MIDSTEER: Optimal Affine Framework for Steering Generative Models

Abstract

Steering intermediate representations has emerged as a powerful strategy for controlling generative models, particularly in post-deployment alignment and safety settings. However, despite its empirical success, it currently lacks a comprehensive theoretical framework. In this paper, we bridge this gap by formalizing the theory of concept steering. First, we establish a link between steering and affine concept erasure, proving that the standard approach for removing unwanted behaviors is a special case of LEACE (a closed-form method for affine erasure). Next, we formulate a principled theoretical framework for concept switching, LEACE-Switch, and characterize the assumptions under which it provides an optimal affine solution. Building on this analysis, we then introduce MidSteer (**Mi**nimal **D**isturbance concept **Steer**ing), a more general affine framework for concept manipulation that relaxes these assumptions and enables directed, minimal-disturbance transformations. We demonstrate that MidSteer performs favorably across a range of tasks, modalities, and architectures, including vision diffusion models and large language models.

1. Introduction

Generative models such as Large Language Models (LLMs) and vision diffusion models have achieved remarkable progress in recent years (Yang et al., 2024b) (Naveed et al., 2023). However, controlling model outputs to enforce desirable behaviors or suppress harmful ones remains challenging (Bartoszcze et al., 2025). Yet, this capability is necessary for improving model safety, reliability, alignment, and usefulness in downstream applications.

Concept steering of intermediate representations is an increasingly popular technique that has already proven to be simple yet powerful for controlling behavior in LLMs. Recently it was also shown to be applicable to vision diffusion models (Gaintseva et al., 2025). The underlying idea is to change the intermediate representations of a generative model during generation by adding or subtracting a "steering vector" that encodes a target concept. This approach has proven effective for tasks such as erasing unwanted behaviors (toxicity, nudity) or amplifying desirable features (helpfulness, truthfulness). However, despite the simplicity of the approach, its theoretical foundations remain underdeveloped with most of the work around it being highly empirical. Existing methods largely rely on heuristic vector manipulations, which can introduce unintended side effects and lack a solid theoretical basis and guarantees. Moreover, naive steering often perturbs unrelated features, undermining the minimal disturbance principle that is critical to maintaining model quality and coherence.

Recently, strong theoretical foundations have been developed for concept erasure. (Ravfogel et al., 2023) introduced the notion of log-linear guardedness. Based on it, (Belrose et al., 2025) developed LEACE, an affine concept erasure framework to remove undesired information from model representations for downstream tasks. However, these methods do not naturally extend to other forms of concept manipulation, such as switching, where the goal is to replace one concept with another rather than just erasing it.

In this work, we address these gaps by developing a unified theoretical framework for affine steering of generative models. We begin by proving a formal equivalence between the standard steering methodology and LEACE, demonstrating that the widely used heuristic of steering for concept erasure is a special case of optimal affine concept erasure. Building on this foundation, we extend the framework from erasure to concept switching. We first consider the setting of bidirectional switching, in which a binary concept partitions the dataset and the goal is to invert the linear dependence of the representation on the concept label. Under these assumptions, we derive LEACE-Switch, an optimal affine transformation that performs a complete and symmetric concept swap while minimally disturbing the representation.

We examine the scope of this formulation and show that its assumptions, dataset partitioning and global label inversion define a practically relevant, though restricted, regime.

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We address more general settings in which the concepts involved do not jointly span the entire dataset, or where asymmetric, one-directional transformations are desired. We introduce MidSteer (Minimal Disturbance Concept Steering), a generalized framework for affine concept manipulation that enables precise switching while minimizing interference with unrelated properties of the representation.

Through experiments with LLMs and vision diffusion models, we demonstrate that LEACE-Switch and MidSteer achieve more reliable concept switching than vanilla steering, allowing controllable generation with minimal side effects. Our results highlight the value of grounding steering methods in theory and provide practical tools for aligning generative models with desired behaviors.

In summary, our **contributions** are as follows:

- We establish a **formal theoretical connection** between standard activation steering and affine concept erasure, showing that commonly used steering heuristics for concept erasure are special cases of LEACE.

- We **extend the affine erasure framework to concept switching** and introduce **LEACE-Switch**, an optimal affine formulation for concept swapping under the assumption that a binary concept partitions the dataset.

- We then relax the dataset partitioning and symmetry requirements for the task of concept switching, and introduce **MidSteer** (Minimal Disturbance Concept Steering), a **generalized affine framework for concept manipulation** that enables precise and directed concept switching with provably minimal interference to unrelated representation components.

- We **empirically validate** LEACE-Switch and MidSteer across modalities and architectures, including LLMs and vision diffusion models, demonstrating improved controllability and reduced side effects compared to existing steering and erasure methods.

2. Related Work

Activation steering and representation manipulation. Activation steering has emerged as a lightweight approach for controlling generative models by modifying intermediate representations, particularly in LLMs (Turner et al., 2023) (Bartoszcze et al., 2025) (Rimsky et al., 2024) and more recently in diffusion models (Tumanyan et al., 2023) (Kwon et al., 2023) (Gaintseva et al., 2025). Most existing methods rely on heuristic vector addition or subtraction, often derived from mean activation differences, and provide limited guarantees on optimality or side effects. Our work formalizes steering as an affine transformation problem and studies when such interventions are provably minimal and well-posed.

Affine concept erasure and guardedness A related line of work focuses on removing concept information from representations. INLP (Ravfogel et al., 2020) and RLACE (Ravfogel et al., 2023) iteratively project out linear subspaces predictive of a protected attribute. LEACE (Belrose et al., 2025) provides a closed-form affine solution for optimal linear concept erasure under the guardedness framework, minimizing representational disturbance while enforcing zero covariance with the concept label. Our work builds directly on this theory, showing that standard erasure-mode steering is a special case of LEACE, and extending the framework beyond erasure. Next, SPLINCE (Holstege et al., 2025) study oblique projections that erase protected attributes while preserving task-relevant subspaces. While these methods address constrained erasure, they do not consider concept switching, which requires translating concept dependence rather than erasing it. Nevertheless, they motivate the importance of minimal-disturbance objectives with structural constraints, which our work addresses in the switching setting.

Distributional alignment and representation surgery. Representation Surgery (Singh et al., 2024) derives affine transformations that match class-conditional means, and optionally covariances, between source and target distributions. This approach performs distributional alignment under Gaussian assumptions and is well-suited to tasks where class-conditional statistics fully characterize the desired transformation. In contrast, MidSteer operates on cross-covariances between representations and concept indicators, preserving the global linear structure of the representation space and explicitly minimizing changes outside the concept-mediating subspace. As a result, MidSteer targets concept switching rather than full distribution matching, and the two approaches optimize distinct objectives.

In summary, while prior methods address erasure or distributional alignment, our work is the first to formalize concept switching as a distinct affine problem and to derive closed-form solutions with explicit minimal-disturbance guarantees across modalities.

3. Preliminaries

3.1. Steering internal representations of models

We formalize **activation steering** as the manipulation of internal model representations to control the presence of a specific concept c in the model's output. This is achieved by adding a scaled steering vector s_c to the intermediate hidden activity h during inference. The **steering vector** s_c is constructed from the concept-conditional means of the hidden activity. Let h be a random vector in $\mathbb{R}^d$ representing the activity at a particular layer, and let $C \in \{0, 1\}$ represent the presence or absence of concept c. The steering vector

$s_c \in \mathbb{R}^d$ is defined as the difference of these means:

$$s_c = \mathbb{E}[h|C = 1] - \mathbb{E}[h|C = 0], \tag{1}$$

s_c can be optionally post-processed (to have unit norm).

The general steering intervention f controls the concept's expressiveness via a scalar $\alpha \in \mathbb{R}$ representing the steering strength and direction. Omitting the subscript c, the operation is:

$$f(h, s) = h + \alpha s \tag{2}$$

We highlight two essential special cases, determined by the choice of the intervention function f.

Concept Erasure. It aims to erase all information aligned with the concept c from the activation vector h. This is achieved by projecting h onto the subspace orthogonal to the steering direction s. The projection $\langle h, s \rangle s$ estimates the conceptual component, which is then removed:

$$f_{\text{delete}}(h, s) = h - \langle h, s \rangle s \tag{3}$$

Concept switch. Multiplying projection by 2 results in a **Householder reflection** of the vector h across the hyperplane orthogonal to s:

$$f_{\text{switch}}(h, s) = h - 2\langle h, s \rangle s \tag{4}$$

This transformation effectively substitutes the component of h aligned with c with its opposite, thereby substituting the representation of concept c with the representation of its absence.

If steering is applied to specific layers (e.g., self-attention outputs in LLMs or cross-attention layers in vision models), both Equation 3 and Equation 4 can be incorporated directly into the model's weight matrices. This allows for achieving **zero inference overhead**, a critical advantage for deployment in large-scale applications.

3.2. Affine guardedness framework

For the task of concept erasure from model representations, (Ravfogel et al., 2023) introduced the notion of log-linear guardedness. (Belrose et al., 2025) generalized it to:

Definition 3.1 (Guardedness). Consider a k-class classification task over jointly defined random vectors X (the input data) and Z (the one-hot labels), with X of finite first moment and taking values in $\mathbb{R}^d$, and Z taking values in $\mathcal{Z} = \{\mathbf{z} \in \{0,1\}^k \mid \|\mathbf{z}\|_1 = 1\}$ with each[1] $\mathbb{P}(Z = j) > 0$. Let $\eta(\cdot;) : \mathbb{R}^d \to \mathbb{R}^k$ be a predictor chosen from a function class $\mathcal{V} = \{\eta(\cdot;) \mid \in \Theta\}$ (presumed to contain all constant functions) so as to minimize the expectation $\big[\mathcal{L}(\eta(X), Z)\big]$ of some $\mathcal{L} : \mathbb{R}^k \times \mathcal{Z} \to [0, \infty)$ in a class $\mathfrak{L}$ of loss functions.

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[1] Integer $j \leq k$ is used to refer to the element of $\mathcal{Z}$ which is 1 at the jth index and 0 elsewhere.

Let χ be the set of all random vectors of finite first moment taking values in $\mathbb{R}^d$, jointly defined with Z.

We say X $(\mathcal{V}, \mathfrak{L})-$**guards** Z if, for all losses $\mathcal{L} \in \mathfrak{L}$, it maximizes the minimum expected loss:

$$X \in \underset{X' \in \chi}{\arg\max} \ \inf_{\theta \in \Theta} \ \mathbb{E}\Big[\mathcal{L}(\eta(X'; \theta), Z)\Big].$$

In other words, its conditional distribution $\mathbb{P}(X \mid Z = \cdot)$ is among the worst possible distributions for predicting Z from X using a predictor of the form $\eta(\cdot; \theta) \in \mathcal{V}$ and a loss function in $\mathfrak{L}$.

Building on Definition 3.1, note that guardedness characterizes inputs whose conditional distributions make the target Z maximally unpredictable under a given model class and loss. In particular, for linear–affine predictors and squared loss, (Belrose et al., 2025) show that this worst-case unpredictability is achieved precisely when the representation is uncorrelated with the concept, i.e., when $\text{Cov}(h, Z) = 0$. Thus, enforcing guardedness in a linear representation amounts to removing all linear statistical dependence between X (or an internal representation h derived from it) and Z.

Theorem 3.2 (Linear Guardedness (Belrose et al., 2025)). *The following statements are equivalent:*

- *The data X linearly guards the labels Z (Def. 3.1)*

- *Every component of X has zero covariance with every component of Z:* $\text{Cov}(X, Z) = 0$.

At the same time, when erasing concepts from model representations, we typically wish to alter the representations as little as possible, so that downstream performance on unrelated tasks is preserved. Thus, it is natural to seek the affine transformation of X whose output is closest to X based on some distance metric, while achieving this covariance-removal property.

Guided by these two principles: (i) guardedness corresponds to zero covariance, and (ii) we prefer minimal deviation from the original representation, (Belrose et al., 2025) prove the following result:

Theorem 3.3 (LEACE, (Belrose et al., 2025)). *Let X, Z be random vectors taking values in $\mathbb{R}^d$ and $\mathbb{R}^k$ respectively, each of finite second moments. Define $\Sigma_{XX} = \text{Cov}(X, X) \in \mathbb{R}^{d \times d}$ and $\Sigma_{XZ} = \text{Cov}(X, Z) \in \mathbb{R}^{d \times k}$. Assume $\text{Im}(\Sigma_{XZ}) \subseteq \text{Im}(\Sigma_{XX})$. The following optimization problem:*

$$\min_{\substack{A \in \mathbb{R}^{d \times d} \\ b \in \mathbb{R}^d}} \mathbb{E}\Big[\|AX + b - X\|_2^2\Big] \quad s.t. \quad \text{Cov}(AX + b, Z) = 0 \tag{5}$$

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has the following solution (almost surely):

$$\widehat{A} = I - W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+ W \,, \qquad (6)$$

$$\widehat{b} = \mathbb{E}[X] - \widehat{A} \cdot \mathbb{E}[X] \,, \qquad (7)$$

where $W = (\Sigma_{XX}^{1/2})^+$ is whitening transformation.

Here and later we use A^+ to denote the pseudo-inverse of (any) matrix A and $A^{1/2}$ to denote the square root of a positive semi-definite symmetric matrix A, i.e. for the singular value decomposition $A = VSV^\top$ with orthonormal matrix V and diagonal matrix S with non-negative singular values on the diagonal, the matrix $A^{1/2}$ is defined as $A^{1/2} := VS^{1/2}V^\top$, where the square root of the diagonal entries of S is computed.

4. Theoretical Results

We theoretically analyze connections between steering approaches (Sec. 3.1) and LEACE (Sec. 3.2), and derive a novel framework for affine concept steering called MidSteer, that unifies and generalizes all these approaches.

This section is organized as follows. We first consider the task of concept erasure and establish a formal connection between the standard steering setup for erasure and LEACE, showing that Eq. 3 arises as a special case of the LEACE framework. We then extend LEACE to the task of optimal affine concept switching and derive **LEACE-Switch**, demonstrating that Eq. 4 is a special case of this bidirectional switching formulation.

Next, we characterize the assumptions under which LEACE-Switch provides an optimal solution and introduce **MidSteer**, a more general affine framework for concept manipulation that enables directed, minimal-disturbance transformations without requiring dataset-wide label inversion. Finally, through experiments on large language models and vision diffusion models, we show that MidSteer consistently outperforms vanilla steering and LEACE-based switching, achieving precise concept control while preserving unrelated features of the generated outputs.

4.1. Connection between steering in erasure mode and LEACE

In this section, we show that steering in erasure mode (Eq. 3) is a special case of LEACE. We formulate and prove a following corollary to the Theorem 3.3:

Corollary 4.1. *Let X be a standardized random vector in $\mathbb{R}^d$, i.e., it has zero mean $\mathbb{E}[x] = 0$ and unit covariance matrix $\Sigma_{XX} = I$. Let $C \in \{0,1\}$ be a concept indicator variable. Let s be defined as in Eq. 1. Let f_{delete} be defined*

(a) Illustrative example of affine concept erasure. In this case the affine transformation is satisfying $\text{cov}(AX + b, Z) = 0$. This figure is inspired by (Belrose et al., 2025).

(b) Illustrative example of affine concept switching. In this case the affine transformation is satisfying $-\text{cov}(AX + b, Z) = \text{cov}(X, Z)$.

Figure 1. Illustrative example of affine concept erasure and affine concept flipping frameworks.

as in Eq. 3. Then f_{delete} as a function of h minimizes

$$\min_{f \in \text{Aff}(\mathbb{R}^d \mapsto \mathbb{R}^d)} \mathbb{E}[\|f(X) - X\|^2] \; s.t. \; \text{Cov}(f(X), C) = 0 \tag{8}$$

This theorem states that steering in erasure mode can be seen as LEACE under the assumptions that the whitening matrix is the identity and that the mean of all vectors is zero. The proof is found in the Appendix D.1.

4.2. Concept switching

We generalize beyond a single binary concept, and consider the task of transforming the representation of one concept c_1 into another c_2. We call this task *concept switching*.

More formally, let c_1 and c_2 denote two distinct concepts, each associated with a subset of the data distribution (not necessarily jointly covering it), and their corresponding binary indicators $C_1, C_2 \in \{0,1\}$. The goal of a *concept switch* operation is to construct a transformation f such that samples exhibiting concept c_1 after transformation exhibit concept c_2, while preserving all other factors of variation as much as possible. Formally, this requires modifying the dependence of the representation on C_1 and introducing a desired dependence on C_2, without enforcing any relationship between C_1 and C_2 outside their observed support.

We now adapt LEACE (Theorem 3.3) framework to the task of concept switching, and formulate a theoretical framework for the optimal affine concept switching, LEACE-Switch.

Additionally, we show that steering in switching mode Eq. 4 can be seen as a special case of this framework. We then characterize the scope of LEACE-Switch by making explicit the assumptions under which it provides an optimal solution. Finally, we introduce MidSteer, a generalized affine framework for concept manipulation that relaxes these assumptions and enables directed, minimal-disturbance concept switching in more general settings.

4.2.1. LEACE FOR CONCEPT SWITCHING

Recall that $Z \in \{0,1\}^k$ denotes a binary concept vector. We now consider the task of *bidirectional concept switching*, in which the concept encoded by Z is assumed to partition the dataset (i.e., $P(Z = 1) + P(Z = 0) = 1$), so that each sample belongs either to the concept or to its complement. Under this assumption, concept switching can be interpreted as a global inversion of the linear dependence between the representation and the concept label.

Within the covariance-based guardedness framework of LEACE, such an inversion admits a natural affine formulation. Rather than removing linear information about the concept as in concept erasure, we seek to preserve the magnitude of the linear dependence while reversing its sign. This leads to the following constraint:

$$\text{Cov}(f(X), \mathbf{1}^k - Z) = \text{Cov}(X, Z), \qquad (9)$$

where $\mathbf{1}^k$ denotes a k-dimensional vector of ones. By linearity of covariance, this condition is equivalent to

$$\text{Cov}(f(X), Z) = -\text{Cov}(X, Z). \qquad (10)$$

See Fig. 1b for a geometric illustration of this.

Equation 9 constitutes the affine analogue of a *perfect concept flip* within the guardedness framework. In LEACE (Theorem 3.3), concept erasure is achieved by enforcing $\text{Cov}(f(X), Z) = 0$, ensuring that the transformed representation carries no linear signal about the concept. In contrast, the constraint above enforces a complete inversion of this signal: samples that previously correlated positively with the concept now correlate equally strongly with its complement, and vice versa. This corresponds to a symmetric, dataset-wide concept swap and mirrors the role of reflection-based switching in vanilla steering.

