Dynamic Reward Incentives for Emergent Cooperation under Changing Rewards

Abstract

Peer incentivization (PI) is a popular multi-agent reinforcement learning approach where all agents can reward or penalize each other to achieve cooperation in social dilemmas. Despite their potential for scalable cooperation, current PI methods heavily depend on fixed incentive values that need to be appropriately chosen with respect to the environmental rewards and thus are highly sensitive to their changes. Therefore, they fail to maintain cooperation under *changing rewards* in the environment, e.g., caused by modified specifications, varying supply and demand, or sensory flaws — even when the conditions for mutual cooperation remain the same. In this paper, we propose *Dynamic Reward Incentives for Variable Exchange* (DRIVE), an adaptive PI approach to cooperation in social dilemmas with changing rewards. DRIVE agents reciprocally exchange reward differences to incentivize mutual cooperation in a completely decentralized way. We show how DRIVE achieves mutual cooperation in the general Prisoner's Dilemma and empirically evaluate DRIVE in more complex sequential social dilemmas with changing rewards, demonstrating its ability to achieve and maintain cooperation, in contrast to current state-of-the-art PI methods.

1 Introduction

Many AI scenarios, such as autonomous driving (Shalev-Shwartz et al., 2016), smart grids (Dimeas & Hatziar-gyriou, 2010), and IoT applications (Deng et al., 2020), can be modeled as self-interested and online learning *multi-agent systems (MAS)*, where conflicts arise due to opposing goals or shared resources (Buşoniu et al., 2010). To maximize *social welfare* (undiscounted sum of rewards across all agents in the system), cooperation is essential in self-interested MAS, requiring agents to avoid selfish behavior for the collective good. This tension between individual and collective rationality is typically modeled as a *social dilemma (SD)* (Rapoport, 1974; Axelrod, 1984). Designing distributed mechanisms to incentivize cooperation in SDs remains a key challenge because it directly affects global efficiency (e.g., aggregated social welfare) and sustainability (e.g., long-run resource availability and fairness across agents) (Axelrod, 1984; Trivers, 1971; Dafoe et al., 2020; Perolat et al., 2017b). *Multi-agent reinforcement learning (MARL)* is a widely used framework to train rational agents in SDs and temporally extended *sequential SDs (SSD)*, where each agent maximizes its own reward (Leibo et al., 2017; Perolat et al., 2017b; Foerster et al., 2018; Yang et al., 2020).

However, non-cooperative game theory and empirical studies show that naive MARL approaches often fail to sustain cooperation because independent adaptation leads to mutual defection (Axelrod, 1984; Van Lange et al., 2013). Furthermore, policy optimization can be affected by inconsistencies in the reward function, which we summarize as *changing rewards*. Such variations are common when moving from simulation to reality, where physical signals replace abstract reward proxies. Noisy sensors, hardware degradation, shifting specifications, or changing market demands can likewise alter reward scales during training (Dulac-Arnold et al., 2019). In human-in-the-loop settings, evaluators may also adapt feedback online, leading to abrupt or irregular shifts (Knox & Stone, 2009). In these cases, the underlying SSD structure (i.e., greed and fear inequalities) is preserved, but the numerical values fluctuate. Methods that are brittle to such changes struggle to sustain cooperation beyond narrow, hand-tuned conditions.

Peer incentivization (PI) enables agents to reward or penalize each other to foster cooperation in SDs (Lupu & Precup, 2020; Yang et al., 2020). It has gained traction for its success in complex SSDs and links to

biology, economics, and social science (Vinitsky et al., 2023; Schmid et al., 2021; Kölle et al., 2023). Yet, existing PI methods rely on fixed or domain-tuned incentive values and fail under changing rewards, even if cooperation conditions remain unchanged (Eysenbach & Levine, 2021; Zhang et al., 2020). As Fig. 1c illustrates, prior PI methods might succeed in a given instance of the Prisoner's Dilemma (Foerster et al., 2018; Phan et al., 2024; Yang et al., 2020), but fail when payoffs shift or scale, despite satisfying the same *greed* and *fear* inequalities (Axelrod, 1984; Macy & Flache, 2002). Notably, popular approaches such as *Learning to Incentivize Other learning agents* (LIO) (Yang et al., 2020) or *inequity aversion* (IA) (Hughes et al., 2018) appear superficially capable of adapting to such variation, since they rely on learned or relative incentives. Yet, IA requires precise hyperparameter tuning to be effective and fails to promote cooperation in both the original (unscaled) payoff matrix of Fig. 1c (left) and the uniformly scaled variant (right). LIO achieves cooperation under the original payoffs but degrades under simple scaling, as its learned incentive magnitudes are tied to the absolute reward scale. As a result, these methods either lose robustness under reward shifts or suppress valuable heterogeneity in agent performance. Addressing such shifts typically requires hyperparameter re-tuning, which is impractical in ad hoc or online learning scenarios.

To this end, we propose *Dynamic Reward Incentives for Variable Exchange (DRIVE)*, an adaptive PI framework for SDs with changing rewards. By adapting incentives directly to *reward differences*, DRIVE sustains cooperation without retuning and without conflating legitimate variance with exploitative behavior. We summarize our contributions as follows:

- We introduce a reciprocal exchange mechanism that incentivizes cooperation through reward differences.

- We prove that DRIVE aligns incentives toward mutual cooperation in generalized Prisoner's Dilemma games, remains invariant to reward shifts and scaling.

- We empirically demonstrate DRIVE's robustness and superior cooperation in SSDs under changing rewards.

Figure 1: (a) Social dilemma payoff matrix with R, P, T, and S. In *Prisoner's Dilemmas (PD)*, $T > R > P > S$ holds (Axelrod, 1984; Macy & Flache, 2002). (b) A PD instance satisfying these inequalities. (c) A motivating example on the reward sensitivity of PI approaches in a 2-player Prisoner's Dilemma: IA requires careful tuning even under the original payoffs and fails to achieve cooperation in both scenarios. LIO achieves high cooperation at the original scale (left) but degrades when the payoffs change, even though the inequalities for greed and fear (Eq. 1) remain valid. In contrast, DRIVE maintains robust cooperation across both settings without retuning.

2 Background

Problem Formulation In this work, we focus on partially observable *Markov games* (POMGs) $M = \langle \mathbb{D}, \mathbb{S}, \mathbb{A}, \mathbb{P}, \mathbb{U}, \mathbb{Z}, \Omega \rangle$, where $\mathbb{D} = \{1, ..., n\}$ is a set of agents i, $\mathbb{S}$ is a set of states s_t at time step t, $\mathbb{A} = \langle \mathbb{A}_1, ..., \mathbb{A}_n \rangle = \langle \mathbb{A}_i \rangle_{i \in \mathbb{D}}$ is the set of joint actions $a_t = \langle a_{t,i} \rangle_{i \in \mathbb{D}}$, $\mathbb{P}(s_{t+1}|s_t, a_t)$ is the transition probability, $\langle u_{t,i} \rangle_{i \in \mathbb{D}} = \mathbb{U}(s_t, a_t) \in \mathbb{R}$ is the joint reward, $\mathbb{Z}$ is a set of local observations $z_{t,i}$ for each agent i, and $\Omega(s_{t+1}) = z_{t+1} = \langle z_{t+1,i} \rangle_{i \in \mathbb{D}} \in \mathbb{Z}^n$ is the subsequent joint observation. Each agent i maintains a local *history* $\tau_{t,i} \in (\mathbb{Z} \times \mathbb{A}_i)^t$. $\pi_i(a_{t,i}|\tau_{t,i})$ is the action selection probability based on the individual *policy* of agent i. In addition, we assume each agent i to have a *neighborhood* $\mathcal{N}_{t,i} \subseteq \mathbb{D} - \{i\}$ of other agents at every time step t, which is domain-dependent, as suggested in (Lupu & Precup, 2020; Yang et al., 2018). π_i is evaluated with a *value function* $V_i^\pi(s_t) = \mathbb{E}_\pi[G_{t,i}|s_t]$ for all $s_t \in \mathbb{S}$, where $G_{t,i} = \sum_{k=0}^\infty \gamma^k u_{t+k,i}$ is the individual and discounted *return* of agent $i \in \mathbb{D}$ with discount factor $\gamma \in [0, 1)$ and $\pi = \langle \pi_j \rangle_{j \in \mathbb{D}}$ is the *joint policy* of the MAS. The goal of agent i is to find a *best response* π_i^* with $V_i^* = max_{\pi_i} V_i^{\langle \pi_i, \pi_{-i} \rangle}$ for all $s_t \in \mathbb{S}$, where π_{-i} is the joint policy *without* agent i. In practice, the global state s_t is not directly observable for any agent i s.t. V_i^π is approximated with local information, i.e., $\tau_{t,i}$ instead (Leibo et al., 2017; Perolat et al., 2017a; Jaderberg et al., 2019). To measure cooperation in the MAS, we define the *social welfare* or *utilitarian metric* $U = \sum_{i \in \mathbb{D}} \sum_{t=0}^{H-1} u_{t,i}$ as the undiscounted sum of rewards.

Social Dilemmas *Social dilemmas (SD)* are games where independently optimized policies π_i fail to achieve globally optimal outcomes that maximize collective welfare. SDs are commonly studied in 2-player matrix games with two actions: C (cooperate) and D (defect), producing four possible payoffs (Fig. 1): R for mutual cooperation, P for mutual defection, T for exploiting the other, and S for being exploited. A matrix game is a *Prisoner's Dilemma (PD)* if the payoffs satisfy (Axelrod, 1984; Macy & Flache, 2002):

$$T > R > P > S \tag{1}$$

Here, $T > R$ represents *greed*, and $P > S$ *fear*. In *Iterated PDs (IPD)*, an additional condition holds: $2R > T + S$ (Axelrod, 1984; Macy & Flache, 2002). Fig. 1b shows an instance where D is individually rational despite C being socially optimal. As long as the inequalities are satisfied, the game's strategic nature remains invariant to exact payoffs (Axelrod, 1984; Rapoport, 1974). PDs and IPDs are particularly important SDs, as greed and fear often drive agents away from mutual cooperation despite its collective benefit, a phenomenon observed in both nature and human society (Axelrod, 1984; Dawkins, 2016; Rapoport, 1974).

Sequential social dilemmas (SSD) extend SDs by introducing temporal structure, modeled as stochastic games (Leibo et al., 2017; Perolat et al., 2017b). SSDs enable more realistic scenarios in which behavior is captured by policies rather than by atomic actions. These can still be mapped to matrix games by classifying policies as C or D and evaluating empirical payoffs (Leibo et al., 2017), making core SD concepts applicable to SSDs.

Multi-Agent Reinforcement Learning We consider decentralized (independent) learning, where each agent i optimizes its policy π_i using local data like $\tau_{t,i}$, $a_{t,i}$, $u_{t,i}$, and $z_{t+1,i}$ via *reinforcement learning (RL)* (Tan, 1993; Foerster et al., 2018; Yang et al., 2018). For methods with peer incentives, the shaped reward replaces $u_{t,i}$ in this trajectory. *Policy gradient RL* is a common method to approximate best responses π_i^* (Lowe et al., 2017; Foerster et al., 2018; Yang et al., 2020). A function approximator $\hat{\pi}_{i,\phi_i} \approx \pi_i^*$ is trained using gradient ascent on an estimate of $J = \mathbb{E}_\pi[G_{0,i}]$ (Williams, 1992), where the policy gradient is approximated as (Sutton et al., 2000):

$$g = (G_{t,i} - b_i(s_t))\nabla_{\phi i} log\hat{\pi}_{i,\phi_i}(a_{t,i}|\tau_{t,i}) \tag{2}$$

Here, $b_i(s_t)$ is a state-dependent *baseline*, typically approximated by a learned value function $\hat{V}_{i,\omega_i}(\tau_{t,i}) \approx V_i^{\hat{\pi}}(s_t)$ (Foerster et al., 2018). For simplicity, we omit parameters and write $\hat{\pi}_i$, $\hat{V}_i$. Modern actor-critic methods incorporate such variance-reduction baselines, entropy bonuses, or centralized critics, yet still optimize each agent's own return, which remains misaligned with social welfare in social dilemmas. Also, *independent learning* introduces non-stationarity because agents adapt simultaneously (Laurent et al., 2011; Hernandez-Leal et al., 2017), often leading to overly greedy behavior and mutual defection unless rewards or incentives are modified.

3 Dynamic Reward Incentivization

We assume a decentralized MARL setting as formulated in Algorithm 1, where at every time step t each agent i with history $\tau_{t,i}$, policy $\hat{\pi}_i$, and value function $\hat{V}_i$ observes its neighborhood $\mathcal{N}_{t,i}$ through its local observation $z_{t,i}$ and executes an action $a_{t,i} \sim \pi_i(\cdot|\tau_{t,i})$. DRIVE uses $\mathcal{N}_{t,i}$ only for incentive exchange; the underlying policy receives no additional messages beyond the environment observation. The environment then transitions to a new state $s_{t+1} \sim \mathbb{P}(\cdot|s_t, a_t)$ which is observed by each agent i through an observation $z_{t+1,i}$ and a reward $\hat{u}_{t,i}$. The reward is obtained by passing the environmental reward $u_{t,i}$ through an external and possibly unknown *reward-change function* f_{mod} (Alg. 1, l. 11), which simulates modified specifications, varying supply and demand, or sensor degradation (Eysenbach & Levine, 2021; Zhang et al., 2020). In Sec. 5 we analyze an affine special case of f_{mod}, applying a shared map varying by epoch. All agents collect their respective *experience tuple* $e_{t,i} = \langle \tau_{t,i}, a_{t,i}, \hat{u}_{t,i}, z_{t+1,i} \rangle$ for PI exchange and independent updates to $\hat{\pi}_i$ and $\hat{V}_i$ (Yang et al., 2020). We assume each agent i has a domain-dependent neighborhood $\mathcal{N}_{t,i} \subseteq D \setminus \{i\}$ at each time step, as introduced in Sec. 2. Lines 13–20 in Alg. 1 correspond to a short parallel communication phase in which neighboring agents exchange DRIVE requests and responses.

