What Do Mixture-of-Depth Routers Learn? Routing Patterns in Gemma 2

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Abstract

Mixture-of-Depths (MoD) routers improve efficiency of transformer models by learning which tokens to process and which to bypass at each layer. However, their learned routing patterns have not been characterized in alternating-attention architectures, which mix local attention with sparse global attention to increase efficiency. We evaluate routing by training token-level MoD routers on Gemma 2 2B and find that the mean routing rate is significantly higher in full-attention layers than at sliding-window layers. We find that a token's part of speech is correlated with whether the router skips or processes it, and that the same category is often routed differently at different layers: for example, determiners tend to be skipped at the shallowest target layer but preserved at deeper ones. Decomposing the router's input with pre-trained sparse autoencoders shows the decision is distributed over ~50–200 predominantly semantic features and suppressing the skip-aligned features causally flips 30.6% of routing decisions at the deepest routing layer.

1. Introduction

Transformer language models process every token at every layer, regardless of how much computation that token actually requires. This is wasteful since not all tokens benefit equally from every layer. Mixture-of-Depths (MoD) (Raposo et al., 2024) addresses this inefficiency by adding a small, per-layer router (typically a single linear layer) that decides, for each token at each transformer block, whether the token receives full attention processing or bypasses the block via the residual stream. Router-Tuning (He et al., 2025) extends MoD to a parameter-efficient variant that trains only the routers on a frozen base model, which allows us to study the behavior of learned MoD routers.

In recent work (Gadhikar et al., 2024; Zhang et al., 2024; Tan et al., 2024; Luo et al., 2025; Laitenberger et al., 2026) the router is treated as an efficiency mechanism: given a target capacity (the fraction of tokens to process per layer), the router is trained to meet it and evaluated by perplexity at that capacity. The question of *what patterns these routers learn* and whether their decisions reflect any identifiable structure beyond standard token-importance heuristics has not been systematically investigated. Existing MoD work has focused on uniform-attention transformers, where every block uses the same attention type. Modern architectures such as Gemma 2 (Team et al., 2024) alternate full and sliding-window attention layer-by-layer, which could result in different router behavior. No prior work, to our knowledge, has trained MoD on such an architecture or characterized learned routing decisions in this regime. This is important because efficient-inference designs typically assume token importance reduces to simple heuristics (e.g., norm, attention scores), but if routers encode layer-conditional functions instead, then routing decisions can also be used for interpretability purposes rather than solely as an efficiency mechanism.[1]

We investigate the following research questions:

- **RQ1:** Do trained MoD routers route differently at full-attention vs. sliding-window layers in Gemma2 2B?
- **RQ2:** Can the differences be explained by simpler architectural properties e.g., (a) layer-aggregate residual-stream norm, (b) per-token residual-stream norm, or (c) per-layer task-loss sensitivity to attention ablation?
- **RQ3:** Do routing decisions encode interpretable linguistic features beyond token importance e.g., can per-token routing rate be predicted from part-of-speech tags?
- **RQ4:** Can routing be decomposed into interpretable sparse-autoencoder (SAE) features, and can those features be verified?

2. Related Work

Raposo et al. (2024) introduced MoD and He et al. (2025) proposed Router-Tuning. Subsequent dynamic-depth work

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[1]Code, trained routers, and evaluation outputs are available at https://github.com/steinpleiter/mod-router-interp.

Figure 1. Setup. Gemma 2 2B alternates full and sliding-window attention layer-by-layer; we add token-level MoD routers to layers 12–24 (∼30K trained parameters, base model frozen). Inset: at each MoD-target block a linear router reads the per-token residual h_t^ℓ and emits $r_t^\ell = \sigma(W_\ell^\top h_t^\ell)$, binarized at 0.5; when $r_t^\ell = 0$ the attention sub-layer is skipped and the residual passes through unchanged. The MLP sub-layer is unaffected.

has explored alternatives to learned routers: attention-based routing (Gadhikar et al., 2024), post-hoc adaptation of pre-trained models (Zhang et al., 2024; Tan et al., 2024), multimodal MoD (Luo et al., 2025), and residual-stream gating (Laitenberger et al., 2026). Lawson & Aitchison (2025) report that learning to skip middle layers fails to improve over dense baselines, motivating the finer-grained per-token routing MoD provides. All of these works treat the router as an efficiency mechanism. In contrast, our work is aimed at analyzing and interpreting what the router has learned.

The work most related to ours is Antoine et al. (2024), who train MLP probes over routing paths in six Mixture-of-Experts models and find that part-of-speech is predictive of expert assignment, treating routing as a multi-class expert-selection problem. Our work differs in the following ways: (1) we ask whether part-of-speech predicts the binary skip/process decision in MoD, rather than the multi-class expert assignment they study, (2) we investigate an alternating-attention architecture rather than the uniform-attention MoE models they study, and (3) we identify layer-conditional sign flips; the same POS preferentially skipped at one target layer can be preserved at another.

