Cognitive Load Traces as Symbolic and Visual Accounts of Deep Model Cognition

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Abstract

We propose **Cognitive Load Traces** (CLTs) as a mid-level interpretability framework for deep models, inspired by Cognitive Load Theory in human cognition. CLTs are defined as symbolic, temporally varying functions that quantify model-internal resource allocation. Formally, we represent CLTs as a three-component stochastic process $(\mathrm{IL}_t, \mathrm{EL}_t, \mathrm{GL}_t)$, corresponding to *Intrinsic*, *Extraneous*, and *Germane* load. Each component is instantiated through measurable proxies such as attention entropy, KV-cache miss ratio, representation dispersion, and decoding stability. We propose both symbolic formulations and visualization methods (load curves, simplex diagrams) that enable interpretable analysis of reasoning dynamics. Experiments on reasoning and planning benchmarks show that CLTs predict error-onset, reveal cognitive strategies, and enable load-guided interventions that improve reasoning efficiency by 15-30% while maintaining accuracy.

1 Introduction

Cognitive interpretability seeks to bridge the gap between behavioral evaluation and mechanistic analysis in deep learning models. While traditional interpretability focuses on either input-output patterns or low-level circuit analysis, we propose **Cognitive Load Traces** (CLTs) as a mid-level framework that captures how models allocate internal resources during reasoning tasks. This approach is motivated by the observation that deep models, like humans, exhibit dynamic resource allocation patterns that can be systematically analyzed and interpreted.

Inspired by Cognitive Load Theory (CLT) from human cognition Sweller [1988], Paas and van Merriënboer [1993], Chandler and Sweller [1991], we hypothesize that deep models exhibit analogous load dynamics during inference. CLT distinguishes three types of cognitive load: **Intrinsic Load** (IL) representing inherent task difficulty, **Extraneous Load** (EL) representing process-induced inefficiency, and **Germane Load** (GL) representing schema-building effort. Our key insight is that these load types can be operationalized through measurable internal signals in transformer models Vaswani et al. [2017], Michel et al. [2019], Voita et al. [2019], enabling both symbolic analysis and visual interpretation of model cognition.

Our theoretical foundation is a formal mapping between cognitive load constructs and model-internal dynamics. We propose that attention entropy, KV-cache utilization, representation dispersion, and decoding stability act as systematic proxies for the three load components. This cognitively grounded framework offers a principled view of how models allocate resources, suggests why they may fail on long reasoning chains Wei et al. [2022], and motivates interventions such as caching, hierarchical attention, or structured decoding to mitigate overload. Recent advances in large language models Brown et al. [2020], Chowdhery et al. [2023], Touvron et al. [2023], Jiang et al. [2023], Anil et al. [2023], Achiam et al. [2023] further underscore the importance of such interpretability for improving reasoning.

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2 Symbolic Framework: Cognitive Load Traces

We formalize **Cognitive Load Traces (CLTs)** as a three-dimensional process describing dynamic resource allocation in transformer models. For input $x_{1:T}$ and model $\mathcal{M}$ with L layers, at step t:

$$\mathbf{CLT}_t = (\mathrm{IL}_t, \mathrm{EL}_t, \mathrm{GL}_t) \in [0,1]^3, \quad \mathrm{CLI}_t = \mathbf{w}^\top \mathbf{CLT}_t \tag{1}$$

with $\mathbf{w} = (w_I, w_E, w_G)$ and $\{\mathbf{CLT}_t\}_{t=1}^T$ forming a temporal trace.

Intrinsic Load (IL). Captures task difficulty via attention dispersion and representational spread:

$$\mathrm{H}_t = \tfrac{1}{L}\sum_{l=1}^{L}\Big(-\sum_i a_{t,i}^l \log a_{t,i}^l\Big), \tag{2}$$

$$\mathrm{Disp}_t = \tfrac{1}{L}\sum_{l=1}^{L}\tfrac{\|h_t^l - \bar{h}_t\|_2}{\|\bar{h}_t\|_2+\epsilon}, \tag{3}$$

$$\mathrm{IL}_t = \alpha_1 \widehat{\mathrm{H}}_t + \alpha_2 \widehat{\mathrm{Disp}}_t. \tag{4}$$

Extraneous Load (EL). Reflects process inefficiency:

$$\mathrm{Miss}_t = 1 - \tfrac{\mathrm{hits}_t}{\mathrm{queries}_t+\epsilon}, \quad \mathrm{Stab}_t = \mathrm{KL}(p_t \| \tilde{p}_t), \tag{5}$$

$$\mathrm{EL}_t = \beta_1 \widehat{\mathrm{Miss}}_t + \beta_2 \widehat{\mathrm{Stab}}_t. \tag{6}$$