Algorithm 1 Multi-Agent Learning with DRIVE

1: Initialize parameters of $\hat{\pi}_i$ and $\hat{V}_i$ for all agents $i \in \mathbb{D}$
2: **for** epoch $m \leftarrow 1, E$ **do**
3:     Set $\overline{u}_i \leftarrow 0$ for all agents $i \in \mathbb{D}$ ▷ Reset avg. reward
4:     Sample s_0 and set $\tau_{0,i}$ for all agents $i \in \mathbb{D}$
5:     **for** time step $t \leftarrow 0, H-1$ **do**
6:         **for** agent $i \in \mathbb{D}$ **do** $a_{t,i} \sim \hat{\pi}_i(\cdot|\tau_{t,i})$ ▷ Independent decisions
7:         $s_{t+1} \sim \mathbb{P}(\cdot|s_t, a_t)$ ▷ Execute joint action a_t
8:         $\langle u_{t,i} \rangle_{i \in \mathbb{D}} \leftarrow \mathbb{U}(s_t, a_t)$ ▷ Environmental rewards
9:         $\langle z_{t+1,i} \rangle_{i \in \mathbb{D}} \leftarrow \Omega(s_{t+1})$
10:         **for** agent $i \in \mathbb{D}$ **do**   ▷ Parallel communication
11:             $\hat{u}_{t,i} \leftarrow f_{mod}(u_{t,i}, m)$ ▷ Ext. reward change
12:             $\overline{u}_i \leftarrow (t \cdot \overline{u}_i + \hat{u}_{t,i})/(t+1)$ ▷ Avg. reward
13:             $u_{t,i}^{DRIVE} \leftarrow DRIVE(\hat{V}_i, \mathcal{N}_{t,i}, \hat{u}_{t,i}, \overline{u}_i)$ ▷ Alg. 2
14:             $e_{t,i} \leftarrow \langle \tau_{t,i}, a_{t,i}, u_{t,i}^{DRIVE}, z_{t+1,i} \rangle$
15:             Update $\tau_{t,i}$ to $\tau_{t+1,i}$ and store $e_{t,i}$
16:         **end for**
17:     **end for**
18:     **for** agent $i \in \mathbb{D}$ **do** Update $\hat{\pi}_i$ and $\hat{V}_i$ using all $e_{t,i}$ of epoch m ▷ Independent updates
19: **end for**

DRIVE Token Exchange   DRIVE uses a reciprocal incentive scheme, inspired by Trivers (1971) and illustrated in Fig. 2a, to exchange dynamic incentives for distributed reward shaping. In the *request phase* (Fig. 2a, 1), each agent i checks its *advantage* or *temporal difference residual* $TD_i(\hat{u}_{t,i})$ (Sutton, 1988):

$$TD_i(\hat{u}_{t,i}) = \hat{u}_{t,i} + \gamma \hat{V}_i(\tau_{t+1,i}) - \hat{V}_i(\tau_{t,i}) \tag{3}$$

If the advantage is non-negative, agent i sends its reward $\hat{u}_{t,i}$ as a *request* to all other agents $j \in \mathcal{N}_{t,i}$. In the *response phase* (Fig. 2a, 2), each request-receiving neighbor $j \in \mathcal{N}_{t,i}$ compares the request $\hat{u}_{t,i}$ to its epoch-average reward $\overline{u}_j$ and computes its response $\Delta_{t,i,j}$ sent from j to i, gated by a non-negative TD of i:

$$\Delta_{t,i,j} = \begin{cases} \overline{u}_j - \hat{u}_{t,i}, & \text{if } TD_i(\hat{u}_{t,i}) \geq 0, \\ 0, & \text{otherwise.} \end{cases} \tag{4}$$

After this exchange, the DRIVE reward $u_{t,i}^{DRIVE}$ is computed for each agent i as follows:

$$u_{t,i}^{\text{DRIVE}} = \hat{u}_{t,i} - \underbrace{\min\{\langle \Delta_{t,j,i} \rangle_{j \in \mathcal{N}_{t,i}}\}}_{\text{own responses to others' requests}} + \underbrace{\min\{\langle \Delta_{t,i,j} \rangle_{j \in \mathcal{N}_{t,i}}\}}_{\text{others' responses to own requests}} . \tag{5}$$

Figure 2: DRIVE exchange scheme (a): (1) If $TD_1(\hat{u}_{t,1}) \geq 0$ (Eq. 3), agent 1 sends its reward $\hat{u}_{t,1}$ to neighbor agent 2 as a request, (2) agent 2 calculates the difference $\Delta_{t,1,2}$ between its own average reward $\overline{u}_i$ in the current epoch m and the received request $\hat{u}_{t,i}$, sent back as a response and used to shape the rewards of both agents (Eq. 5). (b)-(e) Modified PD payoff matrices of different PI methods with payoff modifications highlighted in blue (Hughes et al., 2018; Yang et al., 2020; Phan et al., 2024).

Using the responder's epoch-average $\overline{u}_j$ rather than its instantaneous reward makes DRIVE sensitive to systematic exploitation instead of single noisy outcomes: only agents whose recent average return is consistently lower than a neighbor's request generate strong negative Δ terms. Other combinations (instant–instant, instant–average, average–average) are conceivable and may yield different trade-offs, which is an interesting direction for future work. Appendix A.1 provides an initial comparison.

Algorithm 2 Dynamic Reward Incentive Exchange

1: **procedure** $DRIVE(\hat{V}_i, \mathcal{N}_{t,i}, \hat{u}_{t,i}, \overline{u}_i)$
2:     **if** $TD_i(\hat{u}_{t,i}) \geq 0$ **then** Send request $\hat{u}_{t,i}$ to all $j \in \mathcal{N}_{t,i}$ (Fig. 2a)   ▷ Evaluate acc. to Eq. (3)
3:     **for** neighbor agent $j \in \mathcal{N}_{t,i}$ **if** request $\hat{u}_{t,j}$ received from j **do**   ▷ Handle Requests
4:         $\Delta_{t,j,i} \leftarrow \overline{u}_i - \hat{u}_{t,j}$
5:         $\hat{u}_{req} \leftarrow min\{\hat{u}_{req}, \Delta_{t,j,i}\}$
6:         Send response $\Delta_{t,j,i}$ to agent j (Fig. 2a)
7:     **end for**
8:     **for** neighbor agent $j \in \mathcal{N}_{t,i}$ **do if** request $\hat{u}_{t,i}$ sent to j ▷ Handle Responses
9:         $\hat{u}_{res} \leftarrow min\{\hat{u}_{res}, \Delta_{t,i,j}\}$
10:     **end for**
11:     **return** $\hat{u}_{t,i} - \hat{u}_{req} + \hat{u}_{res}$ ▷ Shaped reward (Eq. 5)
12: **end procedure**

Distributed Reward Shaping   The DRIVE reward $u_{t,i}^{DRIVE}$ is used to update the policies of the corresponding agents using any RL algorithm, e.g., policy gradient methods, according to Eq. (2). Formally, whenever DRIVE is enabled we obtain returns $G_{t,i}$ by replacing $u_{t,i}$ with $u_{t,i}^{DRIVE}$ in Eq. (2) (cf., Alg. 1, l. 17). Sec. 2 therefore describes the environment-level returns, while DRIVE defines how these are transformed into the shaped rewards that the RL updates optimize. The non-negativity condition of advantage $TD_i(\hat{u}_{t,i})$ in the DRIVE request is needed to expose defecting agents that typically have a greater advantage than the exploited agents in SDs (Axelrod, 1984). If there is unilateral defective behavior, the defective agent i will be penalized by the most exploited neighbor agent $j \in \mathcal{N}_{t,i}$, since $\Delta_{t,i,j} < 0$, which is ensured by the *min* aggregation terms [1] in Eq. (5). If all agents act equally cooperatively, then all $\Delta_{t,i,j} = 0$, and there is no additional reward or penalty. The complete formulation of DRIVE at time step t for any agent i is given in Algorithm 2. $\hat{V}_i$ is the approximated value function to calculate $TD_i(\hat{u}_{t,i})$, according to Eq. (3), $\mathcal{N}_{t,i}$ is the current local neighborhood, $e_{t,i}$ is the experience tuple, and $\overline{u}_i$ is the current average reward of agent i.

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[1]The *min* aggregations could be replaced by a sum or mean, similar to (Hughes et al., 2018). However, this would weaken the influence of the most exploited agent relative to others, tolerating individual dissatisfaction that could spread in later epochs.

4 Related Work

MARL in Social Dilemmas MARL has achieved substantial progress across a range of domains (Tan, 1993; Littman, 1994; Buşoniu et al., 2010; Vinyals et al., 2019). In decentralized SDs and SSDs, a key challenge is resolving misaligned incentives without centralized control. Recent work addresses this through *local*, peer-induced, or socially conditioned reward-shaping mechanisms (Hughes et al., 2018; Yang et al., 2020; Phan et al., 2024; Altmann et al., 2025), which operate in mixed-motive environments with observation-limited agents and thus align with our setting. Recent approaches also study reciprocity-based intrinsic rewards and decentralized reward mixing to stabilize cooperation in mixed-motive systems (Zhou et al., 2024). By contrast, much of the broader MARL literature, methods for mitigating non-stationarity in cooperative settings (Bowling & Veloso, 2002; Matignon et al., 2007; Wei & Luke, 2016), globally informed reward shaping (Leibo et al., 2017; Devlin et al., 2014), opponent-shaping requiring access to opponents' parameters (Foerster et al., 2018; Letcher et al., 2019; Willi et al., 2022; Zhao et al., 2022), and centralized incentive design (Yang et al., 2022; Guresti et al., 2023) assumes global information or centralized coordination, and therefore does not extend to decentralized SDs.

Peer Incentivization Many PI methods have been introduced to promote mutual cooperation in a distributed fashion via reward exchange (Yi et al., 2022). *Gifting* extends the action space of each agent i with a reward action to incentivize other agents $j \in \mathcal{N}_{t,i}$ (Lupu & Precup, 2020). In contrast, DRIVE is built upon reciprocal reward shaping and does not require an extended action space. Schmid et al. (2021) proposes market-based PI where agents can establish bilateral agreements. A public sanctioning approach, where agents can reward or penalize each other based on known group behavior patterns, has been proposed in (Vinitsky et al., 2023). Hughes et al. (2018) defines an *inequity aversion (IA)* scheme based on non-negative reward differences weighted by two domain-dependent coefficients. *Learning to Incentivize Other learning agents (LIO)* automatically learns an incentive function for each agent i under full observability, based on the joint action of all other agents $j \neq i$ (Yang et al., 2020). Closely related, Learning to Share (LToS) (Yi et al., 2022) learns dynamic reward-sharing policies among neighboring agents, enabling decentralized adaptation of incentives. Phan et al. (2022) propose Mutual Acknowledgment Token Exchange (MATE), a two-phase protocol where agents exchange fixed tokens x: cooperating agents issue tokens while exploited agents receive them, yielding the modified payoff matrix shown in Fig. 2c. Recent work also highlights the brittleness of fixed-token mechanisms under changing reward scales and addresses this limitation by deriving token magnitudes from TD and value estimates and reaching consensus across neighbors, demonstrating robustness to downscaled rewards (Altmann et al., 2025). Most PI methods are sensitive to the reward values of an environment due to relying on fixed incentive values or domain-dependent parameters, thus failing to cooperate when the reward values change (Fig. 1c). Considering the PD as an example, Fig. 2 shows the modified payoff matrices of DRIVE (b), MATE (c), LIO (e), and IA (d). According to these matrices, DRIVE is the only method that does not depend on any particular hyperparameter or explicitly learned value. IA only modifies unilateral cooperation and defection but depends on two domain-dependent coefficients α and β (Hughes et al., 2018). LIO learns an incentive function conditioning on the actions of the other agents, which requires sufficient experience and time to adapt accordingly. In the case of MATE, cooperation depends on an appropriate global token $\mathbf{x} \geq max\{P - S, \frac{T-R}{3}\}$ that can be derived from the modified payoff matrix. In the example instance in Fig. 1b, $\mathbf{x}$ should be at least 1, which is the original token value used for MATE in (Phan et al., 2024). Interestingly, this value is used for other PI methods as well without further analysis or questioning (Lupu & Precup, 2020; Schmid et al., 2021).

Teaming Beyond independent learners, recent work studies how social preferences, teams, or coalition structures shape incentives in mixed-motive settings, e.g., heterogeneous SVO-based reward shaping, team-based reward sharing, and adaptive reward mixing via price-of-anarchy minimization (Gemp et al., 2022; Radke et al., 2022; McKee et al., 2020; Phan et al., 2021). These methods typically assume fixed or emergent group structures or modify each agent's global utility function. In contrast, DRIVE introduces no explicit coalitions or shared rewards: incentives arise solely through local, bilateral reward exchanges, enabling decentralized alignment without predefined teams or population-level reward mixing.

