Fewer Lessons Make Greater Capabilities: An Adaptive Gradient-Aware Data Selection Method for LLMs

Abstract

Despite large language models (LLMs) have achieved impressive achievements across numerous tasks, supervised fine-tuning (SFT) remains essential for adapting these models to specialized domains. However, SFT for domain specialization can be resource-intensive and sometimes leads to a deterioration in performance over general capabilities due to catastrophic forgetting (CF). To address these issues, we propose a self-adaptive gradient-aware data selection approach (GrADS) for supervised fine-tuning of LLMs, which identifies effective subsets of training data by analyzing gradients obtained from a preliminary training phase. Specifically, we design self-guided criteria that leverage the magnitude and statistical distribution of gradients to prioritize examples that contribute the most to the model's learning process. This approach enables the acquisition of representative samples that enhance LLMs understanding of domain-specific tasks. Through extensive experimentation with various LLMs across diverse domains such as medicine, law, and finance, GrADS has demonstrated significant efficiency and cost-effectiveness. Notably, utilizing merely 5-10% of GrADS's selected data allows the LLMs to substantially outperform those fine-tuned on the entire dataset, thereby improving domain performance and mitigating catastrophic forgetting. We will release our code for GrADS later.

1 Introduction

Although LLMs have achieved remarkable performances in multiple tasks such as open-domain question-answering (Achiam et al., 2023; Yang et al., 2024a), logical inference (Nam et al., 2024), and long-context understanding (Chen et al., 2023c), supervised fine-tuning remains indispensable for domain-specific scenarios (Chen et al., 2023b; Yue et al., 2023; Xiong et al., 2023; Yang et al., 2023). However, incorporating domain-specific knowledge and concepts into the LLM

Figure 1: Pilot study: From left to right on the x-axis, we sort the CMedQA training data by gradients from largest to smallest, and select 10% by rank at each time, conducting 10 subsets, and predict their responses with untuned LLMs.

parameters could be rather costly. For the sake of efficiency promotion, some studies have shown that not all fine-tuning data are useful (Zhou et al., 2024), and removing some of the low-quality data instead can enhance model performance (Chen et al., 2023a; Li et al., 2023; Cao et al., 2023).

Besides, after domain-oriented fine-tuning, LLMs typically experience a decline in general capabilities, a phenomenon named Catastrophic Forgetting (CF) (Kaushik et al., 2021; Cossu et al., 2022). To address this issue, some practices use a mixture of domain-specific and general data (Luo et al., 2024), and other propose additional regularization or adaptation techniques (Ke, 2024; Diao et al., 2023). However, these approaches either increase the computational cost or compromise domain expertise to preserve more general capabilities (Lin et al., 2023).

To promote training efficiency and mitigate CF, we focus on leveraging LLMs to select high-quality subsets of data during training. This idea is grounded in the assumption that strong pre-trained LLMs have acquired sufficient general knowledge through enormous pre-training data, they should be capable of evaluating the quality of the data during fine-tuning, which is analogous to a well-

educated student being able to discern the quality of teaching materials in college. However, rather than employing the more widely applied train loss-based methods (Li et al., 2023), we opt for the **training gradients**, which represent the changes in the loss function with respect to model parameters, as the key metric for data selection. This choice is attributed to the lack of robustness of train loss on noisy data, which may lead the model to overemphasize outliers instead of focusing on more informative and representative instances.

Therefore, we conduct a pilot study that illustrates the performance of vanilla LLMs in predicting outputs for slices of training data, each selected from different gradient intervals (Figure 1). The results show that the LLMs have higher accuracy when predicting data characterized by smaller gradients (right side) as opposed to larger gradients (left side), which confirms the potential of gradients in training data selection.

To effectively identify crucial data from candidate training sets, we propose an adaptive **Gradient-Aware Data Selection** method, namely **GrADS**. First, the entire candidate data would be trained for one epoch with the LLMs to extract gradients for each training instance. Then, a self-adaptive criterion based on the gradient distribution is used to select a subset from the full data of expected volume. This method eschews reliance on expensive, more advanced LLMs like GPT-4 for inference (Chen et al., 2023a; Du et al., 2023; Liu et al., 2023) and the need for manual intervention in creating high-quality seed data (Pan et al., 2024; Ge et al., 2024), thereby offering a cost-effective and pragmatic solution.

To carefully examine the effectiveness of GrADS, we conducted comprehensive experiments on various LLMs including Qwen (Bai et al., 2023), ChatGLM (Zeng et al., 2023), and Llama (AI@Meta, 2024) scaled from 1.8B, around 7B, to 14B, within typical knowledge-intensive and high-demand application domains like medicine (Zhang et al., 2023), law (Cui et al., 2024), and finance (Zhang and Yang, 2023). GrADS exhibits superior advantages in terms of efficiency, cost-effectiveness, and performance. In summary, our contributions are three folds:

- To enhance domain specialization and mitigate CF in SFT, we introduce a novel self-adaptive Gradient-Aware Data Selection method (GrADS), which operates independently of manual intervention.

- Extensive experiments across different LLMs, model scales, and domains validate the efficacy of GrADS. Notably, utilizing only 5-10% of the data selected by GrADS enables LLMs to outperform those fine-tuned on the entire dataset.

- Moreover, GrADS substantially mitigates the catastrophic forgetting problem, achieving an outstanding balance between domain specialization and general capabilities.

2 Related Work

2.1 Data Selection

The recent research by Zhou et al.(Zhou et al., 2024) indicates that most of the knowledge in LLMs is acquired during the pre-training phase, and a limited amount of instruction data is often sufficient to activate the models' capacity to follow instructions. Similarly, through interactions with SoTA LLMs such as GPT-4, Chen et al. (Chen et al., 2023a) introduced ALPAGASUS, while Li et al. (Li et al., 2023) proposed the Instruction-Following Difficulty (IFD) metric to select samples with desired characteristics to enhance LLM instruction tuning. Liu et al. (Liu et al., 2023) and Du et al. (Du et al., 2023) further delineated a series of criteria including quality, complexity, diversity, coverage, and necessity to select data. Additionally, some researchers constructed expert-aligned datasets (Ge et al., 2024) or curated high-quality seed data (Pan et al., 2024). By facilitating interaction between the LLM and these datasets alongside the original data, they aim to obtain feedback on the quality of the data and improve the models' performance.

However, the majority of the previous works necessitate human intervention or the involvement of SoTA LLMs such as GPT-4 for data filtering, which require substantial API quota budgets or significant human labor investments. In contrast, our data selection method addresses efficiency and cost-effectiveness, which is easy to implement and substantially reduces labor and API expenditures.

2.2 Catastrophic Forgetting

Domain-specific fine-tuned LLMs (Ouyang et al., 2022; Chung et al., 2024) have demonstrated substantial potential for knowledge-based question-answering (QA), auxiliary consulting, and per-

sonalized solution recommendation in various fields, such as medicine(Zhang et al., 2023), finance(Zhang and Yang, 2023) and law (Cui et al., 2024). However, as expertise within the domain advances, CF emerges along with a sharp decline in the general capabilities that the LLM had previously mastered during pre-training (Kaushik et al., 2021; Cossu et al., 2022; Luo et al., 2024).

To address this issue, from a data-driven perspective, some researchers trained both domain data and general data to reduce the forgetting of general knowledge (Chen et al., 2020), while others proposed self-distillation (Yang et al., 2024b), which guides the generation of task data through the model itself to minimize the disparity between the information distribution of the generated data and that of the initial model. On the other hand, from the model's perspective, some established end-to-end alignment of modules through shared attention mechanisms (Zhao et al., 2024), while others modified the adapter architecture by reducing the interference caused by fine-tuning tasks in different orthogonal low-rank subspaces (Wang et al., 2023) or by self-regulating the adapter's attention to different parts of the context (Liu et al., 2024).

3 Backgrounds

The **Embedding** layer and the **language model head (LM Head)** layer of LLMs play critical roles in capturing the semantics of input tokens and generating meaningful predictions, respectively. The Embedding layer maps each discrete token into a high-dimensional vector space, where the vectors capture the semantic and syntactic properties of the words they represent. On the other hand, the LM Head layer converts the final hidden states produced by the model into a probability distribution over the vocabulary and directly influences the model's accuracy in predicting the next token.