Michel et al. (2019) and Voita et al. (2019) score each attention head by the impact of removing it and find that many heads can be uniformly pruned with little task degradation; MoD routers instead make a per-token, per-layer, context-dependent decision. To our knowledge, no prior work has trained MoD on an alternating-attention architecture or investigated their routing behavior.

3. Problem Formulation

Routers should not degrade the original model: a severely degraded model would still produce routing structure, but that structure would reflect the decrease in performance rather than the mechanism we want to study. We therefore validate downstream performance before analyzing routing decisions (Table 1, Section 4).

We start from Gemma 2 2B (Team et al., 2024), a 26-layer decoder-only language model whose transformer blocks alternate full and sliding-window attention layer-by-layer. We add token-level MoD routing to the deepest 13 layers (layers 12–24) and leave layer 25 dense, following He et al. (2025)'s convention of targeting the deepest layers except the last, based on prior evidence that deeper layers are more redundant than shallow ones, which carry essential representations. We train only the routers on a frozen base model so that any structure observed in routing decisions reflects what the router has learned to read from fixed base-model representations. This means that any routing structure we observe must already exist in the pre-trained residual stream; it cannot be the result of the base model adapting its representations to make routing easier.

Following He et al. (2025) Eq. 1 (token-level variant), and as illustrated in Figure 1, at each MoD-target layer ℓ a single linear router $W_\ell \in \mathbb{R}^d$ produces a per-token routing score $r_t^\ell = \sigma(W_\ell^\top h_t^\ell)$ (with σ the sigmoid), binarized via a straight-through estimator at threshold 0.5. We freeze the base-model weights and train only the routers (∼30K parameters in total) against a combined loss $\mathcal{L} = \mathcal{L}_{\text{task}} + \lambda \cdot \text{ReLU}(\bar{c} - c^*)$, where $\bar{c}$ is the mean routing rate across the batch, $c^* = 0.5$ is the target capacity (the desired fraction of tokens to process per layer), and λ is the gradient scale on the capacity penalty (higher λ enforces stricter targeting; lower λ lets task loss dominate). Following He et al. (2025), we train routers using causal language-modeling loss (next-token cross-entropy) on the Alpaca instruction-tuning corpus: 52K (instruction, response) pairs from Stanford CRFM and evaluate on a held-out corpus (WikiText-2 (Merity et al., 2016)).

4. Experiments

We train four checkpoints testing $\lambda \in \{0.01, 0.1\}$ with two training scales (5K samples $\times$ 1 epoch; 52K $\times$ 3 epochs), spanning an order of magnitude on each axis: **strict-short** (λ=0.1, 5K $\times$ 1), **gentle-short** (λ=0.01, 5K $\times$ 1), **gentle-long** (λ=0.01, 52K $\times$ 3), and **strict-long** (λ=0.1, 52K $\times$ 3). **Strict-long** serves as our main checkpoint for per-token analyses (RQ2b, RQ3, RQ4, Appendix B).

Validation: Our **strict-long** setting processes 62% of tokens (target 50%), raising WikiText-2 perplexity from 17.1 to 24.4. Because He et al. (2025) validate Router-Tuning on downstream *accuracy*, we measure acc_norm on HellaSwag and ARC-Challenge (300 items per task; Table 1). Although we observe a modest drop in performance, the model is still functioning overall.

Table 1. Base Gemma 2 2B vs. the **strict-long** MoD model, length-normalised accuracy on 300 items per task. Each cell is base $\rightarrow$ MoD; Δ is the mean change on identical items. The 10/25-shot row is the field-standard protocol (HellaSwag 10-shot, ARC-Challenge 25-shot).

Setting	HellaSwag	ARC-Challenge	Avg. Δ
0-shot	$0.640 \rightarrow 0.577$	$0.500 \rightarrow 0.413$	-7.5pp
5-shot	$0.663 \rightarrow 0.613$	$0.520 \rightarrow 0.470$	-5.0pp
10/25-shot	$0.657 \rightarrow 0.600$	$0.517 \rightarrow 0.453$	-6.0pp

To determine if a router that sees *only* per-token norm can reproduce the attention-type difference, we train a 2-parameter-per-layer baseline router $\sigma(s_\ell \|h\| + b_\ell)$: a learned scale and offset on the per-token residual-stream norm under **strict-long**'s training configuration.

All evaluation is on WikiText-2 test (200 documents tokenized and truncated to max-length 256; 33,608 tokens total). For each ℓ, we record the per-token routing decision $r_t^\ell \in \{0, 1\}$ and the per-token residual stream entering the layer. In our per-token analyses, we exclude the first 4 positions per sample to avoid attention-sink outliers (Xiao et al., 2024), leaving 32,808 tokens.

4.1. RQ1: Full vs. Sliding Window Attention

For each WikiText-2 sample and depth range $\mathcal{R}$, we compute mean routing rates across full-attention and sliding-window MoD layers in $\mathcal{R}$ and test significance using a paired t-test. We report effect size as Cohen's d, the standardized mean difference (Cohen, 1988), with thresholds in $\{0.2, 0.5, 0.8\}$ corresponding to small/medium/large effects.