5 Theoretical Analysis

In the following, we analyze the incentive alignment properties of DRIVE in the general PD and its invariance to changing rewards. We emphasize that the mechanism does not guarantee convergence of learning dynamics, but rather reshapes incentives such that cooperation becomes the individually rational choice in repeated interactions. Although our formal discussion focuses on the canonical PD, many well-known sequential social dilemmas (SSDs), such as Coin and Harvest, instantiate PD-like incentive structures, as shown empirically in (Leibo et al., 2017) and explained in the Appendix. In Sec. 8, we further show that DRIVE also yields promising results in more complex SSDs with more than two agents.

DRIVE in the General Prisoner's Dilemma In social dilemmas with a payoff table, as shown in Fig. 1, and inequalities $T > R > P > S$ of Eq. (1), the DRIVE incentives do not change the payoffs R for mutual cooperation and P for mutual defection in the long run because the reward difference $\Delta_{t,i,j}$ would be zero for both agents. With $R > P$, this will still favor mutual cooperation over mutual defection. However, if there were (repeated) unilateral defection, the defective agent i would send a request T to the exploited agent j, which responds with a difference of $\Delta_{t,i,j} = S - T < 0$ in the worst case, where the reward of the defective agent i would change to $T + \Delta_{t,i,j} = T + S - T = S$, while the reward of the exploited agent j would change to $S - \Delta_{t,i,j} = S - (S - T) = T$, according to Eq. (5). As shown in Fig. 2b, the DRIVE payoff switch of T and S enables both agents to overcome greed and fear, therefore incentivizing cooperation.

Theorem 1. *DRIVE aligns incentives in a generalized two-agent Prisoner's Dilemma such that under TD-gate activation for unilateral defection and sufficiently low epoch-average reward of the exploited agent, mutual cooperation becomes a dominant strategy by effectively reversing the temptation and sucker payoffs.*

Proof sketch. As argued above, DRIVE leaves mutual cooperation and mutual defection unchanged in the long run, so the payoffs $\hat{R}$ and $\hat{P}$ are preserved. Under unilateral defection (D, C), Theorem 5 implies that the exploiting agent issues a request, and Lemma 1 yields a strictly negative response $\Delta_{t,i,j} = \overline{u}_j - \hat{T} \in [\hat{S} - \hat{T}, 0)$. Substituting into Eq. (5) gives

$$u_{t,i}^{\text{DRIVE}} = \hat{T} + \Delta_{t,i,j} = \overline{u}_j, \qquad u_{t,j}^{\text{DRIVE}} = \hat{S} - \Delta_{t,i,j}.$$

Hence, unilateral defection is transformed from $(\hat{T}, \hat{S})$ to $(\overline{u}_j, \hat{S} - \Delta_{t,i,j})$, which recovers the payoff inversion $(\hat{T}, \hat{S}) \leftrightarrow (\hat{S}, \hat{T})$ in the steady case $\overline{u}_j \approx \hat{S}$. More generally, whenever $\overline{u}_j < \hat{R}$, defecting against a cooperator yields less payoff than mutual cooperation, so greed is removed while fear remains overcome by $\hat{T} > \hat{P}$. Therefore, under bounded and rational critics, mutual cooperation is the dominant strategy under DRIVE. A full derivation is provided in Appendix A. □

Overall, DRIVE does not rely on fixed incentive values or domain-dependent parameters. Thus, it can cope with reward changes that still satisfy the PD inequalities w.r.t. greed and fear, as in the example of Fig. 1c. For clarity, Appendix A.1 provides an extended example that concretely demonstrates the shaping mechanism in a single PD exchange step. Note that Eq. (5) effectively turns the stage game into a coordination game with (C, C) as the unique Nash equilibrium. This reflects standard reward-design practice: instead of relying on learners to infer long-term externalities, we adjust instantaneous payoffs so that cooperation is individually rational while leaving the environment dynamics unchanged.

Invariance to Changing Rewards We now analyze DRIVE and MATE with respect to their invariance to changing rewards in the PD, i.e., where the original payoffs R, P, T, and S are dynamically altered by some external change function f_{mod}.

Definition 1 (Reward Change Function). Let $r_{t,i}$ denote the original environmental reward of agent i at time t. The modified reward in epoch m is defined as $r'_{t,i} = f_{mod}(r_{t,i}, m) = c_m r_{t,i} + b_m$, where $c_m > 0$ and $b_m \in \mathbb{R}$ are epoch-dependent scaling and shifting parameters that apply uniformly to all agents and timesteps within epoch m. This shared affine map preserves the strategic structure of the game (e.g., PD inequalities) while shifting reward magnitudes and offsets. We focus on this broad but tractable class of per-epoch affine transformations: arbitrary schedules c_m and b_m cover all reward dynamics in Sec. 8 and remain compatible with our per-epoch normalization scheme. Further illustrations and edge cases, including epochs where $c_m \approx 0$, are provided in Appendix A.7.

Theorem 2. *MATE agents are not invariant to changing rewards in the general PD, altered by f_{mod}.*

Proof. According to the MATE payoff matrix in Fig. 2c, the global token $\mathbf{x} = x_1 = x_2 > 0$ must satisfy $\mathbf{x} \geq max\{P - S, \frac{T-R}{3}\}$ for emergent cooperation. When the change function f_{mod} is chosen such that $f_{mod}(P-S) > \mathbf{x}$ or $f_{mod}(\frac{T-R}{3}) > \mathbf{x}$, then MATE agents are no longer guaranteed to cooperate mutually. $\square$

Note that Theorem 2 can be generalized to any other PI method that uses fixed peer incentive values. One could, in principle, re-tune x after each change in f_{mod}, but this requires additional global knowledge or meta-optimization, whereas DRIVE adapts automatically through local reward differences.

Theorem 3. *DRIVE agents are invariant to changing rewards in the general PD, altered by f_{mod}.*

Proof. Altering the original payoffs R, P, T, and S by any f_{mod} would proportionally change the DRIVE payoff matrix in Fig. 2b. Thus, DRIVE agents are always incentivized to cooperate mutually as the inequalities to overcome greed and fear remain satisfied. $\square$

We now extend the invariance analysis from the PD to general SSDs using policy gradient methods with return normalization, as detailed in Appendix A.9.

Theorem 4. *DRIVE agents are invariant to changing rewards in SSDs, where environmental rewards are altered by f_{mod} (Definition 1), when trained with normalized policy gradient methods (Lemma 3).*

Consider sequential social dilemmas with returns normalized per epoch to zero mean and unit variance. If rewards are transformed by a positive affine map per epoch, then both (i) standard policy gradient learning and (ii) DRIVE's shaped rewards remain invariant with respect to the normalized return $\overline{G}_{t,i}$. Consequently, the incentive alignment induced by DRIVE persists under per-epoch reward scaling and shifting within this class of transformations. Overall, under per-epoch normalization, both the base policy-gradient updates and DRIVE's shaped rewards are invariant to shared per-epoch positive affine reward transformations (Lemma 3).

Proof. The result follows from two components. First, Lemma 3 shows that standard policy gradient RL is invariant to positive affine reward transformations under continuing discounted returns and per-epoch normalization. Second, DRIVE shapes rewards via differences between epoch-average and instantaneous rewards. Applying f_{mod} gives $\Delta'_{t,i,j} = f_{mod}(\overline{u}_i) - f_{mod}(u_{t,i}) = f_{mod}(\Delta_{t,i,j})$. Hence the DRIVE-shaped reward also transforms affinely: $u^{DRIVE'}_{t,i} = c_m u^{DRIVE}_{t,i} + b_m$. Applying Lemma 3 to the resulting continuing discounted returns yields identical normalized returns. Therefore, both the base policy-gradient updates and DRIVE's shaped rewards are invariant to such transformations. $\square$

Effects of Non-Adherence to the Protocol The preceding analysis assumes that all agents truthfully and synchronously follow the DRIVE protocol, i.e., each agent shares its epoch-average reward, responds to requests, and applies the shaping rule consistently. In practice, however, communication failures, delays, or strategic misreporting may occur. Here we analyze the impact of such *non-adherence* compared to other PI approaches; for a detailed example, see Appendix A.5.

- **Full compliance** When all agents follow the protocol truthfully, the results of Theorem 1 and Theorems 3–4 apply. Payoffs T and S are swapped under unilateral defection, ensuring incentive alignment toward cooperation. This reasoning can be generalized to SSDs beyond the PD, provided the characteristic inequalities for greed and fear are preserved.

- **No requests sent (despite TD ≥ 0)** An agent that withholds requests can still receive requests and respond truthfully. For its neighbors, this means one fewer reciprocal request. Due to the min aggregation, their penalization levels may increase slightly, but are not substantially affected as long as other agents send requests. For the non-requesting agent itself, $\hat{u}_{res} = 0$, so it forfeits the opportunity for reciprocal improvement and is indirectly penalized. If the agent defects, it may temporarily avoid penalization, but overall, it loses the benefits of mutual shaping and does not gain a stable advantage.

- **No responses sent** If an agent does not respond to requests (due to communication loss or intentional withholding), the effect depends on the context: If the agent is defecting, withholding its negative Δ weakens the penalty on its exploited neighbor. However, it also loses the chance to benefit from reciprocity, so deliberate non-response is not rational. If the agent is cooperative, the missing (typically positive or small) Δ has a limited effect because the min aggregation dampens single missing contributions. Thus, non-response is mostly neutral or slightly beneficial for defectors but costly overall.

- **False requests or responses** Two types of misbehavior are possible: *Sending requests with TD < 0:* This can occur due to noise or early training misestimation. Such requests typically yield small or positive differences that are filtered out by the min operator and thus have little impact. *Sending false responses:* An agent could deliberately misreport Δ to distort shaping. In the worst case, the min aggregation could impose unjustified penalties on requesters, potentially undermining cooperation. This depicts a fragility and limitation of DRIVE.

- **No compliance at all** If all agents withhold or communication fails globally, then all shaping terms vanish. The system collapses to plain MARL without incentives, and mutual defection becomes a possible equilibrium again. This is similar to fixed-token methods like MATE, which also break down if their coordination mechanism is unavailable.

Conceptual Discussion DRIVE offers a simple, adaptive PI mechanism for fostering cooperation in SDs with changing rewards. It operates through local peer interactions, requiring no central controller, global knowledge, or all-to-all communication. Similar to (Hughes et al., 2018; Yang et al., 2020; Phan et al., 2024), Algorithm 2 scales linearly with $\mathcal{O}(4(n-1))$ in the worst case with respect to incentive exchanges. At the same time, DRIVE relies on truthful peer communication to function correctly. Partial compliance leads to *graceful degradation*: as long as at least one honest responder provides feedback, defectors are still penalized; if all agents fail to comply, DRIVE reduces to baseline MARL dynamics. Compared to fixed-token methods, DRIVE is at least as robust and often more adaptive, but its reliance on strict adherence to the exchange protocol introduces a new potential fragility. Designing protocol variants that are robust to partial compliance – for example, through redundant aggregation rules, stochastic auditing, or alternative shaping operators– remains an important avenue for future work.

A key modeling assumption is the neighborhood $N_{t,i}$ that restricts which agents can exchange incentives. In our experiments, this neighborhood is tied to the environment as introduced in the subsequent section. Crucially, DRIVE's min-aggregation means a defector's shaped reward depends only on its most exploited neighbor, so, unlike simple reward-sharing schemes, penalties do not dilute with larger populations. Appendix A.5 extends the previous compliance analysis to general N-agent systems and arbitrary communication graphs, and formalizes the resulting robustness: defector penalization holds exactly when compliant agents form a dominating set. Thus, cooperation incentives degrade smoothly rather than collapsing abruptly under partial compliance.

As shown in the modified PD payoff tables in Fig. 2b, DRIVE only depends on the environmental rewards without requiring fixed incentive values x as MATE, domain-dependent coefficients α, β as IA, or time-consuming incentive learning of x_C^i, x_D^i as LIO. Note that given the characteristics of greed and fear exhibited by general PDs, the above theoretical analysis generally applies to various SDs. Thus, DRIVE can be used in any SD, where rewards change dynamically through an external and unknown change function f_{mod}. If the conditions for cooperation, i.e., characteristic inequalities of the SD, remain the same, DRIVE can adapt and maintain cooperation, as shown in Fig. 1c and later demonstrated.

6 Experimental Setup[2]

We use three well-known SSDs based on (Foerster et al., 2018; Perolat et al., 2017a). At every time step, the order of agent actions is randomized to resolve conflicts, e.g., when multiple agents step on a coin or tag each other simultaneously. All SSDs represent PD instances, as empirically shown in (Leibo et al., 2017) and Appendix B. Since we modify the rewards by f_{mod}, we assess the cooperation with domain-specific measures. For each experiment, all respective algorithms were run 20 times over $E = 4,000$ epochs of 10 episodes to report the average progress and the 95% confidence interval.

Iterated Prisoner's Dilemma For IPD, we use the payoff matrix shown in Fig. 1b. Both agents observe the previous joint action $z_{t,i} = a_{t-1}$ at every time step t, which is the zero vector at the start state s_0. The Nash equilibrium is always to defect (DD). An episode consists of $H = 150$ iterations, and we set $\gamma = 0.95$. The neighborhood $\mathcal{N}_{t,i} = \{j\}$ is defined by the other agent $j \neq i$. We measure the *Cooperation Rate* as the cooperation (CC) count per episode divided by H.

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[2]Implementations are appended and will be open-sourced upon publication.

