Punctuations and Predicates in Language Models

Abstract

In this paper we explore where information is collected and how it is propagated throughout layers in large language models (LLMs). We begin by examining the surprising computational importance of punctuation tokens which previous work has identified as attention sinks and memory aids. Using intervention-based techniques, we evaluate the necessity and sufficiency (for preserving model performance) of punctuation tokens across layers in GPT-2, DeepSeek, and Gemma. Our results show stark model-specific differences: for GPT-2, punctuation is both necessary and sufficient in multiple layers, while this holds far less in DeepSeek and not at all in Gemma. Extending beyond punctuation, we ask whether LLMs process different components of input (e.g., subjects, adjectives, punctuation, full sentences) by forming early static summaries reused across the network, or if the model remains sensitive to changes in these components across layers. Extending beyond punctuation, we investigate whether different reasoning rules are processed differently by LLMs. In particular, through interchange intervention and layer-swapping experiments, we find that conditional statements (if, then), and universal quantification (for all) are processed very differently. Our findings offer new insight into the internal mechanisms of punctuation usage and reasoning in LLMs and have implications for interpretability.

1 Introduction

Recent work has revealed that LLMs often perform tasks in ways that diverge significantly from human reasoning. In particular, punctuation which is often considered negligible in human processing appears to play a surprisingly active and complex role within these models. Studies have shown that punctuation tokens can act as attention sinks (Gu et al., 2025; Barbero et al., 2025), increase computational memory (Pfau et al., 2024), and even serve as information carriers (Tigges et al., 2023).

Despite their seemingly minor status, punctuation marks appear to shoulder a disproportionately large computational burden.

In this work, we examine the role of punctuation in summarization and information propagation through the lens of necessity and sufficiency: how essential are these tokens for preserving meaning and reasoning within the model? We use zeroing out interventions to better understand how punctuation influences layerwise computation dynamics. To test whether the period acts as a boundary for information summarization in the context of reasoning, we also perform targeted activation interchange interventions.

Building on this, we take a mechanistic lens to ask a broader question: How do LLMs internally represent and process reasoning? Previous work on reasoning has investigated reasoning rules using graph-based approaches (Luo et al., 2024; Qu et al., 2021; Tang et al., 2024). In this paper, we investigate whether models interpret inputs compositionally, treating different elements of a sentence (such as subjects, adjectives, punctuation, and full syntactic structures) as functionally distinct units or whether they instead form a static summary early in the forward pass and reuse that across layers. This line of inquiry helps us understand not just whether a model can reason, but how that reasoning unfolds internally. This distinction is an effort to zoom-in on how closely model behaviour aligns or diverges from human reasoning patterns.

To understand how rules are processed by language models, we analyze which layers are responsible for reasoning over different types of logical and syntactic structures. Specifically, we aim to identify whether rule-consistent behavior is distributed across the model or concentrated in particular layers. We use part-of-sentence interventions and layer swaps, with the aim of characterizing how different layers contribute across syntactic and logical dimensions.

Our main findings are:

- For GPT-2 we find that period and question mark tokens are necessary and sufficient in five out of twelve layers. However, in DeepSeek this only holds for one in twentyfour layers, and in Gemma there is no layer for which this holds. See Section 5.1. We are the first to investigate sufficiency and necessity of punctuation tokens, which we do by selectively (non-)zeroing out tokens. Additionally, although interchange interventions have been done on tokens, they were not previously used to investigate attention sinks and memorization.

- We investigate which layers are most swappable, and find different LLMs behave very differently. For GPT-2 and Gemma we find that middle layers are unique, for DeepSeek we find that layers become more and more interchangeable, when prompted on statements containing reasoning rules. See Figure 5. We are the first to compare reasoning rules using layer swaps.

Across models there is a wide variation in necessity and sufficiency of punctuation, sensitivity to interventions on different reasoning rules, and non-uniform swappability of layers. This reveals sharp differences in how internal computations are organized across architectures or training paradigms, and suggests distinct underlying inductive biases in how models learn to represent and perform reasoning.

2 Related Work

Mechanistic interpretability seeks to reverse-engineer neural networks by linking neural components to specific behaviors and computations (Olah et al., 2017). In causal abstraction this linking is done by forming a causal model of the behaviors (Geiger et al., 2021). The following lines of research are most related to our work.