During back-propagation, the gradients computed for the Embedding layer indicate how the word vectors need to be updated to optimize the discriminative and context-aware token representations, which enhance the model's overall performance. Therefore, instances with larger gradients for the Embedding layer could imply the existence of unfamiliar information the model attempts to learn, while those with smaller gradients are rather stable and already well-presented.

In contrast, the gradients computed for the LM Head provide insights into how the model should adjust its parameters to minimize the prediction error in the decoding process, thereby improving its predictive capabilities. High-magnitude gradients show uncertainty and lack of confidence in the model's prediction, which reveals potential high complexity and perplexity of the data, whereas low-gradient tokens are well-understood and straight forward to the model.

With the insight that gradients help discover characteristics of each training instance, we raise a deduction that in a given training dataset D, the actual "effective" data points D' should depend on $feature\ importance\ (F)$, $information\ values$ (I), and $complexity\ (C)$:

$$D' \propto f(F, I, C) \qquad (1)$$

4 GrADS: Gradient-Aware Data Selection

In this section, we introduce GrADS, which can adaptively select beneficial subsets of the data through gradient distribution, integrating both the Embedding layer gradients and LM Head gradients. The method consists of two major steps: gradient extraction from LLM learning, and data selection with a self-adaptive criterion. Specifically, in the first step, we obtain the integrated gradients of each training instance by conducting a single-epoch SFT. Subsequently, we select desired subsets of data based on an adaptive criterion derived from the gradient distribution. Our model architecture is illustrated in Figure 2.

4.1 Gradient Extraction from LLM Learning

Given the entire training data $\mathbf{D}$, we denote the input tokens of each data point $\mathbf{x} = \{x_1, x_2, \ldots, x_T\} \in \mathbb{R}^T$, where T is the length of the input sequence. In the Transformer embedding layer, tokens are mapped to the corresponding embedding vectors $\mathbf{e}$:

$$\mathbf{e} = Embed(\mathbf{x}) \qquad (2)$$

where $\mathbf{e} = \{\mathbf{e}_1, \mathbf{e}_2, \ldots, \mathbf{e}_T\} \in \mathbb{R}^{T*d}$ is the combined vector for input tokens, d denoting the dimension.

Then the embedded vectors $\mathbf{e}$ are passed through multiple Transformer layers, and produce the final hidden states $\mathbf{h} \in \mathbb{R}^{T*d}$ for all training instances.

$$\mathbf{h} = Transformer(\mathbf{e}) \qquad (3)$$

Figure 2: The illustration of the GrADS method.

The LM Head layer takes the final hidden states **h** and generates the probability distribution over the vocabulary for predicting the next token:

$$\mathbf{o} = softmax(LMHead(\mathbf{h})) \qquad (4)$$

where $\mathbf{o} \in \mathbb{R}^{T*V}$ is the probability distribution over the vocabulary for the next token, and V is the size of the vocabulary.

Given a standard cross entropy loss function $\mathcal{L}(\cdot)$ that measures the difference between the model's predictions and the ground truth, the gradients of the loss for the embeddings can be obtained in the forward pass by:

$$\mathbf{g}_{\text{Emb}} = \nabla_\mathbf{e}\mathcal{L} = \left(\frac{\partial \mathbf{h}}{\partial \mathbf{e}}\right)^\top \nabla_\mathbf{h}\mathcal{L} \qquad (5)$$

where $\nabla_\mathbf{h}\mathcal{L}$ is the gradient of the loss for the hidden state **h** and $\frac{\partial \mathbf{h}}{\partial \mathbf{e}}$ represents the Jacobian matrix ([Wilamowski et al., 2008](#)) of the hidden state for the embedding. The gradients $\nabla_\mathbf{h}\mathcal{L}$ can be obtained through backpropagation through the model.

Similarly, we can compute the gradients for the LM Head layer during the back-propagation step:

$$\mathbf{g}_{\text{LM}} = \nabla_\mathbf{o}\mathcal{L} = \frac{\partial \mathcal{L}}{\partial \mathbf{o}} \qquad (6)$$

After extracting the gradients for the input tokens in the Embedding and LM Head layers, we exclude special tokens like $[CLS]$, $[SEP]$, $[PAD]$, $[UNK]$, etc. Since the gradients of the Embedding layer reflect the LLMs' understanding of the input sequence whereas the gradients of the LM Head layer reflect the LLMs' certainty of the output tokens, we take all input tokens for the Embedding layer and only the output token for the LM Head layer into account. Meanwhile, to rule out the impact of input sequence length, we average the token-wise gradients for each training instance. Thus, the combined instance-level gradients for two layers are denoted as $\mathbf{G}_{\text{Emb}}^i$ and $\mathbf{G}_{\text{LM}}^i$, where $\mathbf{i} = \{\mathbf{1}, \mathbf{2}, \dots, \mathbf{K}\}$ and $\mathbf{K}$ being the size of the data $\mathbf{D}$.

Thereafter, we integrate these gradients by adding $\mathbf{G}_{\text{Emb}}$ and $\mathbf{G}_{\text{LM}}$ linearly to derive a GrADS gradient vector $\mathbf{G}_{\text{GrADS}}$, which ultimately serves as the metric for selecting training instances

$$G_{\text{GrADS}} = G_{\text{Emb}} + G_{\text{LM}} \qquad (7)$$

4.2 Self-Adaptive Criterion for Data Selection

To select the subset of training instances that best represents domain knowledge, we introduce the probability density function (PDF) to depict the distribution feature of $\mathbf{G}_{\text{GrADS}}$. The PDF uses a non-parametric method, such as kernel density estimation (KDE) to represent the density of $\mathbf{G}_{\text{GrADS}}$ at different values. A higher density signifies that there are more instances whose $\mathbf{G}_{\text{GrADS}}$ fall close, indicating instances more likely to share common domain characteristics. Just as one can quickly gain an understanding of a domain by reading its classical papers, prioritizing the fine-tuning process on these typical training instances can also enable LLMs to learn domain knowledge more efficiently and effectively.

Therefore, we compute the PDF function of

G_{GrADS} gradients:

$$F_{\text{GrADS}} = PDF(G_{\text{GrADS}}) \tag{8}$$

where $\mathbf{F}_{\text{GrADS}} \in \mathbb{R}^{\mathbf{K}}$ implies the domain representativeness of the instance. Finally, an effectively refined subset of the full data $\mathbf{D}$ can be obtained by calculating the Top N% of instances with the highest PDF values:

$$D^{'} = \text{quantile}\left(F_{\text{GrADS}}, N/100\right) \tag{9}$$

GrADS operates in a self-adaptive manner, as it selects the most probable training instances regardless of the gradient distribution, whether it is left-skewed, right-skewed, normal, bimodal, or otherwise. The selected subset $\mathbf{D}^{'}$ always has the highest $\mathbf{F}_{\text{GrADS}}$, thereby best capturing the critical characteristics of the domain. Also, $\mathbf{D}^{'}$ carries crucial, informative, and reasonably challenging instances that guide the model to learn and acquire domain expertise. Nonetheless, as Figure 2 illustrates, training instances with low $\mathbf{G}_{\text{GrADS}}$ and low $\mathbf{F}_{\text{GrADS}}$ are typically less representative, often characterized as trivial, well-learned, or simple, and thus fail to "surprise" the model with already-known knowledge. In contrast, instances with high $\mathbf{G}_{\text{GrADS}}$ and low $\mathbf{F}_{\text{GrADS}}$ are often noisy, confusing, or overly difficult, and they might introduce misleading information that contradicts the model's established common sense. GrADS excludes these suboptimal instances by automatically adapting to the distribution of domains.

5 Experiments

In this section, we present the experiment results to verify the effectiveness of GrADS. Apart from the main results, we also try to validate the generalizability of GrADS by addressing the following research questions (RQs):(1) Generalizability: Can the GrADS approach be scaled up to larger LLMs and applied across different models? (2) Robustness: Do GrADS consistently perform well with smaller subsets selected?