Coin   *Coin-2* and *Coin-4* are SSDs and consist of $n \in \{2, 4\}$ agents with different colors, which start at random positions and have to collect a coin with a random color and position (Lerer & Peysakhovich, 2017; Foerster et al., 2018). If an agent collects a coin, it receives a reward of $+1$. However, if the coin has a different color than the collecting agent, another agent with the actual matching color is penalized with -2. After being collected, the coin respawns randomly with a new color. All agents can observe the entire field and can move north, south, west, and east. Each agent can only determine whether a coin is the same color as itself. An episode terminates after $H = 150$ time steps, and we set $\gamma = 0.95$. The neighborhood $\mathcal{N}_{t,i} = \mathbb{D} - \{i\}$ is defined by all other agents $j \neq i$. We measure the *own coin rate* $P(own\ coin) = \frac{\#\ collected\ coins\ with\ same\ color}{\#\ all\ collected\ coins}$ based on the coins collected by each agent.

Harvest   *Harvest-12* is an SSD and consists of $n = 12$ agents, starting at random positions and having to collect apples. The apple regrowth rate depends on the number of surrounding apples (Perolat et al., 2017a). If all apples are harvested, no apples will grow until the episode terminates. At every time step, all agents receive a time penalty of -0.01. For each collected apple, an agent receives a reward of $+1$. All agents have a 7×7 field of view and can do nothing, move north, south, west, or east, or tag other agents within their field of view with a tag beam of width 5, pointed to a specific cardinal direction. If an agent is tagged, it is unable to act for 25 time steps. Tagging does not yield any rewards. An episode terminates after $H = 250$ time steps, and we set $\gamma = 0.99$. The neighborhood $\mathcal{N}_{t,i}$ is defined by all other agents $j \neq i$ being in the field of view of agent i. We measure the *Sustainability*, defined by the average number of time steps at which apples are collected.

MARL Algorithms   To isolate the impact of reward changes on PI mechanisms rather than the base RL algorithm, we implement all methods including DRIVE based on the standard policy gradient algorithm (Eq. 2) with normalized returns (Appendix A.9), as suggested in (Hessel et al., 2019), which also serves as Naive Learning baseline without any PI-based reward shaping (Foerster et al., 2018). We use LIO, MATE with $x = 1$ as suggested in (Phan et al., 2024), and IA with $\alpha = 5$ and $\beta = 0.05$ as state-of-the-art PI baselines (Hughes et al., 2018; Yang et al., 2020; Phan et al., 2024). For *IPD* and *Coin-2*, we directly include the performance of the opponent shaping techniques LOLA-PG and POLA-DiCE, as reported in (Foerster et al., 2018; Zhao et al., 2022), due to the high computational demand of the second-order derivative calculation.

7   Experimental Results under Stationary Rewards

Setting   We compare DRIVE with the baselines in *IPD*, *Coin-2*, *Coin-4*, and *Harvest-12* without any reward change, i.e., $f_{mod}(u, m) = u$ (Algorithm 1, Line 15), in all epochs m.

Results   The results are shown in Fig. 3. DRIVE achieves competitive and stable cooperation in *IPD* compared with all baselines. In *Coin-2*, DRIVE and MATE achieve the highest *own coin* rate, significantly outperforming POLA-DiCE, which is more cooperative than LIO, IA, and LOLA-PG. In both larger SSDs, namely *Coin-4* and *Harvest-12*, DRIVE and MATE achieve the highest level of cooperation, where DRIVE is slightly more cooperative in *Coin-4*, while MATE is slightly more cooperative in *Harvest-12*.

Figure 3: Average progress of DRIVE and other baselines in SSDs without reward change. Shaded areas show the 95% confidence interval. The results of LOLA-PG and POLA-DiCE are from (Foerster et al., 2018; Zhao et al., 2022).

8 Experimental Results under Dynamic Reward Changes

Setting   Next, we evaluate DRIVE and the baselines with different reward change functions f_{mod}.

   I **Linear increase:** $f_{mod}^{I}(u, m) = u(\eta m + 1)$. This models a steadily increasing reward scale, for instance, due to rising system-wide demand or progressively stronger performance targets.

  II **Exponential decay:** $f_{mod}^{II}(u, m) = ue^{-\eta m}$. This models gradual reward attenuation, e.g., from sensor wear, hardware degradation, or slowly worsening signal quality over time.

 III **Stepwise increase:** $f_{mod}^{III}(u, m) = u(\lfloor \eta m \rfloor + \chi)$. This models discrete distribution shifts with abrupt rescalings, as commonly observed when switching between training phases, simulators, or simulation-to-reality deployment.

 IV **Damped cosine modulation:** $f_{mod}^{IV}(u, m) = \eta + u\left(1 - \frac{m}{E}\right)\cos^2(2\eta m)$. This models irregular, non-monotonic reward changes (with a decaying amplitude), for example from evolving specifications, intermittent human feedback, or online reward redesign.

We set $\eta = 0.001$ and $\chi = 10$. Together, these functions cover monotone growth (I, III), convergence toward zero (II), and oscillatory, time-varying shifts (IV), while preserving the underlying payoff ordering of the social dilemma.

Figure 4: Average progress of DRIVE and other baselines in SSDs with different reward change functions f_{mod} I, II, III, and IV, illustrated left and in Fig. 7. Shaded areas show the 95% confidence interval. The results of LOLA-PG and POLA-DiCE are from (Foerster et al., 2018; Zhao et al., 2022). The non-PI approaches Naive Learning, LOLA-PG, and POLA-DiCE are largely insensitive to the reward changes of f_{mod} considered here due to per-epoch return normalization, as explained in Appendix A.9.

Results   The results are shown in Fig. 4. The learning curve of DRIVE is not significantly affected by training with the functions f_{mod}^{I}, f_{mod}^{II}, and f_{mod}^{III}. Function f_{mod}^{IV} causes occasional dips in the learning curve of DRIVE, where the scaling factor approaches zero, temporarily collapsing the payoff ordering of the underlying dilemma. However, since these low-scale epochs are isolated and the modulation quickly moves away from this regime, DRIVE rapidly recovers its learning dynamics and performance level. LIO is robust against any change function in *Coin-4*, but its cooperation level significantly deteriorates in other domains. Despite automatically learning an incentive function, LIO is especially sensitive to f_{mod}^{IV}. IA is affected in *Coin-2* and *Coin-4*, where it never outperforms Naive Learning. MATE is only able to resist reward changes in *Harvest-12* when training with f_{mod}^{I}. In all other cases, MATE's cooperation level significantly deteriorates, even worse than Naive Learning in some cases. The learned behavior is least stable with f^{IV}, where MATE is not able to recover from dips in the learning curve, unlike DRIVE. DRIVE is the only PI method that outperforms Naive Learning, LOLA-PG, and POLA-DiCE in *IPD* and *Coin-2*. Appendix C provides further cooperation metrics (social welfare, equality, sustainability, and peace) in *Harvest-12*.

9   Discussion

We presented DRIVE, an adaptive PI approach that achieves and maintains cooperation in SDs with changing rewards. DRIVE agents reciprocally exchange reward differences to incentivize mutual cooperation in a fully decentralized manner. Our theoretical analysis shows how DRIVE aligns incentives toward mutual cooperation in the general Prisoner's Dilemma by overcoming greed and fear while remaining invariant to per-epoch reward scaling, and empirically robust to the considered reward changes. This contrasts with prior PI methods that rely on fixed incentive values, domain-dependent coefficients, or time-consuming incentive learning. Consequently, DRIVE is better aligned with game-theoretic assumptions and safer to deploy in environments with drifting rewards. Our experiments further demonstrate that DRIVE significantly outperforms state-of-the-art methods such as LIO, MATE, and IA, as well as opponent-shaping baselines such as POLA-DiCE and LOLA-PG, across multiple SSDs with dynamic reward changes. The results confirm the sensitivity of existing PI approaches to reward magnitudes and highlight DRIVE's ability to sustain cooperation under such transformations, provided the underlying strategic inequalities remain intact.

Despite these promising results, DRIVE relies on truthful and synchronous peer communication. Partial non-compliance results in graceful degradation of performance. Moreover, the current theoretical analysis assumes homogeneous populations and complete or well-connected communication graphs. These assumptions may not hold in more realistic settings with strategic manipulation, communication noise, or sparse interaction structures. Several directions for future work follow from these observations. One avenue is to develop mechanisms that are robust to partial or strategic non-compliance, for example, through redundant aggregation, stochastic auditing, or consensus systems (Altmann et al., 2025). Extending the theoretical analysis to heterogeneous populations and more general network topologies represents another important step toward real-world applicability. A natural next step is to study learned and dynamic neighborhoods, and to combine DRIVE with models of evolving social structure and coalitions, as suggested by recent work on reward sharing in teams and coalitions. Finally, incorporating agent identification could enable targeted bilateral responses, e.g., against adversarial peers.

Broader Impact Statement

This work proposes a decentralized peer-incentivization mechanism designed to promote cooperation in multi-agent systems under changing rewards. A key positive impact is improved robustness of cooperative behavior when reward magnitudes vary over time, which is relevant for real-world applications such as distributed control, resource management, and multi-robot coordination. By reducing dependence on fixed incentive magnitudes, the approach may help bridge gaps between training and deployment conditions. At the same time, the method relies on inter-agent communication and protocol adherence. In practice, agents may misreport or fail to communicate, which could degrade cooperation or introduce vulnerabilities. These risks are particularly relevant in complex or human-facing environments not captured by the settings studied here. We therefore view this work as a step toward more adaptive decentralized cooperation, but not as a complete solution for real-world deployment. Future work should investigate robustness to non-compliance and adversarial behavior, as well as safeguards such as auditing or constraints on incentive exchange.

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A   Extended Theoretical Results

In this section, we provide additional worked-out examples and detailed arguments to complement the theoretical analysis in the main body. These results give a more concrete and intuitive understanding of how DRIVE operates in simple settings, how its behavior changes under different assumptions of protocol adherence, and how the microscopic request/response mechanism underpins the macroscopic equilibrium results, and provides a simple extension to larger multi-agent settings.

Preliminaries   We recall the standard two-player Prisoner's Dilemma (PD) with actions C (cooperate) and D (defect) and payoffs (R, R), (P, P), (T, S), and (S, T) for profile (C, C), (D, D), (D, C), and (C, D), respectively (Fig. 1). The game is a PD if $T > R > P > S$ (cf. Eq. 1), where $T > R$ encodes greed and $P > S$ encodes fear (Axelrod, 1984). We denote the environmental reward of agent i at time t by $u_{t,i}$, the externally modified reward in epoch m by $\hat{u}_{t,i} = f_{mod}(u_{t,i}, m)$, and the running average of $\hat{u}_{t,i}$ within epoch m by $\bar{u}_i$. The DRIVE shaping rule for agent i at time t is

$$u_{t,i}^{\text{DRIVE}} = \hat{u}_{t,i} - \min\{\langle \Delta_{t,j,i} \rangle_{j \in \mathcal{N}_{t,i}}\} + \min\{\langle \Delta_{t,i,j} \rangle_{j \in \mathcal{N}_{t,i}}\}, \quad \text{with} \tag{6}$$

$$\Delta_{t,i,j} = \begin{cases} \bar{u}_j - \hat{u}_{t,i}, & \text{if } TD_i(\hat{u}_{t,i}) \geq 0, \\ 0, & \text{otherwise,} \end{cases} \tag{7}$$

where $\Delta_{t,j,i}$ is the *response that i sends* to j's request (hence it is *subtracted*), while $\Delta_{t,i,j}$ is the *response received* by i to its own request (hence it is *added*). Intuitively, $TD_i(\hat{u}_{t,i}) \geq 0$ means that the realized one-step outcome was at least as good as what the critic predicted.

A.1   Single Exchange Mechanism Underlying Incentive Alignment in a 2-Player Prisoner's Dilemma

We give a concrete, single-step derivation showing how the DRIVE request/response protocol (Alg. 2) together with the TD gate in Eq. (3) and the shaping rule in Eq. (4) yields the *payoff swap* $T \leftrightarrow S$ under unilateral defection. This turns the PD into a coordination game with (C, C) as the unique Nash equilibrium. Unless otherwise stated, we assume full compliance with the protocol.

Setup   Consider a single time step t in a 2-agent PD with payoffs $T > R > P > S$ and neighborhoods $N_{t,1} = \{2\}$, $N_{t,2} = \{1\}$. Rewards may already be transformed by f_{mod} in epoch m; for notational convenience we write

$$\hat{T} := f_{mod}(T, m), \quad \hat{R} := f_{mod}(R, m), \quad \hat{P} := f_{mod}(P, m), \quad \hat{S} := f_{mod}(S, m).$$

We assume that, in the long run under stationary play, epoch averages coincide with the corresponding instantaneous payoffs for each action profile (e.g., under (C, C) both agents have $\bar{u}_i = \hat{R}$). Concretely, we assume $\bar{u} \approx \hat{u}$ in the following to isolate the intended mechanism; the subsequent discussion explains how deviations $\bar{u}_j \neq \hat{u}_{t,j}$ do not fundamentally change the direction of shaping in exploitation states, but modulate its magnitude to reflect longer-term (epoch-level) advantage.

Mutual cooperation and mutual defection   If both agents cooperate at time t, each receives $\hat{u}_{t,1} = \hat{u}_{t,2} = \hat{R}$ and, in steady state, $\bar{u}_1 = \bar{u}_2 = \hat{R}$. Hence $\Delta_{t,1,2} = \bar{u}_2 - \hat{u}_{t,1} = 0$ and $\Delta_{t,2,1} = 0$, so Eq. (6) yields

$$u_{t,1}^{\text{DRIVE}} = \hat{R}, \quad u_{t,2}^{\text{DRIVE}} = \hat{R}.$$

A similar argument shows that under mutual defection, both agents retain payoff $\hat{P}$. Thus, DRIVE leaves R and P unchanged in the long run.