Table 2 reports the paired t-test for full vs. sliding mean routing rate within each depth range, across all four trained checkpoints. In shallow-middle MoD (layers 12–20), every checkpoint shows positive direction (mean routing rate is higher at full-attention layers than at sliding-window layers,

$d > 0$), with Cohen's $d \in [0.31, 2.06]$ and all $p < 10^{-4}$, where **gentle-long** has the lowest skip rate (24% vs. 29–46% in the others). The spread follows from the capacity penalty's asymmetry: $\text{ReLU}(\bar{c} - c^*)$ supplies no gradient at or below the target, so under the gentle penalty with extended training the task loss dominates. In deep MoD (layers 21–24) the results are more mixed: null in **strict-short**, reversed in **gentle-short**, weakly positive in **gentle-long**, strongly positive in **strict-long**. We note that both long runs (**gentle-long**, **strict-long**) show positive direction in deep MoD, while the two short-training runs (**strict-short**, **gentle-short**) do not. This indicates that the router routes differently by attention type in shallow-middle MoD across all four configurations, while the deep-MoD direction is inconsistent.

Table 2. Paired full vs. sliding t-test across all four trained checkpoints, in shallow-middle MoD (layers 12–20) and deep MoD (layers 21–24). Shallow-middle direction is consistent across all four runs; deep direction varies.

Run	Skip	Cohen's d	full > slid %	p
Shallow-middle MoD (layers 12–20)				
strict-short	45.5%	$+1.33$	86.5%	$4 \cdot 10^{-46}$
gentle-short	28.5%	$+2.06$	98.5%	$1 \cdot 10^{-73}$
gentle-long	23.9%	$+0.31$	62.0%	$2 \cdot 10^{-5}$
strict-long	38.3%	$+0.86$	78.5%	$9 \cdot 10^{-26}$
Deep MoD (layers 21–24)				
strict-short	45.5%	-0.03	53.5%	0.64
gentle-short	28.5%	-1.00	11.5%	$6 \cdot 10^{-32}$
gentle-long	23.9%	$+0.35$	65.0%	$2 \cdot 10^{-6}$
strict-long	38.3%	$+1.23$	88.0%	$1 \cdot 10^{-41}$

The norm-only baseline reproduces the shallow-middle difference more extremely ($d = 6.5$ on **strict-long**'s training configuration) but has $\approx 4.5\times$ higher training perplexity than the learned linear router. The difference is present even from a minimal-capacity router under MoD training, while the learned linear router uses richer signal than norm alone.

4.2. RQ2: Influence of Architectural Properties

Next, we investigate the influence of three architectural properties on routing behavior: layer-aggregated norm, per-token norm, and task-loss asymmetry.

Layer-aggregate norm (RQ2a): If the router preferred high-norm layers, full-attention layers would be preserved if and only if they had higher residual-stream norms at their input. A paired t-test on residual-stream norms in shallow-middle shows the opposite: full-attention layers have *lower* norms than sliding-window layers, both in base Gemma 2 2B (mean $\|h\|$ 83.86 vs. 84.76, $d = -3.02$) and in the strict-long MoD context (82.97 vs. 84.31, $d = -3.86$) – the opposite direction from the routing difference.

Per-token norm (RQ2b): If the router decided based on per-token norm alone, its score should correlate with per-token $\|h\|$ (Pearson correlation). For each MoD layer we compute the Pearson correlation r between the **strict-long** router's score and the per-token residual-stream norm. Mean $|r| = 0.166$ across MoD layers, max $|r| = 0.336$ at layer 17. At maximum, norm explains $r^2 \approx 11\%$ of variance in the router's score, so per-token norm cannot account for the attention-type difference observed in RQ1.

Task-loss asymmetry (RQ2c): If full-attention layers were more important than sliding-window layers, ablating them would raise perplexity more. We ablate each MoD-target attention sub-block in isolation in base Gemma 2 2B by zeroing the layer's attention output while leaving the rest intact, and measuring the resulting WikiText-2 perplexity. In shallow-middle MoD layers, ablating full-attention layers raises perplexity by $+1.56$ on average while ablating sliding-window layers raises it by $+1.22$. The $+0.34$ difference is not statistically significant (Welch's t-test, $p = 0.44$; Welch's variant is used because the two groups have unequal sample sizes and possibly unequal variances). To check for a generic depth effect (any deeper layer costing more to ablate regardless of attention type), we repeat the procedure on each layer's MLP sub-block but do not detect a per-layer-importance asymmetry ($p = 0.88$).