5.1 Datasets

Our study incorporates three domains-specific datasets from three typical domains: CMedQA (Zhang et al., 2018) for medicine, LawQA (Huang et al., 2023b) for law, and FinQA [1] for finance. Specifically, CMedQA includes 20k instances for

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[1] https://aistudio.baidu.com/datasetdetail/34744

training and 0.5k instances for testing. Also, for LawQA, we use the law article-based QA pairs from the Lawyer-LLama project (Huang et al., 2023a) and split 1.6k and 0.4k data for training and testing, respectively. Since FinQA's QA pairs are sourced from webpages, we retained only those designated as "best answers" in the original dataset. Additionally, we removed all duplicate questions and answers, resulting in a training set of 40k and a testing set of 2k.

5.2 Evaluation Metrics

We follow Pan et al. (Pan et al., 2024) to include BLEU (Papineni et al., 2002), along with two other widely applied metrics ROUGE-L (Lin, 2004) and METEOR (Banerjee and Lavie, 2005) to evaluate the response quality. In addition, we employed GPT-4o to score on a 1-5 scale of the response quality. We also provide the consistency test between GPT-4o evaluation and human judgement in Appendix A.

Furthermore, we delve into the CF problem in general capabilities following supervised fine-tuning on domain-specific instances. To this end, we follow the work of Liu et al. (Liu et al., 2024) and collect C-Eval (Huang et al., 2023c) for common sense understanding, GSM8K (Yu et al., 2023) for mathematics, ALPACA (Peng et al., 2023) for instruction following and SafetyPrompts (Sun et al., 2023) for instruction attack and typical safety scenarios awareness. The details of metrics selection regarding the CF problem can be found in Appendix B.

5.3 Baselines

To validate GrADS' efficiency across different model scales and model architectures, we selected the 1.8B, 7B, and 14B chat models from Qwen1.5 (Bai et al., 2023) as our base LLMs. We also select ChatGLM3-6B-Chat (Zeng et al., 2023) and Llama-3-8B-Instruct (AI@Meta, 2024) which are widely used in Chinese and English contexts, respectively. While GrADS permits any proportion of data selection from the original training sets, we uniformly select half in the main experiments for simplicity, while exploring varying proportions in RQ2.

We compare the LLMs fine-tuned with 50% of the data selected by GrADS (*grads50*) with the following baseline models: the base LLMs without SFT (*base*), the LLMs fine-tuned with full data (*all*) and the half the data selected randomly (*rdn50*).

Base Model	Method	CMedQA			LawQA			FinQA		
		BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR
Qwen1.5-1.8B	base	1.547	8.228	13.169	9.860	19.178	24.505	1.888	7.911	12.061
	all	3.238	15.936	11.290	15.066	25.312	25.572	9.048	**21.914**	16.945
	rdn50	3.620	16.128	11.215	14.090	24.851	24.149	8.039	20.828	15.63
	top50	2.630	15.216	9.409	12.287	24.297	21.423	5.724	18.667	12.381
	tail50	_4.265_	16.287	**13.894**	_18.175_	25.050	_31.946_	_10.903_	21.236	**21.450**
	mid50	3.859	_17.006_	12.666	15.809	**25.763**	26.62	8.655	21.447	17.398
	grads50	**4.549**	**17.228**	_13.926_	**18.357**	_25.418_	**32.489**	**11.133**	_21.645_	_21.020_
Qwen1.5-7B	base	2.627	12.180	10.860	9.066	20.050	21.392	3.188	11.194	14.669
	all	3.414	16.347	11.274	15.190	25.803	25.272	9.020	22.074	16.877
	rdn50	3.143	16.272	11.055	14.856	25.198	24.799	8.685	21.614	16.277
	top50	2.768	15.236	9.594	13.273	24.078	22.758	6.252	19.507	13.116
	tail50	_4.466_	16.464	_14.119_	_19.131_	**26.074**	_32.833_	_11.978_	_22.600_	22.769
	mid50	4.071	_17.029_	13.128	16.683	25.806	27.699	9.429	22.304	18.429
	grads50	**4.871**	**17.469**	**14.390**	**19.179**	_26.012_	**32.975**	**12.362**	**22.816**	**22.872**
ChatGLM3-6B	base	2.568	11.274	15.634	7.966	19.733	19.011	3.174	11.437	14.926
	all	3.899	16.418	15.811	15.837	_26.167_	26.497	10.353	20.891	22.899
	rdn50	3.611	15.814	15.492	15.363	25.674	25.884	10.116	20.550	22.203
	top50	2.632	14.474	13.314	13.807	24.792	24.021	7.425	19.978	18.998
	tail50	_4.643_	16.502	**17.834**	_18.838_	25.267	_32.802_	_11.881_	21.853	**26.440**
	mid50	4.430	**16.803**	16.817	17.485	**26.402**	29.035	10.177	_22.214_	23.002
	grads50	**4.898**	_16.727_	_17.272_	**19.075**	26.057	**32.919**	**12.054**	**22.271**	_26.347_
Llama3-8B	base	0.026	0.249	0.291	0.259	1.905	2.164	0.178	1.293	1.225
	all	3.432	16.031	10.897	15.272	_24.301_	25.033	9.116	_21.190_	16.913
	rdn50	2.964	15.335	10.360	14.451	23.671	24.368	8.312	20.766	15.980
	top50	2.500	14.399	8.664	12.262	22.973	21.768	5.814	18.210	12.328
	tail50	_3.738_	16.130	_12.854_	_17.328_	24.255	_31.408_	_10.988_	20.526	_21.425_
	mid50	3.483	**16.809**	12.530	15.389	24.142	26.277	8.943	20.919	17.389
	grads50	**3.872**	_16.354_	**13.098**	**17.739**	**24.610**	**31.601**	**11.199**	**21.778**	**21.507**

Table 1: Main Results.

Base Model	Method	CMedQA	LawQA	FinQA
Qwen1.5-1.8B	all	2.535	3.010	2.530
	grads	**2.868**	**3.464**	**2.806**
Qwen1.5-7B	all	2.622	3.327	2.671
	grads50	**2.988**	**3.971**	**3.179**
ChatGLM3-6B	all	2.576	3.174	2.727
	grads	**3.074**	**3.864**	**3.274**
Llama3-8B	all	2.449	3.035	2.418
	grads50	**2.665**	**3.625**	**2.855**

Table 2: Results by GPT-4o's evaluation, scores range from 1-5.

Additionally, as in GrADS we use sorted gradients, we also add LLMs trained with data from the smallest half (*tail50*), the largest half (*top50*), the middle half (*mid50*) as baseline models. Note that all results reported are average of three runs.

5.4 Main Results

5.4.1 Domain Performance

Results in Table 1 and Table 2 show that **fine-tuning LLMs with the data selected by GrADS has a significant advantage over the full data and randomly selected data in enhancing models' domain performances.** Table 1 demonstrates that (1) GrADS obtained the best or second-best performance over almost all domains and LLMs in the experiments, and demonstrated very strong robustness. Notably, with only half the data, GrADS has achieved remarkable improvements on BLEU and METEOR metrics, registering an average gains of 25.48% and 24.18% respectively, compared to LLMs fine-tuned on the entire dataset. Considering that the question-answering tasks require domain expertise, the higher BLEU, and METEOR indicate that the LLMs advance in both accuracy and richness of professional expression. Apart from that, the improvement on ROUGE-L also indicates that the LLMs have considerable enhancements in terms of long-sequence content coherence and comprehensive information coverage.