Analogous to Theorem 3.3, we now characterize the optimal affine transformation that satisfies the constraint in Eq. 9 while minimally disturbing the original representation:

Theorem 4.2 (LEACE-Switch, Optimal Concept Switching). *Let $X, Z, \Sigma_{XX}, \Sigma_{XZ}$ be defined as in Theorem 3.3. Assume $\text{Im}(\Sigma_{XZ}) \subseteq \text{Im}(\Sigma_{XX})$. Then the optimization*

problem

$$\min_{\substack{A \in \mathbb{R}^{d \times d}, \\ b \in \mathbb{R}^d}} \text{E}\left[\|AX + b - X\|_2^2\right] \qquad (11)$$

$$s.t. \ \text{Cov}(AX + b, Z) = -\text{Cov}(X, Z) \qquad (12)$$

has the following solution (almost surely):

$$\widehat{A} = I - 2W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+W, \qquad (13)$$

$$\widehat{b} = \mathbb{E}[X] - \widehat{A}\mathbb{E}[X], \qquad (14)$$

The proof is found in the Appendix D.2. Also note, since the transform is affine, it can be incorporated into the weight matrix of the model, thus achieving zero inference overhead. Similar to corollary 4.1, we now show that concept switching as defined in Eq. 4 is a special case of Theorem 4.2.

Corollary 4.3. *Let X be a standardized random vector in $\mathbb{R}^d$, i.e. it has zero mean $\mathbb{E}[x] = 0$ and unit covariance matrix $\Sigma_{XX} = I$. Let $C \in \{0,1\}$ be a concept indicator variable. Let s be defined as in Eq. 1. Let f_{switch} be defined as in Eq. 4. Then f_{switch} as a function of h minimizes*

$$\min_{f \in \text{Aff}(\mathbb{R}^d \mapsto \mathbb{R}^d)} \text{E}[\|f(X) - X\|^2] \qquad (15)$$

$$s.t. \quad \text{Cov}(f(X), C) = -\text{Cov}(X, C) \qquad (16)$$

The proof is found in the Appendix Sec. D.3. This theorem shows that steering in switching mode can be seen as LEACE-Switch under the assumptions that the whitening matrix is the identity and the mean of all vectors is zero.

Scope of LEACE-Switch. While the constraint in Eq. 9 precisely captures the algebraic notion of inverting a linear concept signal, it does so under a specific set of assumptions that define the regime in which LEACE-Switch is theoretically well-posed.

First, Eq. 9 assumes that the binary concept variable Z partitions the dataset, i.e., $P(Z = 1) + P(Z = 0) = 1$. Under this condition, the linear dependence between X and Z is defined globally over the data distribution and admits a dataset-wide inversion. When instead considering two concepts c_1 and c_2 with corresponding indicators Z_1 and Z_2 that do not jointly span the dataset, this assumption is violated. In such cases, the notion of a dataset-wide bidirectional concept flip is no longer well-posed, and Theorem 4.2 does not apply. Second, even when Z does partition the dataset, the constraint in Eq. 9 enforces a *complete* inversion of the linear dependence on the concept label. As a result, LEACE-Switch implements a symmetric transformation: representations associated with c_1 are mapped to those of c_2, and representations associated with c_2 are simultaneously mapped to those of c_1. While this behavior is desirable in settings that explicitly require bidirectional

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swapping, it may be overly restrictive in applications where only a one-directional transformation is intended.

Together, these considerations delineate the scope of LEACE-Switch as an optimal solution for symmetric concept inversion under dataset partitioning. In the next section, we relax these assumptions and introduce a more general formulation for affine concept manipulation that enables directed, minimal-disturbance concept switching.

4.3. Optimal Affine Concept Manipulation

We now move beyond bidirectional concept switching and formulate a more general framework for affine concept manipulation. Our goal is to enable *directed* concept transformations that do not require dataset-wide label inversion or the assumption that the involved concepts jointly span the entire distribution.

Let Z_1 and Z_2 represent indicators of two groups of concepts $C_s = \{c_1^{(s)}, \dots, c_l^{(s)}\}$ and $C_t = \{c_1^{(t)}, \dots, c_l^{(t)}\}$. Let $Z = (Z_1, Z_2)$, where $Z_1, Z_2 \in \{0, 1\}^l$. Our goal is to have $\mathrm{Cov}(f(X), Z_1) = \mathrm{Cov}(X, Z_2)$, meaning for each i, the concept $c_i^{(s)}$ maps to to $c_i^{(t)}$. Now we formulate the following theorem:

Theorem 4.4 (MidSteer, affine optimal concept manipulation). *Let X, Z be defined as in Theorem 4.2 and assume $k = 2l$ for $l > 0$. Let $Z = (Z_1, Z_2)$, where $Z_1, Z_2 \in \{0, 1\}^l$. Let $\Sigma_{XZ_i} = \mathrm{Cov}(X, Z_i), i \in \{1, 2\}$ be the cross-covariance matrices between X and Z_i. Assume $\mathrm{Im}(\Sigma_{XZ_i}) \subseteq \mathrm{Im}(\Sigma_{XX})$ for $i \in \{1, 2\}$. Assume Σ_{XZ_1} has full column rank: $\mathrm{rk}\left(\Sigma_{XZ_1}\right) = l$. Let $W = (\Sigma_{XX}^{1/2})^+$ be the whitening transformation. Let $\Sigma_{WX, Z_i} = W\Sigma_{XZ_i}$.*

Then we have the following optimization problem:

$$\min_{\substack{A \in \mathbb{R}^{d \times d} \\ b \in \mathbb{R}^d}} \mathrm{E}[\|AX + b - X\|_2^2] \tag{17}$$

$$s.t. \quad \mathrm{Cov}(AX + b, Z_1) = \mathrm{Cov}(X, Z_2) \tag{18}$$

which has the following solution (almost surely):

$$\widehat{A} = I + W^+(\Sigma_{WX,Z_2} - \Sigma_{WX,Z_1})\Sigma_{WX,Z_1}^+ W \tag{19}$$

$$\widehat{b} = \mathbb{E}[X] - \widehat{A}\mathbb{E}[X] \tag{20}$$

The proof can be found in Sec. D.4. Unlike LEACE, we now have two covariance matrices for each group of concepts, and do not require the labels to be flipped, but translated from one group to another.

Connection between MidSteer and LEACE. Note that if Z_2 is a constant indicator (e.g., representing no item in the dataset), then $\mathrm{Cov}(X, Z_2) = 0$, and the MidSteer formula turns into concept erasure (LEACE). Thus we refer to

MidSteer as *affine optimal concept manipulation*, as it generalizes several concept manipulation tasks (erasure, switch) under one framework.

4.4. Steering strength

Let us now introduce the steering strength β for erasure and switching. Note that in vanilla steering (i.e. steering defined by Eq. 3 and Eq. 4), we can unify Eq. 3 and Eq. 4 in the following way:

$$f(h, s) = h - \beta \cdot \langle h, s\rangle s \tag{21}$$

For LEACE, $\widehat{b}$ is unaffected, and Eq. 6 and Eq. 13 become:

$$\widehat{A} = I - \beta \cdot W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+ W \tag{22}$$

Now, $\beta = 1$ represents concept erasure, $0 < \beta < 1$ represents lesser degree of erasure. $\beta = 2$ represents concept switching, and $\beta > 2$ refers to switching where the switched concept is more expressed than the base concept.

For MidSteer, we update Eq. 19 as:

$$\widehat{A} = I + \beta \cdot W^+(\Sigma_{WX,Z_2} - \Sigma_{WX,Z_1})\Sigma_{WX,Z_1}^+ W \tag{23}$$

$\beta = 1$ represents normal steering mode, $\beta < 1$ represent steering where Z_2 has less expression compared to what Z_1 had in original representation. Vice versa, $\beta > 1$ represent more expression for Z_2 compared to Z_1.

5. Experiments

5.1. Experimental setup

We conduct experiments comparing MidSteer to vanilla steering and LEACE-Switch on the task of concept switching. We focus on concept switching in the main experiments, as concept erasure is recovered as a special case when the target concept is constant. However, we provide comparison of all the approaches on concept erasure in the Appendix Sec. J. We consider two modalities: (1) text, for which we use Large Language Models (LLMs); (2) images, for which we use Diffusion Models.

Evaluation setup. In each case, given a pair of concepts (c_s, c_t) to switch, we estimate class-conditional covariances $\Sigma_{XZ_1}, \Sigma_{XZ_2}$ based on a sample of size $N = 1000$, and self-covariances Σ_{XX} on a sample of size $M = 50000$. We ablate the number of prompts needed for estimating Σ_{XX} in the Appendix Sec. H, and provide pseudocode for the algorithm on covariance estimation in the Sec. A.

As no standard benchmarks currently exist for concept switching, we introduce a dedicated evaluation setup. Our procedure is largely based on established concept erasure benchmarks used for vision generative models (Lyu et al., 2024; Wu et al., 2025). To test switching from the source

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(a) ΔCS vs CS of unrelated concepts for the Llama-2-7b model.

(b) ΔCS vs 1 - BERT Precision on MMLU for the Llama-2-7b model.

(c) ΔCS vs CS of unrelated concepts for the SDXL model.

(d) ΔCS vs FID of unrelated concepts for the SDXL model.

Figure 2. Pareto efficiency frontiers for concept *switching* experiments with steering, LEACE, and MidSteer highlighting different βs.

concept c_s to the target concept c_t, we use 80 template prompts prompting the model to generate output related to c_s or c_t. For each prompt we run 10 such generations varying the random seed. We run the generation on these prompts with and without steering. Templates for LLMs and diffusion models can be found in Sec. G. We use *Concept Score (CS)* to estimate the amount of concepts c_s and c_t present in the model's output. In the case of ideal switching, CS for concept c_t should be high, and CS for concept c_s should be low for prompts related to both c_s or c_t.

To evaluate content preservation beyond the switched concepts, we additionally generate outputs for four unrelated concepts $\{c_i\}_{i=1}^4$. These concepts are chosen to span varying levels of semantic proximity to c_s and c_t. We compute CS over $\{c_i\}_{i=1}^4$ to quantify the extent to which these concepts are retained in the generated outputs, which ideally should not decrease under steering. This design enables a more fine-grained comparison of concept switching methods

with respect to semantic interference.

We use the following pairs $p_i = (c_s \rightarrow c_t)$ of concepts: $p_1 = ($"Horse" $\rightarrow$ "Motorcycle"$)$, $p_2 =$"Dog" $\rightarrow$ "Cat", p_3 ="Chihuahua" $\rightarrow$ "Muffin"$)$. Note that none of these pairs span the whole dataset. Corresponding unrelated concepts $t_i = \{c_i\}_{i=1}^4$ are : $t_1 = ($"Cow", "Dog", "Pig", "Legislator"$)$, $t_2 = ($"Cow", "Wolf", "Pig", "Legislator"$)$, $t_3 = ($"Cat", "Dog", "Wolf", "Legislator"$)$.

Details on LLM experiments. We test on instruction-tuned Llama 2 (Touvron et al., 2023) and Qwen 2.5 (Yang et al., 2024a) models. We apply steering at every self-attention (SA) layer ans use SA activations corresponding to the last token in prompt. The dataset we used to estimate class-conditional covariances was obtained by prompting GPT o4-mini to generate various questions about each concept. Details of the prompt used and examples can be found in Sec. E. To estimate Σ_{XX}, we use a sample of size M

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Figure 3. Qualitative results on switching to steer "horses" into "motorcycles". While all methods similarly successfully performed switching from "horse" to "motorcycle", vanilla steering (CASteer) and LEACE fail when presented with prompt for the target concept ("motorcycle"), unable to distinguish between forward and reverse steering. CASteer also additionally failed on the "cow" concept, and more significantly altered images of the concept "dog".

from the Alpaca dataset (Taori et al., 2023).

We calculate the *Concept Score (CS)* for a concept c using LLM as a judge. More specifically, we use the Llama-3.1-8B-Instruct (Dubey et al., 2024) model, and prompt it to estimate the amount of c present in the generated output on a scale from 0 to 10. Prompts used are outlined in the Appendix Sec. F. We additionally test how much outputs for testing concepts differ with and without steering by calculating BERT scores (Zhang et al., 2020) on the MMLU (Hendrycks et al., 2021) dataset generations. Lower values of BERT Precision represent more change in the underlying output.

Details on Diffusion Models experiments For visual diffusion models, we test on SDXL (Podell et al., 2024) and SANA (Xie et al., 2025) models. Following recent work (Gaintseva et al., 2025), we apply steering on activations of every cross-attention (CA) layer. CA activations corresponding to all images patches are used.

We use a sample of image captions from RELAION (Schuhmann et al., 2022) to estimate both the class-conditional covariances Σ_{XZ_i}, and self-covariances Σ_{XX}. For Σ_{XZ_i} we filtered the dataset to only captions that contain a specific word, mentioning the required concept.

We use CLIP score (Hessel et al., 2021) as *Concept Score (CS)*. Additionally, we measure the change between generations based on the testing concepts when steering is applied, by calculating FID (Heusel et al., 2017) between images generated by steered model and vanilla model. Higher values of FID represent more change to the underlying image.

5.2. Experimental results

We compare results on concept switching by applying vanilla steering, LEACE-Switch and MidSteer with different values of β. We present results on LLama-2-7b and SDXL models aggregated for all three concept pairs p_1, p_2, p_3 in

Table 1. Results on SDXL when flipping from "horse" to "motorcycle". Reported are CLIP-scores (cs) and FID for target and non-target concepts.

method	strength	horse		motorcycle			cow		pig		dog		legislator	
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	fid↓	cs↑	fid↓	cs↑	fid↓	cs↑	fid↓	cs↑	fid↓
orig	-	71.0	49.1	51.8	70.7	-	72.7	-	71.8	-	66.3	-	60.8	-
CASteer	2.0	52.1	69.5	68.3	52.9	212.4	70.9	42.7	71.9	18.9	66.1	28.6	60.9	24.6
LEACE	2.0	51.2	68.8	67.6	53.3	207.6	72.2	25.2	71.7	12.6	66.1	20.8	60.6	28.2
MidSteer (ours)	1.0	51.2	68.7	51.9	70.7	12.7	72.2	23.9	71.8	12.4	66.1	20.7	60.7	27.2

Fig. 2. We see that in each case MidSteer achieves much better balance between level of concept switch between c_1 and c_2 and preservation of other concepts across different values of β. Pareto plots for other models, as well as Pareto plots for individual concept and metric pairs can be found in the Appendix Sec. I.0.1, I.1.

To better illustrate differences between vanilla steering, LEACE and MidSteer for concept flipping, in Tab. 1 we present results on switching a concept of $c_1 = $ "horse" to $c_2 = $ "motorcycle" on the SDXL model. We compare Vanilla switching and LEACE with $\beta = 2$ and MidSteer with $\beta = 1$, as these are default parameters for these methods as suggested by Eqs. 25, 13, and 19. First note, that all the methods successfully flip "horse" to "motorcycle", having similar CS scores on source ("horse") and target ("motorcycle") concepts. Second, it can be seen that as suggested by definitions Eqs. 25, 13, vanilla steering and LEACE fail to keep the "motorcycle" concept intact when flipping "horse" to "motorcycle", as target CS score goes down. In contrast, MidSteer keeps "motorcycle" intact. This is also illustrated in Fig. 3. Next, CS score of "cow" and FID scores of "cow", "pig" and "dog" are worse for vanilla than for other methods, showing superiority of LEACE and MidSteer over vanilla steering in ability to keep unrelated concepts intact. Results on other concepts flipping on both LLMs and diffusion models show similar patterns. We observe the same trend over all the concept pairs and models. We give more details in Appendix Sec. I.2, I.3.

6. Conclusion

In this work, we bridge the gap between previous empirical research in steering generative models and the theory of affine concept steering. We extend this theoretical framework to concept switching. We define the corresponding optimisation problem and solve it in closed form. We then present MidSteer, a general steering method, that is theoretically optimal under certain conditions. It outperforms other methods on concept switching for both LLMs and image diffusion models, while having the advantage of clear matrix form representation. To our knowledge, this is the first theoretical treatment of steering beyond erasure, connecting empirical heuristics and principled affine methods, while reaching state-of-the-art results.

8

Impact Statement

This paper presents work whose goal is to advance the field of machine learning. There are many potential societal consequences of our work, none of which we feel must be specifically highlighted here.

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A. Algorithm for computing covariances

To estimate the covariances we use the algorithm by (Welford, 1962) on a sample of broad prompts (unrelated to the steering concepts). Given X with the dimension of $batch\_size \times num\_heads \times seq\_len \times hidden\_dim$, the algorithm estimates the covariance matrix $\Sigma_X X$ of size $hidden\_dim \times hidden\_dim$. It does this by maintaining sample-level statistics of size $O(hidden\_dim^2)$ in memory and takes $O(batch\_size * seq\_len * hidden\_dim^2)$ time to update them for the output of a particular layer on a particular batch. In practice, estimating the covariances for 50,000 samples for SANA 1.6 finished in under 15 minutes, and for Qwen2.5 14B in under 30 minutes on our hardware setup.

In Algorithm 1 we provide pseudocode of the algorithm.

Algorithm 1 Welford's Algorithm for Online Mean and Covariance Estimation

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1: **Input:** Stream of data batches $\{\mathbf{X}_1, \mathbf{X}_2, \ldots, \mathbf{X}_K\}$ where $\mathbf{X}_k \in \mathbb{R}^{h \times m_k \times d}$
2: **Output:** Mean $\boldsymbol{\mu}$ and covariance $\boldsymbol{\Sigma}$ estimates
3: **Initialization:**
4: $n \leftarrow 0$ ▷ Total count of samples seen
5: $\mathbf{M} \leftarrow \mathbf{0} \in \mathbb{R}^{h \times d}$ ▷ Running sum
6: $\mathbf{S} \leftarrow \mathbf{0} \in \mathbb{R}^{h \times d \times d}$ ▷ Running sum of squared differences
7:
8: **for** $k = 1$ to K **do**   ▷ Process each batch
9:     $m_k \leftarrow$ number of samples in batch $\mathbf{X}_k$
10:     **if** $n = 0$ **then**   ▷ First batch - initialize
11:        $n \leftarrow m_k$
12:        $\mathbf{M} \leftarrow \sum_{j=1}^{m_k} \mathbf{x}_{k,j}$ ▷ Sum over samples
13:        $\boldsymbol{\mu} \leftarrow \mathbf{M}/n$
14:        $\boldsymbol{\Delta} \leftarrow \mathbf{X}_k - \boldsymbol{\mu} \otimes \mathbf{1}_{m_k}^{\top}$ ▷ Center vectors
15:        $\mathbf{S} \leftarrow \boldsymbol{\Delta}^{\mathsf{H}} \boldsymbol{\Delta}$
16:     **else**   ▷ Subsequent batches - update
17:        $\boldsymbol{\mu}_{\text{old}} \leftarrow \mathbf{M}/n$ ▷ Mean before update
18:        $n \leftarrow n + m_k$ ▷ Update count
19:        $\mathbf{M} \leftarrow \mathbf{M} + \sum_{j=1}^{m_k} \mathbf{x}_{k,j}$ ▷ Update sum
20:        $\boldsymbol{\mu}_{\text{new}} \leftarrow \mathbf{M}/n$ ▷ Mean after update
21:        $\boldsymbol{\Delta}_{\text{old}} \leftarrow \mathbf{X}_k - \boldsymbol{\mu}_{\text{old}} \otimes \mathbf{1}_{m_k}^{\top}$
22:        $\boldsymbol{\Delta}_{\text{new}} \leftarrow \mathbf{X}_k - \boldsymbol{\mu}_{\text{new}} \otimes \mathbf{1}_{m_k}^{\top}$
23:        $\mathbf{S} \leftarrow \mathbf{S} + \boldsymbol{\Delta}_{\text{old}}^{\mathsf{H}} \boldsymbol{\Delta}_{\text{new}}$ ▷ Welford update
24:     **end if**
25: **end for**
26:
27: **Finalization:**
28: $\boldsymbol{\mu} \leftarrow \mathbf{M}/n$ ▷ Final mean estimate
29: $\boldsymbol{\Sigma} \leftarrow \frac{1}{n-1} \cdot \frac{\mathbf{S}+\mathbf{S}^{\mathsf{H}}}{2}$ ▷ Final covariance estimate
30: **return** $\boldsymbol{\mu}, \boldsymbol{\Sigma}$

B. Incorporating steering into model weights

Recall that the last layer of self-attention block in LLMs or cross-attention block in SDXL/SANA is a Linear layer with no bias and no activation function, i.e., essentially is a matrix multiplication with bias correction term: $h_{out} = W_{proj\_out}h_{in} + b$. Here W_{proj_out} is a weight matrix of the last $proj\_out$ layer of SA/CA block of LLM/SDXL/SANA, h_{in} and h_{out} are input and output to that layer, h_{out} being the final output of SA/CA layer.