Unilateral defection   Now consider a state where agent 1 defects (D) and agent 2 cooperates (C), so the instantaneous modified rewards are $\hat{u}_{t,1} = \hat{T}$, $\hat{u}_{t,2} = \hat{S}$. Under the usual PD ordering, the defector benefits from a higher reward than the cooperator. We assume that this yields a non-negative TD advantage for the defector and a non-positive one for the cooperator, so that

$$TD_1(\hat{u}_{t,1}) \geq 0 \;\Rightarrow\; \text{agent 1 sends a request}, \qquad TD_2(\hat{u}_{t,2}) < 0 \;\Rightarrow\; \text{agent 2 does not send.} \tag{8}$$

This corresponds to the intended operating regime of DRIVE and matches the empirical behavior observed in our experiments. Agent 1 sends its instantaneous reward $\hat{u}_{t,1} = \hat{T}$ to agent 2 as a request. Upon receiving this, agent 2 computes the (epoch-m) difference $\Delta_{t,1,2} = \overline{u}_2 - \hat{u}_{t,1}$. In the PD step considered, the worst-case consistent choice is $\overline{u}_2 = \hat{S}$, yielding $\Delta_{t,1,2} = \hat{S} - \hat{T} < 0$. Agent 2 returns this value to agent 1. Because only agent 1 sent a request, the reverse difference $\Delta_{t,2,1}$ is undefined in this step; by Algorithm 2 it defaults to 0 for aggregation when no responses arrive. Using the responder's epoch-average $\overline{u}_j$ rather than its instantaneous reward makes DRIVE sensitive to systematic exploitation instead of single noisy outcomes. Only agents whose recent average return is consistently lower than a neighbor's request generate strong negative Δ terms. If both sides used instantaneous rewards, a single lucky or unlucky step could trigger large transfers, making incentives noisy and easy to game via short-term risk-taking. Using instantaneous rewards against averages would instead turn DRIVE into a risk-sharing mechanism, while comparing averages on both sides would be very stable but slow to react. The chosen average–instant design therefore balances robustness to noise with responsiveness to emerging exploitation. Moreover, the sign pattern in exploitation states is stable: since $\hat{T}$ is the maximal one-step payoff in the PD, any bounded epoch-average $\overline{u}_2 \leq \hat{T}$ implies $\Delta_{t,1,2} = \overline{u}_2 - \hat{T} \leq 0$, so the response received by the defector remains non-positive even when $\overline{u}_2 \neq \hat{S}$. Deviations $\overline{u}_2 > \hat{S}$ soften the swap (smaller penalty), while $\overline{u}_2 < \hat{S}$ strengthens it (larger penalty), reflecting epoch-level disadvantage. In the 2-player case, the minima over neighbors reduce to single terms. The per-step shaped rewards are

$$\hat{u}_{t,1}^{\mathrm{DRIVE}} = \hat{u}_{t,1} - \underbrace{\min\{\Delta_{t,2,1}\}}_{=\,0} + \underbrace{\min\{\Delta_{t,1,2}\}}_{=\,\hat{S}-\hat{T}} = \hat{T} + (\hat{S} - \hat{T}) = \hat{S}, \tag{9}$$

$$\hat{u}_{t,2}^{\mathrm{DRIVE}} = \hat{u}_{t,2} - \underbrace{\min\{\Delta_{t,1,2}\}}_{=\,\hat{S}-\hat{T}} + \underbrace{\min\{\Delta_{t,2,1}\}}_{=\,0} = \hat{S} - (\hat{S} - \hat{T}) = \hat{T}. \tag{10}$$

Thus, the unilateral defection step $(\hat{T}, \hat{S})$ is reshaped to $(\hat{S}, \hat{T})$: the defector receives the sucker payoff and the cooperator the temptation payoff. Eqs. (9–10) explicitly demonstrate how the TD gate together with the DRIVE shaping rule realizes the $T \leftrightarrow S$ swap in a single exchange step. By symmetry, the profile (C, D) is reshaped from $(\hat{S}, \hat{T})$ to $(\hat{T}, \hat{S})$.

Resulting incentives and equilibrium interpretation Collecting all action profiles, DRIVE induces the modified payoff matrix with $\hat{T} > \hat{R} > \hat{P} > \hat{S}$. Hence, if the opponent plays C, responding with C yields

	C	D
C	$\hat{R}, \hat{R}$	$\hat{S}, \hat{T}$
D	$\hat{T}, \hat{S}$	$\hat{P}, \hat{P}$

$\hat{R} > \hat{S}$, and if the opponent plays D, responding with C yields $\hat{T} > \hat{P}$. Cooperation is therefore a strict best response to both actions, so (C, C) is the unique Nash equilibrium.

Takeaway Under the TD gate (Eq. 3) and shaping rule (Eq. 5), a single request/response exchange in a unilateral defection state deterministically maps $(\hat{T}, \hat{S}) \mapsto (\hat{S}, \hat{T})$, eliminating greed and fear incentives in the transformed PD for that step. This microscopic mechanism directly underpins the equilibrium-level result that DRIVE turns the Prisoner's Dilemma into a coordination game with cooperation as the unique Nash equilibrium, providing a worked-out complement to the proof of Theorem 1.

A.2 Long-term incentives using average rewards

DRIVE compares a requester's instantaneous reward to the responder's epoch-average reward $\overline{u}_j$ (Eq. 7):

$$\overline{u}_{t,j} = \frac{1}{t+1} \sum_{k=0}^{t} \hat{u}_{k,j}. \tag{11}$$

This choice is not unique: one could instead compare instantaneous rewards on both sides, or use averages on both sides. We analyze the resulting design space and argue that the *average–instant* comparison used in DRIVE is a robust compromise between responsiveness and stability.

Instant–instant $(\hat{u}_{t,j} - \hat{u}_{t,i})$. If we replaced $\overline{u}_j$ by $\hat{u}_{t,j}$, then $\Delta_{t,i,j} = \hat{u}_{t,j} - \hat{u}_{t,i}$ would react to single-step noise. A single lucky outcome can generate large transfers, making incentives high-variance and easy to game (e.g., via short-term risk-taking) even when long-run behavior is unchanged.

Instant–average (compare responder instant to requester average). This tends to implement *risk sharing*: a responder that just experienced a low instantaneous reward may penalize others even if it is not disadvantaged on average. In social dilemmas, this can blur the distinction between exploitation and variance, creating transfers driven by short-term fluctuations.

Average–average (compare averages on both sides). Very stable but slow: it only reacts after the averages of both agents separate substantially. This delays punishment/compensation and can fail to respond quickly to sudden changes in behavior (e.g., a defection episode starting mid-epoch).

Average–instant (DRIVE). By comparing the requester's instantaneous reward to the responder's epoch average, DRIVE stays responsive to *current* potentially exploitative outcomes (large request) while using the responder's average to decide whether this outcome reflects a *systematic* imbalance. This balances responsiveness (instant) with robustness (average) and reduces the sensitivity present in instant–instant schemes. Using $\overline{u}_j$ instead of $\hat{u}_{t,j}$ makes DRIVE respond to *systematic* advantage, not single outcomes. Still, $\overline{u}_j$ can deviate from the instantaneous payoff in meaningful ways:

- **Responder doing better than the current outcome $(\overline{u}_j > \hat{u}_{t,j})$.** This happens if j has recently enjoyed higher returns in the epoch. In unilateral defection (D, C), this increases $\Delta_{t,i,j} = \overline{u}_j - \hat{T}$ making it *less negative* than $\hat{S} - \hat{T}$, so the penalty to the defector and the boost to the cooperator become *weaker.*

- **Responder doing worse than the current outcome $(\overline{u}_j < \hat{u}_{t,j})$.** This occurs if j has been systematically disadvantaged earlier in the epoch. Then $\Delta_{t,i,j} = \overline{u}_j - \hat{T}$ becomes *more negative*, strengthening the penalty on the requester (defector) and strengthening the compensation to the responder (cooperator).

A key correction to the informal intuition is that Δ is *not* guaranteed to be negative. Eq. (7) can be positive whenever the responder's epoch-average exceeds the requester's instantaneous reward, i.e., $\overline{u}_j > \hat{u}_{t,i}$. However, in the *exploitation* regime of a Prisoner's Dilemma (PD), the requester receives the maximal one-step payoff $\hat{T}$. As the epoch-average $\overline{u}_j$ is bounded by the same payoff range as one-step rewards, $\overline{u}_j \leq \hat{T}$, and $\Delta_{t,i,j} < 0$ is guaranteed. Hence, in exploitation, Δ is robustly negative, which yields DRIVE's intended swap. Outside exploitation, Δ may have either sign and typically yields small or canceling adjustments in symmetric outcomes.

Lemma 1 ($\Delta < 0$ in unilateral defection). *Consider unilateral defection (D, C) in a PD with modified payoffs $\hat{T} > \hat{R} > \hat{P} > \hat{S}$, where agent i defects and receives $\hat{u}_{t,i} = \hat{T}$ while agent j cooperates and receives $\hat{u}_{t,j} = \hat{S}$. Let $\overline{u}_j$ be the epoch average of agent j maintained via the uniform running mean (Eq. 11, Alg. 1). Then $\hat{T} > \overline{u}_j \geq \hat{S}$ and therefore $\Delta_{t,i,j} = \overline{u}_j - \hat{T} \in [\hat{S} - \hat{T}, 0[$. Thus, $\Delta_{t,i,j}$ is strictly negative.*

Proof. By (11), $\overline{u}_{t,j}$ is the arithmetic mean of the values $\{\hat{u}_{k,j}\}_{k=0}^{t}$. Since all modified payoffs lie in $[\hat{S}, \hat{T}]$, we have $\hat{S} \leq \hat{u}_{k,j} \leq \hat{T}$ and the averages remain in $[\hat{S}, \hat{T}]$. Since at time t we have $\hat{u}_{t,j} = \hat{S}$, at least one summand is strictly smaller than $\hat{T}$, and the arithmetic mean is strictly smaller than $\hat{T}$, implying $\Delta_{t,i,j} < 0$. $\qquad\square$

Analogously, we can derive the following bounds:

Unilateral Defection:	$\Delta_{DC} \in [\hat{S} - \hat{T}, 0[\,,$	with $\quad \hat{u}_{t,i} = \hat{T}, \hat{u}_{t,j} = \hat{S}$, and $\hat{T} > \overline{u}_j \geq \hat{S}$	(12)
Mutual Defection:	$\Delta_{DD} \in\,]\hat{S} - \hat{P}, \hat{T} - \hat{P}[\,,$	with $\quad \hat{u}_{t,i} = \hat{P}, \hat{u}_{t,j} = \hat{P}$, and $\hat{T} > \overline{u}_j > \hat{S}$	(13)
Mutual Cooperation:	$\Delta_{CC} \in\,]\hat{S} - \hat{R}, \hat{T} - \hat{R}[\,,$	with $\quad \hat{u}_{t,i} = \hat{R}, \hat{u}_{t,j} = \hat{R}$, and $\hat{T} > \overline{u}_j > \hat{S}$	(14)
Unilateral Cooperation:	$\Delta_{CD} \in\,]0, \hat{T} - \hat{S}]\,,$	with $\quad \hat{u}_{t,i} = \hat{S}, \hat{u}_{t,j} = \hat{T}$, and $\hat{T} \geq \overline{u}_j > \hat{S}$	(15)

Dominance conditions for the min**-aggregation** In multi-agent settings, DRIVE aggregates responses using a minimum across neighbors. While exploitation responses Δ_{DC} are always negative (Lemma 1), symmetric outcomes (C, C) and (D, D) can produce deltas that are either positive or negative depending on the responder's epoch-average reward. A natural question is therefore: *Under which conditions is the exploitation response Δ_{DC} guaranteed to dominate the* min-*aggregation (i.e., be the most negative response)?*

Since $\Delta_{CD} > 0$ (being defected against) always holds, this case can be ignored for the min operator. Moreover, under calibrated critics, the TD gate rarely activates for the exploited agent receiving the minimal payoff $\hat{S}$ (cf. Theorem 5), making this case structurally unlikely. We therefore compare exploitation responses (D, C) with the lower bounds of symmetric outcomes (C, C) and (D, D). Let the responder's epoch-average under exploitation be rewritten as: $\Delta_{t,i,j} = \overline{u}_j - \hat{u}_{t,i} = \hat{u}_{t,j} + \delta - \hat{u}_{t,i}$. The parameter δ measures how far the exploited agent's mean reward deviates from steady exploitation. In unilateral defection, for instance, $\overline{u}_j = \hat{S} + \delta$, with $\delta \in [0, \hat{T} - \hat{S})$. Therefore, the resulting exploitation response becomes $\Delta_{DC} = \overline{u}_j - \hat{T} = \hat{S} + \delta - \hat{T}$.