Besides, we found that (2) **GrADS has attention on the domain characteristics when selecting data**. When we sort all training instances by gradient magnitude in ascending order, the average percentiles of selected data for CMedQA,

Domain	Method	C-Eval		GSM8k			ALPACA		Safety	Attack
		Acc.	Instruct	Acc.	BLEU	ROUGE	BLEU	ROUGE	Acc.	Acc.
	base	65.189	87.427	55.497	14.967	29.207	15.097	27.529	43.807	51.365
CMedQA	all	11.285	22.674	1.895	2.286	12.809	1.815	12.252	13.594	22.007
	rdn50	14.628	**35.107**	2.880	3.006	13.410	2.443	13.305	14.446	28.503
	grads50	**21.345**	33.293	**4.700**	**5.572**	**18.082**	**3.340**	**15.626**	**24.560**	**33.656**
LawQA	all	24.201	8.067	15.466	9.985	20.917	8.987	20.055	23.571	39.961
	rdn50	30.305	11.846	26.384	10.772	22.049	9.486	19.889	29.378	44.938
	grads50	**31.206**	**12.762**	**26.547**	**10.913**	**22.368**	**9.506**	**20.145**	**32.596**	**48.452**
FinQA	all	10.756	21.802	0.758	0.855	8.266	0.895	8.864	6.480	10.921
	rdn50	15.77	28.488	0.758	0.795	7.665	1.073	9.563	9.688	15.141
	grads50	**25.250**	**47.359**	**1.373**	**2.416**	**10.838**	**1.873**	**10.974**	**19.139**	**25.889**

Table 3: Catastrophic forgetting results of Qwen1.5-7B.

Method	Qwen1.5-1.8B Gradients			Qwen1.5-14B Gradients		
	BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR
base	3.308	11.443	14.954	3.308	11.443	14.954
all	10.286	23.541	18.553	10.286	23.541	18.553
rdn50	9.464	22.685	17.527	9.464	22.685	17.527
top50	6.217	19.385	13.243	6.325	19.665	13.341
tail50	12.379	22.777	23.178	12.298	22.860	23.262
mid50	10.245	23.173	19.341	10.696	23.472	20.021
grads50	**12.664**	**23.635**	23.529	**12.696**	**23.954**	23.742

Table 4: The left side selects data via Qwen1.5-1.8B gradients and fine-tuned on Qwen1.5-14B. The right side is selected via Qwen1.5-14B and fine-tuned on Qwen1.5-14B. The *base*, *all* and *rdn50* are all based on Qwen1.5-14B, so they share the same results.

LawQA, and FinQA are 35.8%, 27.4%, and 28.9%, respectively. In more specialized domains such as medicine where all base LLMs perform poorly, GrADS inclines to select instances with larger gradients, i.e., instances with more unfamiliar information (new knowledge).

5.4.2 Catastrophic Forgetting

To keep the paper reasonably concise, we only present the results of Qwen1.5-7B-Chat regarding the catastrophic forgetting problem on the general capabilities evaluation datasets in the main text, Table 3. For the results of other models, please refer to the Appendix F. Compared to LLMs fine-tuned on the entire dataset, **GrADS brings substantial mitigation on CF**, i.e. 82.2%, 79.5%, 41.8%, 104.8%, 70.4% improvements for C-Eval, GSM8K, ALPACA Instruct, Typical Safety and Instruct Attack.

From the domain perspective, we observe improvements of 79.3%, 28.8%, and 112.5% on Medical, Legal, and Financial, respectively. Nevertheless, in medical (20k) and financial domains (40k) with larger training volumes, the gain of GrADS in alleviating CF problems is extremely significant.

5.5 Indepth Analysis

5.5.1 RQ1: GrADS Generalizability

The scaling law indicates that Larger models are significantly more sample-efficient (Kaplan et al., 2020; Zhang et al., 2024), so it is crucial to investigate whether GrADS is still valid in larger LLMs. Therefore, we selected Qwen1.5-14B and FinQA as our illustrative case. Meanwhile, to validate the transferability of GrADS, we initially train on Qwen1.5-1.8B for one epoch to acquire gradients for each instance and subsequently employ GrADS and other baseline methods for data selection. Thereafter, the selected subdata is fine-tuned on Qwen1.5-14B. We present more experiments regarding the transferability of GrADS across various LLMs in Appendix C.

The results presented in Table 4 demonstrate that GrADS not only **remains effective for larger LLMs** such as Qwen1.5-14B but also **can be applied across different LLMs**. Both findings highlight the strong generalizability of the GrADS method, offering exciting insights for researchers in the field of LLMs.

For instance, when confronted with voluminous training data, researchers can first leverage smaller LLMs, applying the GrADS strategy, before refining with relatively more efficacious larger LLMs. This strategy optimizes resource utilization, enabling the attainment of superior model performance while mitigating computational expenses – a pivotal consideration in large-scale machine-learning endeavors.

5.5.2 RQ2: GrADS Robustness

This section extends the main results by selecting 1k, 2k, 3k, 5k, and 10k training instances from FinQA with GrADS alongside other baseline ap-

Figure 3: Experiments of fine-tuning Qwen1.5-1.8B and Qwen1.5-7B with subsets of different sizes selected from FinQA. Baselines 'base' and 'all' represent performances of the base models without SFT and the models fine-tuned on the entire data.

proaches. These new experiments extend our prior analysis that was based on a 20k (half) selection, offering a broader perspective on GrADS' performance across varying data volumes. The experiment results are provided in Figure 3.

The results in Figure 3 indicate that **the advantage of GrADS becomes even more evident in identifying subsets of smaller proportions**. While the performance of *tail50* is somewhat sub-optimal in our main experiments, we observe a notable trend in this section: as the proportion of data selected decreases, the divergence between the *tail* and *grads* method becomes increasingly pronounced. This is intuitive, aligning with insights from our pilot study, which revealed that the subdata selected from *tail* often includes knowledge already mastered by the base LLMs. The satisfactory performance of *tail50* in Table 1 can be attributed to its broad coverage across a sufficient range of instances, encompassing both those concepts firmly grasped by LLMs and those yet to be learned. However, when we downscale to select merely 1k sub-instances, the fine-tuning performances based on *tail* are merely on par with the untrained base LLMs.

Conversely, when fine-tuning with data selected via the *top*, the LLMs exhibit performances inferior to the untuned base LLM. This is primarily attributed to the nature of the data selected: the *top* method tends to select instances that are confusing or delusional for the well-trained LLMs. This phenomenon is more pronounced when smaller proportions of data are selected.

Furthermore, in terms of the BLEU score, fine-tuning with as little as 3-5k (7.5-12.5% of the entire dataset) of data selected by GrADS attains performance comparable to that achieved with the entire dataset. Even more remarkably, in the context of the METEOR metric, GrADS, with just 1-2k (a mere 2.5-5% subset) of meticulously selected data, surpasses the performances derived from fine-tuning with the entire dataset. This finding holds immense implications for practical applications, showcasing a staggering efficiency-cost benefit ratio that could significantly transform the landscape of data utilization in language model tuning.

6 Conclusion

In this paper, to improve the fine-tuning efficiency and mitigate catastrophic forgetting simultaneously, we develop an adaptive gradient-aware data selection method, GrADS. Inspired by the insight that not all training data are helpful, GrADS integrates gradients extracted from the Embedding layer and LM Head layer and introduces self-guided criteria embracing statistic distributions to recognize the model's most desired data. Experimental results carried out on various LLMs and domain-specific datasets provide empirical evidence of the efficacy, efficiency, and cost-effectiveness of GrADS. Apart from extraordinary performance on domain-specific specialties, GrADS substantially mitigates catastrophic forgetting to preserve the general capabilities that the base LLMs mastered. Moreover, extensive analyses reveal that GrADS is also valid in the learning process of LoRA training, and can be scaled up to larger LLMs, delineating its great versatility and potential for generalizability.

Limitations

In this paper, we introduce the GrADS method, which aims to enhance the efficiency of domain-specific fine-tuning. While extensive experiments validate the effectiveness of GrADS, our implementation was constrained by computational resource limitations, preventing us from applying GrADS to larger-scale language models (LLMs) with parameter sizes of 30B or 72B. Nevertheless, our focus primarily lies in resource-constrained scenarios; thus, experiments conducted with models ranging from 1.8B to 14B parameters are deemed sufficiently informative for our study. Investigations of GrADS on larger LLMs can be considered for future research endeavors.

