An Autoregressive Approach For Material Generation

Niklas Dobberstein [1 2] **Jan Hamaekers** [1]

[1]*Fraunhofer Institute for Algorithms and Scientific Computing SCAI, Schloss Birlinghoven, 53757 Sankt Augustin, Germany* [2]*University Münster, Institute for Organic Chemistry, Corrensstraße 40, 48149 Münster, Germany*. Correspondence to: Niklas Dobberstein niklas.dobberstein@uni-muenster.de.

1. Introduction

Discovering and designing materials with specific properties is of high relevance for industries ranging from energy to electronics. However, exploring the vast combinatorial chemical space remains a significant challenge. While *in silico* methods such as Density Functional Theory (DFT) have enabled systematic screening, their computational cost remains a bottleneck.

In this work, we introduce Materium, an autoregressive transformer for crystal structure generation. Unlike diffusion approaches, Materium places atoms at precise fractional coordinates in a single pass. Our method discretizes continuous 3D material representations into token sequences, enabling the model to be trained in a few hours on a single GPU, orders of magnitude faster than current state-of-the-art diffusion models.

2. Materium Framework and Evaluation

Materium is a decoder-only transformer based on the Llama 2 architecture [1], comprising approximately 43 million parameters. The core innovation lies in our tokenization strategy, which converts an inherently unordered set of atoms into an ordered, one-dimensional sequence.

2.1 Tokenization and Quantization

We represent a crystal structure as a sequence of discrete tokens including atomic elements, oxidation states, fractional coordinates, and lattice parameters. To handle continuous values, we employ a quantization technique where fractional coordinates $r_{\text{frac}} \in [0, 1)^3$ are discretized into 1024 bins. Lattice parameters are similarly normalized and quantized.

A fundamental challenge is defining the order of atoms. We investigated several deterministic strategies and found that sorting atoms by the heaviest element first (M_{high}) yielded the most stable results. The final sequence structure is represented as:

$$[\text{SOS}] \ldots [\text{Elem}|\text{Ox}][x][y][z] \ldots [\text{LATTICE}] \ldots [\text{EOS}] \tag{1}$$

This design allows the model to learn precise 3D structures without the complex post-processing required by invariant representations like SLICES.

2.2 Conditional Generation and Training

To enable controlled generation, we condition the model on various properties, including band gap, magnetic density, space group, and density. Property values are projected into embeddings and prepended

Fig. 1: Visualization of the Materium tokenizer. Continuous coordinates are discretized into 1024 bins, creating a unified sequence of atomic and lattice tokens.

to the material token sequence. We utilize a conditional dropout strategy during training to ensure robustness against missing data.

We trained Materium on the Alex-MP-20 dataset [2] (approx. 600k materials) using a single A100 40GB GPU. Due to the token processing and fast algorithms like FlashAttention [3], the model can be trained in a couple of hours.

2.3 Results

We evaluated the model on 1024 generated structures. First, we compared the match rate using pymatgen's StructureMatcher [4] to measure how many generated structures successfully matched their relaxed counterparts. As shown in Table 1, Materium (M_{high}) achieves a high match rate of 85.3%, indicating that it can successfully generate new structures near their local energy minima.

Table 1: Comparison of structural match rates (relaxed vs. generated). Note that baselines were trained on MP20, while Materium utilized Alex-MP-20.

Model	Training Data	Match Rate (%)
Materium (Ours)	Alex-MP-20	85.30
FlowMM	MP20	61.39
DiffCSP	MP20	51.49
CDVAE	MP20	45.31

We further assessed the quality of generated structures using the Stability, Uniqueness, and Novelty

(S.U.N.) metrics. As detailed in Table 2, Materium (M_{high}) demonstrated excellent uniqueness (99.8%) and good stability (73.9%). However, the novelty rate (46.5%) and the combined S.U.N. score (22.7%) are lower than the state-of-the-art diffusion model MatterGen. While Materium generates fewer novel stable crystals, it offers a significant advantage in training and generation speed.

Table 2: S.U.N. metrics comparison. Materium achieves high stability and uniqueness, though with lower novelty than diffusion baselines.

Model	Stab. (%)	Uniq. (%)	Nov. (%)	S.U.N. (%)
Materium (Ours)	73.9	99.8	46.5	22.7
Matter-Gen [2]	73.2	99.8	61.6	38.9

For conditional generation, Materium performs consistently well on fundamental properties like density and space group. We observed that the model generalizes reasonably well even in data-sparse regions, such as high magnetic density or large band gaps, though variance increases.

2.4 Related Work

Recently, generative models have emerged as powerful tools for inverse design. Diffusion-based approaches, such as MatterGen [2], have shown great promise but rely on iterative denoising steps that are computationally expensive to train and sample. Alternatively, language model-based methods like CrystaLLM [5] generate structures using text-based formats (e.g., CIF), but often suffer from inefficient tokenization where coordinates are split into multiple character tokens.

In terms of structural match rates, we compared our approach to recent models including FlowMM [6], DiffCSP [7], and CDVAE [8]. While these baselines were trained on the MP20 dataset (unlike Alex-MP-20 used here), the comparison highlights the effectiveness of our specialized tokenization strategy in generating physically valid structures.

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