4.3. RQ3: POS Probe for Layer-Dependent Routing

POS is a syntactic property densely encoded in transformer residual streams (Tenney et al., 2019) and is the analysis target in the related MoE-routing study (Antoine et al., 2024), enabling direct comparison. For 200 WikiText-2 samples we tokenize once with spaCy (Honnibal et al., 2020) (word-level POS) and once with the Gemma 2 SentencePiece tokenizer (Team et al., 2024) (subword), assigning each subword token the POS of the spaCy word whose character span contains the subword's midpoint. Per layer, we compute (i) for each POS tag, whether its routing rate differs from the layer's marginal rate $\bar{P}(\text{process})$ using a binomial test (since each routing decision is binary), Bonferroni-corrected across 16 tags per layer; and (ii) a logistic regression from POS one-hot to router decision.

Figure 2 shows five selected tags (full 16-tag tables in Section A); all plotted values are Bonferroni-significant at $\alpha' = 0.0031$.

Aggregate probe: A logistic regression from POS one-hot to router decision achieves test accuracy 0.576 at layer 13 and 0.597 at layer 24, vs. majority baselines of 0.510 and 0.506. At layer 23 the aggregate probe matches the majority baseline. This indicates that POS predicts routing better than majority chance at L13 and L24, indicating that routing decisions encode part-of-speech information.

Figure 2. Per-POS deviation from the layer's marginal routing rate, $(P(\text{process} \mid \text{POS}) - \bar{P}(\text{process})) \times 100\text{pp}$, at the three target layers. Determiners and punctuation invert between layers; SPACE (dashed) swings from universally skipped to universally preserved and back.

Layer-dependent inversions: Determiners tend to be skipped at layer 13 (-11pp) and preserved at deeper layers ($+11\text{pp}$ at layer 23, $+14\text{pp}$ at layer 24) – a shallow-vs-deep inversion. Punctuation preserves the same direction across full-attention layers (kept: $+17\text{pp}$ at layer 13, $+7.5\text{pp}$ at layer 23) but flips at the deepest sliding-window layer (-22pp at layer 24). Space tokens are universally skipped at layer 13 (0%), universally preserved at layer 23 (100%), and tend to be skipped at layer 24 (17%). This indicates that the router treats the same syntactic category differently at different layers, rather than applying a fixed priority across layers.

4.4. RQ4: SAE Decomposition and Causal Intervention

RQ3 shows routing correlates with syntax but not what exactly the features are. We decompose the residual entering each target layer with pre-trained Gemma Scope SAEs (Lieberum et al., 2024) (width 16K; reconstruction quality on MoD activations in Section B). Because the router at layer ℓ takes $\text{resid\_pre}(\ell) = \text{resid\_post}(\ell - 1)$ as input, we use the SAE trained at layer $\ell - 1$; hooking $\text{resid\_post}(\ell)$ instead would be confounded, since that residual already contains the attention output the layer-ℓ gate decided to add or skip. Because the router is linear, a feature it can read must appear as a linear correlate of its score, so we rank features by Pearson correlation with the router score.

Collective decomposition: We find that no single feature governs routing: the strongest correlation found across the three layers is $|r| = 0.362$ ($r^2 \approx 0.13$). We believe this is due to feature superposition, and therefore a linear router will integrate many overlapping directions by construction. We rank features on a training split of tokens, fit ridge regression on the top-k, and evaluate R^2 on a held-out set (split by document). At $k = 200$, selected features reach $R^2 \approx 0.44$–0.49 across the three layers, against ≈ 0.09–0.12 for k

Figure 3. The intervention on one real token (layer 24): suppressing the 64 skip-cue features (circled) among 216 active moves the router from $P(\text{process}) = 0.19$ to 0.61, flipping the decision from skip to process.

random features, indicating that the routing decision is distributed over a collection of features, rather than specified by one particular feature. Classifying the top-200 by *POS-retention*, i.e., the fraction of a feature's routing correlation that remains after controlling for the token's POS tag, shows 64–78% of features per layer carry content beyond POS.

Causal intervention: To test whether these features are responsible for routing or if they are simply correlated with it, we investigate what happens if we suppress or amplify specific features. We encode each token's residual, suppressing/amplifying a feature set, decode, and recompute the router score. Two controls are necessary: (1) the counterfactual runs through the same SAE pipeline, since comparing against the *real* model score would mix reconstruction error into the measured effect and (2) every effect is compared against a *frequency-matched null* of random features from the same activation-frequency deciles, since zeroing many high-firing features changes the residual regardless of relevance. We pre-registered a success criterion of a $\geq 10\text{pp}$ conditional flip rate with $\geq 70\%$ of flips in the predicted direction (the *direction rate*).

Suppressing the skip-cue (negative-sign) feature collection shifts routing toward *process* at every layer, exceeding the null-adjusted criterion (Figure 3): at layer 24 it flips 30.6% of active-token decisions with a 100% direction rate, $+27.4\text{pp}$ above the null, and amplifying the same collection moves routing the opposite way. A held-out replication (identify features on one document half, intervene on the other, disjoint half) retains 97–99% of the margin (Section C), so the effect is not token-level selection bias. Among features that fire often enough to measure, the correlation sign predicts causal direction for 76–96% per layer, indicating that the features discovered by the SAE can be used to enforce routing behavior.