References

Josh Achiam, Steven Adler, Sandhini Agarwal, Lama Ahmad, Ilge Akkaya, Florencia Leoni Aleman, Diogo Almeida, Janko Altenschmidt, Sam Altman, Shyamal Anadkat, et al. 2023. Gpt-4 technical report. *arXiv preprint arXiv:2303.08774*.

AI@Meta. 2024. Llama 3 model card.

Jinze Bai, Shuai Bai, Yunfei Chu, Zeyu Cui, Kai Dang, Xiaodong Deng, Yang Fan, Wenbin Ge, Yu Han, Fei Huang, Binyuan Hui, Luo Ji, Mei Li, Junyang Lin, Runji Lin, Dayiheng Liu, Gao Liu, Chengqiang Lu, Keming Lu, Jianxin Ma, Rui Men, Xingzhang Ren, Xuancheng Ren, Chuanqi Tan, Sinan Tan, Jianhong Tu, Peng Wang, Shijie Wang, Wei Wang, Shengguang Wu, Benfeng Xu, Jin Xu, An Yang, Hao Yang, Jian Yang, Shusheng Yang, Yang Yao, Bowen Yu, Hongyi Yuan, Zheng Yuan, Jianwei Zhang, Xingxuan Zhang, Yichang Zhang, Zhenru Zhang, Chang Zhou, Jingren Zhou, Xiaohuan Zhou, and Tianhang Zhu. 2023. Qwen technical report. *arXiv preprint arXiv:2309.16609*.

Satanjeev Banerjee and Alon Lavie. 2005. Meteor: An automatic metric for mt evaluation with improved correlation with human judgments. In *Proceedings of the acl workshop on intrinsic and extrinsic evaluation measures for machine translation and/or summarization*, pages 65–72.

Yihan Cao, Yanbin Kang, and Lichao Sun. 2023. Instruction mining: High-quality instruction data selection for large language models. *arXiv preprint arXiv:2307.06290*.

Lichang Chen, Shiyang Li, Jun Yan, Hai Wang, Kalpa Gunaratna, Vikas Yadav, Zheng Tang, Vijay Srinivasan, Tianyi Zhou, Heng Huang, et al. 2023a. Alpagasus: Training a better alpaca with fewer data. *arXiv preprint arXiv:2307.08701*.

Sanyuan Chen, Yutai Hou, Yiming Cui, Wanxiang Che, Ting Liu, and Xiangzhan Yu. 2020. Recall and learn: Fine-tuning deep pretrained language models with less forgetting. *Preprint*, arXiv:2004.12651.

Wei Chen, Qiushi Wang, Zefei Long, Xianyin Zhang, Zhongtian Lu, Bingxuan Li, Siyuan Wang, Jiarong Xu, Xiang Bai, Xuanjing Huang, and Zhongyu Wei. 2023b. Disc-finllm: A chinese financial large language model based on multiple experts fine-tuning. *arXiv preprint arXiv:2310.15205*.

Yukang Chen, Shengju Qian, Haotian Tang, Xin Lai, Zhijian Liu, Song Han, and Jiaya Jia. 2023c. Longlora: Efficient fine-tuning of long-context large language models. *arXiv preprint arXiv:2309.12307*.

Hyung Won Chung, Le Hou, Shayne Longpre, Barret Zoph, Yi Tay, William Fedus, Yunxuan Li, Xuezhi Wang, Mostafa Dehghani, Siddhartha Brahma, Albert Webson, Shixiang Shane Gu, Zhuyun Dai, Mirac Suzgun, Xinyun Chen, Aakanksha Chowdhery, Alex Castro-Ros, Marie Pellat, Kevin Robinson, Dasha Valter, Sharan Narang, Gaurav Mishra, Adams Yu, Vincent Zhao, Yanping Huang, Andrew Dai, Hongkun Yu, Slav Petrov, Ed H. Chi, Jeff Dean, Jacob Devlin, Adam Roberts, Denny Zhou, Quoc V. Le, and Jason Wei. 2024. Scaling instruction-finetuned language models. *Journal of Machine Learning Research*, 25(70):1–53.

Andrea Cossu, Tinne Tuytelaars, Antonio Carta, Lucia Passaro, Vincenzo Lomonaco, and Davide Bacciu. 2022. Continual pre-training mitigates forgetting in language and vision. *Preprint*, arXiv:2205.09357.

Jiaxi Cui, Munan Ning, Zongjian Li, Bohua Chen, Yang Yan, Hao Li, Bin Ling, Yonghong Tian, and Li Yuan. 2024. Chatlaw: A multi-agent collaborative legal assistant with knowledge graph enhanced mixture-of-experts large language model. *Preprint*, arXiv:2306.16092.

Shizhe Diao, Tianyang Xu, Ruijia Xu, Jiawei Wang, and Tong Zhang. 2023. Mixture-of-domain-adapters: Decoupling and injecting domain knowledge to pretrained language models memories. *arXiv preprint arXiv:2306.05406*.

Qianlong Du, Chengqing Zong, and Jiajun Zhang. 2023. Mods: Model-oriented data selection for instruction tuning. *arXiv preprint arXiv:2311.15653*.

Yuan Ge, Yilun Liu, Chi Hu, Weibin Meng, Shimin Tao, Xiaofeng Zhao, Hongxia Ma, Li Zhang, Hao Yang, and Tong Xiao. 2024. Clustering and ranking: Diversity-preserved instruction selection through expert-aligned quality estimation. *arXiv preprint arXiv:2402.18191*.

Quzhe Huang, Mingxu Tao, Chen Zhang, Zhenwei An, Cong Jiang, Zhibin Chen, Zirui Wu, and Yansong Feng. 2023a. Lawyer llama. https://github.com/AndrewZhe/lawyer-llama.

Quzhe Huang, Mingxu Tao, Chen Zhang, Zhenwei An, Cong Jiang, Zhibin Chen, Zirui Wu, and Yansong Feng. 2023b. Lawyer llama technical report. *Preprint*, arXiv:2305.15062.

Yuzhen Huang, Yuzhuo Bai, Zhihao Zhu, Junlei Zhang, Jinghan Zhang, Tangjun Su, Junteng Liu, Chuancheng Lv, Yikai Zhang, Jiayi Lei, Yao Fu, Maosong Sun, and Junxian He. 2023c. C-eval: A multi-level multi-discipline chinese evaluation suite for foundation models. *arXiv preprint arXiv:2305.08322*.

Jared Kaplan, Sam McCandlish, Tom Henighan, Tom B Brown, Benjamin Chess, Rewon Child, Scott Gray, Alec Radford, Jeffrey Wu, and Dario Amodei. 2020. Scaling laws for neural language models. *arXiv preprint arXiv:2001.08361*.

Prakhar Kaushik, Alex Gain, Adam Kortylewski, and Alan Yuille. 2021. Understanding catastrophic forgetting and remembering in continual learning with optimal relevance mapping. *Preprint*, arXiv:2102.11343.

Zixuan Ke. 2024. *Continual Learning with Language Models*. Ph.D. thesis, University of Illinois at Chicago.

Ming Li, Yong Zhang, Zhitao Li, Jiuhai Chen, Lichang Chen, Ning Cheng, Jianzong Wang, Tianyi Zhou, and Jing Xiao. 2023. From quantity to quality: Boosting llm performance with self-guided data selection for instruction tuning. *arXiv preprint arXiv:2308.12032*.

Chin-Yew Lin. 2004. Rouge: A package for automatic evaluation of summaries. In *Text summarization branches out*, pages 74–81.

Yong Lin, Lu Tan, Hangyu Lin, Zeming Zheng, Renjie Pi, Jipeng Zhang, Shizhe Diao, Haoxiang Wang, Han Zhao, Yuan Yao, et al. 2023. Speciality vs generality: An empirical study on catastrophic forgetting in fine-tuning foundation models. *arXiv preprint arXiv:2309.06256*.

Chengyuan Liu, Shihang Wang, Yangyang Kang, Lizhi Qing, Fubang Zhao, Changlong Sun, Kun Kuang, and Fei Wu. 2024. More than catastrophic forgetting: Integrating general capabilities for domain-specific llms. *arXiv preprint arXiv:2405.17830*.