Assuming s is normalized ($\|s\| = 1$), vanilla concept erasure represents orthogonal projection onto the subspace orthogonal to s and can be written in a matrix form:

$$f_{\text{delete}}(h, s) = (I - ss^T)h \tag{24}$$

Vanilla concept switching is a Householder reflection of the vector h across the hyperplane orthogonal to s:

$$f_{\text{switch}}(h, s) = (I - 2ss^T)h \tag{25}$$

LEACE / MidSteer are already presented in this paper in matrix form.

Thus, by combining last layer of SA/CA block with matrix formulation of steering/LEACE/MidSteer, we can incorporate the transformation directly into weights of the model, by multiplying weight matrix of the last layer of SA/CA block with A^* matrix from of steering/LEACE/MidSteer:

$$h_{out} = A^*(W_{proj\_out}h_{in} + b) + b^* = W^s_{proj\_out}h_{in} + b^s \tag{26}$$

$W^s_{proj\_out}$ is a matrix of the same size as W_{proj_out}. This results in having zero inference overhead compares to original LLM/SDXL/SANA models.

	Horse	Motorcycle	Cow	Dog
Vanilla model	In the heart of a vast, rolling green valley lay a secluded meadow embraced by ancient oaks and wildflowers in bloom. Here, the **horses** lived a simple, joyous life...	In the heart of the bustling city of San Francisco, there lived a **motorcycle** named Thunder. Unlike the other shiny, new **bikes** lining the streets, Thunder was an old Kawasaki with rusted edges...	In the lush, rolling hills of Green Meadows Farm, there lived a herd of contented **cows** that grazed under the warm sun and shared the soft, dewy grass. Among them was Daisy, a golden **cow** with spots as vivid as a child's imagination...	In the quiet town of Willowbrook, nestled between rolling hills and whispering woods, lived a small **terrier** named Bella. Bella was not just a **dog**; she was the heart of the household...
Steering	In the heart of a bustling city, there was once a forgotten corner, nestled between towering skyscrapers and hidden behind a rusty iron gate, where a vintage **bike** shop and a small garage sat side by side. Among the neglected treasures within the **garage** were forgotten car parts...	In the heart of a bustling city, amidst towering skyscrapers and winding streets, lived an old **stallion** named Max. Unusual for the concrete jungle, Max was never your typical **beast**...	In the quiet countryside of Green Valley, there lived a community of **cows**, but not just any **cows**. This was a town of the most unique and quirky cows you could imagine. Each cow had its own style of living, its way of seeing the world, and even its own personality, much like humans...	In the heart of a bustling city where skyscrapers kissed the sky and the streets were a maze of hurried footsteps and whispering winds, lived a small, golden **retriever** named Buddy. Buddy wasn't your ordinary family pet; his world was the park near the city's old library...
LEACE-Switch	In the heart of a quaint countryside stood a grand old barn that was more than just a shelter; it was the soul of a **motorcycle** club known as The Thunder, but hidden deep within its walls was a story of grace, freedom, and unexpected friendship...	In the heart of a sprawling, bustling city, there lived an old man named Jack who harbored a long-lost passion for **horses** until the day he met his first **motorcycle**. It was a sleek, black **beast** he spotted outside a garage one rainy evening...	In the peaceful, sun-drenched fields of Green Meadows Farm, there lived a herd of contented **cows**, each with its own personality and quirks. At the heart of this herd was a gentle giant named Bessie, known for her creamy coat and kind eyes...	In the quiet town of Millbrook, nestled among rolling hills and vibrant green landscapes, lived a **dog** named Buddy. Buddy wasn't just any **dog**; he was a loyal companion to the Smith family, known for his boundless energy and affectionate nature...
MidSteer	In the heart of the sprawling Wilden Plains, there thrived a community of **motorcycles** and cars, but it was the Rusty Rims Speedway that drew the greatest attention. Yet, hidden within the shadow of this bustling speedway, lived a group of **motorcycles**...	In the heart of a bustling city, where the sound of the urban jungle was constant, there lived a **motorcycle** named Racer. More than just a machine, Racer was an embodiment of freedom and adventure, cherished by his owner, Jake...	In the verdant fields of Sunny Meadows, where the sun bathed golden light onto rolling hills blanketed in lush grass, there lived a community of cheerful **cows**. Among them was Daisy, known not only for her creamy coat and gentle moo but for her adventurous spirit...	Once upon a time, in a small town nestled between rolling hills and a whispering forest, there lived a **dog** named Rusty. Rusty wasn't like the other **dogs** in town. While they were mostly interested in chasing balls and squirrels, Rusty loved nothing more than exploring the woods that bordered the town...

Figure 4. Qualitative text steering results for four content categories (*horse*, *motorcycle*, *cow*, *dog*). Results are reported using vanilla Qwen2.5-14B-instruct model, and three steering methods: *Vanilla Steering*, *LEACE-Switch*, *MidSteer*). Each cell shows the generated text for the prompt *"Write a short story about a X"*, where X is a corresponding category.

C. LLM qualitative results

In this section in fig. 4 we present qualitative results for different steering methods on LLM (Qwen2.5-14B-instruct). Results show similar pattern to that of images (see fig. 3). While all methods similarly successfully performed switching from "horse" to "motorcycle", vanilla steering and LEACE failed when presented with prompt for the target concept ("motorcycle"), since they do not distinguish between forward and reverse steering. Vanilla steering also more significantly altered texts of concepts "cow" and "dog".

D. Theorem proofs

D.1. Proof of Thm. ?? (vanilla erasure is a special case of LEACE)

Proof. We have $k = 1, Z = C$. According to **Theorem 3.3**, $f(X) = A^*X + b^*$, where A^* is defined as in (6) and b^* is defined as in (7), minimizes (5).

We conclude $b^* = 0$ since $\mathrm{E}[X] = 0$. Further, it can be shown that $W = \Sigma_{XX}^{-1/2} = I^{-1/2} = I$; hence, the transform f (that is optimal according to **Theorem 3.3**) simplifies to

$$f(X) = \left(I - \Sigma_{XZ}\Sigma_{XZ}^+\right)X. \tag{27}$$

Recall that we are working in $k = 1$, so $\Sigma_{XZ} \in \mathbb{R}^{d \times 1}$ is a column-vector. By definition of the Moore-Penrose inverse for column-vectors,

$$\Sigma_{XZ}^+ = \frac{\Sigma_{XZ}^T}{\|\Sigma_{XZ}\|^2},$$

hence

$$f(X) = X - s's'^T X = X - \langle X, s'\rangle s',$$

for $s' = \Sigma_{XZ}/\|\Sigma_{XZ}\|$,

Now,

$$\Sigma_{XZ} = \mathrm{Cov}(X, Z) = \mathrm{E}[XZ] - \mathrm{E}[X] \cdot \mathrm{E}[Z] = \mathrm{E}[X \cdot 1|Z = 1] \cdot P(Z = 1) + \\ \mathrm{E}[X \cdot 0|Z = 0] \cdot P(Z = 0) - \mathrm{E}[X] \cdot P(Z = 1) = \\ P(Z = 1) \cdot \left(\mathrm{E}[X|Z = 1] - \mathrm{E}[X]\right)$$

Now recall that $P(Z = 1) + P(Z = 0) = 1$, so

$$\Sigma_{XZ} = P(Z = 1) \cdot \left(\mathrm{E}[X|Z = 1] - \mathrm{E}[X]\right) = \\ P(Z = 1) \cdot \left(\mathrm{E}[X|Z = 1] - \mathrm{E}[X|Z = 1]P(Z = 1) - \mathrm{E}[X|Z = 0]P(Z = 0)\right) = \\ P(Z = 1) \cdot P(Z = 0) \cdot \left(\mathrm{E}[X|Z = 1] - \mathrm{E}[X|Z = 0]\right)$$

, so $s' = s$ and f is equivalent to f_{delete}. Hence, f_{delete} is the transformation that minimises (8).

$\square$

D.2. Proof of Thm. 4.2 (LEACE-Switch)

Proof. The sketch for the rest of the proof will look like this:

1. Find necessary conditions for optimality using Lagrange multipliers method

2. Show that A^*, b^* satisfy the necessary conditions

3. Show that optimisation problem is convex over linear constraints, and such, if a local solution exists, it is globally optimal and unique.

Let us formulate the Lagrangian. Here $\Lambda \in \mathbb{R}^{d \times k}$, because we have $d \cdot k$ constraints on covariance matrix.

$$\mathcal{L}(A, b, \Lambda) = \frac{1}{2}\mathrm{E}\Big[\|AX + b - X\|_2^2\Big] + \langle \Lambda, \mathrm{Cov}(AX + b, Z) + \mathrm{Cov}(X, Z)\rangle_F =$$
$$\frac{1}{2}\mathrm{E}\Big[(AX + b - X)^T(AX + b - X)\Big] + \mathrm{Tr}\Big(\Lambda^T(A + I)\Sigma_{XZ}\Big) =$$
$$\mathrm{E}\Big[\frac{1}{2}X^T A^T AX + b^T AX - X^T AX - X^T b + \frac{1}{2}b^T b + \frac{1}{2}X^T X\Big] + \mathrm{Tr}\Big(\Lambda^T(A + I)\Sigma_{XZ}\Big) \quad (28)$$

The partial derivatives of the Lagrangian with respect to A, b, Λ are

$$\frac{\partial \mathcal{L}}{\partial A} = \mathrm{E}[AXX^T + bX^T - XX^T] + \Lambda \Sigma_{XZ}^T\,,$$
$$= A\mathrm{E}[XX^T] + b\mathrm{E}[X]^T - \mathrm{E}[XX^T] + \Lambda \Sigma_{XZ}^T\,,$$
$$\frac{\partial \mathcal{L}}{\partial b} = \mathrm{E}[AX + b - X]\,,$$
$$= A\mathrm{E}[X] + b - \mathrm{E}[X]\,,$$
$$\frac{\partial \mathcal{L}}{\partial \Lambda} = (A + I)\Sigma_{XZ}\,.$$

Next, we use $\mu = \mathrm{E}(X)$ and $\mathrm{E}[XX^T] = \Sigma_{XX} + \mu\mu^T$ to formulate the necessary conditions

$$0 = \frac{\partial \mathcal{L}}{\partial A} = (A - I)\Big(\Sigma_{XX} + \mu\mu^T\Big) + b\mu^T + \Lambda \Sigma_{XZ}^T\,, \quad (29)$$
$$0 = \frac{\partial \mathcal{L}}{\partial b} = A\mu + b - \mu\,, \quad (30)$$
$$0 = \frac{\partial \mathcal{L}}{\partial \Lambda} = (A + I)\Sigma_{XZ}\,. \quad (31)$$

We note that the optimal b^* as defined in (14) satisfies 30. Plugging (30) in (29) leads to

$$(A - I)\Big(\Sigma_{XX} + \mu\mu^T\Big) + (\mu - A\mu)\mu^T + \Lambda \Sigma_{XZ}^T\,,$$
$$= A\Sigma_{XX} - \Sigma_{XX} + A\mu\mu^T - \mu\mu^T + \mu\mu^T - A\mu\mu^T + \Lambda \Sigma_{XZ}^T\,,$$
$$= (A - I)\Sigma_{XX} + \Lambda \Sigma_{XZ}^T = 0\,. \quad (32)$$

Now let us check that A^* satisfies 31 and 32. By plugging A^* into 31 we get

$$0 = (2I - 2W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+ W)\Sigma_{XZ}\,,$$
$$= 2\Sigma_{XZ} - 2W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+(W\Sigma_{XZ})\,,$$
$$= 2\Big(\Sigma_{XZ} - W^+ W\Sigma_{XZ}\Big)\,,$$
$$= 2\left(\Sigma_{XZ} - \big(I - P_{\mathcal{N}(W)}\big)\Sigma_{XZ}\right)\,,$$
$$= 2P_{\mathcal{N}(W)}\Sigma_{XZ}\,, \quad (33)$$

because Moore-Penrose inverses B^+ of B satisfy $BB^+ B = B$ and $B^+ B = I - P_B$. Here P_B denotes the orthogonal projection onto the nullspace $\mathcal{N}(B)$ of B. Since the columns of Σ_{XZ} always lie within the image of Σ_{XX} (which is the orthogonal complement of the kernel of Σ_{XX}, which is also the kernel of W), we can conclude that (33) is always satisfied.

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Plugging A^* into 32 we observe

$$- 2 \cdot (W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+ W)\Sigma_{XX} + \Lambda \Sigma_{XZ}^T =$$
$$- 2 \cdot W^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+ W^+ + \Lambda \Sigma_{XZ}^T = 0 \quad (34)$$

The identity $W\Sigma_{XX} = W^+$ holds because Σ_{XX} is symmetric p.s.d., so $\Sigma_{XX} = UDU^T$ and $\Sigma_{XX}^{-1/2}\Sigma_{XX} = UD^{-1/2}U^T UDU^T = UD^{1/2}U^T = \Sigma_{XX}^{1/2}$ for some orthogonal U and non-negative diagonal D, and because $D^{-1/2}$ ignores zero diagonal values.

Next, multiplying (34) by W from both sides leads to

$$- 2WW^+(W\Sigma_{XZ})(W\Sigma_{XZ})^+ W^+ W + W\Lambda \Sigma_{XZ}^T W =$$
$$- 2(W\Sigma_{XZ})(W\Sigma_{XZ})^+ + W\Lambda(W\Sigma_{XZ})^T = -2\Sigma_{WX,Z}\Sigma_{WX,Z}^+ + \Lambda_W \Sigma_{WX,Z}^T = 0, \quad \text{(almost surely)}$$

where again $WW^+ = W^+W = I$ on a subspace covered by X, and thus, almost surely.

We seek Λ_W such that $-2\Sigma_{WX,Z}\Sigma_{WX,Z}^+ + \Lambda_W \Sigma_{WX,Z}^T = 0$. Let $\Lambda_W = 2(\Sigma_{WX,Z}^+)^T$. This choice satisfies the condition because $\Sigma_{WX,Z}\Sigma_{WX,Z}^+$ is an orthogonal projection matrix, and is thus symmetric, so

$$(\Sigma_{WX,Z}^+)^T \Sigma_{WX,Z}^T = (\Sigma_{WX,Z}\Sigma_{WX,Z}^+)^T = \Sigma_{WX,Z}\Sigma_{WX,Z}^+,$$

which again proves the Lagrange conditions for partial derivative w.r.t. A.

Thus we have shown that the said optimisation problem has a local solution. But because the constraint is linear in A, and it follows from the triangle inequality that $\|\cdot\|$ is convex, the local optimum is actually the global minimum.

$\square$

D.3. Proof of Thm. 4.3 (vanilla concept switching is a special case of LEACE-Switch)

Proof. Let $k = 1, Z = C, M = I$. According to **Theorem 4.2**, $f(X) = A^*X + b^*$, where A^* is defined in (13) and b^* is defined in (14) minimizes (11).

$b = 0$ since $\mathrm{E}[X] = 0$. Also it can be shown $W = \Sigma_{XX}^{-1/2} = I^{-1/2} = I$, so the transform becomes:

$$f(X) = \left(I - 2 \cdot \Sigma_{XZ}\Sigma_{XZ}^+\right)X \quad (35)$$

Recall that we are working in $k = 1$, so $\Sigma_{XZ} \in \mathbb{R}^{d \times 1}$ is a column-vector. So

$$\Sigma_{XZ} = \mathrm{Cov}(X, Z) = \mathrm{E}[XZ] - \mathrm{E}[X] \cdot \mathrm{E}[Z] = \mathrm{E}[X \cdot 1 | Z = 1] \cdot P(Z = 1) +$$
$$\mathrm{E}[X \cdot 0 | Z = 0] \cdot P(Z = 0) - \mathrm{E}[X] \cdot P(Z = 1) =$$
$$P(Z = 1) \cdot \left(\mathrm{E}[X | Z = 1] - \mathrm{E}[X]\right)$$

Now recall that $P(Z = 1) + P(Z = 0) = 1$, so

$$\Sigma_{XZ} = P(Z = 1) \cdot \left(\mathrm{E}[X | Z = 1] - \mathrm{E}[X]\right) =$$
$$P(Z = 1) \cdot \left(\mathrm{E}[X | Z = 1] - \mathrm{E}[X | Z = 1]P(Z = 1) - \mathrm{E}[X | Z = 0]P(Z = 0)\right) =$$
$$P(Z = 1) \cdot P(Z = 0) \cdot \left(\mathrm{E}[X | Z = 1] - \mathrm{E}[X | Z = 0]\right)$$

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, which is equal to s up to normalization constant. By definition of Moore-Penrose inverse for column-vectors,

$$\Sigma_{XZ}^+ = \frac{\Sigma_{XZ}^T}{\|\Sigma_{XZ}\|^2}$$

, so

$$f(X) = X - 2 \cdot ss^T X = X - 2 \cdot s(s^T X) = X - 2 \cdot (s^T X)s = X - 2 \cdot \langle X, s \rangle s$$

, so f is equivalent to f_{switch}.