5. Discussion and Conclusion

We trained four MoD router configurations on Gemma 2 2B. Across all four, routing rate is higher at full-attention than

sliding-window layers in shallow-middle MoD (Cohen's d up to 2.06, all $p < 10^{-4}$); this is the attention-type difference posed by RQ1. None of the three properties tested in RQ2 explains it: layer-aggregate norm is negatively correlated with token processing, per-token norm explains at most $\sim$11% of router-score variance, and per-layer ablation shows no detectable importance asymmetry. In RQ3, we find that part of speech predicts routing at every target layer, with a layer-conditional prediction function i.e., the same POS can be preferentially preserved at one layer and skipped at another. In RQ4, we show that the routing decisions are reflected by $\sim$50–200 predominantly semantic SAE features. Our results contradict the implicit assumption in efficiency-oriented MoD work that token importance reduces to simple heuristics. *We find that the router makes distributed, mostly content-based decisions.*

Our work has some limitations. First, the probing results in RQ3 are primarily correlational since the residual stream encodes POS densely (residual-to-POS probe accuracy > 0.93 at all three target layers), so any direction in residual space will correlate with some POS structure. All RQ4 results are tested using the pretrained Gemma Scope SAE, trained on base Gemma, not on our MoD-tuned activations, therefore every intervention is compared within the SAE pipeline.

In Gemma 2, every full-attention layer has an odd index and every sliding-window layer has an even index, so the RQ1 result could mean either: "the router prefers full attention" or "the router prefers odd layers". Separating them would require a model where the two vary independently. The RQ3 POS results aren't subject to this since each per-tag effect exists within a single layer where attention type and parity are both fixed.

Replication on a second alternating-attention architecture would disentangle the parity confound, and patching POS-specific directions would test whether the router reads part of speech itself (Section 4.3).

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A. Full Per-POS Effect Tables

Tables 3 to 5 report the full per-POS routing analysis on strict-long MoD activations at each target layer, for all 16 POS tags with $n \geq 30$ tokens. Each entry shows the number of tokens with that POS, the empirical $P(\text{process} \mid \text{POS})$, the deviation from the layer's marginal routing rate $\Delta = P(\text{process} \mid \text{POS}) - \bar{P}(\text{process})$, and the binomial test p-value. The pre-committed threshold from Section 3 requires both Bonferroni significance at $\alpha' = 0.05/16 = 0.0031$ and effect size $|\Delta| \geq 5\text{pp}$; entries meeting both are marked ✓.

Table 3. Layer 13 (full attention, shallow). Marginal $\bar{P}(\text{process}) = 0.490$, $n_{\text{total}} = 31{,}229$.

POS	n	$P(\text{process} \mid \text{POS})$	Δ (pp)	p	Pass
ADJ	1,919	0.447	-4.4	$1.4 \cdot 10^{-4}$	
ADP	3,273	0.591	$+10.0$	$1.2 \cdot 10^{-30}$	✓
ADV	760	0.566	$+7.6$	$3.4 \cdot 10^{-5}$	✓
AUX	868	0.536	$+4.6$	$7.3 \cdot 10^{-3}$	
CCONJ	772	0.808	$+31.8$	$1.8 \cdot 10^{-74}$	✓
DET	2,812	0.377	-11.3	$1.6 \cdot 10^{-33}$	✓
NOUN	5,634	0.414	-7.7	$1.0 \cdot 10^{-30}$	✓
NUM	3,064	0.547	$+5.7$	$3.1 \cdot 10^{-10}$	✓
PART	628	0.465	-2.5	$2.2 \cdot 10^{-1}$	
PRON	872	0.412	-7.8	$3.9 \cdot 10^{-6}$	✓
PROPN	4,635	0.485	-0.5	$4.7 \cdot 10^{-1}$	
PUNCT	3,052	0.661	$+17.1$	$1.7 \cdot 10^{-80}$	✓
SCONJ	214	0.388	-10.2	$3.2 \cdot 10^{-3}$	
SPACE	165	0.000	-49.0	$6.7 \cdot 10^{-49}$	✓
SYM	65	0.415	-7.5	$2.6 \cdot 10^{-1}$	
VERB	2,468	0.361	-13.0	$2.1 \cdot 10^{-38}$	✓

Table 4. Layer 23 (full attention, deep). Marginal $\bar{P}(\text{process}) = 0.613$, $n_{\text{total}} = 31{,}229$.