Wei Liu, Weihao Zeng, Keqing He, Yong Jiang, and Junxian He. 2023. What makes good data for alignment? a comprehensive study of automatic data selection in instruction tuning. *arXiv preprint arXiv:2312.15685*.

Yun Luo, Zhen Yang, Fandong Meng, Yafu Li, Jie Zhou, and Yue Zhang. 2024. An empirical study of catastrophic forgetting in large language models during continual fine-tuning. *Preprint*, arXiv:2308.08747.

Daye Nam, Andrew Macvean, Vincent Hellendoorn, Bogdan Vasilescu, and Brad Myers. 2024. Using an llm to help with code understanding. In *Proceedings of the IEEE/ACM 46th International Conference on Software Engineering*, pages 1–13.

Long Ouyang, Jeffrey Wu, Xu Jiang, Diogo Almeida, Carroll Wainwright, Pamela Mishkin, Chong Zhang, Sandhini Agarwal, Katarina Slama, Alex Ray, John Schulman, Jacob Hilton, Fraser Kelton, Luke Miller, Maddie Simens, Amanda Askell, Peter Welinder, Paul F Christiano, Jan Leike, and Ryan Lowe. 2022. Training language models to follow instructions with human feedback. In *Advances in Neural Information Processing Systems*, volume 35, pages 27730–27744. Curran Associates, Inc.

Xingyuan Pan, Luyang Huang, Liyan Kang, Zhicheng Liu, Yu Lu, and Shanbo Cheng. 2024. G-dig: Towards gradient-based diverse and high-quality instruction data selection for machine translation. *arXiv preprint arXiv:2405.12915*.

Kishore Papineni, Salim Roukos, Todd Ward, and Wei-Jing Zhu. 2002. Bleu: a method for automatic evaluation of machine translation. In *Proceedings of the 40th annual meeting of the Association for Computational Linguistics*, pages 311–318.

Baolin Peng, Chunyuan Li, Pengcheng He, Michel Galley, and Jianfeng Gao. 2023. Instruction tuning with gpt-4. *arXiv preprint arXiv:2304.03277*.

Hao Sun, Zhexin Zhang, Jiawen Deng, Jiale Cheng, and Minlie Huang. 2023. Safety assessment of chinese large language models. *arXiv preprint arXiv:2304.10436*.

Xiao Wang, Tianze Chen, Qiming Ge, Han Xia, Rong Bao, Rui Zheng, Qi Zhang, Tao Gui, and Xuanjing Huang. 2023. Orthogonal subspace learning for language model continual learning. *Preprint*, arXiv:2310.14152.

Bogdan M Wilamowski, Nicholas J Cotton, Okyay Kaynak, and GÜnhan Dundar. 2008. Computing gradient vector and jacobian matrix in arbitrarily connected neural networks. *IEEE Transactions on Industrial Electronics*, 55(10):3784–3790.

Honglin Xiong, Sheng Wang, Yitao Zhu, Zihao Zhao, Yuxiao Liu, Qian Wang, and Dinggang Shen. 2023. Doctorglm: Fine-tuning your chinese doctor is not a herculean task. *arXiv preprint arXiv:2304.01097*.

An Yang, Baosong Yang, Binyuan Hui, Bo Zheng, Bowen Yu, Chang Zhou, Chengpeng Li, Chengyuan Li, Dayiheng Liu, Fei Huang, et al. 2024a. Qwen2 technical report. *arXiv preprint arXiv:2407.10671*.

Kailai Yang, Tianlin Zhang, Ziyan Kuang, Qianqian Xie, and Sophia Ananiadou. 2023. Mentalllama: Interpretable mental health analysis on social media with large language models. *arXiv preprint arXiv:2309.13567*.

Zhaorui Yang, Tianyu Pang, Haozhe Feng, Han Wang, Wei Chen, Minfeng Zhu, and Qian Liu. 2024b. Self-distillation bridges distribution gap in language model fine-tuning. *Preprint*, arXiv:2402.13669.

Longhui Yu, Weisen Jiang, Han Shi, Jincheng Yu, Zhengying Liu, Yu Zhang, James T Kwok, Zhenguo Li, Adrian Weller, and Weiyang Liu. 2023. Metamath: Bootstrap your own mathematical questions for large language models. *arXiv preprint arXiv:2309.12284*.

Shengbin Yue, Wei Chen, Siyuan Wang, Bingxuan Li, Chenchen Shen, Shujun Liu, Yuxuan Zhou, Yao Xiao, Song Yun, Xuanjing Huang, and Zhongyu Wei. 2023. Disc-lawllm: Fine-tuning large language models for intelligent legal services. *Preprint*, arXiv:2309.11325.

Aohan Zeng, Xiao Liu, Zhengxiao Du, Zihan Wang, Hanyu Lai, Ming Ding, Zhuoyi Yang, Yifan Xu, Wendi Zheng, Xiao Xia, Weng Lam Tam, Zixuan Ma, Yufei Xue, Jidong Zhai, Wenguang Chen, Zhiyuan Liu, Peng Zhang, Yuxiao Dong, and Jie Tang. 2023. GLM-130b: An open bilingual pre-trained model. In *The Eleventh International Conference on Learning Representations (ICLR)*.

Biao Zhang, Zhongtao Liu, Colin Cherry, and Orhan Firat. 2024. When scaling meets llm finetuning: The effect of data, model and finetuning method. *arXiv preprint arXiv:2402.17193*.

Hongbo Zhang, Junying Chen, Feng Jiang, Fei Yu, Zhihong Chen, Jianquan Li, Guiming Chen, Xiangbo Wu, Zhiyi Zhang, Qingying Xiao, Xiang Wan, Benyou Wang, and Haizhou Li. 2023. Huatuogpt, towards taming language model to be a doctor. *Preprint*, arXiv:2305.15075.

Sheng Zhang, Xin Zhang, Hui Wang, Lixiang Guo, and Shanshan Liu. 2018. Multi-scale attentive interaction networks for chinese medical question answer selection. *IEEE Access*, 6:74061–74071.

Xuanyu Zhang and Qing Yang. 2023. Xuanyuan 2.0: A large chinese financial chat model with hundreds of billions parameters. In *Proceedings of the 32nd ACM International Conference on Information and Knowledge Management*, CIKM '23, page 4435–4439, New York, NY, USA. Association for Computing Machinery.

Weixiang Zhao, Shilong Wang, Yulin Hu, Yanyan Zhao, Bing Qin, Xuanyu Zhang, Qing Yang, Dongliang Xu, and Wanxiang Che. 2024. Sapt: A shared attention framework for parameter-efficient continual learning of large language models. *Preprint*, arXiv:2401.08295.

Chunting Zhou, Pengfei Liu, Puxin Xu, Srinivasan Iyer, Jiao Sun, Yuning Mao, Xuezhe Ma, Avia Efrat, Ping Yu, Lili Yu, et al. 2024. Lima: Less is more for alignment. *Advances in Neural Information Processing Systems*, 36.

A Consistency between GPT-4o and Human Evaluation

To ensure the validity of GPT-4o's assessments, we conduct supplementary manual evaluations. For the GPT-4o's response quality scores in main results, we sampled 200 question-answer pairs rated by GPT-4o and enlisted the expertise of three professional data annotators to independently score the response quality on a scale of 1 to 5, in alignment with GPT-4o's scoring criteria. Subsequently, we calculated the average score for the three individuals and applied rounding to the nearest integer. We find that there are 147 samples for which the scores given by GPT-4o completely align with those of the annotators, and the scores from both sides yields a Pearson product-moment correlation coefficient of 0.79. This indicates a substantial agreement between the GPT-4o and human evaluations of response quality.

Meanwhile, for the safety judgement of catastrophic forgetting experiments in main results, we also sample 200 instances for each category, i.e., Typical Safety and Instruction Attack, respectively. With the same approach, we measure the consistency between GPT-4o's judgments and the three annotators evaluations. We obtain a correlation coefficient score of 0.879 for Typical Safety and a correlation coefficient score of 0.815 for Instruction Attack.