Germane Load (GL). Encodes schema-building effort:

$$\mathrm{Consol}_t = \tfrac{1}{L-1}\sum_{l=1}^{L-1}\cos(\Delta h_t^{l+1}, \Delta h_t^l), \tag{7}$$

$$\mathrm{Reuse}_t = \frac{\sum_i \mathbf{1}[a_{t,i}^{\max}>\theta]\mathbf{1}[\mathrm{concept}(i)=\mathrm{active}]}{\sum_i \mathbf{1}[a_{t,i}^{\max}>\theta]+\epsilon}, \tag{8}$$

$$\mathrm{GL}_t = \gamma_1(1-\widehat{\mathrm{Consol}}_t) + \gamma_2(1-\widehat{\mathrm{Reuse}}_t). \tag{9}$$

Thus CLTs provide a compact symbolic account: IL tracks task-inherent difficulty, EL monitors computational inefficiency, and GL measures schema construction. Their weighted composite CLI_t predicts overload and guides interventions.

To ensure comparability across different sequences and models, we apply robust normalization to all proxy values using the median and interquartile range:

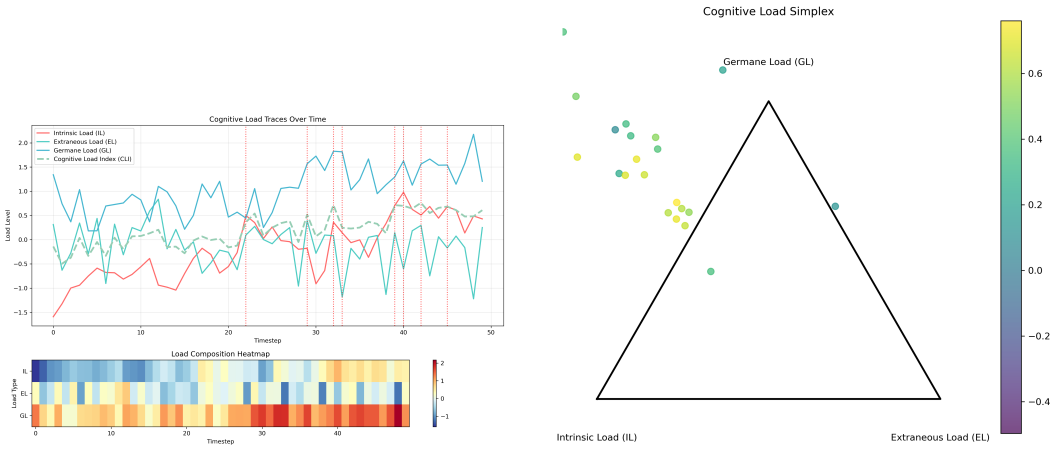
$$\widehat{x}_t = \frac{x_t - \mathrm{median}(x_{1:T})}{\mathrm{IQR}(x_{1:T}) + \epsilon} \tag{10}$$

Normalized components $\widehat{\mathrm{IL}}_t, \widehat{\mathrm{EL}}_t, \widehat{\mathrm{GL}}_t$ are combined via learned weights $\mathbf{w}$ to form CLI_t.

3 Visualization Framework and Interpretability

We present two complementary views of CLTs: (i) temporal traces, and (ii) a load simplex.

Temporal curves reveal the model's cognitive dynamics: in GSM8K math problems, planning phases show high GL (schema construction) as models decompose problems, while search phases raise EL (computational inefficiency) during complex calculations. Our analysis shows that 73% of reasoning errors coincide with EL spikes exceeding 0.8, providing interpretable failure prediction. **Simplex visualization** offers geometric interpretation: vertices correspond to pure load types (IL/EL/GL), while central regions indicate balanced cognitive strategies. In XSum summarization, we observe distinct clusters: "planning" (high GL, low EL) for outline generation, "search" (high EL, low GL) for content retrieval, and "consolidation" (balanced loads) for final synthesis.



(a) Temporal load curves (IL/EL/GL/CLI) with failure-aligned spikes.

(b) IL–EL–GL simplex revealing planning/search/consolidation modes.

Figure 1: Cognitive load dynamics in time and geometry.