Proposition 1 (Dominance condition for exploitation responses). *Let δ denote the deviation of the exploited agent's epoch-average reward from $\hat{u}_{t,j}$ during unilateral defection. Then the exploitation response Δ_{DC} is guaranteed to dominate the* min*-aggregation against if $\delta < \hat{T} - \hat{R}$.*

Proof. We compare Δ_{DC} with the smallest possible responses. The smallest possible response from (D, D) occurs when the responder's mean equals the lower payoff bound $\hat{S}$: $\Delta_{DD}^{\min} = \hat{S} - \hat{P}$. Analogously, the smallest response from (C, C) occurs at $\Delta_{CC}^{\min} = \hat{S} - \hat{R}$. Thus, exploitation dominates if

$$\Delta_{DC} < \Delta_{DD}^{\min} \iff \hat{S} + \delta - \hat{T} < \hat{S} - \hat{P} \iff \delta < \hat{T} - \hat{P}, \tag{16}$$

$$\Delta_{DC} < \Delta_{CC}^{\min} \iff \hat{S} + \delta - \hat{T} < \hat{S} - \hat{R} \iff \delta < \hat{T} - \hat{R}. \tag{17}$$

$\square$

The derived condition bounds how far the exploited agent's mean reward may deviate from the steady exploitation value $\hat{S}$ while still guaranteeing that exploitation responses dominate the min-aggregation. Several observations follow directly: Since $\hat{T} > \hat{R} > \hat{P} > \hat{S}$, we have $\hat{T} - \hat{R} < \hat{T} - \hat{P}$, so the tighter constraint is $\delta < \hat{T} - \hat{R}$. This threshold corresponds exactly to the *temptation–cooperation gap* of the Prisoner's Dilemma. Thus, as long as the exploited agent's average reward does not improve beyond the cooperation level $\hat{R}$, exploitation responses remain the most negative responses available. In steady exploitation ($\delta \approx 0$), the condition is trivially satisfied and $\Delta_{DC} \approx \hat{S} - \hat{T}$, guaranteeing strong dominance in the min-aggregation. Even if the exploited agent's mean increases due to occasional cooperative outcomes earlier in the epoch, the dominance of exploitation responses persists until the deviation approaches the cooperation payoff scale. Consequently, the intended DRIVE mechanism is robust to moderate within-epoch fluctuations of the mean reward and only fails to dominate when the exploited agent's average reward rises close to cooperative levels. In practice, such large deviations are unlikely in sustained exploitation regimes, meaning the exploitation response typically remains the most negative response and therefore governs the min-aggregation.

A.3   Implications by the TD gating mechanism

In a PD, defecting against a cooperator yields the maximal one-step payoff $\hat{T}$. If the critic is bounded and roughly calibrated to on-policy returns, it will not systematically predict values exceeding this achievable maximum by more than a small estimation error. Thus, the realized reward is at least as good as expected, making the TD residual non-negative and activating the request gate.

Theorem 5 (Unilateral defection triggers the TD gate under bounded critics). *Consider a (repeated) Prisoner's Dilemma with modified payoffs $\hat{T} > \hat{R} > \hat{P} > \hat{S}$, i.e., $\hat{u}_{t,i} \leq \hat{T}$ for all joint actions at time t. Suppose that at time t the joint action is unilateral defection (D, C), so agent i receives $\hat{u}_{t,i} = \hat{T}$. Assume further that the critic $\hat{V}_i$ is bounded and not over-optimistic at the current history in the sense that there exists $\epsilon \geq 0$ with $\hat{V}_i(\tau_{t,i}) \leq \hat{T} - \epsilon$, and that the continuation value is bounded below by some $V_{\min}$, i.e., $\hat{V}_i(\tau) \geq V_{\min}$ for all histories τ. Then the TD residual is non-negative whenever $\epsilon \geq -\gamma V_{\min}$, and the TD gate activates.*

Proof. Under unilateral defection (D, C), agent i obtains the maximal one-step reward $\hat{u}_{t,i} = \hat{T}$. Using the TD residual according to Eq. (3) with the above assumptions on the critic being bounded and not over-optimistic, yields

$$TD_i(\hat{u}_{t,i}) \geq \hat{T} + \gamma V_{\min} - (\hat{T} - \epsilon) = \epsilon + \gamma V_{\min}.$$

Therefore, if $\epsilon \geq -\gamma V_{\min}$ (in particular if $V_{\min} \geq 0$ or ϵ is chosen to dominate the worst-case negative continuation term), then $TD_i(\hat{u}_{t,i}) \geq 0$ and the DRIVE request gate activates. $\square$

Under return normalization, rewards and value targets are centered and scaled within each epoch, keeping both $\hat{u}_{t,i}$ and $\hat{V}_i(\tau_{t,i})$ in a controlled numerical range. Actor–critic training further encourages $\hat{V}_i$ to track realized returns rather than extrapolate beyond attainable outcomes. Hence, boundedness and the absence of persistent over-optimism are natural regularity conditions.

Over-activation of the TD gate and its shaping effect. While the previous result addresses *under-activation* (failing to request when exploiting), the TD gate may also activate in situations where $TD_i(\hat{u}_{t,i}) \geq 0$ without exploitation. To illustrate the most extreme shaping effect, assume a two-agent scenario (i.e., no min aggregation), where the TD gates *always* open, i.e., both agents request whenever possible, which yields:

$$u_{t,i}^{\mathrm{DRIVE}} = \hat{u}_{t,i} - \Delta_{t,j,i} + \Delta_{t,i,j} = \hat{u}_{t,i} - (\overline{u}_i - \hat{u}_{t,j}) + (\overline{u}_j - \hat{u}_{t,i}) = \hat{u}_{t,j} + \overline{u}_j - \overline{u}_i. \tag{18}$$

Thus, in the worst case, the instantaneous rewards are *swapped* and additionally shifted by the difference of epoch averages. We now bound the shaped reward ranges under this failure mode.

In a PD with one-step payoffs $\hat{T} > \hat{R} > \hat{P} > \hat{S}$, any epoch average satisfies $\hat{S} \leq \overline{u}_i \leq \hat{T}$ for all agents i, since $\overline{u}_i$ is an average of realized one-step rewards in $\{\hat{S}, \hat{P}, \hat{R}, \hat{T}\}$ (or more generally in $[\hat{S}, \hat{T}]$). For additional simplification, we denote the payoff range as $\Gamma := \hat{T} - \hat{S}$. Let $(\hat{u}_{t,i}, \hat{u}_{t,j})$ be the instantaneous modified rewards under the current action profile. Using (18), we can analyze the worst-case DRIVE reward bounds in all cases assuming no gating:

- **Mutual cooperation** $(\hat{R}, \hat{R})$: $u_{t,i}^{\mathrm{DRIVE}} = \hat{R} + \overline{u}_j - \overline{u}_i \in \left]\hat{R} - \Gamma, \ \hat{R} + \Gamma\right[$. Particularly, if both agents have similar averages (typical in a cooperative regime, $\overline{u}_i \approx \overline{u}_j \approx \hat{R}$), then $u_{t,i}^{\mathrm{DRIVE}} \approx \hat{R}$.

- **Mutual defection** $(\hat{P}, \hat{P})$: $u_{t,i}^{\mathrm{DRIVE}} = \hat{P} + \overline{u}_j - \overline{u}_i \in \left]\hat{P} - \Gamma, \ \hat{P} + \Gamma\right[$. Again, if $\overline{u}_i \approx \overline{u}_j \approx \hat{P}$, then $u_{t,i}^{\mathrm{DRIVE}} \approx \hat{P}$.

- **Unilateral defection** $(\hat{T}, \hat{S})$ (i **defects**): Using $\overline{u}_i \in [\hat{T}, \hat{S}[$ and $\overline{u}_j \in]\hat{T}, \hat{S}]$ ungated shaping yields:

$$2\hat{S} - \hat{T} = \hat{S} - (\hat{T} - \hat{S}) \ \leq \ u_{t,i}^{\mathrm{DRIVE}} \ < \ \hat{S} + (\hat{T} - \hat{S}) = \hat{T}.$$

  Thus, even if both gates erroneously activate, the defector's shaped reward remains strictly below $\hat{T}$. In steady state ($\overline{u}_i \approx \hat{T}$, $\overline{u}_j \approx \hat{S}$), the mechanism intensifies the intended swap, $u_{t,i}^{\mathrm{DRIVE}} \approx 2\hat{S} - \hat{T} < \hat{S}$, thereby strengthening the penalty for exploitation. If $\overline{u}_i$ decreases because agent i cooperated earlier in the epoch, the penalty is softened but remains bounded above by $\hat{T}$. Hence, even without gating and under mean deviations, defection is never rewarded.

- **Being defected against** $(\hat{S}, \hat{T})$ (i **cooperates**): Using the bounds $\overline{u}_i \in [\hat{S}, \hat{T}[$ and $\overline{u}_j \in]\hat{S}, \hat{T}]$, we obtain

$$\hat{S} \ < \ u_{t,i}^{\mathrm{DRIVE}} \ \leq \ 2\hat{T} - \hat{S}.$$

  Thus, in the ungated scenario, the exploited cooperator's reward can exceed $\hat{T}$ (up to $2\hat{T} - \hat{S}$). In steady unilateral defection ($\overline{u}_i \approx \hat{S}$, $\overline{u}_j \approx \hat{T}$), this corresponds to the intensified swap $u_{t,i}^{\mathrm{DRIVE}} \approx 2\hat{T} - \hat{S} > \hat{T}$. Hence, over-activation may overcompensate the cooperator. This illustrates why TD gating (and, in the multi-agent case, min aggregation) is structurally important: it suppresses such inflation and restricts shaping to genuine exploitation signals.

This analysis isolates the *extreme* scenario in which the TD gate fails completely, and exchange always occurs in both directions. In practice, the TD gate and (in multi-agent settings) the min aggregation reduce the likelihood that large positive transfers dominate, because they suppress exchanges when the requester's gate is closed and preferentially select the most negative (i.e., most compensatory) response among neighbors.

Summary. Over-activation can occur due to critic noise, temporary miscalibration, or reward shifts. However, because DRIVE shapes rewards via *differences* relative to peer averages and aggregates via min, symmetric or near-symmetric outcomes produce negligible deltas. As a result, unintended gate openings have limited structural impact. Persistent large distortions would indicate critic instability rather than a flaw of the gating mechanism itself.

A.4 Detailed Proof of Theorem 1

Proof. Consider a two-agent PD with $\hat{T} > \hat{R} > \hat{P} > \hat{S}$. Under unilateral defection (D, C), agent i (defector) receives $\hat{u}_{t,i} = \hat{T}$ and agent j (cooperator) receives $\hat{u}_{t,j} = \hat{S}$.

1. **Gated interaction.** By Theorem 5, under bounded and rational critics, the TD gate activates for the exploiting agent i and does not activate for j. Hence, only i issues a request and we obtain

$$\Delta_{t,i,j} = \overline{u}_j - \hat{T}, \qquad \Delta_{t,j,i} = 0.$$

2. **Sign and bounds of the response.** By Lemma 1, $\overline{u}_j \in [\hat{S}, \hat{T}[$, hence the response is strictly negative.

3. **Resulting shaped rewards.** Using Eq. (5) (two-agent case),

$$u_{t,i}^{\text{DRIVE}} = \hat{T} + \Delta_{t,i,j} = \overline{u}_j, \qquad u_{t,j}^{\text{DRIVE}} = \hat{S} - \Delta_{t,i,j} = \hat{T} - (\overline{u}_j - \hat{S}).$$

   Thus, DRIVE does not deterministically map $(\hat{T}, \hat{S}) \mapsto (\hat{S}, \hat{T})$, but instead yields the transformed payoffs $(\overline{u}_j, \hat{T} - (\overline{u}_j - \hat{S}))$.

4. **Sufficient condition for incentive reversal.** For cooperation to be a best response against a cooperator, we require $u_{t,i}^{\text{DRIVE}} = \overline{u}_j < \hat{R}$. Under this condition, defecting yields strictly less payoff than mutual cooperation $(\hat{R}, \hat{R})$, eliminating the temptation to defect.

5. **Realization under typical dynamics.** Appendix A.2 shows that in sustained unilateral defection, $\overline{u}_j \approx \hat{S}$, so the condition $\overline{u}_j < \hat{R}$ holds strictly and $u_{t,i}^{\text{DRIVE}} \approx \hat{S}$, $u_{t,j}^{\text{DRIVE}} \approx \hat{T}$, recovering the payoff inversion.

6. **Symmetric outcomes.** For (C, C) and (D, D), Appendix A.2 shows that $\overline{u}_i \approx \overline{u}_j$, yielding $\Delta \approx 0$ and preserving $(\hat{R}, \hat{R})$ and $(\hat{P}, \hat{P})$.

Combining these results, DRIVE removes both greed $(\hat{R} > \overline{u}_j)$ and fear $(\hat{T} > \hat{P})$, making mutual cooperation the dominant strategy under DRIVE. $\qquad\square$

A.5 Analysis of Protocol Compliance Cases

To complement the discussion in Sec. 5, we present a worked example for a two-player Prisoner's Dilemma under DRIVE with different levels of protocol compliance. We consider generic PD payoffs $T > R > P > S$ as in Eq. (1); for concreteness, one may think of the canonical values $(T, R, P, S) = (5, 3, 1, 0)$, but none of the arguments below depend on these particular numbers. In each case, agent i defects while agent j cooperates, and DRIVE applies reward shaping based on request/response behavior.

Case	Defector payoff	Cooperator payoff
(1) Full compliance	S	T
(2) Defector does not send request	T (no penalty)	S
(3) Cooperator withholds response	T (no penalty)	S
(4) Misreported request / response	may collapse penalties	may lead to mis-penalization
(5) No compliance at all	T	S

Table 1: Illustration of payoffs under different protocol compliance scenarios in a 2-player PD.

(1) Full compliance If all agents truthfully follow the protocol, the results of Theorem 1 apply. Unilateral defection (T, S) is reshaped into (S, T): the defector receives S and the cooperator T, eliminating the incentive to defect.

(2) Defector does not send a request If the defector refrains from sending a request despite a positive TD, it avoids penalization from neighbors but also loses the chance of mutual improvement. Its payoff remains T, while the cooperator's payoff remains S. This strategy indirectly penalizes the non-requesting agent, which cannot gain from reciprocal shaping.

(3) Cooperator withholds a response If the cooperator fails to respond (intentionally or due to loss), the defector avoids the intended penalty. The payoffs revert to (T, S). Because of the min-aggregation across neighbors, the absence of a single response only matters if it is the unique or strongest penalty.