B CF Evaluation Metrics

For C-Eval, we write a rule-based method to extract the options predicted by LLMs, and report the accuracy and whether the LLMs follow the instruction of "Single-choice questions". For GSK8k, we apply its publicly released Chinese version which is translated by GPT3.5-Turbo [2]. We follow previous work [3] to extract the numerical results predicted by LLMs and report the accuracy, BLEU, and ROUGE-L. For ALPACA, we report BLEU and ROUGE-L. For SafetyPrompts (Typical Safety and Instruction Attack subdata), we write a few-shot prompt to instruct GPT-4o to conduct a 2 choice task on whether the LLMs' responses are safe or not. The responses are considered as correct if GPT-4o labels them as "safe".

C GrADS Transferability on Different LLMs

In this section, we adhere to the setting in RQ1 which initially train on Qwen1.5-1.8B for one epoch to acquire gradients and employ other LLMs for fine-tuning. Our findings in Table 5 reveal

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[2]https://huggingface.co/datasets/meta-math/GSM8K_zh
[3]https://github.com/QwenLM/Qwen

that data selected using Qwen1.5-1.8B in conjunction with GrADS not only prove effective for larger LLMs of the same architecture (Qwen-1.5-7B), but also yield substantial improvements for larger LLMs of different architectures, including ChatGLM3-6B and Llama3-8B. This experimentation **further validates the transferability of the GrADS methodology**.

D Ablation Study

In this section, we conducted an ablation study using Qwen1.5-7B as a case example across three domains. Specifically, we examined the impacts of incorporating only the gradients from the Embed Layer or only from the LM Head Layer. Subsequently, we applied the methods *top50*, *tail50*, *mid50*, and *grads50* following the settings in the main experiments. Additionally, we explored alternative integration methods for the gradients obtained from the Embed Layer and the LM Head Layer. In Table6, *weight* refers to the gradients from the Embed Layer and LM Head Layer that are normalized and summed to derive a gradient distribution. Besides, *weightr* entails ranking the gradients of each instance from the Embed Layer and LM Head Layer in descending order and summing their ranks' reciprocals to obtain the distribution. Subsequently, both *weight* and *weightr* utilize the same data selection criteria as GrADS. The experimental results indicate that our original GrADS consistently achieves optimal or sub-optimal performance, thereby validating the rationale behind our methodological design.

E Implementation Details

Our experiment is conducted on 8 A100 GPUs, each with 80G memories. All experiments are conducted with LLaMA-Factory[4] training architecture and deepspeed_z3. For all methods, we set the learning rate of 3e-5, warmup ratio of 0.1, batch size of 8. Regarding LLMs' API, we adopt GPT-4o. For LoRA experiments, the rank is set to 16. For all randomly selected data, we set the random seed of 42.

F Supplementary Experiments

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[4]https://github.com/hiyouga/LLaMA-Factory/tree/main

Base Model	Method	CMedQA			LawQA			FinQA		
		BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR
Qwen1.5-7B	base	2.627	12.180	10.860	9.066	20.050	21.392	3.188	11.194	14.669
	all	3.414	16.347	11.274	15.190	25.803	25.272	9.020	22.074	16.877
	rdn50	3.143	16.272	11.055	14.856	25.198	24.799	8.685	21.614	16.277
	top50	2.763	15.276	9.249	13.518	24.821	22.985	6.126	19.275	13.098
	tail50	4.282	16.594	**14.181**	18.678	25.629	**32.416**	11.303	21.764	22.125
	mid50	4.170	**17.332**	12.932	17.072	25.923	27.893	9.877	22.442	18.725
	grads50	**4.316**	16.771	13.785	**18.847**	26.088	32.394	**12.230**	**22.885**	**22.888**
ChatGLM3-6B	base	2.568	11.274	15.634	7.966	19.733	19.011	3.174	11.437	14.926
	all	3.899	16.418	15.811	15.837	26.167	26.497	10.353	20.891	22.899
	rdn50	3.611	15.814	15.492	15.363	25.674	25.884	10.116	20.550	22.203
	top50	2.935	14.865	13.807	14.248	24.977	24.256	7.093	19.562	18.515
	tail50	4.736	16.516	17.910	18.716	25.669	32.784	11.689	21.739	26.138
	mid50	4.405	16.929	16.860	17.174	**26.598**	28.310	9.843	22.150	23.099
	grads50	**5.005**	**17.274**	**18.063**	**18.918**	26.459	**33.146**	**12.562**	**22.894**	**26.757**
Llama3-8B	base	0.026	0.249	0.291	0.259	1.905	2.164	0.178	1.293	1.225
	all	3.432	16.031	10.897	15.272	24.301	25.033	9.116	21.190	16.913
	rdn50	2.964	15.335	10.360	14.451	23.671	24.368	8.312	20.766	15.980
	top50	2.723	15.488	9.591	12.812	24.159	22.442	5.476	18.507	12.108
	tail50	4.256	16.801	**14.036**	18.217	24.984	32.007	11.551	21.847	22.359
	mid50	3.948	17.084	12.661	16.377	**25.796**	27.400	9.484	20.078	18.487
	grads50	**4.281**	**17.145**	13.533	**18.491**	25.316	**32.423**	**11.881**	**22.544**	**22.567**

Table 5: Experiment results of implementing GrADS with Qwen1.5-1.8B, and leverage the selected data for SFT on other larger LLMs

Gradients	Method	CMedQA			LawQA			FinQA		
		BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR
	base	2.627	12.180	10.860	9.066	20.050	21.392	3.188	11.194	14.669
	all	3.414	16.347	11.274	15.190	25.803	25.272	9.020	22.074	16.877
	rdn50	3.143	16.272	11.055	14.856	25.198	24.799	8.685	21.614	16.277
Embed Only	top50	2.564	14.776	9.376	13.696	24.446	23.493	6.252	19.553	13.225
	tail50	4.184	17.134	13.399	18.253	24.859	32.501	11.553	22.043	22.147
	mid50	3.698	16.693	12.050	17.579	**26.262**	28.785	9.969	22.800	18.871
	grads50	4.253	16.891	14.135	18.464	25.350	32.817	11.774	**23.106**	22.530
LMHead Only	top50	2.682	15.335	9.582	13.513	24.797	23.095	6.381	19.421	13.137
	tail50	4.466	16.780	14.322	18.102	25.545	31.750	11.969	22.311	22.681
	mid50	4.389	17.463	13.156	17.257	26.012	27.981	10.004	22.880	19.032
	grads50	4.769	17.210	14.263	18.485	26.031	32.327	11.888	22.579	22.703
Integration	weight	4.464	16.961	13.843	18.675	25.763	31.980	11.762	22.293	22.119
	weightr	4.327	16.914	13.511	17.569	25.334	31.022	10.860	21.176	22.010
	ours	**4.871**	**17.469**	**14.390**	**19.179**	26.221	**32.975**	**12.362**	22.816	**22.872**

Table 6: Ablation Study

Domain	Method	C-Eval		GSM8k			ALPACA		Safety	Attack
		Acc	Instruct	Acc	BLEU	ROUGE	BLEU	ROUGE	Acc	Acc
	base	54.360	73.328	46.020	18.593	33.002	16.362	28.321	44.681	50.686
CMedQA	all	8.794	5.523	3.942	4.271	16.108	4.782	16.971	16.783	23.068
	rdn50	15.480	18.023	6.823	5.811	18.120	6.636	19.507	16.879	27.863
	grads50	**16.480**	**19.695**	**10.008**	**6.468**	**19.098**	**7.810**	**20.765**	**25.679**	**31.484**
LawQA	all	30.451	25.363	34.572	14.833	28.227	13.966	25.468	26.137	40.017
	rdn50	32.756	**38.227**	36.012	**16.103**	**29.974**	**15.284**	**27.242**	28.995	41.983
	grads50	**33.717**	37.974	**37.225**	15.709	29.080	13.637	26.671	**37.681**	**42.036**
FinQA	all	13.953	2.947	1.365	1.418	9.869	2.832	12.448	7.416	11.678
	rdn50	18.823	5.794	2.578	2.032	11.751	3.638	14.495	10.861	14.884
	grads50	**26.017**	**19.089**	**4.250**	**3.717**	**15.649**	**4.911**	**16.776**	**21.025**	**24.481**