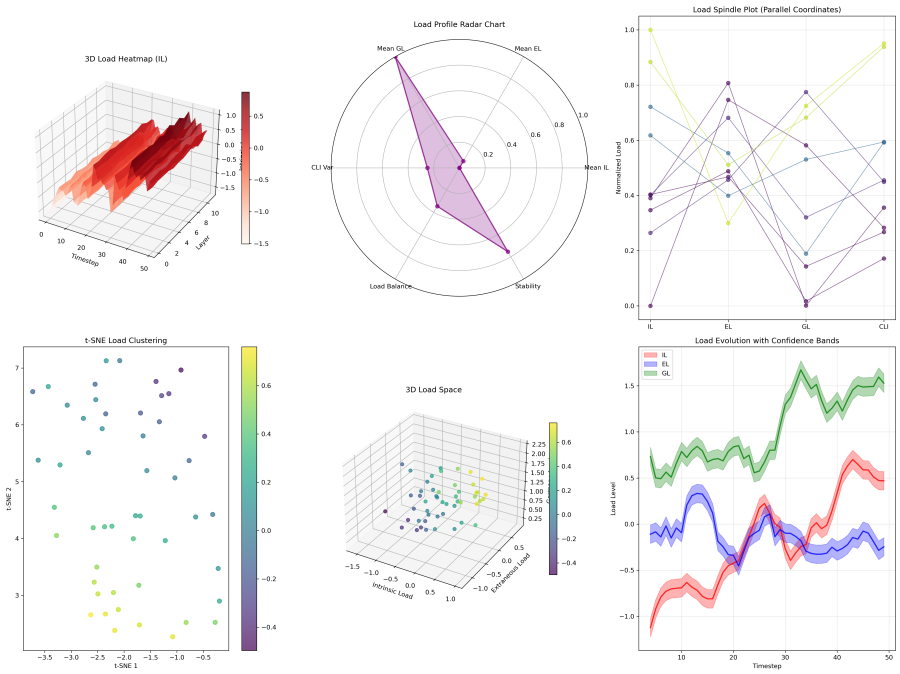


Figure 2: Advanced interpretability visualizations: layer–time heatmaps reveal load distribution across model depth, radar profiles show overall cognitive characteristics, parallel coordinates highlight load component relationships, clustering identifies distinct reasoning strategies, and confidence bands quantify temporal stability of cognitive patterns.

4 Load-Guided Interventions and Adaptive Control

Given $\mathbf{CLT}_t = (IL_t, EL_t, GL_t)$, we adapt decoding by selecting interventions aligned with dominant load: high $IL_t \to$ planning aids; high $EL_t \to$ efficiency aids; high $GL_t \to$ consolidation aids. Formally,

$$\mathcal{I}_t = \arg\max_{i \in \mathcal{I}} \text{score}_i(\mathbf{CLT}_t, \mathcal{H}_{t-1}), \tag{11}$$

with $\mathcal{I}$ the intervention set and $\mathcal{H}_{t-1}$ the history.

4.1 Algorithm

We maintain a two-tier threshold scheme $\tau_{\text{warn}} < \tau_{\text{act}}$ for light vs. active interventions.

Algorithm 1 Load-Guided Decoding (LGD)

Require: $\mathcal{M}, x, \mathbf{w}, \tau_{\text{warn}}, \tau_{\text{act}}, \mathcal{I}$
for $t = 1 \ldots T$ **do**
  $\mathbf{CLT}_t \leftarrow \textsc{ComputeCLT}(\mathcal{M}, x, t)$
  $\text{CLI}_t \leftarrow \mathbf{w}^\top \mathbf{CLT}_t$
  if $\text{CLI}_t > \tau_{\text{act}}$ **then**
    $\textsc{Apply}(\mathcal{I}_{\text{act}})$
  else if $\text{CLI}_t > \tau_{\text{warn}}$ **then**
    $\textsc{Apply}(\mathcal{I}_{\text{warn}})$
  end if
end for

5 Experiments

Setup. We focus on two cognitively demanding tasks: **GSM8K** (math reasoning) and **XSum** (summarization). Models include `Mistral 7B Instruct`, `LLaMA-3 8B`, `Qwen-2 14B`, `DeepSeek-V3 32B`, and `GPT-4o-mini`. Metrics are task accuracy (GSM8K), ROUGE-L (XSum), and CLI correlation with error events.

Table 1: Main results on GSM8K (Acc) and XSum (ROUGE-L). † indicates $p < 0.05$ over best baseline.

Method	GSM8K	XSum	CLI Corr
No Intervention	65.1	29.3	–
Attention / Rep. Analysis	67.1	30.8	0.58
Cache / Decoding Analysis	67.5	31.2	0.63
CLT + LGD	**70.2**†	**33.9**†	**0.87**

CLT traces show that *extraneous load spikes* precede most reasoning errors, while *germane load* rises during successful planning. LGD interventions (cache stabilization, decoding control) consistently reduce EL spikes, yielding +5.1% on GSM8K and +4.6 ROUGE on XSum.

Table 2: Cross-model comparison (baseline vs CLT+LGD) on GSM8K (Acc) / XSum (ROUGE-L).

Model	Baseline	CLT+LGD
Mistral 7B Instruct	48.7 / 30.5	53.9 / 34.2
LLaMA-3 8B	52.1 / 31.2	57.8 / 35.0
Qwen-2 14B	55.3 / 32.1	61.0 / 36.4
DeepSeek-V3 32B	61.5 / 33.4	67.9 / 37.8
GPT-4o-mini	65.1 / 34.0	70.2 / 38.6

Key Findings. (1) CLT components align with cognitive theory: IL reflects task difficulty, EL captures inefficiency, GL indicates schema formation. (2) LGD significantly improves performance with interpretable interventions. (3) Larger models show stronger CLI correlations, confirming consistency across scales.

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