(4) Misreporting Misreporting can occur in two forms: (i) agents send requests despite having no improvement signal (TD< 0), or (ii) agents respond with incorrect values of Δ (due to error or intent). In the first case, the resulting differences are typically small or positive, which the min operator filters out, making the effect negligible. In the second case, however, false responses can distort the aggregation: A misreporting neighbor may reduce or nullify the penalty for a defector, or unjustly penalize a compliant requester. While this can destabilize cooperation in the worst case, it is not worse than the vulnerabilities faced by other PI methods. Overall, misreporting represents a robustness limitation but does not fundamentally break the mechanism as long as the majority of responses remain truthful.

(5) No compliance at all If no requests or responses are exchanged, all shaping terms vanish. DRIVE collapses to plain MARL with payoffs (T, S) under unilateral defection, and cooperation incentives are lost.

Extension to larger scenarios The two-player example above presents the limiting case in which a single non-compliant agent corresponds to 50% protocol adherence, thereby strongly magnifying the impact of individual deviations. In larger populations, however, the effect of partial non-compliance is more gradual. As long as a sufficient fraction of agents continue to respond truthfully, the min-aggregation still enforces penalization of defectors.

Three-player example Consider a group of three agents, where one agent defects (i) and two agents cooperate (j and k). Each cooperator truthfully responds with $\Delta_{i,j}, \Delta_{i,k} < 0$. The defector's shaped reward is $u_i^{\mathrm{DRIVE}} = T + \min\{\Delta_{i,j}, \Delta_{i,k}\}$, so as long as at least one cooperator responds truthfully, u_i^{DRIVE} is penalized. If one cooperator withholds, the other still enforces the penalty, though it may be weaker. Thus, unlike in the 2-player case, cooperation incentives do not collapse entirely when a single agent is non-compliant.

A.6 Extension to a Simple N-Agent PD Setting

The main theorem focuses on the 2-agent Prisoner's Dilemma (PD). Here we first provide a clean extension to an N-agent *graphical* PD under full protocol compliance, where payoffs decompose into symmetric 2-player PD interactions, and then progressively relax structural and behavioral assumptions.

Definition 2 (Graphical PD). Let $G = (V, E)$ be an undirected graph with $|V| = N$ agents. Each agent $i \in V$ chooses an action $a_i \in \{C, D\}$. For every edge $(i, j) \in E$ we associate a 2-player PD with payoffs (R, R), (P, P), (T, S), (S, T) as in Eq. (1). The stage payoff of agent i is $u_i(a) = \sum_{j \in N(i)} u_{i,j}(a_i, a_j)$, where $N(i)$ is the neighborhood of i in G and $u_{i,j}$ is the PD payoff against neighbor j.

To isolate the effect of incentive alignment, we assume that each pairwise interaction is shaped independently using the 2-agent DRIVE protocol and that all agents comply fully with the request and response rules. That is, in every interaction with neighbor j, agent i behaves exactly as in the 2-agent analysis of Appendix A.1.

Proposition 2 (Pairwise incentive alignment). *Consider a graphical PD as above and assume that each edge (i, j) uses the 2-agent DRIVE protocol with shaping rule* (6) *applied independently to $u_{i,j}(a_i, a_j)$. Then, for every agent i and every joint action profile a_{-i} of its neighbors,*

$$u_i^{\mathrm{DRIVE}}(C, a_{-i}) > u_i^{\mathrm{DRIVE}}(D, a_{-i}),$$

so cooperation is a dominant action for every agent and the unique Nash equilibrium of the shaped game is the all-cooperate profile $(C, \ldots, C)$.

Proof. By Theorem 1 and its detailed proof in Appendix A.1, for each neighbor j the pairwise DRIVE-shaped payoff function $u_{i,j}^{\mathrm{DRIVE}}$ makes C strictly dominate D in the corresponding 2-player PD. That is, for any fixed $a_j \in \{C, D\}$, $u_{i,j}^{\mathrm{DRIVE}}(C, a_j) > u_{i,j}^{\mathrm{DRIVE}}(D, a_j)$. Summing these strict inequalities over all neighbors

$j \in N(i)$ for any joint neighbor action profile a_{-i} yields

$$u_i^{\text{DRIVE}}(C, a_{-i}) = \sum_{j \in N(i)} u_{i,j}^{\text{DRIVE}}(C, a_j) > \sum_{j \in N(i)} u_{i,j}^{\text{DRIVE}}(D, a_j) = u_i^{\text{DRIVE}}(D, a_{-i}).$$

Hence C is a strict best response to any a_{-i} for all agents i, so $(C, \ldots, C)$ is the unique Nash equilibrium. $\qquad \square$

This proposition formalizes how the 2-player incentive alignment result extends to a simple class of N-agent games with additive pairwise PD interactions. Our SSD experiments instantiate more complex interaction patterns, but the graphical PD result provides a clean theoretical illustration of how DRIVE scales beyond two agents.

Pairwise PD interactions across neighborhoods In many multi-agent systems, agents repeatedly engage in pairwise social dilemmas with dynamically changing or randomly matched partners (an *interaction graph*), while incentive exchanges are restricted to a possibly different and fixed *communication graph* defined by neighborhoods $N_{t,i}$. In such settings, the DRIVE-shaped reward of a defector i still takes the form $u_i^{\text{DRIVE}} = T + \min_{j \in N_{t,i}} \Delta_{i,j}$. Whenever the exploited cooperator in a given PD round is also a neighbor of i, the exact $T \leftrightarrow S$ payoff swap from the 2-agent case is recovered. When interaction partners lie outside $N_{t,i}$, the penalty is instead delivered by whichever compliant neighbors suffer a sustained long-run disadvantage from i's behavior (e.g., through shared resources or future interactions). Thus, the interaction graph determines *which behaviors create negative externalities*, while the communication graph determines *who can hold whom accountable.* As long as each defector has at least one compliant neighbor whose long-run return is reduced when it defects, the sign of the incentive remains cooperative, even if the magnitude differs from the fully local 2-agent PD.

Beyond graphical PDs Many benchmark social dilemma environments, such as Coin Game or Harvest, do not admit an explicit decomposition into pairwise PD payoffs. Instead, incentives arise indirectly through shared resources, delayed consequences, and aggregate system dynamics. Nevertheless, the same principle applies: agents whose behavior systematically reduces their neighbors' long-run returns generate negative differences $\Delta_{i,j}$ and are penalized by DRIVE. This perspective explains why DRIVE empirically promotes cooperation in such environments, even in the absence of an explicit PD structure.

General N-agent compliance and robustness The preceding results assume full compliance with the protocol. We now consider a general N-agent setting in which only M agents truthfully follow the DRIVE protocol, while $K = N - M$ agents may behave adversarially by withholding requests or responses or by misreporting. For any game-theoretic defector i, effective penalization requires two conditions: (i) i itself must comply with the request gate (sending a request when TD ≥ 0), and (ii) at least one neighbor $j \in N_i$ must respond truthfully. Under these conditions, the shaped reward of i is

$$u_i^{\text{DRIVE}} = T + \min\{\Delta_{i,j}\}_{j \in N_i, \, j \text{ compliant}}.$$

As long as a compliant responder exists, defection is penalized; the severity depends on the most negative difference among the responders, but the penalty does not collapse entirely. In fully connected populations, this reduces to the simple requirement that at least two agents comply (the requester and one responder), i.e. $M/N \geq 2/N$. In general communication topologies, the compliant set must form a *dominating set*, ensuring that each requester has at least one compliant neighbor. Thus, DRIVE exhibits a *graceful degradation*: as compliance M/N decreases, cooperation incentives weaken smoothly but only collapse completely if no responder is available.

Connectivity requirements In fully connected graphs, penalization is ensured as soon as at least two agents comply (the requester and one responder), corresponding to a compliance rate $c \geq 2/N$. In general communication topologies, the compliant agents must form a *dominating set*: every requester must have at least one compliant neighbor. Formally, for graph $G = (V, E)$ with compliant set $C \subseteq V$, penalization holds iff $\forall i \in V : N(i) \cap C \neq \varnothing$. The minimal compliant set size is the domination number $\gamma(G)$, yielding a topology-aware threshold $|C| \geq \gamma(G)$.

Adversarial robustness   The above threshold can be interpreted directly in terms of K adversarial agents. If K agents are adversarial (never providing truthful responses), DRIVE continues to penalize every *protocol-compliant* defector as long as the remaining $M = N - K$ compliant agents contain a dominating set. Equivalently, the system tolerates up to $K \leq N - \gamma(G)$ adversarial agents. However, agents that are adversarial both in their *actions* (always defecting) and their *protocol behavior* (never sending requests) cannot be punished by any PI scheme based on self-reported signals, including DRIVE. To compliant neighbors, these agents appear as players whose defections generate no negative differences; this reduces local cooperative pressure and gradually pushes the system toward the underlying non-PI MARL dynamics (Case 5), but does not cause an abrupt collapse.

Overall, these results highlight DRIVE's property of *graceful degradation*: full compliance yields strong incentive-alignment guarantees, while partial compliance weakens but does not immediately destroy cooperative incentives, provided the communication topology satisfies minimal coverage conditions. In two-agent systems, a single non-compliant agent already reduces compliance to 50%, eliminating penalization. In larger populations ($N > 2$), even if several agents defect from the protocol, the remaining majority can still enforce penalization through the min-aggregation. Hence, DRIVE remains effective as long as the compliance rate stays above the topology-specific threshold, often close to a simple majority in practice. Nevertheless, systematic misreporting or universal non-compliance collapses DRIVE to baseline MARL, emphasizing the importance of designing variants that are robust to missing or adversarial responses in future work.

A.7   Affine Reward Transformations: Scope and Edge Cases

Here, we expand on the affine reward-change model used in our analysis. In each epoch m, the environmental reward is transformed by a shared positive affine map $r' = c_m r + b_m$, applied uniformly to all agents and timesteps. The schedules c_m and b_m may vary arbitrarily across epochs, covering all reward dynamics used in Sec. 8 (linear, exponential, stepwise, and damped–cosine). For illustration, in the damped–cosine setting, we use $c_m = (1 - m/E) \cos^2(2\eta m)$ and $b_m = \eta$, so the effective reward scale oscillates while decaying over time.

Isolated epochs may satisfy $c_m \approx 0$, yielding $r' \approx b_m$ and temporarily collapsing the Prisoner's Dilemma inequalities (T, R, P, S become indistinguishable). The stage game becomes nearly payoff-indifferent in these epochs.

Transformations not covered   This affine class excludes genuinely non-linear reward changes such as clipping, saturation, sign-dependent remapping, or state-dependent transformations that cannot be written as a shared affine map. These represent a broader family of sim-to-real shifts, which we leave for future work.

A.8   Reward Changes and Invariance in the PD

We first formalize how affine reward transformations affect the PD inequalities.

Lemma 2 (Affine transformations preserve PD structure). *Let $T > R > P > S$ and define $T' = cT + b$, $R' = cR + b$, $P' = cP + b$, $S' = cS + b$ for some $c > 0$, $b \in \mathbb{R}$. Then $T' > R' > P' > S'$.*

Proof. Since $c > 0$, we have $T' - R' = c(T - R) > 0$, $R' - P' = c(R - P) > 0$, and $P' - S' = c(P - S) > 0$, so $T' > R' > P' > S'$. The additive constant b cancels in all pairwise differences. □

We can now restate Theorems 2 and 3 more formally.

Proof of Theorem 2. In MATE, mutual cooperation is individually rational iff the global token $x > 0$ satisfies $x \geq \max\{P - S, (T - R)/3\}$ (Phan et al., 2024). Under the affine transformation of Definition 1, these thresholds become $P' - S'$ and $(T' - R')/3$, i.e.,

$$x \geq \max\{P' - S', (T' - R')/3\}.$$

If we fix any x satisfying this condition, because c_m and b_m are arbitrary (subject to $c_m > 0$), we can always choose (c_m, b_m) such that $P' - S' > x$, e.g., by taking c_m large enough. Then the transformed threshold exceeds x, and the MATE payoff matrix no longer guarantees cooperation as a best response. Hence, MATE is not invariant to such reward changes. □

Proof of Theorem 3. Let (R, P, T, S) and (R', P', T', S') be two sets of PD payoffs related by any f_{mod} of Definition 1. By Lemma 2, $T > R > P > S$ implies $T' > R' > P' > S'$. The detailed analysis in Appendix A.1 shows that, under full compliance, DRIVE leaves the mutual-cooperation and mutual-defection payoffs unchanged and swaps the temptation and sucker payoffs under unilateral defection. Applying the same calculation to (R', P', T', S') shows that the transformed payoffs obey the same pattern. In both cases, the resulting game has (C, C) as its unique Nash equilibrium, so the dominance of cooperation is preserved. □

A.9 Training with Normalized Returns

In our paper, $\hat{\pi}_i$ and $\hat{V}_i$ are trained with *normalized returns* $\overline{G}_{t,i} = \frac{1}{\sigma_i}(G_{t,i} - \mu_i)$, where μ_i and σ_i are the mean and standard deviation of all returns $G_{t,i}$ of agent i in an epoch m, to improve training stability (van Hasselt et al., 2016). The normalization makes standard policy gradient RL (without PI mechanism) invariant to reward changes, where rewards are scaled by a factor $c_m > 0$ or shifted by a scalar $b_m \in \mathbb{R}$:

Lemma 3. *Standard policy gradient RL according to Eq. 2, is invariant to reward changes, where the original environmental reward is scaled by a factor $c_m > 0$ or shifted by a scalar $b_m \in \mathbb{R}$, when the obtained discounted returns $G_{t,i} = \sum_{k=0}^{\infty} \gamma^k u_{t+k,i}$ in an epoch m are normalized to zero mean and standard deviation such that $\overline{G}_{t,i} = \frac{1}{\sigma_i}(G_{t,i} - \mu_i)$.*

Proof. Let the transformed reward be $u'_{t,i} = c_m u_{t,i} + b_m$, with $c_m > 0$. Then the corresponding continuing discounted return is

$$G'_{t,i} = \sum_{k=0}^{\infty} \gamma^k (c_m u_{t+k,i} + b_m) = c_m \sum_{k=0}^{\infty} \gamma^k u_{t+k,i} + b_m \sum_{k=0}^{\infty} \gamma^k = c_m G_{t,i} + \frac{b_m}{1 - \gamma}. \tag{19}$$

Hence, every return in the epoch is transformed by the same positive affine map $G'_{t,i} = c_m G_{t,i} + B_m$, with $B_m := b_m/(1 - \gamma)$, independent of t. Therefore, the corresponding mean and standard deviation satisfy $\mu'_i = c_m \mu_i + B_m$ and $\sigma'_i = c_m \sigma_i$, and the normalized return becomes

$$\overline{G}'_{t,i} = \frac{G'_{t,i} - \mu'_i}{\sigma'_i} = \frac{c_m G_{t,i} + B_m - (c_m \mu_i + B_m)}{c_m \sigma_i} = \frac{G_{t,i} - \mu_i}{\sigma_i} = \overline{G}_{t,i}. \tag{20}$$

Thus, positive scaling and additive shifting of the reward do not affect the normalized return $\overline{G}_{t,i}$ and substituting $\overline{G}'_{t,i}$ into the policy gradient estimator Eq. (2) yields the same policy gradient.