Table 7: Catastrophic Forgetting Results of ChatGLM3-6B

| Domain | Method | C-Eval | | GSM8k | | | ALPACA | | Safety | Attack |
		Acc	Instruct	Acc	BLEU	ROUGE	BLEU	ROUGE	Acc	Acc
	base	46.657	97.832	58.226	3.903	16.089	3.229	7.443	27.150	44.167
CMedQA	all	0.291	0.000	0.682	0.894	9.215	0.861	9.317	7.061	6.333
	rdn50	0.390	0.036	0.076	0.777	8.749	0.860	9.310	10.535	5.583
	grads50	**0.509**	**0.073**	**0.758**	**1.679**	**10.827**	**1.131**	**10.800**	**14.672**	**10.250**
LawQA	all	3.634	3.343	2.729	4.438	13.415	4.624	14.708	15.643	32.333
	rdn50	4.506	0.727	3.033	4.105	12.859	4.298	13.869	22.714	37.250
	grads50	**4.869**	**6.017**	**4.701**	**6.311**	**15.585**	**5.326**	**16.081**	**25.143**	**41.583**
FinQA	all	0.363	1.817	0.227	0.491	6.985	0.558	10.297	1.500	2.750
	rdn50	1.438	9.084	0.455	0.683	7.019	0.667	8.091	**2.571**	**3.917**
	grads50	**6.541**	**21.148**	**0.607**	**1.019**	**7.514**	**0.739**	**8.473**	1.929	3.833

Table 8: Catastrophic Forgetting Results of Llama3-8B

| Base Model | Method | CMedQA | | | LawQA | | | FinQA | | |
		BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR	BLEU	ROUGE	METEOR
Qwen1.5-1.8B	base	1.547	8.228	13.169	9.860	19.178	24.505	1.888	7.911	12.061
	all	3.329	16.307	11.657	12.089	**23.355**	23.118	5.339	**18.021**	12.417
	rdn50	3.236	16.102	11.399	11.947	22.745	22.509	4.552	17.144	11.438
	grads50	**4.310**	**17.181**	**13.933**	**14.062**	22.796	**27.382**	**6.202**	16.804	**15.364**
Qwen1.5-7B	base	2.627	12.180	10.860	9.066	20.050	21.392	3.188	11.194	14.669
	all	3.857	17.279	12.169	13.782	**24.382**	24.377	6.630	**19.902**	14.063
	rdn50	3.730	16.909	12.020	14.079	23.560	25.489	5.812	18.919	13.180
	grads50	**4.608**	**17.643**	**14.292**	**15.983**	23.776	**29.507**	**7.112**	18.135	**16.627**
ChatGLM3-6B	base	2.568	11.274	10.634	7.966	19.733	19.011	3.174	11.437	14.926
	all	3.341	15.260	11.783	**12.923**	**22.506**	**25.066**	7.724	**19.825**	16.198
	rdn50	3.491	15.404	11.674	9.053	19.948	19.619	7.595	19.716	16.112
	grads50	**3.893**	**16.202**	**13.087**	8.741	19.914	19.979	**7.968**	18.040	**17.464**
Llama3-8B	base	0.026	0.249	0.291	0.259	1.905	2.164	0.178	1.293	1.225
	all	2.828	**15.659**	10.686	**15.140**	**23.985**	27.735	8.761	**21.281**	17.566
	rdn50	2.510	15.197	10.190	13.873	23.152	26.610	7.901	20.297	16.491
	grads50	**2.962**	14.419	**11.743**	14.371	22.718	**28.961**	**8.991**	19.187	**18.953**

Table 9: LoRA Results

| Domain | Method | C-Eval | | GSM8k | | | ALPACA | | Safety | Attack |
		Acc	Instruct	Acc	BLEU	ROUGE	BLEU	ROUGE	Acc	Acc
	base	65.189	87.427	55.497	14.967	29.207	15.097	27.529	43.807	51.365
CMedQA	all	**35.512**	**42.124**	22.592	7.368	23.634	5.681	19.265	23.087	31.415
	rdn50	29.420	29.940	33.131	10.441	27.717	7.044	21.033	28.596	37.847
	grads50	34.101	40.638	**44.806**	**14.600**	**31.424**	**8.644**	**22.966**	**31.138**	**42.636**
LawQA	all	34.323	32.615	53.373	14.408	28.252	14.031	26.393	28.650	41.684
	rdn50	39.673	**39.598**	53.146	**14.841**	**29.121**	**14.970**	**27.211**	33.757	**50.220**
	grads50	**41.307**	38.484	**53.980**	12.970	26.678	13.504	25.160	**35.766**	49.814
FinQA	all	48.365	68.870	17.664	3.528	18.015	4.178	15.660	17.174	24.269
	rdn50	**50.817**	**70.653**	20.849	3.976	19.035	4.356	16.408	21.235	33.471
	grads50	27.637	22.956	**28.506**	**8.582**	**26.069**	**6.000**	**18.344**	**27.451**	**36.045**

Table 10: Catastrophic Forgetting Results of LoRA on Qwen1.5-7B

Domain	Method	C-Eval		GSM8k			ALPACA		Safety	Attack
		Acc	Instruct	Acc	BLEU	ROUGE	BLEU	ROUGE	Acc	Acc
	base	54.360	73.328	46.020	18.593	33.002	16.362	28.321	44.681	50.686
CMedQA	all	25.186	28.232	25.929	11.616	27.839	11.079	24.465	25.318	33.572
	rdn50	**30.163**	29.822	30.857	13.497	29.993	12.162	25.685	31.664	38.055
	grads50	28.678	**40.416**	**33.207**	**14.455**	**31.127**	**12.426**	**25.974**	**32.042**	**39.776**
LawQA	all	39.673	60.327	42.077	17.661	32.429	14.814	27.301	30.285	40.069
	rdn50	39.004	**64.859**	43.821	**17.929**	**32.610**	**15.249**	**27.640**	35.460	46.734
	grads50	**40.119**	64.636	**44.655**	17.895	32.517	15.065	27.446	**37.261**	**48.588**
FinQA	all	23.031	42.422	22.214	10.278	26.400	10.022	22.785	16.292	25.106
	rdn50	28.158	40.416	**26.005**	11.090	27.576	10.744	23.197	22.234	30.217
	grads50	**31.055**	**45.840**	24.867	**11.863**	**28.318**	**12.641**	**25.519**	**28.656**	**35.785**

Table 11: Catastrophic Forgetting Results of LoRA on ChatGLM3-6B

Domain	Method	C-Eval		GSM8k			ALPACA		Safety	Attack
		Acc	Instruct	Acc	BLEU	ROUGE	BLEU	ROUGE	Acc	Acc
	base	46.657	97.832	58.226	3.903	16.089	3.299	7.443	27.150	44.167
CMedQA	all	2.674	1.783	15.693	6.706	21.267	3.343	14.913	15.714	20.333
	rdn50	9.212	14.413	17.664	6.666	21.489	3.149	15.131	21.071	26.750
	grads50	**9.509**	**18.127**	**23.730**	**8.970**	**25.342**	**5.402**	**18.493**	**22.286**	**29.167**
LawQA	all	39.376	81.278	54.814	17.542	**33.502**	**10.398**	**21.001**	24.643	31.250
	rdn50	**44.428**	**92.422**	55.800	16.637	32.829	9.611	19.168	26.143	34.333
	grads50	43.908	91.976	**58.302**	**17.660**	33.339	8.545	17.339	**28.643**	**40.667**
FinQA	all	22.140	28.826	30.857	6.806	25.282	5.200	17.511	7.214	14.250
	rdn50	**28.158**	**54.309**	32.980	7.548	26.324	5.536	18.784	11.857	19.417
	grads50	23.626	35.364	**34.117**	**9.022**	**27.687**	**6.566**	**19.203**	**14.143**	**24.083**

Table 12: Catastrophic Forgetting Results of LoRA on Llama3-8B