POS	n	$P(\text{process} \mid \text{POS})$	Δ (pp)	p	Pass
ADJ	1,919	0.747	$+13.4$	$3.0 \cdot 10^{-35}$	✓
ADP	3,273	0.570	-4.3	$5.4 \cdot 10^{-7}$	
ADV	760	0.670	$+5.6$	$1.4 \cdot 10^{-3}$	✓
AUX	868	0.631	$+1.8$	$3.0 \cdot 10^{-1}$	
CCONJ	772	0.812	$+19.9$	$1.1 \cdot 10^{-32}$	✓
DET	2,812	0.729	$+11.5$	$9.3 \cdot 10^{-38}$	✓
NOUN	5,634	0.555	-5.9	$2.6 \cdot 10^{-19}$	✓
NUM	3,064	0.676	$+6.2$	$9.8 \cdot 10^{-13}$	✓
PART	628	0.699	$+8.6$	$9.1 \cdot 10^{-6}$	✓
PRON	872	0.507	-10.7	$2.1 \cdot 10^{-10}$	✓
PROPN	4,635	0.489	-12.5	$4.7 \cdot 10^{-66}$	✓
PUNCT	3,052	0.688	$+7.5$	$1.1 \cdot 10^{-17}$	✓
SCONJ	214	0.561	-5.3	$1.2 \cdot 10^{-1}$	
SPACE	165	1.000	$+38.7$	$1.2 \cdot 10^{-35}$	✓
SYM	65	0.415	-19.8	$1.3 \cdot 10^{-3}$	✓
VERB	2,468	0.546	-6.8	$8.4 \cdot 10^{-12}$	✓

Table 5. Layer 24 (sliding-window attention, deep). Marginal $\bar{P}(\text{process}) = 0.494$, $n_{\text{total}} = 31{,}229$.

POS	n	$P(\text{process} \mid \text{POS})$	Δ (pp)	p	Pass
ADJ	1,919	0.599	+10.5	$2.6 \cdot 10^{-20}$	✓
ADP	3,273	0.386	−10.8	$1.2 \cdot 10^{-35}$	✓
ADV	760	0.437	−5.7	$1.8 \cdot 10^{-3}$	✓
AUX	868	0.626	+13.2	$7.2 \cdot 10^{-15}$	✓
CCONJ	772	0.635	+14.1	$5.0 \cdot 10^{-15}$	✓
DET	2,812	0.636	+14.2	$1.3 \cdot 10^{-51}$	✓
NOUN	5,634	0.491	−0.3	$7.1 \cdot 10^{-1}$	
NUM	3,064	0.723	+22.9	$8.4 \cdot 10^{-146}$	✓
PART	628	0.457	−3.7	$6.6 \cdot 10^{-2}$	
PRON	872	0.416	−7.8	$4.6 \cdot 10^{-6}$	✓
PROPN	4,635	0.460	−3.4	$4.9 \cdot 10^{-6}$	
PUNCT	3,052	0.272	−22.2	$4.0 \cdot 10^{-138}$	✓
SCONJ	214	0.551	+5.7	$1.0 \cdot 10^{-1}$	
SPACE	165	0.170	−32.4	$4.7 \cdot 10^{-18}$	✓
SYM	65	0.323	−17.1	$6.1 \cdot 10^{-3}$	
VERB	2,468	0.438	−5.6	$2.7 \cdot 10^{-8}$	✓

B. SAE Reconstruction Quality on MoD Activations

Sparse autoencoders trained on residual stream activations have become a standard tool for decomposing transformer representations into interpretable features (Bricken et al., 2023; Cunningham et al., 2023; Lieberum et al., 2024); benchmarks such as SAEBench (Karvonen et al., 2025) evaluate SAE quality on the base-model distribution. We do not train SAEs in this work; the per-feature analysis of Section 4.4 uses pre-trained Gemma Scope SAEs. As a methodology check, we verify that Gemma Scope canonical SAEs (release `gemma-scope-2b-pt-res-canonical`, width 16K) transfer to strict-long MoD residual-stream activations with modest reconstruction degradation relative to the SAE's training distribution (base Gemma 2 2B). Activations are taken at the canonical residual-stream hook `blocks.ℓ.hook_resid_post` for each target $\ell \in \{13, 23, 24\}$ on 200 WikiText-2 test samples (32,808 tokens after excluding the first 4 positions per sample, which are known to be out-of-distribution for Gemma Scope SAEs due to attention-sink behaviour (Xiao et al., 2024)).

Table 6. SAE reconstruction quality on strict-long MoD activations and a base-Gemma reference at layer 13. Cosine = mean per-token cosine similarity between residual stream and SAE reconstruction; v.e. (global) is pooled variance explained across all tokens; v.e. (per-feat.) is the mean of per-feature variance explained; L_0 = mean number of active features per token. The base Gemma layer-13 row is a one-off diagnostic measured on the SAE's training distribution; — denotes metrics not recorded for the reference run.

Setting	cosine	v.e. (global)	v.e. (per-feat.)	L_0	dead frac
strict-long MoD, L13	0.895	0.695	0.554	78.6	0.132
strict-long MoD, L23	0.876	0.652	0.622	115.5	0.009
strict-long MoD, L24	0.871	0.630	0.586	102.1	0.022
Base Gemma, L13 (ref.)	0.927	0.754	—	78.3	—

Cosine drops by ∼3pp on MoD activations relative to the in-distribution base-Gemma reference at layer 13; global variance explained drops by ∼6–12pp; L_0 remains in the 78–115 range expected for canonical Gemma Scope SAEs. Dead-feature fraction is highest at the shallow layer (13.2%) and drops below 3% at the deep layers, consistent with deeper layers recruiting broader feature support. The degradation is modest enough that the per-feature analysis of Section 4.4 is feasible on MoD activations using off-the-shelf Gemma Scope SAEs. Note that Section 4.4 reads the residual *entering* each routing layer, $\text{resid\_pre}(\ell) = \text{resid\_post}(\ell - 1)$, i.e., SAE layers $\{12, 22, 23\}$; on the MoD activations at those hooks, cosine is 0.907, 0.883, and 0.876 respectively, in the same quality band as the table above.