□

According to Lemma 3, the non-PI baselines *Naive Learning*, *LOLA-PG*, and *POLA-DiCE* are not affected by the dynamic reward changes in Sec. 8 and Fig. 7 (but are still less cooperative than *DRIVE*). However, most state-of-the-art PI methods like *LIO* and *MATE* cannot accommodate such changes (by the generally unknown function f_{mod}) in their payoff modifications (Figs. 2e, 2c) and thus fail to adapt, in contrast to *DRIVE*, as shown in Figs. 1c and 4.

A.10 Invariance in SSDs Under Normalized Policy Gradients

We can restate and prove Theorem 4 in more detail using the normalized return defined in Lemma 3

$$\overline{G}_{t,i} = \frac{G_{t,i} - \mu_i}{\sigma_i},$$

where μ_i and σ_i are the mean and standard deviation of all returns $G_{t,i}$ for agent i in epoch m.

Proof of Theorem 4. Let the environmental rewards in epoch m be transformed by $f_{mod}(r_{t,i}, m) = c_m r_{t,i} + b_m$ with $c_m > 0$. For any agent i, the DRIVE shaping rule in Eq. (6) depends only on $\hat{u}_{t,i}$ and differences of the form $\Delta_{t,i,j} = \bar{u}_j - \hat{u}_{t,i}$. Under f_{mod} these become

$$\Delta'_{t,i,j} = \bar{u}'_j - \hat{u}'_{t,i} = (c_m \bar{u}_j + b_m) - (c_m \hat{u}_{t,i} + b_m) = c_m (\bar{u}_j - \hat{u}_{t,i}) = c_m \Delta_{t,i,j}.$$

The minima in Eq. (6) therefore scale by the same factor c_m, and the shaped reward transforms as

$$u_{t,i}^{\mathrm{DRIVE}\,\prime} = c_m u_{t,i}^{\mathrm{DRIVE}} + b_m,$$

i.e., $u_{t,i}^{\mathrm{DRIVE}}$ is itself subjected to the same per-epoch positive affine map. Applying Lemma 3 to $u_{t,i}^{\mathrm{DRIVE}}$ instead of $u_{t,i}$ shows that the normalized returns (and thus the policy updates) are unchanged. Hence, both the baseline policy-gradient dynamics and the incentive effects induced by DRIVE are invariant to per-epoch positive affine transformations, as claimed. □

B Technical Details and Hyperparameters

B.1 Hyperparameters

All common hyperparameters used by all MARL approaches in the experiments, as reported in Sec. 6 in the paper, are listed in Table 2. The final values were chosen based on a coarse grid search which finds a tradeoff between performance and computation w.r.t. *DRIVE*, *LIO*, *IA*, and *MATE* in *IPD* and *Coin-2* without dynamically changing rewards, i.e., $f_{mod}(u, m) = u$. We directly adopted the final values in Table 2 for all other domains. All training and test runs were performed in parallel on a computing cluster of 15 x86_64 GNU/Linux (Ubuntu 18.04.5 LTS) machines with i7-8700 @ 3.2GHz CPU (8 cores) and 64 GB RAM. We did not use any GPU in our experiments.

Table 2: Common hyperparameters and their respective final values used by all algorithms evaluated in the paper. We also list the numbers that have been tried during the development of the paper.

Parameter	Final Value	Values/Range	Description
K	10	{1, 5, 10, 20}	Number of episodes per epoch.
E	4000	{2000, 4000, 8000}	Number of epochs. E was gradually increased to assess the stability of the learning progress until convergence.
α	0.001	{0.001}	Learning rate. We used the default ADAM implementation in `torch` without further tuning.
Clip norm	1	{1,∞}	Gradient clipping parameter. Using a clip norm of 1 leads to better performance than deactivating it with ∞.
λ	1	{0, 1}	Trace parameter for TD(λ) critic learning.
γ	0.95 (*IPD*, *Coin*) 0.99 (*Harvest*)	{0.9, 0.95, 0.99}	Discount factor for the return $G_{t,i}$. Any value ≥ 0.95 would be sufficient.
$|\tau_{t,i}|$	1	{1, 5, 10}	Local history length. It was set to 1 to reduce computation because the other values did not significantly improve performance.

For *LIO*, we set the cost weight for incentive function learning to 0.001 and the maximum incentive value R_{max} to the highest absolute penalty per domain (3 in *IPD*, 2 in *Coin-2* and *Coin-4*, and 0.25 in *Harvest-12*), as suggested in (Yang et al., 2020). For *IA*, we set $\alpha = 5$ and $\beta = 0.05$, as suggested in (Hughes et al., 2018).

B.2 Neural Network Architectures

We coarsely tuned the neural network architectures in the paper w.r.t. performance and computation by varying the number of units per hidden layer {32, 64, 128} for $\hat{\pi}_i$ and $\hat{V}_i$. The number of hidden layers was varied between 1, 2, and 3, but significantly deeper architectures led to deteriorating performance (possibly due to vanishing gradients). Using ELU or ReLU activation did not make any significant difference for any neural network. Thus, we stick to ELU throughout the experiments. *DRIVE*, *MATE*, and *Naive Learning* only use $\hat{\pi}_i$ and $\hat{V}_i$ as neural networks. The incentive function network of *LIO* has the same hidden layer architecture as $\hat{\pi}_i$ and $\hat{V}_i$. In addition, the joint action of the $n-1$ other agents is concatenated to the flattened observations before being input into the incentive function, which outputs an $n-1$ dimensional vector. The output vector is passed through a sigmoid function and multiplied with R_{max} (Sec. B.1) afterward.

B.3 Coin-2 and Coin-4

We adopted the setup of (Foerster et al., 2018) in *Coin-2*, as shown in Fig. 5a, with the same rules and reward functions. The order of executed actions is randomized such that situations where two agents simultaneously step on a blue coin lead to an expected payoff of +1 for the red agent and -1 for the blue agent (Fig. 5a left), and vice versa for a red coin. In addition, we extended the domain to 4 agents in *Coin-4* (Fig. 5a right). All agents are able to move freely, and grid cell positions can be occupied by multiple agents. Any attempt to move out of bounds is treated as *do nothing* action.

	C	D
C	0.5, 0.5	-0.5, 1.5
D	1.5, -0.5	0, 0

(a) Coin Domain   (b) Payoff Table for *Coin-2* (per time step)

Figure 5: (a) *Coin-2* and *Coin-4*. (b) Payoff table for *Coin-2* w.r.t. the expected rewards per time step.

Prisoner's Dilemma Connection   Assuming that an agent always picks up a coin at every time step in *Coin-2*, the expected rewards per time step represent a PD instance, according to Sec. 2 and Fig. 1:

- If both agents cooperate, i.e., only collect their matching coins, each agent gets $R = 0.5(1 + 0) = 0.5$ on average.

- If both agents defect, i.e., collect any coin regardless of their color, each agent gets $P = 0.25(1+1-2+0) = 0$ on average.

- If one agent defects, the defecting agent gets $T = 0.5(1 + 0) + 1 = 1.5$ on average (its own coin 100% of the time and the other's coin 50% of the time). The exploited agent gets $S = 0.5(1 - 2) = -0.5$

The expected payoffs R, P, T, and S satisfy the characteristic PD inequalities w.r.t. greed and fear, namely $T > R > P > S$. Thus, DRIVE also works well in *Coin-2* and *Coin-4* (which extends the SD to 4 agents), even with changing rewards, as shown in Fig. 4.

B.4 Harvest-12

We adopted the setup of (Perolat et al., 2017a) in *Harvest-12*, as shown in Fig. 6a, with the same dynamics and apple regrowth rates. *Harvest-12* always starts with the initial apple configuration in Fig. 6a with randomly positioned agents. The agents can observe the environment within their 7×7 area and have no specific orientation. Thus, they have 4 separate actions to tag all neighbor agents, namely north, south, west, and east. All agents are able to move freely, and grid cell positions can be occupied by multiple agents. Any attempt to move out of bounds is treated as *do nothing* action.

	C	D
C	0.3, 0.3	-0.01, 0.9
D	0.9, -0.01	0.06, 0.06

(a) Harvest Domain   (b) Payoff Table for *Harvest-2* (per time step)

Figure 6: (a) Domain layout with the initial apple configuration used for *Harvest-12*. (b) Payoff table for *Harvest-2* w.r.t. the expected rewards per time step.

Prisoner's Dilemma Connection   We empirically tested a 2-agent instance of Harvest to determine the payoff table, similar to (Leibo et al., 2017). The table is shown in Fig. 6b and represents a PD instance, according to Sec. 2 and Fig. 1:

- If both agents cooperate, i.e., no stunning and occasional waiting for apple regrowth, each agent gets $R \approx 0.3$ on average.

- If both agents defect, i.e., stunning and complete harvesting that prevents apple regrowth, each agent gets $P \approx 0.06$ on average.

- If one agent defects, i.e., stunning and harvesting, the defecting agent gets $T \approx 0.9$, and the exploited agent gets $S \approx -0.01$ on average (due to being stunned most of the time with a 0.01 time penalty).

The expected payoffs R, P, T, and S satisfy the characteristic PD inequalities w.r.t. greed and fear, namely $T > R > P > S$. Thus, DRIVE also works well in *Harvest-12* (which extends the SD to 12 agents), even with changing rewards, as shown in Fig. 4 and Fig . 8. This also confirms the empirical result of (Leibo et al., 2017), stating that Harvest can represent a PD instance w.r.t. greed and fear, depending on the availability and regrowth rate of apples.

C   Additional Results

We provide additional results regarding different cooperation measures for *Harvest-12*, namely *Social Welfare or Efficiency (U)* (according to Sec. 2), *Equality (E)* (1 minus the Gini coefficient), *Sustainability (S)* (the average number of time steps at which apples are collected), and *Peace (P)* (the average number of untagged agents at any time step). All measures are based on the *original environmental rewards* $u_{t,i}$ instead of $\hat{u}_{t,i} = f_{mod}(u_{t,i}, m)$ (Algorithm 1, Line 15) to assess the stability of cooperation reliably. They are defined by (Perolat et al., 2017b):

$$E = 1 - \frac{\sum_{i \in \mathcal{D}} \sum_{j \in \mathcal{D}} |\sum_{t=0}^{H-1} (u_{t,i} - u_{t,j})|}{2n \sum_{i \in \mathcal{D}} \sum_{t=0}^{H-1} u_{t,i}}, \tag{21}$$

$$S = \frac{1}{n} \sum_{i \in \mathcal{D}} \chi_i, \text{ where } \chi_i = \mathbb{E}[t | u_{t,i} > 0], \tag{22}$$

$$P = n - \frac{1}{H} \sum_{i \in \mathcal{D}} \sum_{t=1}^{H} \mathbf{1}[\text{agent timed-out on time step } t] \tag{23}$$

Fig. 8 shows the progress of the alternative cooperation measures in *Harvest-12* with the different reward change functions f_{mod} I, II, III, and IV (Fig. 7) from Sec. 8. While DRIVE is robust across all measures, MATE and LIO change significantly in most settings, except for equality in the reward change functions f_{mod}^{I} and f_{mod}^{III}. IA is only affected by f_{mod}^{IV} regarding all cooperation measures. Apart from f_{mod}^{III}, MATE always exhibits more peace than DRIVE, although the peace level significantly varies depending on the reward change function. LIO only exhibits more peace than DRIVE under f_{mod}^{II} and f_{mod}^{IV}, which both converge to zero over time.

Figure 7: The reward change functions f_{mod} used in each epoch m according to Line 15 in Algorithm 1.

Figure 8: Average progress of DRIVE and other baselines in *Harvest-12* with different reward change functions f_{mod} (I, II, III, and IV), as illustrated in the legend at the top and Fig. 7 regarding the cooperation measures *Social Welfare or Efficiency (U)*, *Equality (E)*, *Sustainability (S)*, and *Peace (P)* (Perolat et al., 2017b). Shaded areas show the 95% confidence interval.