$\square$

D.4. Proof of Thm. 4.4 (MidSteer)

Proof. We will use the same method as in D.2 to prove this. Indeed, the objective is same, and thus convex. The constraint is still linear:

$$\text{Cov}(Ax + b, Z_1) = A\Sigma_{XZ_1} = \Sigma_{XZ_2} = \text{Cov}(X, Z_2) \tag{36}$$

So let us define the Lagrangian, where $\Lambda \in \mathbb{R}^{d \times l}$:

$$\mathcal{L}(A, b, \Lambda) = \frac{1}{2}\text{E}\left[(AX + b - X)^T(AX + b - X)\right] + Tr\left(\Lambda^T(A\Sigma_{XZ_1} - \Sigma_{XZ_2})\right) \tag{37}$$

The derivatives w.r.t. parameters are the following:

$$\frac{\partial \mathcal{L}}{\partial A} = (A - I)(\Sigma_{XX} + \mu\mu^T) + b\mu^T + \Lambda\Sigma_{XZ_1}^T \qquad = 0 \tag{38}$$

$$\frac{\partial \mathcal{L}}{\partial b} = A\mu - \mu + b \qquad = 0 \tag{39}$$

$$\frac{\partial \mathcal{L}}{\partial \Lambda} = A\Sigma_{XZ_1} - \Sigma_{XZ_2} \qquad = 0 \tag{40}$$

Trivially b^* satisfies (39) for suitable A^*.

Let us see that (40) is satisfied. We can plug A^* and then multiply by W on the left, to get:

$$W\Sigma_{XZ_1} + WW^+(\Sigma_{WX,Z_2} - \Sigma_{WX,Z_1})\Sigma_{WX,Z_1}^+ W\Sigma_{XZ_1} - W\Sigma_{XZ_2} =$$
$$\Sigma_{WX,Z_1} - \Sigma_{WX,Z_1}\Sigma_{WX,Z_1}^+ \Sigma_{WX,Z_1} + \Sigma_{WX,Z_2}\Sigma_{WX,Z_1}^+ \Sigma_{WX,Z_1} - \Sigma_{WX,Z_2} =$$
$$\Sigma_{WX,Z_2}I_l - \Sigma_{WX,Z_2} = 0 \quad \text{(almost surely)}$$

Here we used $YY^+Y = Y$ for any Y. Furthermore, since Σ_{WX,Z_1} has linearly independent columns (full column rank), we use the property $Y^+Y = I$.

Next, plugging (39) into (38) we get:

$$(A - I)\Sigma_{XX} + \Lambda\Sigma_{XZ_1}^T = 0 \tag{41}$$

Let us now proceed to show that for A^* there exists $\Lambda \in \mathbb{R}^{d \times l}$ so this equality holds. After plugging in A^* and using previously shown fact $W\Sigma_{XX} = W^+$:

$$W^+(\Sigma_{WX,Z_2} - \Sigma_{WX,Z_1})\Sigma_{WX,Z_1}^+ W^+ + \Lambda\Sigma_{XZ_1}^T = 0 \tag{42}$$

Again, multiplying by W on both sides and recalling that W is symmetric we get:

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$$(\Sigma_{WX,Z_2} - \Sigma_{WX,Z_1})\Sigma_{WX,Z_1}^+ + \Lambda_W \Sigma_{WX,Z_1}^T = 0 \qquad \text{(almost surely)}$$

Now, Σ_{WX,Z_1} is also full column rank, so $\Sigma_{WX,Z_1}^+ = \left(\Sigma_{WX,Z_1}^T \Sigma_{WX,Z_1}\right)^{-1} \Sigma_{WX,Z_1}^T$. Thus, $\Lambda_W = -\left(\Sigma_{WX,Z_2} - \Sigma_{WX,Z_1}\right)\left(\Sigma_{WX,Z_1}^T \Sigma_{WX,Z_1}\right)^{-1}$ satisfies the equation.

$\square$

E. Example LLM prompts for Estimating Class-Conditional Covariance

To obtain class-conditional means for LLMs, we constructed 1000 prompts across several categories. In each case, last token activation was used to compute steering vectors, before first token of model output and after corresponding chat template tokens. Below we provide illustrative subsets of the prompts used:

- **Horse-related prompts**

  - How did horses evolve from their early ancestors?
  - What factors contributed to the domestication of horses?
  - What anatomical features enable a horse to run at high speeds?

- **Motorcycle-related prompts**

  - What was the significance of the earliest gasoline powered motorcycle in the evolution of personal transportation?
  - How does the engine cycle mechanism influence power delivery and efficiency in a motorbike?
  - What are the primary considerations when selecting the appropriate tire for varying riding conditions?

- **Dog-related prompts**

  - What is believed to be the origin of dog domestication?
  - How do dogs communicate through body language?
  - Which genetic factors influence coat color in dogs?

- **Cat-related prompts**

  - What is the origin of domestic cats and how did they become companion animals?
  - How did ancient Egyptians incorporate cats into their society and religion?
  - Why did cats spread globally alongside human trade routes?

F. Prompt for Concept Scoring in LLMs

To assess the quality of steering, we compute a *concept score* that gauges the presence of a specific concept in generated text. The score ranges from 0 to 10:

- A score of 0 indicates the text is completely irrelevant to the concept.

- A score of 10 indicates strong and explicit relevance to the concept.

- Scores from 1 through 9 represent gradations of partial relevance.

The following prompt was used to query the model for concept scoring:

```
Score the text on a scale of 0 to 10, where the score reflects the extent
to which it demonstrates relevance to the concept of {concept}. A score of 0
indicates the text is completely irrelevant and shows no connection to {concept},
whereas a score of 10 signifies strong and explicit relevance to {concept}. For
texts that suggest varying degrees of relevance, use the intermediate numbers
(1 through 9) to represent the gradation of connection to {concept}.
Output just a single number.

Text to evaluate: ```
{text}
```
```

The exact score is obtained by doing a forward pass of Llama3.1-7B model and taking argmax across token probabilities corresponding to score tokens (from 0 to 10).

# G. Template Prompts for Steering Quality Assessment

To evaluate the effectiveness of steering, we constructed a set of template prompts. In each case, the {} placeholder was substituted with the concept under consideration (as defined in **??**). Each template was used to generate multiple model responses. These responses were then evaluated either by a judge model (for text/LLM outputs) or by CLIP score (for images), to compute the Concept Score as well as related metrics such as FID and BERTScore.

## G.1. LLM Assessment Prompts

The following template prompts were used for large language model (LLM) evaluation. The placeholder {} is substituted with a concept.

```
 1.  Write a short story about a {}
 2.  Write a poem about a {}
 3.  What is the history of {}
 4.  What is the most famous {}?
 5.  What is the most expensive {}?
 6.  How to make a {}?
 7.  How to maintain a {}?
 8.  How to dispose of a {}?
 9.  How to store a {}?
10.  How to transport a {}?
11.  How to use a {}?
12.  What is important to know about {}?
13.  How to tell age of a {}?
14.  What is a {}?
15.  What types of {} are there?
16.  What are the most common {}?
17.  Describe an appearance of {} in detail.
18.  How does {} look like?
19.  How does {} sound like?
20.  How does {} feel like?
21.  How does {} behave like?
22.  What is the purpose of {}?
23.  What are the main components of a {}?
24.  How to identify a {}?
25.  Where can you find a {}?
26.  What are the dangers of a {}?
27.  What tools do you need for a {}?
28.  How much does a {} typically cost?
29.  What are alternatives to a {}?
30.  How to choose a good {}?
31.  What are common problems with a {}?
32.  How long does a {} typically last?
33.  What size is a typical {}?
34.  How to clean a {}?
35.  What skills are needed to handle a {}?
36.  What are the benefits of having a {}?
37.  How has {} changed over time?
38.  What cultures use {} the most?
39.  How to test if a {} is working properly?
40.  What safety precautions are needed for a {}?
41.  How to upgrade or improve a {}?
42.  How does weather affect a {}?
43.  What are the environmental impacts of a {}?
```

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44. How to measure the quality of a {}?
45. What accessories go with a {}?
46. How to protect a {} from damage?
47. What are myths about {}?
48. How to teach someone about a {}?
49. What industries use {}?
50. How is a {} different from similar things?
51. What are the legal considerations for owning a {}?
52. How to pack a {} for moving?
53. What are seasonal considerations for a {}?
54. How to customize a {}?
55. What are expert tips for using a {}?
56. How to troubleshoot issues with a {}?
57. What is the lifecycle of a {}?
58. How to estimate the value of a {}?
59. What are cultural significances of a {}?
60. How to take a picture of a {}?
61. How to make a sculpture of a {}?
62. What is the future of {}?
63. How to draw a {}?
64. When was {} first mentioned in human history?
65. Can one ride a {}?
66. Write a song about {}
67. Define a {}
68. Write a positive review on a book about {}
69. Write a negative review on a book about {}
70. Do people make toys of {}?
71. How is {} used in the economy?
72. Write an abstract for a science paper about {}
73. How does temperature affect a {}?
74. What are the origins of the word {}?
75. What are superstitions about {}?
76. How to simulate a {} digitally?
77. What are the physics of a {}?
78. How to teach children about {}?
79. What are famous artworks featuring {}?
80. What are the nutritional aspects of a {}?
81. Describe the most famous {} competitions.

G.2. Image Assessment Prompts

The following template prompts were used for image model evaluation. The placeholder {} was substituted with a concept.

```
 1.  a bad photo of a {}.
 2.  a photo of many {}.
 3.  a sculpture of a {}.
 4.  a photo of the hard to see {}.
 5.  a low resolution photo of the {}.
 6.  a rendering of a {}.
 7.  graffiti of a {}.
 8.  a bad photo of the {}.
 9.  a cropped photo of the {}.
10.  a tattoo of a {}.
11.  the embroidered {}.
12.  a photo of a hard to see {}.
13.  a bright photo of a {}.
14.  a photo of a clean {}.
15.  a photo of a dirty {}.
16.  a dark photo of the {}.
17.  a drawing of a {}.
18.  a photo of my {}.
19.  the plastic {}.
20.  a photo of the cool {}.
21.  a close-up photo of a {}.
22.  a black and white photo of the {}.
23.  a painting of the {}.
24.  a painting of a {}.
25.  a pixelated photo of the {}.
26.  a sculpture of the {}.
27.  a bright photo of the {}.
28.  a cropped photo of a {}.
29.  a plastic {}.
30.  a photo of the dirty {}.
31.  a jpeg corrupted photo of a {}.
32.  a blurry photo of the {}.
33.  a photo of the {}.
34.  a good photo of the {}.
35.  a rendering of the {}.
36.  a {} in a video game.
37.  a photo of one {}.
38.  a doodle of a {}.
39.  a close-up photo of the {}.
40.  a photo of a {}.
41.  the origami {}.
42.  the {} in a video game.
43.  a sketch of a {}.
44.  a doodle of the {}.
45.  a origami {}.
46.  a low resolution photo of a {}.
47.  the toy {}.
48.  a rendition of the {}.
49.  a photo of the clean {}.
50.  a photo of a large {}.
51.  a rendition of a {}.
```

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```
52.  a photo of a nice {}.
53.  a photo of a weird {}.
54.  a blurry photo of a {}.
55.  a cartoon {}.
56.  art of a {}.
57.  a sketch of the {}.
58.  a embroidered {}.
59.  a pixelated photo of a {}.
60.  itap of the {}.
61.  a jpeg corrupted photo of the {}.
62.  a good photo of a {}.
63.  a plushie {}.
64.  a photo of the nice {}.
65.  a photo of the small {}.
66.  a photo of the weird {}.
67.  the cartoon {}.
68.  art of the {}.
69.  a drawing of the {}.
70.  a photo of the large {}.
71.  a black and white photo of a {}.
72.  the plushie {}.
73.  a dark photo of a {}.
74.  itap of a {}.
75.  graffiti of the {}.
76.  a toy {}.
77.  itap of my {}.
78.  a photo of a cool {}.
79.  a photo of a small {}.
80.  a tattoo of the {}.
```

H. Number of prompts for covariance calculation

To find the optimal number of prompts used to calculate unconditional covariances Σ_{XX} for concept switching, we perform the following ablation study. For each number of prompts used for covariances generation from the set $\{100, 500, 1000, 5000, 10000, 20000\}$ we run the same base experiment as outlined in Sec. 5. We then compute ΔCS and 1 - BERT Precision @ MMLU metrics on a small set of MidSteer steering strengths (to show if the steering strength can affect the optimal number of prompts). We do it on LLM experiment setup (sec. 5.1) and use LLama2-7B model.

We then plot these values of a 2D plane similar to Pareto charts, but this time varying the number of prompts instead. This in essence forms a curve that, after a certain threshold, settles in a small region of metric space. As can be seen from the chart below, increasing the number of prompts used beyond 5000 has limited impact.

I. More results on concept switching

I.0.1. PARETO CHARTS FOR LLM CONCEPT SWITCHING

In this section, we provide more Pareto charts for LLM concept switching. When switching concept c_s to c_t, for each LLM model we provide 9 types of Pareto plots:

- 1 - BERT Precision score for unrelated concepts (horizontal axis) vs Δ Concept Score (CS) for the target c_t and source c_s concepts (fig. 11b, 12b, 13b)

- 1 - BERT Precision score for MMLU (horizontal axis) vs Δ Concept Score (CS) for the target c_t and source c_s concepts (vertical axis) (fig. 11a, 12a, 13a)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Δ Concept Score (CS) for the target c_t and source c_s concepts (vertical axis) (fig. 11c, 12c, 13c)

- 1 - BERT Precision score for unrelated concepts (horizontal axis) vs Concept Score (CS) for the **source** c_s concept (vertical axis) (fig. 5b, 6b, 7b)

- BERT Precision score for MMLU (horizontal axis) vs Concept Score (CS) for the **source** c_s concept (vertical axis) (fig.5a, 6a, 7a)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Concept Score (CS) for the **source** c_s concept (vertical axis) (fig.5c, 6c, 7c)

- 1 - BERT Precision score for unrelated concepts (horizontal axis) vs Concept Score (CS) for the **target** c_s concept (vertical axis) (fig. 5b, 9b, 7b)

- BERT Precision score for MMLU (horizontal axis) vs Concept Score (CS) for the **target** c_s concept (vertical axis) (fig.5a, 6a, 7a)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Concept Score (CS) for the **target** c_s concept (vertical axis) (fig.5c, 6c, 7c)

In each case, we see clear superiority of MidSteer over other steering approaches.

We additionally provide detailed breakdown of scores for all β values and all concepts c_s, c_t, c_i in the tables in sec. I.2

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(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 5. Pareto plot for concept flip on model llama2-7b (Source-CS axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 6. Pareto plot for concept flip on model qwen-14b (Source-CS axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 7. Pareto plot for concept flip on model qwen-7b (Source-CS axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 8. Pareto plot for concept flip on model llama2-7b (Target-CS axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 9. Pareto plot for concept flip on model qwen-14b (Target-CS axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 10. Pareto plot for concept flip on model qwen-7b (Target-CS axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 11. Pareto plot for concept flip on model llama2-7b (Other axes axes)

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 12. Pareto plot for concept flip on model qwen-14b (Other axes axes)

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(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 13. Pareto plot for concept flip on model qwen-7b (Other axes axes)

I.1. Pareto charts for image diffusion concept switching

In this section, we provide more Pareto charts for Diffusion Models concept switching. When switching concept c_s to c_t, for each LLM model we provide 9 types of Pareto plots:

- FID score for unrelated concepts (horizontal axis) vs Δ Concept Score (CS) for the target c_t and source c_s concepts (fig. 18b, 19b)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Δ Concept Score (CS) for the target c_t and source c_s concepts (vertical axis) (fig. 18a, 19a)

- FID score for unrelated concepts (horizontal axis) vs Concept Score (CS) for the **source** c_s concept (vertical axis) (fig. 14b, 15b)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Concept Score (CS) for the **source** c_s concept (vertical axis) (fig.14a, 15a)

- FID score for unrelated concepts (horizontal axis) vs Concept Score (CS) for the **target** c_s concept (vertical axis) (fig. 16b, 17b)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Concept Score (CS) for the **target** c_s concept (vertical axis) (fig.16a, 17a)

In each case, we see clear superiority of MidSteer over other steering approaches.

We additionally provide detailed breakdown of scores for all β values and all concepts c_s, c_t, c_i in the tables in sec. I.3

(a) Unrelated vs CS   *(b)* Unrelated vs FID

Figure 14. Pareto plot for concept flip on model SANA (Source-CS axes)

(a) Unrelated vs CS   *(b)* Unrelated vs FID

Figure 15. Pareto plot for concept flip on model SDXL (Source-CS axes)

(a) Unrelated vs CS   *(b)* Unrelated vs FID

Figure 16. Pareto plot for concept flip on model SANA (Target-CS axes)

(a) Unrelated vs CS   *(b)* Unrelated vs FID

Figure 17. Pareto plot for concept flip on model SDXL (Target-CS axes)

(a) Unrelated vs CS *(b)* Unrelated vs FID

Figure 18. Pareto plot for concept flip on model SANA (Other axes axes)

(a) Unrelated vs CS *(b)* Unrelated vs FID

Figure 19. Pareto plot for concept flip on model SDXL (Other axes axes)

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I.2. Detailed results for LLM concept switching

In this section, in tab. 2,3,6,7,4,5 we provide detailed breakdown of scores for all β values and all concepts c_s, c_t, c_i. Pareto plots in sec. I.0.1 were created based on the scores provided in these tables.