C. RQ4 Details: Collective Decomposition and Intervention

Collective decomposition

Table 7 reports held-out R^2 of ridge regression on the top-k features selected by training-split correlation, against a random-feature baseline, on the strict-long checkpoint; Figure 4 traces the full R^2-vs-k curve. Selection beats random at every k. Ranking on the training split is essential: ranking on the full data and then evaluating "held-out" would leak the selection and inflate R^2. The random baseline matters because in a 16K-feature space any k features fit something; the meaningful quantity is how far selection exceeds random.

Table 7. Held-out R^2 of ridge on the top-k features selected by training-split correlation (sel), versus k random features (rand), on the strict-long checkpoint.

Layer	k=10 sel/rand	k=50 sel/rand	k=200 sel/rand
13	0.28/0.02	0.41/0.03	0.49/0.12
23	0.22/0.01	0.32/0.03	0.44/0.10
24	0.25/0.01	0.39/0.03	0.49/0.09

Intervention conditions and held-out replication

Figure 5 reports every collective-intervention condition per layer against its frequency-matched null, including the conditions that do not clear the criterion. Table 8 reports the held-out replication of the skip-cue suppression: features are identified on one document half and suppressed on the disjoint other, so no token used to select a feature is also used to test it. The

Figure 4. Held-out R^2 on the router score as a function of the number of selected features k (log axis), for the three studied layers (solid, selected by training-split correlation) against a random-feature baseline (dotted, mean±sd over draws). Selection separates from random within the first few features and reaches roughly half the score variance by $k \approx 200$. That so many features are needed, while no single feature explains more than a small fraction, is why the decision is distributed rather than carried by any one feature.

held-out margins match the in-corpus margins almost exactly; were the margin an overfitting artefact, the held-out value would have collapsed rather than held. The two halves select overlapping but non-identical feature sets (Jaccard 0.53–0.70), so the specific features differ while the same kind of collection delivers the same causal strength. This rules out token-level selection bias within the WikiText-2 distribution; it is not a claim of transfer to a different corpus.

Table 8. Held-out replication of the skip-cue collective suppression. The in-corpus margin identifies and tests on the same document half (averaged over both halves); the held-out margin identifies on one half and tests on the disjoint other (averaged over both directions). Margins are null-adjusted; the direction rate was 100% in every cell.

Layer	in-corpus margin	held-out margin	retention
13	+14.2pp	+13.8pp	97%
23	+17.0pp	+16.8pp	99%
24	+27.8pp	+27.5pp	99%

Retracted effects

Applying the frequency-matched null removed several effects that passed the raw 10pp/70% criterion. Ablating the syntactic (POS-categorical) feature bin at layer 24 reaches 11.5% raw conditional flip but only +9.6pp above the null, below our threshold; we therefore do *not* claim it as causal. Two amplification conditions at layer 13 and one suppression condition at layer 23 fail the same way.

D. Pre-Committed Thresholds and Revisions

This appendix documents the pre-committed thresholds for the three RQ2 controls and the POS probe, plus two pre-commit revisions made during the study, each with reasoning. All thresholds were recorded in project decision logs before the corresponding measurements were collected.

RQ2 control thresholds

(a) Layer-aggregate norm. *Threshold for "explains the preference":* shallow-middle norm Cohen's $d > 0$ in the *same* direction as the routing preference (full $>$ sliding). *Rationale:* a router that preferred high-norm layers would incidentally preserve full-attention layers if and only if those layers had higher norms. *Outcome:* $d = -3.02$ in base Gemma 2 2B and $d = -3.86$ in the strict-long MoD context – opposite direction. Strongly rejected.

Figure 5. Causal effect of the collective interventions, grouped by layer. Each point is the conditional flip rate (fraction of active-token decisions that change) with its 95% CI; the grey tick is the frequency-matched null; the right-margin percentage is the direction rate. Conditions that clear the null-adjusted 10pp criterion are blue. Suppressing or boosting the skip-aligned collection is the reliable causal handle, peaking at layer 24's suppress-skip (30.6%, 100% directed); the process-aligned designs are weaker.

(b) Per-token norm dependence. *Threshold:* mean $|r| > 0.4$ across MoD layers between strict-long router score and per-token $\|h\|$ entering the router. *Rationale:* a Pearson r of 0.4 implies norm explains $\sim 16\%$ of router-score variance per layer, the rough boundary above which "the router is mostly a norm-thresholder" would be substantively true. *Outcome:* mean $|r| = 0.166$, max $|r| = 0.336$ at layer 17 (at most $r^2 \approx 11\%$ of variance explained at any MoD layer). Below threshold; rejected.

