939
1145	I.12.5	$F = q_2 E_f$	0.9999
1146	I.12.11	$F = Q(E_f + Bv \sin \theta)$	0.9983
1147	I.13.4	$K = \frac{1}{2}m(v^2 + u^2 + w^2)$	0.9913
1148	I.13.12	$U = Gm_1 m_2 (\frac{1}{r_2} - \frac{1}{r_1})$	0.9859
1149	I.14.3	$U = mgz$	1.0
1150	I.14.4	$U = \frac{k_{spring}x^2}{2}$	0.9926
1151	I.15.3x	$x_1 = \frac{x - ut}{\sqrt{1-u^2/c^2}}$	0.9828
1152	I.15.3t	$t_1 = \frac{t - ux/c^2}{\sqrt{1-u^2/c^2}}$	0.9732
1153	I.15.10	$p = \frac{m_0 v}{\sqrt{1-v^2/c^2}}$	0.9810
1154	I.16.6	$v_1 = \frac{u+v}{\sqrt{1+uv/c^2}}$	0.9984
1155	I.18.4	$r = \frac{m_1 r_1 + m_2 r_2}{m_1 + m_2}$	0.9818
1156	I.18.12	$\tau = r F \sin \theta$	0.9928
1157	I.18.16	$L = mr v \sin \theta$	0.9993
1158	I.24.6	$E = \frac{1}{4}m(\omega^2 + \omega_0^2)x^2$	0.9981
1159	I.25.13	$V_e = \frac{q}{C}$	1.0
1160	I.26.2	$\theta_1 = \arcsin(n \sin \theta_2)$	0.9992
1161	I.27.6	$f_f = \frac{1}{d_1 + d_2}$	0.9914
1162	I.29.4	$k = \frac{\omega}{c}$	1.0
1163	I.29.16	$x = \sqrt{x_1^2 + x_2^2 - 2x_1 x_2 \cos(\theta_1 - \theta_2)}$	0.9827
1164	I.30.3	$I_* = I_{*0} \frac{\sin^2(n\theta/2)}{\sin^2(\theta/2)}$	0.9937
1165	I.30.5	$\theta = \arcsin(\frac{\lambda}{nd})$	0.9917
1166	I.32.5	$P = \frac{q^2 a^2}{6\pi\epsilon c^3}$	0.9933
1167	I.32.17	$P = (\frac{1}{2}\epsilon c E_f^2)(8\pi r^2/3)(\omega^4/(\omega^2 - \omega_0^2)^2)$	0.991
1168	I.34.8	$\omega = \frac{qvB}{\rho}$	0.9999
1169	I.34.10	$\omega = \frac{p_0}{1-v/c}$	0.9913
1170	I.34.14	$\omega = \frac{1+v/c}{\sqrt{1-v^2/c^2}}\omega_0$	0.9918
1171	I.34.27	$E = \hbar\omega$	0.9972
1172	I.37.4	$I_* = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$	0.9827
1173	I.38.12	$r = \frac{4\pi\epsilon h^2}{mq^2}$	0.9983
1174	I.39.10	$E = \frac{3}{2}p_F V$	0.9965
1175	I.39.11	$E = \frac{1}{\gamma-1}p_F V$	0.9792
1176	I.39.22	$P_F = \frac{n k_b T}{V}$	0.9935
1177	I.40.1	$n = n_0 e^{-\frac{\hbar\omega^3}{k_b T}}$	0.9799
1178	I.41.16	$L_{rad} = \frac{\hbar\omega^3}{\pi^2 c^2 (e^{\frac{\hbar\omega}{k_b T}} - 1)}$	0.9983
1179	I.43.16	$v = \frac{\mu_{drift} q V_e}{d}$	0.9981
1180	I.43.31	$D = \mu_e k_b T$	1.0
1181	I.43.43	$\kappa = \frac{1}{\gamma-1} \frac{k_b v}{A}$	0.9347
1182	I.44.4	$E = n k_b T \ln(\frac{V_2}{V_1})$	0.9024
1183	I.47.23	$c = \sqrt{\frac{\gamma p r}{\rho}}$	0.9724
1184	I.48.20	$E = \frac{mc^2}{\sqrt{1-v^2/c^2}}$	0.8902
1185	I.50.26	$x = x_1 [\cos(\omega t) + \alpha \cos(\omega t)^2]$	0.9999

Table 12: Tested Feynman Equations, part 1.