Table 2. Model LLama2-7b, flipping from dogs to cats

		dogs		cats				wolves				pigs				cows				legislators		
method	strength	src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑
Steering	1.0	8.6	1.1	2.9	7.5	0.91	8.5	7.8	1.5	0.91	8.5	1.5	0.4	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	1.5	8.1	1.9	6.4	3.8	0.90	8.5	7.8	1.5	0.90	8.5	1.5	0.4	0.91	8.4	0.6	0.3	0.90	8.5	0.4	0.2	0.90
	2.0	5.9	3.9	7.1	2.8	0.89	8.4	7.8	1.4	0.90	8.5	1.5	0.4	0.90	8.4	0.7	0.3	0.90	8.5	0.3	0.2	0.90
	2.5	5.0	4.4	7.0	3.0	0.89	8.5	7.7	1.4	0.90	8.4	1.4	0.4	0.90	8.4	0.7	0.3	0.90	8.4	0.4	0.2	0.89
	3.0	4.8	4.6	6.6	2.8	0.89	8.5	7.7	1.4	0.90	8.4	1.4	0.4	0.90	8.4	0.7	0.3	0.90	8.5	0.3	0.2	0.89
	3.5	4.6	4.7	6.5	3.0	0.89	8.4	7.7	1.4	0.90	8.5	1.4	0.3	0.90	8.3	0.9	0.3	0.90	8.5	0.4	0.2	0.90
	4.0	4.6	4.7	6.5	2.9	0.89	8.4	7.7	1.5	0.90	8.4	1.4	0.4	0.90	8.2	0.9	0.3	0.90	8.4	0.4	0.2	0.89
	4.5	4.5	4.9	6.5	2.9	0.89	8.3	7.6	1.5	0.90	8.3	1.5	0.5	0.90	8.2	1.0	0.4	0.90	8.4	0.4	0.2	0.89
	5.0	4.4	4.9	6.5	2.7	0.88	8.3	7.6	1.5	0.89	8.2	1.5	0.6	0.89	7.9	1.2	0.5	0.89	8.2	0.4	0.2	0.89
LEACE	1.0	8.5	1.4	2.1	8.2	0.91	8.4	7.8	1.5	0.91	8.5	1.5	0.5	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	1.5	5.4	4.5	3.4	6.6	0.91	8.4	7.8	1.5	0.91	8.5	1.4	0.4	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.1	0.90
	2.0	4.0	5.5	4.9	4.8	0.91	8.4	7.7	1.7	0.91	8.5	1.4	0.4	0.91	8.4	0.6	0.3	0.91	8.5	0.3	0.2	0.90
	2.5	3.8	5.6	5.3	4.1	0.90	8.4	7.7	1.5	0.91	8.5	1.5	0.5	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	3.0	3.7	5.6	5.6	4.1	0.90	8.4	7.7	1.6	0.91	8.5	1.5	0.4	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	3.5	3.7	5.7	5.5	3.9	0.90	8.4	7.7	1.5	0.91	8.4	1.5	0.5	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	4.0	3.6	5.6	5.5	3.9	0.90	8.4	7.6	1.6	0.91	8.5	1.5	0.4	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	4.5	3.6	5.6	5.5	3.9	0.90	8.4	7.7	1.6	0.91	8.5	1.4	0.4	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.2	0.90
	5.0	3.6	5.5	5.4	3.9	0.90	8.4	7.7	1.6	0.91	8.4	1.5	0.5	0.91	8.3	0.7	0.3	0.91	8.5	0.3	0.1	0.90
MidSteer	1.0	8.0	1.8	1.6	8.6	0.92	8.4	7.8	1.6	0.91	8.5	1.4	0.4	0.91	8.4	0.7	0.3	0.91	8.5	0.3	0.1	0.91
	1.5	4.1	6.1	1.5	8.6	0.91	8.5	7.8	1.6	0.91	8.4	1.5	0.5	0.91	8.4	0.6	0.3	0.91	8.5	0.4	0.2	0.90
	2.0	2.6	7.7	1.5	8.6	0.91	8.4	7.7	1.7	0.91	8.5	1.5	0.5	0.91	8.4	0.6	0.3	0.91	8.5	0.3	0.2	0.90
	2.5	2.1	8.2	1.5	8.6	0.91	8.3	7.5	1.8	0.91	8.4	1.4	0.5	0.91	8.2	0.7	0.4	0.91	8.4	0.3	0.2	0.90
	3.0	1.9	8.4	1.4	8.7	0.91	7.9	7.0	2.2	0.91	8.3	1.5	0.8	0.91	8.0	0.7	0.8	0.91	8.5	0.3	0.2	0.90
	3.5	1.7	8.5	1.3	8.7	0.91	7.4	6.5	3.2	0.90	7.8	1.6	1.5	0.90	7.7	0.9	1.4	0.91	8.4	0.3	0.2	0.90
	4.0	1.6	8.5	1.4	8.6	0.90	7.3	5.6	4.2	0.90	7.3	1.7	2.3	0.90	6.8	1.1	2.3	0.90	8.4	0.4	0.4	0.90
	4.5	1.6	8.6	1.3	8.7	0.90	5.4	4.8	5.1	0.89	6.5	1.8	3.2	0.90	5.8	1.2	3.8	0.90	8.3	0.5	0.9	0.90
	5.0	1.6	8.6	1.4	8.7	0.90	4.6	4.1	5.8	0.89	5.5	2.0	4.4	0.89	4.6	1.2	4.8	0.89	8.1	0.6	1.4	0.90

Table 3. Model LLama2-7b, flipping from horses to motorcycles

		horses		motorcycles				cows				pigs				dogs				legislators		
method	strength	src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑
Steering	1.0	8.6	0.7	1.3	8.5	0.92	8.4	1.7	0.1	0.91	8.5	1.2	0.1	0.91	8.6	1.5	0.2	0.92	8.5	0.3	0.3	0.90
	1.5	6.5	2.9	1.4	8.5	0.92	8.4	1.7	0.1	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.2	0.91	8.5	0.3	0.3	0.90
	2.0	2.7	6.9	2.1	7.9	0.91	8.3	1.6	0.1	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.2	0.91	8.5	0.3	0.3	0.90
	2.5	2.6	7.2	3.7	5.5	0.91	8.1	1.4	0.2	0.90	8.3	1.2	0.1	0.91	8.5	1.5	0.2	0.91	8.5	0.3	0.3	0.90
	3.0	2.9	6.8	4.4	4.2	0.90	7.8	1.3	0.3	0.90	8.2	1.2	0.1	0.90	8.6	1.4	0.2	0.91	8.5	0.3	0.2	0.90
	3.5	3.0	6.5	4.7	3.6	0.90	7.2	1.3	0.3	0.90	8.1	1.1	0.1	0.90	8.5	1.3	0.2	0.91	8.4	0.3	0.3	0.90
	4.0	3.0	6.1	4.6	3.4	0.89	6.9	1.1	0.4	0.90	8.1	1.1	0.2	0.90	8.3	1.4	0.3	0.90	8.5	0.3	0.3	0.90
	4.5	3.1	5.8	5.0	3.2	0.89	6.4	1.1	0.4	0.89	7.9	1.1	0.2	0.90	8.2	1.4	0.3	0.90	8.4	0.4	0.4	0.90
	5.0	3.0	5.7	4.8	3.1	0.89	6.4	1.1	0.5	0.89	7.7	1.0	0.3	0.89	8.0	1.3	0.3	0.90	8.4	0.4	0.4	0.90
LEACE	1.0	8.5	0.7	1.2	8.5	0.92	8.4	1.7	0.1	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.1	0.92	8.5	0.3	0.3	0.90
	1.5	8.2	1.0	1.7	8.2	0.92	8.4	1.6	0.2	0.91	8.4	1.3	0.1	0.91	8.6	1.5	0.2	0.92	8.5	0.4	0.3	0.90
	2.0	5.4	3.5	4.0	5.4	0.91	8.3	1.7	0.2	0.91	8.4	1.3	0.1	0.91	8.6	1.5	0.2	0.92	8.5	0.3	0.2	0.90
	2.5	4.0	4.9	4.9	3.9	0.90	8.3	1.6	0.2	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.2	0.91	8.5	0.3	0.2	0.91
	3.0	3.7	5.2	5.5	3.2	0.90	8.2	1.5	0.2	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.2	0.91	8.5	0.3	0.3	0.90
	3.5	3.6	5.3	5.4	3.0	0.90	8.1	1.4	0.2	0.91	8.3	1.2	0.1	0.91	8.6	1.4	0.2	0.91	8.5	0.3	0.2	0.90
	4.0	3.5	5.5	5.5	2.9	0.90	8.0	1.3	0.2	0.90	8.3	1.1	0.1	0.91	8.6	1.5	0.2	0.91	8.5	0.4	0.3	0.90
	4.5	3.4	5.2	5.5	2.8	0.90	7.7	1.2	0.2	0.90	8.2	1.2	0.1	0.91	8.5	1.5	0.2	0.91	8.5	0.3	0.2	0.90
	5.0	3.4	5.3	5.6	2.9	0.90	7.6	1.3	0.3	0.90	8.2	1.1	0.1	0.91	8.5	1.5	0.2	0.91	8.5	0.4	0.3	0.90
MidSteer	1.0	8.6	0.7	1.2	8.5	0.92	8.4	1.6	0.1	0.91	8.5	1.2	0.1	0.91	8.6	1.4	0.2	0.92	8.5	0.3	0.3	0.90
	1.5	5.9	3.5	1.2	8.5	0.92	8.4	1.6	0.1	0.91	8.4	1.2	0.1	0.91	8.6	1.6	0.2	0.92	8.4	0.3	0.3	0.90
	2.0	2.6	7.2	1.2	8.5	0.92	8.3	1.5	0.1	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.2	0.91	8.4	0.3	0.3	0.90
	2.5	1.8	8.2	1.2	8.5	0.92	8.3	1.6	0.2	0.91	8.4	1.2	0.1	0.91	8.6	1.5	0.2	0.91	8.4	0.3	0.3	0.90
	3.0	1.7	8.4	1.2	8.5	0.92	8.3	1.6	0.2	0.91	8.2	1.1	0.1	0.91	8.6	1.6	0.2	0.91	8.5	0.3	0.3	0.90
	3.5	1.6	8.4	1.2	8.5	0.92	8.0	1.4	0.4	0.90	8.2	1.0	0.2	0.90	8.5	1.5	0.2	0.91	8.4	0.4	0.3	0.90
	4.0	1.6	8.4	1.2	8.5	0.91	7.6	1.3	0.7	0.90	8.0	1.1	0.4	0.90	8.4	1.4	0.2	0.91	8.4	0.3	0.3	0.90
	4.5	1.6	8.5	1.2	8.5	0.91	7.0	1.3	1.4	0.90	7.6	1.0	0.6	0.90	8.3	1.4	0.4	0.91	8.5	0.3	0.3	0.90
	5.0	1.4	8.5	1.2	8.5	0.91	6.1	1.2	2.2	0.89	7.3	0.9	0.9	0.90	8.2	1.4	0.5	0.90	8.4	0.3	0.3	0.90

Table 4. Model Qwen2.5-7b, flipping from dogs to cats

method	strength	dogs		cats				wolves				pigs				cows				legislators		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑
Steering	1.0	5.6	6.9	1.9	8.4	0.89	8.3	7.6	2.0	0.89	8.4	1.6	0.6	0.89	8.4	0.8	0.4	0.89	8.5	0.3	0.2	0.89
	2.0	3.2	7.5	2.2	7.8	0.88	7.6	6.4	3.7	0.88	8.1	1.6	1.9	0.88	7.9	1.1	1.8	0.89	8.4	0.5	0.9	0.89
	3.0	3.4	7.5	2.3	7.6	0.87	7.3	6.2	3.9	0.87	7.2	1.7	3.0	0.88	7.0	1.4	3.0	0.88	8.4	0.7	2.0	0.88
	4.0	3.0	7.1	2.4	7.2	0.86	7.2	6.2	3.7	0.87	7.4	1.6	2.2	0.87	7.1	1.3	2.8	0.87	8.3	0.6	1.6	0.88
	5.0	2.9	6.8	2.4	6.6	0.85	5.9	5.2	4.3	0.85	7.3	1.6	1.7	0.86	7.5	1.2	1.8	0.86	8.3	0.5	1.0	0.87
LEACE	1.0	8.7	1.0	1.8	8.5	0.89	8.3	7.7	1.6	0.89	8.4	1.6	0.4	0.89	8.4	0.9	0.3	0.89	8.5	0.3	0.2	0.89
	2.0	7.4	4.2	6.0	6.7	0.88	8.3	7.6	1.6	0.89	8.4	1.4	0.4	0.89	8.4	0.9	0.3	0.89	8.5	0.3	0.2	0.89
	3.0	6.3	6.7	7.1	5.5	0.88	8.3	7.6	1.7	0.89	8.4	1.6	0.4	0.89	8.4	0.9	0.3	0.89	8.5	0.3	0.2	0.89
	4.0	5.8	6.6	6.9	4.7	0.87	8.3	7.5	1.7	0.89	8.4	1.5	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.3	0.2	0.89
	5.0	5.3	6.5	6.7	4.3	0.87	8.3	7.6	1.8	0.89	8.4	1.5	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.4	0.2	0.89
MidSteer	1.0	8.7	1.0	1.7	8.5	0.89	8.3	7.6	1.6	0.89	8.5	1.5	0.5	0.89	8.4	0.8	0.3	0.89	8.5	0.4	0.2	0.89
	2.0	7.3	5.0	1.7	8.5	0.89	8.4	7.6	1.7	0.89	8.5	1.5	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.3	0.2	0.89
	3.0	5.7	7.7	1.7	8.5	0.89	8.3	7.5	2.0	0.89	8.4	1.4	0.6	0.89	8.4	0.8	0.5	0.89	8.5	0.3	0.2	0.89
	4.0	5.0	8.2	1.7	8.5	0.89	8.1	7.4	2.5	0.89	8.3	1.6	1.0	0.89	8.3	1.0	0.7	0.89	8.5	0.4	0.3	0.89
	5.0	4.3	8.3	1.7	8.5	0.89	7.8	6.9	3.2	0.89	8.3	1.7	1.1	0.89	8.2	1.1	1.0	0.89	8.4	0.4	0.3	0.89

Table 5. Model Qwen2.5-7b, flipping from horses to motorcycles

method	strength	horses		motorcycles				cows				pigs				dogs				legislators		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑
Steering	1.0	8.6	0.8	1.2	8.4	0.90	8.4	1.8	0.2	0.89	8.4	1.1	0.1	0.89	8.6	1.4	0.3	0.89	8.5	0.4	0.4	0.89
	2.0	4.3	5.7	5.7	4.4	0.87	8.2	1.6	0.3	0.89	8.3	0.9	0.1	0.88	8.6	1.3	0.2	0.89	8.5	0.4	0.3	0.89
	3.0	4.1	5.5	6.1	3.2	0.86	7.4	1.3	0.8	0.88	8.0	0.8	0.3	0.87	8.5	1.3	0.3	0.88	8.5	0.3	0.3	0.89
	4.0	4.2	5.2	6.2	2.8	0.86	6.6	1.5	1.3	0.86	7.5	0.9	0.4	0.87	8.1	1.3	0.4	0.88	8.4	0.3	0.3	0.89
	5.0	3.8	5.3	6.4	2.9	0.85	6.3	1.4	1.2	0.86	7.1	0.9	0.6	0.86	7.8	1.3	0.5	0.87	8.4	0.3	0.3	0.88
LEACE	1.0	8.6	0.7	1.0	8.4	0.90	8.4	1.9	0.2	0.89	8.4	1.2	0.1	0.89	8.7	1.5	0.2	0.89	8.5	0.4	0.3	0.89
	2.0	4.4	6.2	2.8	7.7	0.89	8.4	1.8	0.2	0.89	8.4	1.1	0.1	0.89	8.7	1.5	0.2	0.89	8.6	0.4	0.3	0.89
	3.0	3.1	6.7	5.3	5.0	0.88	8.3	1.7	0.2	0.89	8.4	1.0	0.1	0.89	8.7	1.4	0.2	0.89	8.5	0.4	0.3	0.89
	4.0	3.2	6.3	5.5	4.1	0.87	8.2	1.6	0.4	0.89	8.3	1.0	0.1	0.89	8.6	1.4	0.2	0.89	8.5	0.4	0.4	0.89
	5.0	3.2	6.1	5.6	3.8	0.87	7.9	1.5	0.7	0.88	8.3	0.9	0.2	0.88	8.6	1.3	0.2	0.89	8.5	0.4	0.4	0.89
MidSteer	1.0	8.6	0.8	0.9	8.5	0.90	8.3	1.9	0.2	0.89	8.4	1.1	0.1	0.89	8.7	1.5	0.2	0.89	8.5	0.3	0.3	0.89
	2.0	2.9	7.1	0.8	8.5	0.90	8.4	1.8	0.2	0.89	8.4	1.1	0.1	0.89	8.7	1.4	0.2	0.89	8.5	0.3	0.3	0.89
	3.0	1.4	8.2	0.9	8.5	0.90	8.2	1.7	0.3	0.89	8.4	1.0	0.2	0.89	8.6	1.4	0.3	0.89	8.5	0.3	0.3	0.89
	4.0	1.3	8.4	0.8	8.5	0.89	7.7	1.7	1.0	0.89	8.2	0.9	0.3	0.88	8.6	1.2	0.3	0.89	8.4	0.3	0.4	0.89
	5.0	1.2	8.4	0.9	8.6	0.90	6.3	1.5	2.8	0.88	7.8	1.0	1.0	0.88	8.2	1.4	0.8	0.89	8.5	0.3	0.4	0.89

Table 6. Model Qwen2.5-14b, flipping from dogs to cats

method	strength	dogs		cats				wolves				pigs				cows				legislators		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑
Steering	1.0	8.7	0.9	2.7	8.2	0.89	8.4	7.7	1.3	0.89	8.5	1.4	0.4	0.89	8.4	0.8	0.3	0.90	8.5	0.3	0.2	0.89
	2.0	7.8	4.5	7.3	4.9	0.86	8.4	7.7	1.4	0.89	8.5	1.4	0.4	0.89	8.4	0.8	0.2	0.89	8.5	0.3	0.2	0.89
	3.0	7.0	5.9	7.3	4.3	0.86	8.4	7.6	1.3	0.89	8.5	1.3	0.3	0.89	8.4	0.8	0.3	0.89	8.5	0.4	0.2	0.89
	4.0	6.8	6.2	7.2	4.6	0.86	8.4	7.6	1.3	0.89	8.5	1.3	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.4	0.2	0.89
	5.0	6.8	6.1	7.3	5.1	0.86	8.3	7.5	1.3	0.89	8.5	1.3	0.4	0.89	8.3	0.8	0.2	0.89	8.5	0.4	0.2	0.89
LEACE	1.0	8.7	1.0	1.9	8.4	0.89	8.4	7.7	1.3	0.89	8.5	1.5	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.3	0.2	0.89
	2.0	7.9	4.2	6.0	7.3	0.88	8.4	7.7	1.3	0.89	8.5	1.4	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.3	0.2	0.89
	3.0	6.9	6.5	7.0	5.4	0.86	8.4	7.6	1.4	0.89	8.5	1.3	0.3	0.89	8.4	0.8	0.3	0.90	8.5	0.3	0.1	0.89
	4.0	6.2	6.7	6.9	4.2	0.86	8.4	7.7	1.4	0.89	8.5	1.4	0.4	0.89	8.4	0.8	0.3	0.90	8.5	0.3	0.2	0.89
	5.0	6.0	6.6	6.9	3.7	0.85	8.4	7.7	1.4	0.89	8.4	1.4	0.4	0.89	8.4	0.8	0.2	0.89	8.5	0.3	0.2	0.89
MidSteer	1.0	8.7	1.2	1.8	8.5	0.89	8.4	7.7	1.4	0.89	8.5	1.5	0.4	0.89	8.5	0.8	0.3	0.89	8.5	0.3	0.1	0.89
	2.0	7.1	6.4	1.6	8.5	0.89	8.4	7.7	1.5	0.89	8.5	1.4	0.4	0.89	8.4	0.8	0.3	0.89	8.5	0.4	0.2	0.89
	3.0	4.8	7.8	1.6	8.6	0.89	8.4	7.6	1.8	0.89	8.4	1.5	0.5	0.89	8.4	0.7	0.3	0.89	8.5	0.3	0.2	0.89
	4.0	3.3	8.2	1.6	8.5	0.89	8.3	7.5	2.3	0.89	8.4	1.6	0.8	0.89	8.4	0.9	0.5	0.89	8.5	0.4	0.2	0.89
	5.0	2.1	8.3	1.6	8.6	0.89	8.1	7.0	2.9	0.89	8.3	1.8	1.2	0.89	8.3	0.9	0.7	0.89	8.5	0.4	0.3	0.89