(c) Per-layer task-loss asymmetry. *Threshold:* shallow-middle $\Delta(\text{full}) - \Delta(\text{sliding}) > 1.0$ PPL with $p < 0.05$, AND MLP-ablation specificity control flat (rules out a generic "deeper layers always cost more" confound). *Rationale:* a 1 PPL difference between attention types within shallow-middle would be a substantive layer-importance asymmetry defensible as a routing rationale. *Outcome:* $\Delta = +0.34$ PPL, $p = 0.44$, MLP control flat ($p = 0.88$). Below threshold; the test does not detect an asymmetry, with the power caveat noted in Section 4.2.

POS probe thresholds

Two complementary criteria, both pre-committed:

(A) Per-tag. At least one POS tag X at any target layer $\ell \in \{13, 23, 24\}$ satisfies $|P(\text{process} \mid \text{POS} = X) - \bar{P}_{\text{marginal}}| > 5\text{pp}$, Bonferroni-significant at $\alpha' = 0.05/n_{\text{tags}}$ where $n_{\text{tags}} = 16$ tags with $n \geq 30$ tokens.

(B) Aggregate probe. Logistic regression POS-onehot $\rightarrow$ router decision achieves test accuracy > majority-class baseline +5pp at any target layer.

Either (A) or (B) clearing at any of layers $\{13, 23, 24\}$ counted as the probe-side criterion for workshop submission.

Outcome: (A) clears at all three layers (10/12/11 tags pass at L13/L23/L24 respectively); (B) clears at L13 (+6.6pp lift) and

L24 ($+9.1$pp lift). At L23 (B) does not clear because the marginal $\bar{P} = 0.61$ leaves the binary classifier with insufficient operating range to register lift, even though per-tag asymmetries are large and pass (A). Both criteria met.

RQ4 intervention criterion

Feature-intervention success. *Threshold:* conditional flip rate ≥ 10pp among tokens where a manipulated feature was active in baseline, with $\geq 70\%$ of flips in the predicted direction, evaluated as the margin above a frequency-matched null of random features drawn from the same activation-frequency deciles; plus a bidirectional-consistency requirement (suppressing and amplifying the same feature set must move routing in opposite directions). *Rationale:* raw flip rates are inflated by two artefacts. SAE reconstruction error alone flips $\sim 17\%$ of binary decisions at the 0.5 threshold, which is why the counterfactual is the SAE's own unmodified reconstruction rather than the real model score; and zeroing many high-firing features moves the residual substantially regardless of relevance, which is what the frequency-matched null controls for. *Outcome:* the skip-cue collective clears the criterion at all three layers (e.g., $+27.4$pp above null at layer 24, 100% direction rate), and amplification moves routing the opposite way; several other conditions fail after null adjustment and are not claimed (Section C).

Pre-commit revisions

Revision 1: strict-long capacity band. *Original commit:* "strict-long overall skip $\in [0.40, 0.55] \rightarrow$ strict-long becomes the lead checkpoint; otherwise fall back to strict-short." *Result:* strict-long landed at 38.3% skip – 1.7pp below the band. *Revision:* strict-long promoted to lead despite the band miss, on substantive grounds: (i) strict-long has $\sim 10\times$ the training of strict-short (52K Alpaca samples $\times$ 3 epochs vs. 5K $\times$ 1) and is closer to the paper-spec configuration; (ii) strict-long has comparable per-layer balance to strict-short (10 of 13 layers in $[0.3, 0.7]$); (iii) 1.7pp below an intuited band is one unit of noise, not a substantively different routing regime. *Procedural lesson* (recorded with the revision): future pre-commits should attach decision bands to substantive criteria (e.g., "no layer in $\{23, 24\}$ degenerates" or "shallow-middle Cohen's $d > 0.5$") rather than arbitrary capacity windows.

Revision 2: SAE reconstruction-quality thresholds. *Original commit:* cosine $> 0.95 \rightarrow$ proceed; cosine in $[0.90, 0.95] \rightarrow$ proceed with caveat; cosine $< 0.90 \rightarrow$ pivot away from SAE-based analysis. Drawn from general SAE-literature intuition, not anchored to measured Gemma Scope performance. *Result:* a base-Gemma layer-13 diagnostic on the same evaluation pipeline gave cosine 0.927 – the original "proceed" threshold was unreachable even on the SAE's training distribution. *Revision:* thresholds re-anchored to measured base-Gemma performance. Excellent: cosine > 0.92 AND var. explained > 0.7 (base-Gemma parity); good: cosine > 0.85 AND var. explained > 0.5 (modest degradation, usable); pivot below cosine 0.85 OR var. explained 0.3. strict-long MoD landed in the "good" band (B). *Procedural lesson:* reconstruction-metric pre-commits should anchor to a measured ceiling on the in-distribution case before being set, not to a guessed expected quality.