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Feynman	Equation	$R^2$
II.2.42	$P = \frac{\kappa(T_2 - T_1)A}{P^d}$	0.8824
II.3.24	$F_E = \frac{P^d}{4\pi r^2}$	0.9820
II.4.23	$V_e = \frac{1}{4\pi\epsilon r} p_d \cos\theta$	0.9888
II.6.11	$V_e = \frac{1}{4\pi\epsilon} \frac{p_d z}{r^2}$	0.9837
II.6.15a	$E_f = \frac{3}{4\pi\epsilon} \frac{p_d z}{r^5} \sqrt{x^2 + y^2}$	0.9235
II.6.15b	$E_f = \frac{3}{4\pi\epsilon} \frac{p_d}{r^3} \cos\theta \sin\theta$	0.9928
II.8.7	$E = \frac{3}{5} \frac{q^2}{4\pi\epsilon d^2}$	0.9827
II.8.31	$E_{den} = \frac{\epsilon E_f}{2}$	0.9999
II.10.9	$E_f = \frac{\sigma_{den}}{\epsilon} \frac{1}{1+\chi}$	0.9933
II.11.3	$x = \frac{qE_f}{m(\omega_0^2 - \omega^2)}$	0.9918
II.11.7	$n = n_0(1 + \frac{p_d E_f \cos\theta}{k_b T})$	0.8927
II.11.20	$P_* = \frac{n_0 p_d^2 E_f}{3k_b T}$	0.8355
II.11.27	$P_* = \frac{n\alpha}{1-n\alpha/3} \epsilon E_f$	0.9925
II.11.28	$\theta = 1 + \frac{n\alpha}{1-(n\alpha/3)}$	0.9992
II.13.17	$B = \frac{1}{4\pi\epsilon c^2} \frac{2I}{r}$	0.9993
II.13.23	$\rho_c = \frac{1}{\sqrt{1-v^2/c^2}}$	0.9902
II.13.34	$j = \frac{\sqrt{1-v^2/c^2}}{\sqrt{1-\omega^2/c^2}}$	0.9827
II.15.4	$E = -\mu_M B \cos\theta$	0.9997
II.15.5	$E = -p_d E_f \cos\theta$	0.9973
II.21.32	$V_e = \frac{q}{4\pi\epsilon r(1-v/c)}$	0.9910
II.24.17	$k = \sqrt{\frac{\omega^2}{c^2} - \frac{\pi^2}{d^2}}$	0.9837
II.27.16	$F_E = \epsilon c E_f^2$	0.9935
II.27.18	$E_{den} = \epsilon E_f^2$	0.9972
II.34.2a	$I = \frac{qv}{2\pi r}$	0.9980
II.34.2	$\mu_M = \frac{qv}{qvr}$	0.9903
II.34.11	$\omega = \frac{g q B}{2m}$	0.9937
II.34.29a	$\mu_M = \frac{g q h}{4\pi m}$	0.9938
II.34.29b	$E = \frac{g \mu_M B J_z}{\hbar}$	0.9037
II.35.18	$n = \frac{n_0}{\exp(\mu_m B/(k_b T)) + \exp(-\mu_m B/(k_b T))}$	0.9738
II.35.21	$M = n_\rho \mu_M \tanh(\frac{\mu_M B}{k_b T})$	0.8537
II.36.38	$f = \frac{\mu_m B}{k_b T} + \frac{\mu_m \alpha M}{\epsilon c^2 k_b T}$	0.9928
II.37.1	$E = \mu_M(1 + \chi)B$	0.9999
II.38.3	$F = \frac{YA_x}{d}$	0.9985
II.38.14	$\mu_S = \frac{Y}{2(1+\sigma)}$	0.9988
III.4.32	$n = \frac{1}{e^{\frac{\hbar\omega}{k_b T}} - 1}$	0.9903
III.4.33	$E = \frac{\hbar\omega}{e^{\frac{\hbar\omega}{k_b T}} - 1}$	0.9984
III.7.38	$\omega = \frac{\hbar}{2\mu_M B}$	0.9973
III.8.54	$p_\gamma = \sin(\frac{Et}{\hbar})^2$	0.9973
III.9.52	$p_\gamma = \frac{p_d E_f t}{\hbar} \frac{\sin((\omega - \omega_0)t/2)^2}{((\omega - \omega_0)t/2)^2}$	0.8036
III.10.19	$E = \mu_M \sqrt{B_x^2 + B_y^2 + B_z^2}$	0.9935
III.12.43	$L = n\hbar$	0.9999
III.13.18	$v = \frac{2Ed^2 k}{\hbar}$	0.9935
III.14.14	$I = I_0(e^{\frac{qV_e}{k_b T}} - 1)$	0.9927
III.15.12	$E = 2U(1 - \cos(kd))$	0.9993
III.15.14	$m = \frac{\hbar^2}{2E d^2}$	0.9927
III.15.27	$k = \frac{n^d}{2\pi\alpha}$	0.9999
III.17.37	$f = \beta(1 + \alpha \cos\theta)$	0.9938
III.19.51	$E = \frac{-mg^4}{2(4\pi\epsilon)^2 \hbar^2} \frac{1}{n^2}$	0.9974
III.21.20	$j = \frac{-\rho_{c0} q A_{vec}}{m}$	0.8668

Table 13: Tested Feynman Equations, part 2.