Table 7. Model Qwen2.5-14b, flipping from horses to motorcycles

method	strength	horses		motorcycles				cows				pigs				dogs				legislators		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑	cs↑	src-cs↓	tgt-cs↓	bertp↑
Steering	1.0	8.7	0.7	1.2	8.6	0.90	8.4	1.7	0.2	0.89	8.4	1.1	0.1	0.89	8.7	1.4	0.2	0.90	8.5	0.3	0.3	0.89
	2.0	6.4	4.4	4.9	6.0	0.87	8.3	1.5	0.3	0.89	8.4	1.0	0.1	0.89	8.6	1.4	0.2	0.89	8.4	0.3	0.3	0.89
	3.0	5.9	5.0	6.9	2.9	0.84	7.9	1.4	0.5	0.88	8.4	0.9	0.2	0.88	8.6	1.3	0.2	0.89	8.5	0.3	0.3	0.89
	4.0	6.0	4.4	7.3	1.8	0.84	7.6	1.4	0.6	0.87	8.1	0.9	0.3	0.87	8.5	1.4	0.3	0.88	8.5	0.3	0.3	0.89
	5.0	5.5	4.3	7.4	1.6	0.83	7.5	1.3	0.5	0.86	7.9	0.9	0.3	0.86	8.3	1.4	0.3	0.88	8.5	0.3	0.3	0.89
LEACE	1.0	8.6	0.7	1.1	8.6	0.90	8.4	1.8	0.2	0.90	8.5	1.1	0.1	0.89	8.7	1.4	0.2	0.90	8.5	0.4	0.3	0.89
	2.0	6.4	4.6	3.8	7.5	0.88	8.4	1.6	0.2	0.89	8.4	1.0	0.1	0.89	8.7	1.3	0.2	0.90	8.5	0.4	0.4	0.89
	3.0	4.2	6.0	6.1	4.6	0.85	8.2	1.5	0.4	0.89	8.4	1.0	0.1	0.89	8.7	1.4	0.2	0.89	8.5	0.3	0.3	0.89
	4.0	4.2	6.1	6.6	3.5	0.84	7.9	1.5	0.6	0.89	8.3	1.0	0.2	0.88	8.7	1.4	0.3	0.89	8.5	0.4	0.4	0.89
	5.0	4.1	5.9	6.8	3.1	0.83	7.7	1.4	0.7	0.88	8.3	1.0	0.2	0.88	8.6	1.3	0.4	0.89	8.5	0.4	0.3	0.89
MidSteer	1.0	8.7	0.7	0.9	8.6	0.90	8.4	1.8	0.1	0.89	8.5	1.1	0.1	0.89	8.7	1.4	0.2	0.90	8.5	0.4	0.3	0.89
	2.0	3.9	6.5	0.9	8.6	0.90	8.4	1.6	0.2	0.89	8.4	1.1	0.1	0.89	8.7	1.3	0.2	0.90	8.5	0.3	0.3	0.89
	3.0	1.4	8.2	0.9	8.6	0.90	8.3	1.5	0.2	0.89	8.4	1.0	0.1	0.89	8.7	1.4	0.3	0.89	8.5	0.3	0.3	0.89
	4.0	1.2	8.2	0.9	8.6	0.90	8.3	1.5	0.2	0.89	8.4	1.0	0.2	0.89	8.7	1.3	0.3	0.89	8.4	0.4	0.4	0.89
	5.0	1.2	8.2	0.8	8.6	0.90	8.1	1.6	0.7	0.89	8.3	0.9	0.4	0.89	8.6	1.3	0.3	0.89	8.5	0.3	0.3	0.89

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I.3. Detailed results for for Diffusion Models concept switching

In this section, in tab. 11,12,8,9 we provide detailed breakdown of scores for all β values and all concepts c_s, c_t, c_i. Pareto plots in sec. I.0.1 were created based on the scores provided in these tables.

Table 8. Model SDXL, flipping from horse to motorcycle

method	strength	horse src-cs↓	tgt-cs↑	motorcycle src-cs↓	tgt-cs↑	fid↓	cow cs↑	src-cs↓	tgt-cs↓	fid↓	pig cs↑	src-cs↓	tgt-cs↓	fid↓	dog cs↑	src-cs↓	tgt-cs↓	fid↓	legislator cs↑	src-cs↓	tgt-cs↓	fid↓
No Steering	-	71.0	49.1	51.8	70.7	-	72.7	54.6	41.5	-	71.8	49.5	43.6	-	66.3	52.4	44.9	-	60.8	44.8	42.4	-
CASteer	1.0	70.0	50.8	52.6	71.3	27.8	72.3	54.4	42.4	21.9	71.8	49.0	43.8	13.3	66.2	52.0	45.0	20.0	60.9	44.8	42.5	16.3
	1.5	53.4	68.3	60.1	63.7	121.3	72.0	54.4	43.0	28.7	71.9	48.9	44.1	16.2	66.1	51.9	45.1	24.7	60.9	44.8	42.5	21.0
	2.0	52.1	69.5	68.3	52.9	212.4	70.9	54.4	44.9	42.7	71.9	48.9	44.4	18.9	66.1	51.8	45.4	28.6	60.9	44.8	42.6	24.6
	2.5	51.7	69.4	69.4	51.7	213.0	62.5	54.2	55.8	105.2	72.0	48.7	44.6	22.0	66.1	51.7	45.6	33.0	60.9	44.8	42.7	27.0
	3.0	51.4	69.1	69.9	50.9	210.0	52.4	53.2	66.2	186.9	72.0	48.5	44.9	25.8	66.0	51.6	45.7	37.2	60.9	44.9	42.7	29.7
	4.0	51.0	68.7	70.6	49.9	207.9	48.6	52.3	69.5	222.6	72.0	48.5	46.5	37.2	65.7	51.4	46.7	46.5	60.9	44.9	42.8	35.0
	5.0	50.7	68.5	70.9	49.5	207.4	47.8	51.8	69.6	231.6	70.5	49.1	50.6	63.7	64.3	51.4	49.0	61.6	61.0	45.1	43.0	39.0
LEACE	1.0	65.0	56.5	52.7	71.2	28.6	72.5	54.4	42.0	17.0	71.7	49.3	43.6	8.9	66.2	52.3	44.8	14.1	60.7	44.8	42.5	21.1
	1.5	52.1	68.6	57.1	67.0	84.6	72.2	54.4	42.3	21.3	71.7	49.3	43.7	10.9	66.2	52.3	44.8	17.7	60.7	44.8	42.5	24.9
	2.0	51.2	68.8	67.6	53.3	207.6	72.2	54.5	42.7	25.2	71.7	49.3	43.7	12.6	66.1	52.3	44.8	20.8	60.6	44.8	42.4	28.2
	2.5	50.8	68.5	69.0	51.5	213.3	71.9	54.5	43.1	30.0	71.7	49.4	43.7	14.0	66.1	52.3	44.8	22.6	60.6	44.9	42.5	31.0
	3.0	50.5	68.2	69.6	50.5	210.6	71.4	54.4	43.8	37.0	71.7	49.4	43.8	15.1	66.0	52.2	44.8	24.5	60.6	44.8	42.5	33.2
	4.0	50.2	68.0	70.4	49.6	206.7	64.6	54.2	52.6	85.7	71.8	49.4	43.9	17.2	66.0	52.2	44.7	28.1	60.5	44.8	42.6	37.3
	5.0	49.9	67.7	70.8	49.1	204.4	54.4	53.2	63.6	166.2	71.8	49.4	44.0	19.4	65.9	52.2	44.7	31.2	60.4	44.8	42.7	42.0
MidSteer	1.0	51.2	68.7	51.9	70.7	12.7	72.2	54.5	42.5	23.9	71.8	49.2	43.9	12.4	66.1	52.3	44.8	20.7	60.7	45.0	42.3	27.2
	1.5	50.4	68.1	51.9	70.7	15.1	71.6	54.6	43.5	34.5	71.9	49.1	44.1	15.2	66.1	52.2	44.8	25.3	60.5	45.1	42.3	32.3
	2.0	50.0	67.8	52.0	70.8	17.2	65.9	54.3	50.9	77.3	71.9	49.0	44.3	17.6	66.1	52.1	44.8	28.8	60.6	45.2	42.3	35.9
	2.5	49.5	67.4	52.0	70.7	18.6	55.1	53.3	62.6	162.3	71.9	49.0	44.5	20.2	66.0	52.1	44.8	32.2	60.5	45.5	42.4	39.8
	3.0	49.2	67.2	52.0	70.6	20.0	51.0	52.7	66.7	199.3	72.0	49.0	44.8	23.5	66.0	52.0	44.8	35.3	60.2	45.5	42.4	43.1
	4.0	48.8	67.2	52.0	70.5	22.9	48.4	51.9	68.7	222.5	72.1	49.0	45.5	29.5	65.8	51.9	44.9	41.4	59.7	46.0	42.7	49.9
	5.0	48.3	66.9	52.0	70.4	28.0	47.9	51.5	68.7	229.8	71.9	49.2	46.8	40.0	65.5	51.9	45.2	48.7	59.1	46.7	43.2	58.2

Table 9. Model SDXL, flipping from chihuahua to muffin

method	strength	chihuahua src-cs↓	tgt-cs↑	muffin src-cs↓	tgt-cs↑	fid↓	dog cs↑	src-cs↓	tgt-cs↓	fid↓	wolf cs↑	src-cs↓	tgt-cs↓	fid↓	cat cs↑	src-cs↓	tgt-cs↓	fid↓	legislator cs↑	src-cs↓	tgt-cs↓	fid↓
No Steering	-	75.9	54.6	42.6	68.2	-	66.3	57.9	52.5	-	71.8	52.7	45.6	-	67.5	53.4	54.2	-	60.8	42.6	40.1	-
CASteer	1.0	71.7	54.7	59.3	61.5	145.9	65.7	54.4	52.4	37.4	71.9	51.7	44.7	19.1	67.2	52.8	53.9	26.2	60.8	42.4	39.9	19.2
	1.5	47.0	61.0	66.5	57.3	211.5	65.2	53.1	52.4	53.3	71.8	51.2	44.3	24.4	67.1	52.4	53.8	33.8	60.8	42.3	39.6	23.2
	2.0	43.7	63.2	69.5	56.7	226.4	63.2	51.7	53.0	79.7	71.8	51.0	43.9	30.4	66.8	52.0	53.6	41.7	60.8	42.3	39.6	26.7
	2.5	42.3	63.8	71.5	56.3	241.1	55.2	48.9	55.5	140.5	71.5	50.6	43.6	36.8	66.3	51.7	53.6	53.8	60.9	42.3	39.6	29.8
	3.0	41.4	64.0	72.9	56.3	253.8	48.1	45.8	58.2	192.4	70.8	50.3	43.6	45.7	63.6	50.7	54.3	82.4	60.9	42.4	39.5	32.7
	4.0	40.1	64.3	74.8	56.2	276.0	44.2	43.5	60.3	226.9	65.6	49.0	45.6	96.6	52.5	47.2	57.0	168.7	60.9	42.4	39.4	38.0
	5.0	39.3	64.1	75.6	56.1	291.6	42.9	42.5	60.8	243.3	53.5	47.0	51.5	206.1	46.9	45.2	58.0	213.0	60.8	42.5	39.3	43.9
LEACE	1.0	67.1	55.7	60.4	60.6	160.6	66.0	55.8	52.4	25.4	72.0	52.1	45.3	11.9	67.5	53.2	54.1	17.5	60.8	42.5	40.2	20.0
	1.5	46.2	61.5	66.4	57.3	212.1	65.9	54.9	52.3	33.1	72.1	52.0	45.1	14.7	67.5	53.1	54.0	21.1	60.9	42.4	40.3	24.6
	2.0	42.8	63.3	69.3	56.9	227.7	65.8	54.2	52.3	40.3	72.1	51.8	44.9	16.9	67.6	53.0	53.9	24.6	60.9	42.3	40.3	28.1
	2.5	41.4	63.6	71.0	56.7	240.7	65.5	53.4	52.2	48.6	72.1	51.5	44.7	19.0	67.6	52.9	53.9	27.8	61.0	42.3	40.4	31.3
	3.0	40.6	63.9	72.3	56.7	250.8	65.1	52.5	52.3	57.1	72.2	51.4	44.6	21.5	67.6	52.7	53.8	30.4	61.0	42.5	40.5	34.0
	4.0	39.3	63.8	73.7	56.6	269.4	63.8	51.3	52.6	76.7	72.2	51.0	44.2	25.7	67.5	52.6	53.8	35.4	60.9	42.7	40.6	39.4
	5.0	38.5	63.7	74.6	56.5	282.5	60.3	49.7	53.7	104.1	72.2	50.7	44.0	29.8	67.4	52.4	53.7	41.1	61.0	43.0	41.1	43.4
MidSteer	1.0	44.3	62.5	42.0	68.3	23.9	65.9	54.7	52.4	35.1	72.2	51.7	44.9	16.9	67.6	53.0	54.1	22.7	60.8	42.5	40.1	23.9
	1.5	41.5	63.9	41.9	68.2	28.3	65.5	53.5	52.4	48.8	72.2	51.2	44.6	21.2	67.7	52.8	54.1	27.7	60.8	42.4	40.2	29.0
	2.0	39.8	64.0	41.7	68.2	32.2	64.5	52.2	52.7	65.6	72.2	50.8	44.1	25.4	67.7	52.6	54.1	31.6	60.9	42.5	40.4	32.5
	2.5	38.9	64.3	41.6	68.1	35.7	63.2	51.3	53.1	83.0	72.2	50.6	44.0	29.0	67.6	52.4	54.0	35.7	61.0	42.4	40.5	36.3
	3.0	38.0	64.2	41.5	68.0	39.5	59.4	49.7	54.4	109.8	72.2	50.3	43.8	33.4	67.5	52.2	54.0	40.1	60.9	42.4	40.7	39.4
	4.0	37.5	64.0	41.3	67.9	48.2	48.3	44.8	58.7	178.3	71.6	50.3	44.2	43.9	67.0	51.8	54.3	50.7	60.6	42.4	41.1	45.1
	5.0	37.9	63.6	41.3	67.5	58.9	43.4	42.2	61.1	209.8	70.2	50.4	44.8	63.1	64.5	50.7	54.5	69.6	60.4	42.5	41.5	51.4

Table 10. Model SDXL, flipping from snoopy to mickey

method	strength	snoopy src-cs↓	tgt-cs↑	mickey src-cs↓	tgt-cs↑	fid↓	pikachu cs↑	src-cs↓	tgt-cs↓	fid↓	spongebob cs↑	src-cs↓	tgt-cs↓	fid↓	dog cs↑	src-cs↓	tgt-cs↓	fid↓	legislator cs↑	src-cs↓	tgt-cs↓	fid↓
No Steering	-	74.3	58.7	56.0	73.1	-	72.6	41.3	51.2	-	75.1	49.0	52.5	-	66.3	56.1	52.0	-	60.8	41.6	45.0	-
CASteer	1.0	65.6	68.4	58.9	70.8	47.5	72.7	41.4	51.2	13.8	75.1	48.9	52.5	25.0	66.4	55.0	52.1	25.4	60.8	41.6	45.0	14.9
	1.5	59.8	71.2	61.7	68.6	59.6	72.7	41.4	51.2	17.1	75.1	48.9	52.6	29.7	66.3	54.4	52.1	33.9	60.7	41.6	45.0	18.4
	2.0	57.0	72.4	66.8	65.3	72.3	72.7	41.5	51.1	19.4	75.1	48.9	52.6	33.5	66.4	53.9	52.2	40.6	60.8	41.6	45.0	21.1
	2.5	55.4	72.7	69.6	61.3	83.9	72.7	41.6	51.2	21.2	75.0	48.8	52.5	36.5	66.4	53.3	52.2	48.5	60.9	41.6	45.0	23.3
	3.0	54.5	72.7	70.3	59.4	91.8	72.7	41.6	51.2	22.9	75.1	48.9	52.6	39.1	66.4	52.8	52.3	54.8	60.8	41.6	45.0	25.6
	4.0	53.0	71.9	70.8	57.4	106.3	72.7	41.7	51.2	25.9	75.2	48.7	52.6	43.3	66.4	52.1	52.6	66.5	60.7	41.6	45.0	28.9
	5.0	52.0	71.3	71.2	56.4	117.5	72.7	41.7	51.2	28.9	75.0	48.7	52.7	47.7	66.3	51.3	52.8	79.9	60.7	41.5	44.9	31.5
LEACE	1.0	65.9	67.9	58.8	70.6	50.0	72.8	41.4	51.1	18.5	75.0	48.9	52.5	33.5	66.3	55.8	52.0	18.6	60.9	41.7	45.1	22.2
	1.5	60.1	71.0	61.0	68.1	62.6	72.8	41.5	51.1	22.0	75.0	48.8	52.5	39.0	66.3	55.8	52.1	23.9	60.9	41.7	45.0	26.4
	2.0	57.5	72.2	64.3	64.6	77.0	72.9	41.5	51.1	24.5	75.1	48.9	52.5	44.5	66.3	55.6	52.1	28.4	60.9	41.9	45.1	29.7
	2.5	56.0	72.7	67.3	60.7	89.9	72.9	41.6	51.1	26.7	75.2	48.9	52.5	47.7	66.3	55.5	52.2	32.0	61.0	41.9	45.1	31.9
	3.0	55.1	72.7	68.2	58.2	101.5	73.0	41.7	51.2	29.1	75.2	48.8	52.5	51.3	66.4	55.4	52.3	35.7	61.0	41.9	45.1	34.8
	4.0	53.7	72.3	68.7	55.9	118.6	73.2	41.9	51.2	33.4	75.0	49.0	52.6	57.7	66.5	55.3	52.5	43.4	60.9	42.1	45.2	38.9
	5.0	53.0	72.0	69.5	52.3	134.6	73.4	42.4	51.4	37.6	74.8	49.1	52.7	64.0	66.5	55.2	52.7	50.0	60.9	42.3	45.3	42.2
MidSteer	1.0	59.7	71.0	55.5	72.8	30.1	72.8	41.3	51.3	19.0	74.7	48.9	52.6	36.5	66.2	55.9	52.1	20.4	60.9	41.7	45.0	24.5
	1.5	56.0	72.5	55.3	72.7	34.8	72.9	41.2	51.2	22.3	74.6	48.6	52.6	42.7	66.2	55.8	52.1	25.9	60.8	41.8	45.0	29.1
	2.0	54.5	72.7	55.0	72.4	38.9	72.9	41.3	51.3	25.3	74.5	48.6	52.6	46.8	66.3	55.6	52.1	30.6	60.7	42.0	45.1	32.6
	2.5	53.4	72.4	54.8	72.4	42.2	73.0	41.2	51.3	27.3	74.3	48.5	52.6	50.8	66.3	55.6	52.3	34.4	60.7	42.1	45.1	35.2
	3.0	52.5	71.8	54.7	72.2	44.7	73.1	41.3	51.3	30.0	74.2	48.5	52.7	55.2	66.4	55.5	52.5	38.3	60.7	42.1	45.3	37.6
	4.0	51.5	71.2	54.6	71.9	49.6	73.2	41.4	51.4	34.5	73.4	48.4	53.0	64.7	66.4	55.3	52.7	47.2	60.4	42.3	45.4	43.3
	5.0	51.0	70.4	54.4	71.5	55.1	73.3	41.3	51.4	39.1	72.7	48.6	53.4	72.9	66.5	55.1	52.9	55.3	60.3	42.5	45.6	48.8

Table 11. Model SANA, flipping from horse to motorcycle

method	strength	horse		motorcycle			cs↑	cow			cs↑	pig			cs↑	dog			cs↑	legislator		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓
No Steering	-	72.1	50.6	50.9	70.5	-	73.8	55.3	42.5	-	73.5	48.3	44.5	-	68.1	51.7	46.1	-	60.4	45.8	43.9	-
CASteer	1.0	71.0	52.0	52.2	71.3	48.1	73.6	54.8	43.0	22.1	73.8	48.0	44.8	13.8	68.1	51.6	46.2	15.7	60.2	46.0	44.3	15.9
	2.0	65.5	60.4	67.5	56.0	229.0	73.1	54.2	43.7	37.9	74.0	47.7	45.0	22.6	68.1	51.4	46.3	24.1	60.0	46.0	44.5	21.5
	3.0	54.9	68.7	69.5	51.8	234.6	72.3	54.0	45.0	55.8	74.2	47.4	45.3	30.5	68.1	51.3	46.5	32.2	59.7	46.3	44.9	25.9
	4.0	52.6	70.3	70.2	50.7	228.7	69.3	55.1	53.0	107.1	74.5	47.4	45.9	39.9	68.2	51.2	46.7	40.4	59.5	46.5	45.3	31.1
	5.0	51.8	71.0	70.5	50.3	224.9	62.3	54.8	61.7	167.0	74.7	47.5	46.9	48.9	68.2	51.2	47.0	51.3	59.3	46.7	45.8	36.8
LEACE	1.0	68.7	56.2	51.6	71.6	36.3	73.7	55.2	42.6	10.2	73.6	48.2	44.7	8.0	68.1	51.8	46.0	8.1	60.4	45.7	43.9	11.6
	2.0	53.1	70.7	58.7	69.4	125.0	73.7	55.2	42.8	16.2	73.7	48.1	44.7	12.6	68.1	51.8	46.0	13.1	60.5	45.7	43.8	17.0
	3.0	51.9	71.3	65.7	58.2	229.3	73.7	55.1	43.1	21.0	69.8	57.6	52.1	220.6	68.0	51.8	46.0	17.7	60.7	45.8	43.8	21.6
	4.0	51.9	71.1	67.4	53.7	242.8	73.7	55.0	43.3	25.9	73.9	48.0	44.9	20.4	68.0	51.8	46.0	21.5	55.1	52.2	51.9	294.6
	5.0	51.7	70.8	68.4	52.6	236.2	73.7	54.9	43.6	31.8	74.0	48.0	45.0	24.0	68.0	51.8	45.9	25.0	60.8	45.8	43.8	30.1
MidSteer	1.0	55.5	68.9	50.9	70.4	8.7	73.6	55.1	42.7	14.7	73.7	48.2	44.7	10.4	68.0	51.8	46.1	9.3	60.5	45.8	44.0	13.0
	2.0	51.7	71.1	50.9	70.4	11.7	73.6	55.0	43.1	23.2	73.9	48.1	44.8	16.5	68.0	51.7	46.1	15.0	60.6	45.9	44.0	19.1
	3.0	51.4	70.7	50.9	70.4	13.9	73.4	54.7	43.4	32.5	74.1	48.0	45.0	22.2	67.9	51.7	46.1	19.8	60.8	45.9	44.0	23.9
	4.0	51.4	70.9	50.9	70.4	15.9	73.1	54.5	43.9	43.8	74.3	48.1	45.3	27.4	67.9	51.6	46.1	24.3	60.8	45.9	44.1	28.9
	5.0	51.5	71.4	51.0	70.4	18.0	69.8	55.2	50.0	78.2	74.5	48.1	45.7	34.3	67.9	51.6	46.2	28.4	61.0	46.0	44.2	34.3

Table 12. Model SANA, flipping from chihuahua to muffin

method	strength	chihuahua		muffin			cs↑	dog			cs↑	wolf			cs↑	cat			cs↑	legislator		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓
No Steering	-	76.4	55.0	43.4	66.3	-	68.1	62.0	52.7	-	73.2	52.8	46.1	-	68.5	53.4	53.0	-	60.4	42.7	40.8	-
CASteer	1.0	75.8	55.8	45.3	65.6	46.6	73.6	58.4	52.9	39.4	73.1	52.7	45.8	16.3	68.3	52.8	53.5	24.5	60.2	42.8	41.0	13.8
	2.0	55.3	60.1	62.0	60.4	200.7	67.1	56.3	54.1	78.8	72.9	52.4	45.6	28.4	68.3	52.1	54.3	39.2	60.1	42.7	41.1	18.9
	3.0	45.4	60.5	60.0	47.6	278.5	50.6	49.0	59.2	198.9	72.4	52.4	45.8	46.2	67.9	51.0	55.0	61.7	59.9	42.8	41.3	23.4
	4.0	44.7	60.7	70.6	54.9	250.7	45.1	46.0	60.8	223.3	68.6	52.0	46.6	113.8	65.5	50.1	55.5	109.2	59.9	42.7	41.4	27.6
	5.0	44.1	60.7	72.1	54.2	260.7	43.4	45.3	61.1	229.3	58.9	51.1	50.3	216.2	56.9	48.0	57.6	179.1	59.9	42.7	41.6	31.3
LEACE	1.0	72.3	58.3	46.1	65.0	57.7	67.9	59.9	52.7	21.0	73.2	52.9	46.1	5.8	68.4	53.2	52.9	8.9	60.4	42.7	40.8	9.1
	2.0	48.9	61.4	59.8	63.0	185.8	67.8	58.3	52.8	35.1	73.2	52.9	46.1	9.4	68.4	53.1	53.0	13.6	60.4	42.5	40.8	13.7
	3.0	45.5	60.7	65.7	57.2	227.5	67.7	57.1	52.8	48.4	73.2	52.9	46.0	12.5	68.5	53.1	53.0	17.5	60.4	42.7	40.7	16.9
	4.0	44.6	60.5	68.1	55.8	240.4	67.7	56.3	53.0	60.8	73.2	52.9	46.0	15.4	68.5	53.0	53.0	21.0	60.4	42.7	40.7	19.4
	5.0	44.2	60.1	69.4	55.1	246.3	67.4	55.9	53.6	76.7	73.1	52.9	46.0	18.1	68.6	52.9	53.0	24.0	60.4	42.9	40.6	21.5
MidSteer	1.0	53.3	60.5	43.4	66.2	7.8	66.2	62.5	48.3	216.4	73.2	52.8	45.9	7.1	68.4	53.2	53.1	12.1	60.4	42.6	40.8	10.7
	2.0	44.4	58.7	43.4	66.0	13.1	67.6	56.8	53.0	57.9	73.1	52.8	45.8	11.2	68.4	52.9	53.1	17.8	60.4	42.5	40.8	15.8
	3.0	44.1	56.4	43.5	65.8	17.7	65.8	55.4	54.4	96.5	73.0	52.8	45.7	14.5	68.5	52.7	53.2	23.0	60.3	42.4	40.8	19.8
	4.0	45.0	53.8	43.6	65.6	22.3	56.4	51.6	56.3	154.4	73.0	52.9	45.6	17.3	68.5	52.5	53.2	27.2	60.2	42.5	40.8	22.9
	5.0	46.1	51.8	43.6	65.5	27.3	49.3	48.5	57.2	193.2	73.0	52.9	45.5	19.9	68.5	52.2	53.4	31.3	60.1	42.4	40.6	25.9

Table 13. Model SANA, flipping from snoopy to mickey

method	strength	snoopy		mickey			cs↑	pikachu			cs↑	spongebob			cs↑	dog			cs↑	legislator		
		src-cs↓	tgt-cs↑	src-cs↓	tgt-cs↑	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓		src-cs↓	tgt-cs↓	fid↓
No Steering	-	79.7	58.0	56.3	76.1	-	74.0	41.5	50.9	-	79.0	50.7	53.8	-	67.3	57.0	57.1	-	60.4	42.9	46.6	-
CASteer	1.0	77.9	61.7	57.8	76.3	31.8	74.1	41.5	50.8	8.6	79.0	50.7	53.8	14.5	68.1	54.0	52.0	218.8	60.3	43.0	46.8	12.5
	2.0	65.6	71.0	61.0	76.5	53.8	74.1	41.6	50.8	13.9	78.9	50.8	53.8	19.8	68.2	53.5	52.0	218.3	60.2	43.0	46.9	17.7
	3.0	55.8	72.3	71.7	74.8	78.8	74.2	41.7	50.7	18.6	78.9	50.8	53.8	23.9	68.1	53.2	52.1	218.3	60.1	43.0	46.8	21.4
	4.0	52.0	71.4	78.5	67.6	102.9	74.3	41.8	50.7	22.7	78.9	50.8	53.8	27.9	68.2	52.8	52.1	218.5	60.1	43.0	47.0	25.4
	5.0	50.0	70.4	79.8	61.9	121.0	74.5	42.0	50.7	26.7	79.0	50.8	53.8	31.8	68.2	52.4	52.2	218.0	60.1	43.0	47.2	28.5
LEACE	1.0	76.6	63.0	58.2	76.4	36.0	74.1	41.6	51.0	3.2	79.0	50.7	53.7	10.8	68.1	54.2	52.0	219.3	60.2	42.9	46.6	5.9
	2.0	62.6	71.3	57.9	72.9	170.9	74.1	41.7	51.0	5.5	78.9	50.7	53.7	15.1	68.0	54.0	52.0	220.0	60.2	42.9	46.6	9.6
	3.0	55.9	71.7	75.1	73.4	88.9	74.2	41.7	51.0	7.5	78.9	50.7	53.7	18.2	68.0	53.7	52.1	218.7	60.1	42.9	46.7	12.2
	4.0	52.9	68.8	79.2	66.4	111.0	74.2	41.8	51.1	9.5	78.9	50.8	53.8	21.1	68.0	53.6	52.1	218.8	60.1	42.9	46.7	14.6
	5.0	51.0	65.5	79.6	60.8	130.5	74.3	41.9	51.1	11.2	78.9	50.8	53.8	24.1	68.0	53.3	52.2	219.7	59.9	42.9	46.7	16.4
MidSteer	1.0	64.9	70.8	56.0	76.2	16.0	74.1	41.5	51.0	5.8	79.2	50.6	53.8	12.3	68.1	54.0	52.0	219.2	60.2	42.9	46.7	8.3
	2.0	53.5	71.1	55.6	76.2	25.2	74.2	41.5	51.1	10.0	79.2	50.6	53.9	17.4	68.1	53.6	52.1	218.2	60.1	42.9	46.7	12.4
	3.0	50.0	67.4	55.2	76.2	34.8	74.4	41.5	51.2	13.5	79.2	50.6	54.0	21.6	68.0	53.2	52.2	218.6	59.9	42.8	46.7	15.6
	4.0	48.4	62.6	54.9	76.4	45.4	74.5	41.6	51.3	16.8	79.2	50.5	54.0	25.8	67.9	52.6	52.3	216.6	59.8	42.8	46.7	17.8
	5.0	48.1	60.7	54.5	76.6	55.3	74.6	41.5	51.3	20.0	79.2	50.3	54.1	29.6	68.0	52.3	52.4	215.1	55.0	47.5	52.8	271.2

J. Concept erasure

In this section, we provide experiments for concept erasure. The reason for such is to show that unified MidSteer framework, that also includes erasure in case Z_2 is constant, performs favourably on a variety of tasks. Note that in case of erasure, both MidSteer and LEACE provide the same solutions, so we will label the results as LEACE / MidSteer in charts.

For concept erasure, we use evaluation setup seimilar to that of concept switching. For LLM, We test erasure of the concepts $c_s \in$ ("Horse", c_2 ="Dog"). Corresponding testing concepts are $t_i = \{c_i\}_{i=1}^5$: t_1 = ("Motorcycle", "Cow", "Dog", "Pig", "Legislator"), t_2 = ("Cat", "Cow", "Wolf", "Pig", "Legislator"). For Diffusion Models, We test erasure of the concepts $c_s \in$ ("Horse", c_2 ="Chichuahua"). Corresponding testing concepts are $t_i = \{c_i\}_{i=1}^5$: t_1 = ("Motorcycle", "Cow", "Dog", "Pig", "Legislator"), t_2 = ("Muffin", "Cat", "Dog", "Wolf", "Legislator"),

The setup for erasure is similar to those of main paper experiments (Sec. 5). The only difference is that there is no target concept (i.e. it is a dummy concept). We utilise similar pairs of prompts (c_1, c_2) as in switching experiments, with the goal of removing c_1.

Fig. 20b,20d,20a,20c present Pareto plots for concept erasure similar to that for concept switching in sec. 5. More precisely, we compare results on concept switching by applying vanilla steering, LEACE (which is equivalent to MidSteer in the case of erasure) with different values of β. We present results on LLama-2-7b and SDXL models aggregated for all three erase concepts. It can be clearly seen, that in each case, MidSteer achieves much better balance between level of concept switch between c1 and c2 and preservation of other concepts across different values of β.

Next, in sec. J.1, J.2 we provide detailed Pareto plots for each model, and in sec. J.3,J.4 we provide Tables with detailed breakdown of scores for all β values and all erased concepts.

(a) Erased concept score vs CS of unrelated concepts on Llama-2-7b model.

(b) Erased concept score vs 1 - BERT Precision on MMLU on Llama-2-7b model.

(c) Erased concept score vs CS of unrelated concepts on SDXL model.

(d) Erased concept score vs FID of unrelated concepts on SDXL model.

Figure 20. Pareto efficiency frontiers for concept *erasure* experiments with vanilla steering and LEACE / MidSteer highlighting different β.

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J.1. Pareto charts for LLM concept erasure

In this section, we provide more Pareto charts for LLM concept erasure. When erasing concept c_s, for each LLM model we provide 3 types of Pareto plots:

- 1 - BERT Precision score for unrelated concepts (horizontal axis) vs Concept Score (CS) for the erased c_s concept (vertical axis) (fig. 21b,22b,23a)

- 1 - BERT Precision score for MMLU (horizontal axis) vs Concept Score (CS) for the erased c_s concept (vertical axis) (fig. 21a,22a,23a)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Concept Score (CS) for the erased c_s concept (vertical axis) (fig. 21c,22c,23c)

In each case, we see clear superiority of LEACE/MidSteer over other steering approaches.

We additionally provide detailed breakdown of scores for all β values and all concepts c_s, c_i in the tables in sec. J.3

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 21. Pareto plot for concept erasure on model llama2-7b

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 22. Pareto plot for concept erasure on model qwen-14b

(a) MMLU vs BERTP

(b) Unrelated vs BERTP

(c) Unrelated vs CS

Figure 23. Pareto plot for concept erasure on model qwen-7b

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J.2. Pareto charts for image diffusion concept erasure

In this section, we provide more Pareto charts for LLM concept erasure. When erasing concept c_s, for each Diffusion model we provide 2 types of Pareto plots:

- FID score for unrelated concepts (horizontal axis) vs Concept Score (CS) for the erased c_s concept (vertical axis) (fig. 25b,25b)

- Average Concept Score (CS) for unrelated concepts c_i (horizontal axis) vs Concept Score (CS) for the erased c_s concept (vertical axis) (fig. 25a,24a)

In each case, we see clear superiority of LEACE/MidSteer over other steering approaches.

We additionally provide detailed breakdown of scores for all β values and all concepts c_s, c_i in the tables in sec. J.4

(a) Unrelated vs CS   *(b)* Unrelated vs FID

Figure 24. Pareto plot for concept erase on model sana

(a) Unrelated vs CS   *(b)* Unrelated vs FID

Figure 25. Pareto plot for concept erase on model sdxl

J.3. Results for LLM concept erasure

In this section, in tab. 14,15,18,19,18,17 we provide detailed breakdown of scores for all β values and all concepts c_s, c_i. Pareto plots in sec. J.1 were created based on the scores provided in these tables.

Table 14. Model LLama2-7b, erasure of horses

		horses	motorcycles		cows		pigs		dogs		legislators	
method	strength	cs ↓	cs ↑	bertp ↑	cs ↑	bertp ↑	cs ↑	bertp ↑	cs ↑	bertp ↑	cs ↑	bertp ↑
No Steering	-	8.6	8.5	-	8.4	-	8.5	-	8.7	-	8.4	-
Steering	1.0	8.6	8.5	0.91	8.4	0.90	8.4	0.90	8.6	0.90	8.5	0.89
	2.0	8.4	8.5	0.90	8.4	0.89	8.3	0.89	8.5	0.90	8.3	0.89
	3.0	1.5	3.4	0.80	2.4	0.78	1.4	0.78	2.9	0.79	2.6	0.79
	4.0	0.4	0.0	0.76	0.1	0.76	0.0	0.77	0.0	0.77	0.0	0.77
	5.0	1.0	0.0	0.76	0.1	0.77	0.0	0.77	0.0	0.77	0.0	0.77
LEACE	1.0	8.5	8.5	0.91	8.3	0.91	8.4	0.90	8.6	0.91	8.3	0.90
	2.0	5.0	8.3	0.89	7.3	0.87	7.4	0.88	8.0	0.89	7.8	0.88
	3.0	0.2	4.6	0.86	3.3	0.85	3.7	0.85	4.0	0.86	4.6	0.86
	4.0	0.0	1.0	0.82	0.2	0.81	0.2	0.81	0.4	0.82	1.1	0.82
	5.0	0.0	0.1	0.81	0.0	0.81	0.0	0.81	0.1	0.81	0.2	0.81

Table 15. Model LLama2-7b, erasure of dogs

		dogs	cats		wolves		cows		pigs		legislators	
method	strength	cs ↓	cs ↑	bertp ↑	cs ↑	bertp ↑	cs ↑	bertp ↑	cs ↑	bertp ↑	cs ↑	bertp ↑
No Steering	-	8.6	8.6	-	8.5	-	8.4	-	8.4	-	8.5	-
Steering	1.0	8.6	8.5	0.90	8.4	0.90	8.4	0.90	8.4	0.90	8.5	0.90
	2.0	8.5	8.5	0.90	8.3	0.89	8.3	0.89	8.3	0.89	8.4	0.89
	3.0	2.1	3.1	0.79	3.6	0.80	3.0	0.79	1.9	0.78	3.4	0.79
	4.0	0.1	0.0	0.76	0.1	0.76	0.0	0.75	0.0	0.75	0.0	0.76
	5.0	0.3	0.0	0.76	0.0	0.75	0.0	0.76	0.0	0.76	0.0	0.75
LEACE	1.0	8.5	8.5	0.91	8.4	0.91	8.3	0.91	8.4	0.91	8.4	0.90
	2.0	6.5	7.8	0.88	7.6	0.88	7.2	0.88	7.5	0.88	7.7	0.88
	3.0	1.3	3.8	0.86	4.2	0.86	3.4	0.85	3.7	0.85	4.6	0.86
	4.0	0.1	0.4	0.82	0.2	0.83	0.5	0.82	0.3	0.82	1.0	0.82
	5.0	0.0	0.1	0.81	0.1	0.82	0.1	0.82	0.1	0.81	0.1	0.81

Table 16. Model Qwen2.5-7b, erasure of horses

method	strength	horses cs ↓	motorcycles cs ↑	bertp ↑	cows cs ↑	bertp ↑	pigs cs ↑	bertp ↑	dogs cs ↑	bertp ↑	legislators cs ↑	bertp ↑
No Steering	-	8.7	8.6	-	8.4	-	8.4	-	8.7	-	8.5	-
Steering	1.0	8.6	8.5	0.89	8.4	0.88	8.4	0.88	8.7	0.88	8.6	0.88
	2.0	8.0	7.8	0.84	8.1	0.84	7.8	0.83	8.1	0.83	8.1	0.83
	3.0	3.6	4.0	0.72	5.1	0.73	4.5	0.73	4.7	0.73	3.9	0.72
	4.0	1.2	2.8	0.69	2.6	0.70	1.9	0.70	2.6	0.70	2.0	0.69
	5.0	0.6	1.0	0.70	0.7	0.70	0.3	0.70	0.7	0.70	0.9	0.69
LEACE	1.0	8.5	8.5	0.89	8.4	0.89	8.4	0.89	8.7	0.89	8.5	0.89
	2.0	6.9	8.5	0.89	8.4	0.88	8.4	0.88	8.7	0.88	8.5	0.88
	3.0	0.6	8.5	0.87	8.3	0.85	8.3	0.85	8.6	0.86	8.4	0.86
	4.0	0.2	8.3	0.85	8.1	0.83	8.1	0.82	8.4	0.83	8.2	0.83
	5.0	0.0	7.3	0.76	6.7	0.73	6.2	0.73	6.9	0.73	7.2	0.74

Table 17. Model Qwen2.5-7b, erasure of dogs

method	strength	dogs cs ↓	cats cs ↑	bertp ↑	wolves cs ↑	bertp ↑	cows cs ↑	bertp ↑	pigs cs ↑	bertp ↑	legislators cs ↑	bertp ↑
No Steering	-	8.7	8.5	-	8.3	-	8.4	-	8.4	-	8.5	-
Steering	1.0	8.6	8.5	0.88	8.3	0.88	8.4	0.88	8.4	0.88	8.5	0.88
	2.0	8.0	8.1	0.84	8.0	0.84	8.1	0.84	7.9	0.84	8.3	0.84
	3.0	3.9	5.0	0.74	4.6	0.74	5.4	0.75	4.8	0.75	4.6	0.75
	4.0	1.4	2.2	0.71	1.7	0.71	2.4	0.71	1.6	0.71	2.1	0.71
	5.0	0.3	0.7	0.71	0.4	0.71	0.7	0.71	0.4	0.72	0.8	0.71
LEACE	1.0	8.7	8.5	0.89	8.4	0.88	8.4	0.89	8.4	0.88	8.5	0.89
	2.0	8.7	8.5	0.88	8.3	0.87	8.4	0.88	8.4	0.87	8.5	0.88
	3.0	7.8	8.5	0.85	8.2	0.84	8.3	0.85	8.3	0.85	8.4	0.86
	4.0	3.2	8.2	0.83	7.7	0.79	8.1	0.83	7.9	0.81	8.2	0.82
	5.0	0.6	6.5	0.72	5.6	0.71	6.6	0.72	5.9	0.72	6.9	0.72

Table 18. Model Qwen2.5-14b, erasure of horses

method	strength	horses cs ↓	motorcycles cs ↑	bertp ↑	cows cs ↑	bertp ↑	pigs cs ↑	bertp ↑	dogs cs ↑	bertp ↑	legislators cs ↑	bertp ↑
No Steering	-	8.7	8.6	-	8.4	-	8.4	-	8.7	-	8.5	-
Steering	1.0	8.7	8.6	0.90	8.4	0.90	8.5	0.89	8.7	0.90	8.5	0.89
	2.0	8.7	8.6	0.89	8.4	0.89	8.5	0.89	8.7	0.89	8.5	0.89
	3.0	8.5	8.5	0.86	8.4	0.86	8.4	0.86	8.6	0.86	8.4	0.87
	4.0	2.9	4.2	0.78	5.0	0.78	5.0	0.78	4.3	0.79	4.3	0.79
	5.0	0.8	1.5	0.73	1.2	0.73	2.0	0.74	1.4	0.74	0.6	0.73
LEACE	1.0	8.7	8.6	0.90	8.4	0.89	8.4	0.88	8.7	0.89	8.5	0.88
	2.0	8.0	8.5	0.88	8.3	0.87	8.3	0.86	8.7	0.87	8.4	0.86
	3.0	3.0	8.5	0.85	8.3	0.84	8.3	0.83	8.6	0.84	8.3	0.83
	4.0	1.2	8.3	0.82	8.1	0.81	8.0	0.80	8.4	0.81	8.1	0.80
	5.0	0.3	7.8	0.79	7.5	0.79	7.5	0.78	7.9	0.79	7.7	0.79

Table 19. Model Qwen2.5-14b, erasure of dogs

method	strength	dogs cs ↓	cats cs ↑	bertp ↑	wolves cs ↑	bertp ↑	cows cs ↑	bertp ↑	pigs cs ↑	bertp ↑	legislators cs ↑	bertp ↑
No Steering	-	8.7	8.5	-	8.4	-	8.4	-	8.5	-	8.5	-
Steering	1.0	8.7	8.5	0.90	8.4	0.89	8.5	0.89	8.5	0.89	8.6	0.89
	2.0	8.7	8.5	0.89	8.4	0.88	8.4	0.89	8.5	0.89	8.5	0.89
	3.0	8.4	8.5	0.86	8.3	0.86	8.4	0.86	8.4	0.86	8.4	0.87
	4.0	3.5	3.7	0.79	3.1	0.77	4.2	0.78	4.2	0.78	3.4	0.79
	5.0	1.9	0.9	0.73	1.6	0.73	0.9	0.73	1.2	0.73	0.4	0.73
LEACE	1.0	8.7	8.5	0.89	8.4	0.88	8.4	0.89	8.4	0.89	8.5	0.89
	2.0	8.7	8.4	0.87	8.4	0.86	8.3	0.87	8.4	0.86	8.4	0.86
	3.0	7.7	8.4	0.84	8.2	0.83	8.3	0.84	8.2	0.83	8.3	0.83
	4.0	4.7	8.3	0.82	7.9	0.81	8.2	0.82	8.0	0.80	8.1	0.80
	5.0	2.3	7.9	0.79	7.5	0.79	7.7	0.80	7.5	0.78	7.7	0.79

J.4. Results for image diffusion concept erasure

In this section, in tab. 22,25,21,25 we provide detailed breakdown of scores for all β values and all concepts c_s, c_i. Pareto plots in sec. J.2 were created based on the scores provided in these tables.

Table 20. Model SDXL, erasure of snoopy

method	strength	snoopy cs ↓	mickey cs ↑	fid ↓	pikachu cs ↑	fid ↓	spongebob cs ↑	fid ↓	dog cs ↑	fid ↓	legislator cs ↑	fid ↓
No Steering	-	74.3	73.1	-	72.6	-	75.1	-	66.3	-	60.8	-
CASteer	1.0	55.8	70.1	54.9	72.5	30.3	73.9	50.9	66.2	30.6	60.9	22.6
	1.5	49.9	67.9	71.8	72.5	39.9	72.8	66.0	66.2	39.4	60.9	27.5
	2.0	47.0	65.2	90.5	72.6	51.2	71.0	85.2	66.2	48.1	60.8	31.7
	2.5	45.6	62.2	111.0	72.5	65.7	68.6	109.4	66.1	58.1	60.9	35.3
	3.0	45.3	58.8	132.1	72.2	83.7	65.3	138.2	66.2	68.0	60.8	38.7
	4.0	45.3	53.5	169.0	71.6	123.4	59.0	189.5	66.1	83.3	60.9	45.8
	5.0	45.9	50.7	195.3	69.3	153.0	55.7	218.2	65.6	99.9	61.0	52.9
LEACE	1.0	56.7	72.2	35.7	72.9	21.3	74.1	42.2	66.3	20.7	60.6	26.9
	1.5	51.2	71.7	42.3	73.0	25.8	73.7	50.1	66.3	26.5	60.5	32.5
	2.0	48.3	71.0	48.2	73.2	29.6	73.3	57.8	66.3	31.6	60.4	36.4
	2.5	46.5	70.3	53.9	73.3	33.0	72.8	66.5	66.4	36.5	60.2	41.3
	3.0	45.8	69.6	59.8	73.5	36.7	72.1	75.3	66.4	40.8	60.0	46.5
	4.0	45.8	67.9	72.2	73.7	44.8	70.8	91.8	66.5	49.5	59.4	56.1
	5.0	47.0	66.1	85.9	73.7	53.8	69.4	114.1	66.4	57.1	58.6	69.2

Table 21. Model SDXL, erasure of chihuahua

method	strength	chihuahua cs ↓	muffin cs ↑	fid ↓	dog cs ↑	fid ↓	wolf cs ↑	fid ↓	cat cs ↑	fid ↓	legislator cs ↑	fid ↓
No Steering	-	75.9	68.2	-	66.3	-	71.8	-	67.5	-	60.8	-
CASteer	1.0	54.6	68.1	19.7	65.0	58.2	72.5	25.9	67.0	35.2	60.9	22.7
	1.5	48.5	68.2	24.0	61.2	99.9	72.6	34.0	66.5	48.9	60.8	27.8
	2.0	47.6	68.0	27.3	54.1	155.5	72.6	44.1	64.6	69.0	60.9	31.9
	2.5	47.2	67.9	31.1	50.7	177.8	72.2	61.2	60.5	102.6	60.8	35.8
	3.0	46.9	67.9	34.6	49.7	187.7	70.0	96.2	55.8	141.5	60.8	39.4
	4.0	47.8	67.7	42.2	49.0	198.2	62.2	191.6	50.7	186.3	60.7	45.7
	5.0	49.7	67.6	49.5	48.9	209.3	57.8	228.4	49.4	201.5	60.7	52.1
LEACE	1.0	55.0	68.2	20.0	65.8	35.2	72.3	17.1	67.4	22.1	60.9	21.8
	1.5	48.5	68.1	25.0	65.5	47.6	72.5	21.3	67.3	27.1	60.8	27.0
	2.0	47.4	68.1	29.0	65.0	61.1	72.6	25.0	67.3	31.4	60.9	31.0
	2.5	47.0	68.2	32.6	64.1	74.8	72.8	28.6	67.2	35.1	60.8	34.2
	3.0	47.2	68.1	36.0	62.7	92.4	72.9	32.4	67.1	38.5	60.8	36.5
	4.0	48.6	68.0	42.3	57.6	131.4	73.1	39.4	66.9	45.1	60.7	41.9
	5.0	50.2	68.0	49.4	53.7	162.6	73.1	48.3	66.5	52.5	60.5	48.3

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Table 22. Model SDXL, erasure of horse

method	strength	horse cs ↓	motorcycle cs ↑	fid ↓	cow cs ↑	fid ↓	pig cs ↑	fid ↓	dog cs ↑	fid ↓	legislator cs ↑	fid ↓
No Steering	-	71.0	70.7	-	72.7	-	71.8	-	66.3	-	60.8	-
CASteer	1.0	59.3	70.7	12.9	71.9	30.1	71.8	20.8	65.9	29.9	61.0	21.3
	1.5	49.8	70.7	15.6	71.2	46.6	71.8	27.6	65.8	36.5	61.1	26.2
	2.0	48.3	70.6	17.4	69.2	79.8	71.9	36.5	65.7	42.2	61.0	30.3
	2.5	47.9	70.7	19.5	62.1	152.5	72.0	45.9	65.4	48.4	60.9	33.6
	3.0	47.8	70.7	21.7	54.7	211.1	72.0	60.1	65.0	54.7	60.9	37.0
	4.0	48.0	70.7	26.9	51.1	227.9	71.8	92.3	63.9	69.4	60.8	43.3
	5.0	49.3	70.8	35.1	50.4	238.4	69.8	138.4	62.2	89.4	60.6	49.4
LEACE	1.0	57.1	70.6	11.5	72.3	20.5	71.8	11.6	66.1	19.7	60.7	25.1
	1.5	49.6	70.6	14.0	72.0	26.0	71.9	14.1	66.1	23.7	60.5	29.6
	2.0	48.4	70.6	15.9	71.8	33.1	71.9	16.2	66.0	28.0	60.4	34.1
	2.5	48.0	70.6	17.5	71.4	39.9	72.0	17.3	66.1	30.9	60.3	38.2
	3.0	48.1	70.6	19.3	70.7	53.5	72.0	19.1	66.1	33.6	60.3	41.6
	4.0	48.4	70.5	23.0	64.5	115.1	72.1	23.1	66.1	38.6	59.9	49.2
	5.0	49.7	70.3	27.4	56.4	197.4	72.2	27.8	66.1	44.6	59.4	58.8

Table 23. Model SDXL, erasure of horse

method	strength	horse cs ↓	motorcycle cs ↑	fid ↓	cow cs ↑	fid ↓	pig cs ↑	fid ↓	dog cs ↑	fid ↓	legislator cs ↑	fid ↓
No Steering	-	72.1	70.5	-	73.8	-	73.5	-	68.1	-	60.4	-
CASteer	1.0	70.8	70.1	21.3	74.1	36.4	73.7	28.2	67.8	29.2	60.2	21.2
	2.0	52.2	70.9	45.3	72.0	93.0	74.1	49.3	67.4	44.2	59.8	36.3
	3.0	51.3	69.3	105.0	61.5	216.9	65.9	261.3	65.5	71.9	59.3	58.4
	4.0	56.7	62.3	186.2	59.0	242.8	67.3	175.3	62.5	118.4	58.9	90.1
	5.0	52.5	60.4	221.0	58.7	249.9	65.0	205.0	59.3	161.3	58.4	130.3
LEACE	1.0	71.1	70.5	7.5	73.8	14.4	73.4	11.4	68.0	9.2	60.4	11.1
	2.0	52.0	70.4	10.0	73.9	20.9	73.5	16.7	68.0	14.2	60.4	15.6
	3.0	49.7	70.3	12.2	74.0	25.8	73.5	21.4	67.9	18.4	60.3	19.1
	4.0	48.8	70.4	13.8	74.2	30.9	73.5	25.6	67.8	21.3	60.2	21.8
	5.0	53.7	70.3	15.2	74.1	36.2	73.6	29.7	67.8	24.4	60.1	24.2

Table 24. Model SANA, erasure of snoopy

method	strength	snoopy cs ↓	mickey cs ↑	fid ↓	pikachu cs ↑	fid ↓	spongebob cs ↑	fid ↓	dog cs ↑	fid ↓	legislator cs ↑	fid ↓
No Steering	-	79.7	76.1	-	74.0	-	79.0	-	68.1	-	60.4	-
CASteer	1.0	60.6	75.3	64.0	74.1	41.3	79.0	43.9	68.0	42.1	60.8	23.3
	2.0	46.0	70.5	168.3	74.3	103.6	74.7	146.6	68.0	74.3	61.1	38.2
	3.0	42.4	64.2	189.7	72.0	164.1	63.4	222.2	67.7	100.9	60.8	55.3
	4.0	40.9	58.5	202.0	62.6	204.2	55.7	258.7	66.8	116.9	60.4	74.8
	5.0	40.9	55.4	208.1	55.5	231.6	52.9	276.5	65.1	127.6	60.0	94.8
LEACE	1.0	57.0	76.1	18.2	74.1	6.7	79.0	13.9	68.1	17.3	60.3	9.1
	2.0	44.8	76.2	30.5	74.1	11.7	78.9	19.3	68.1	25.3	60.2	13.6
	3.0	41.6	76.1	49.0	74.2	16.4	75.2	200.5	68.0	32.2	60.2	16.8
	4.0	40.9	75.6	73.4	74.2	21.3	78.7	29.0	68.0	38.0	60.1	19.5
	5.0	41.4	74.4	109.4	74.2	26.1	78.7	34.1	68.1	44.1	60.0	22.0

Table 25. Model SANA, erasure of chihuahua

method	strength	chihuahua cs ↓	muffin cs ↑	fid ↓	dog cs ↑	fid ↓	wolf cs ↑	fid ↓	cat cs ↑	fid ↓	legislator cs ↑	fid ↓
No Steering	-	76.4	66.3	-	68.1	-	73.2	-	68.5	-	60.4	-
CASteer	1.0	75.6	66.6	19.8	67.4	49.4	73.6	25.6	68.3	32.5	55.3	268.2
	2.0	49.5	66.8	30.8	59.9	143.6	73.4	53.4	66.4	65.2	60.5	33.7
	3.0	48.9	67.1	44.1	52.6	214.4	64.6	265.3	58.6	151.2	60.4	48.6
	4.0	49.5	67.0	58.0	52.3	223.8	62.0	263.8	54.6	205.0	60.2	71.9
	5.0	50.4	66.3	76.7	53.2	233.5	59.8	282.5	53.6	220.9	59.8	102.3
LEACE	1.0	73.0	66.3	5.8	68.0	28.1	73.2	6.4	68.5	10.4	60.4	9.9
	2.0	49.3	66.2	9.7	67.8	47.1	73.3	9.7	68.5	16.0	60.4	14.7
	3.0	47.3	66.2	12.6	67.6	68.1	73.3	12.3	68.6	20.6	60.4	17.9
	4.0	47.2	66.1	15.2	67.1	88.7	73.3	14.7	68.6	24.6	60.3	20.9
	5.0	48.5	66.1	17.7	66.2	113.6	73.3	16.8	68.7	27.5	60.3	23.0