Layerwise Process Analyses. Previous work has shown earlier layers process initial structure of the input (Yang et al., 2025), and ablating them leads to substantial degradation (Zhang et al., 2024). Middle layers have been found to build intermediate representations (Yang et al., 2025), to be essential for a variety of reasoning tasks (Skean et al., 2025; Liu and Niehues, 2025), and they often operate in a

shared representational space, swapping them has little effect for general tasks but this does not hold true for structured domains like math and logical reasoning (Sun et al., 2025). Later layers focus on task-specific specialization (Yang et al., 2025), contain attention heads specialized for generalization (Ye et al., 2025), and may primarily serve to consolidate and finalize already-inferred information (Ben-Artzy and Schwartz, 2024).

Attention Sinks emerge naturally during pre-training giving disproportionate attention to the first token (Gu et al., 2025). Such attention sinks may be functionally necessary to prevent representational collapse and ensure smooth information flow in long-context scenarios (Barbero et al., 2025). Tigges et al. (2023) demonstrate that punctuation symbols act as aggregation points for sentiment signals within the model's activation space. Punctuation tokens serve as structural anchors, influencing factual consistency, context retention, and reasoning (Razzhigaev et al., 2025; Zhu et al., 2025). Punctuation may also act as computation enablers, providing additional "thinking steps" irrespective of their linguistic function (Pfau et al., 2024).

Reasoning. Techniques like steering vectors (Venhoff et al., 2025), chain-of-thought prompting (Plaat et al., 2024; Dutta et al., 2024) and multi-hop reasoning analysis (Wang et al., 2024) aim to make the implicit reasoning steps of LLMs more interpretable and controllable. LLMs may construct internal reasoning trees, recoverable via attention-based probes (Hou et al., 2023), indicating genuine multi-hop reasoning beyond memorization. Benchmarks like Cladder (Jin et al., 2024) systematically evaluate a model's ability to extract and utilize causal structures from text. Bogdan et al. (2025) perform sentence-level reasoning analysis using thought vectors, revealing that a small subset of these vectors disproportionately governs the model's reasoning process. Ibeling and Icard (2021); Chauhan and Geiger (2024) have explored reasoning from a causal perspective.

3 Models and Datasets

Models: We conduct our experiments using three models of varying sizes and architectures: GPT-2 Small (Lee and Hsiang, 2019), Gemma (Team et al., 2024), and DeepSeek (Guo et al., 2024). A clear distinction in the characteristics of the models can be seen in Table A in the appendix.

We use these models to answer questions based on the context provided; each question can have three possible answers 1. *True*, 2. *False*, 3. *Unknown*. Our main aim of having an experimental setup like this is to check how the model processes context and then check the understanding of the context with the help of questions.

RuleTaker Dataset (Clark et al., 2020) tests the reasoning and implication abilities of LLMs. It includes facts and rules, followed by questions that assess whether the rules are correctly applied. Answers to these questions are labeled as True, False, or Unknown.

An example prompt is: *"Harry is tall. Tall people are round. Is Harry round?"* In the above example, the first sentence is a fact, the second sentence is a (universal quantification) rule, followed by a question that the model answers.

Fine-tuning on RuleTaker Dataset: We fine-tuned GPT2, DeepSeek, and Gemma on the rule-taker dataset. We fine-tune all models using Adam optimizer with 1e-3 learning rate to specialize their knowledge for our targeted reasoning task by taking a 80-20% split of the data, which involves structured logical rules beyond the scope of general pre-training. Furthermore, since our data set is formulated as a supervised classification problem with three labels, task-specific fine-tuning is necessary to align the outputs of the models with the label space. While GPT-2 is fine-tuned using full parameter training, we apply LoRA (Hu et al., 2021) for Gemma and DeepSeek due to their larger sizes, allowing efficient adaptation with minimal parameter updates. After finetuning, GPT-2 and Gemma achieve 96% classification accuracy on a held-out validation set, while DeepSeek achieves 93%.

Interchange Intervention Dataset: We curate subsets of the original RuleTaker dataset to assess model predictions and interchange intervention effectiveness. These datasets follow the format: *base prompt*, *override prompt*, *base answer*, *override answer*, *question*. The model is prompted with `<base> Question: <question > `. The *base answer* is the model's original response, while the *expected answer* is what it should output after a successful interchange intervention. Questions are designed based on the type of interchange intervention performed, where we have questions that check the base information is removed and questions that check whether the information from the

override prompt has been introduced. Here is an idealized example (without distractor sentences):

> **Base prompt:** Rabbit like squirrel. If something like squirrel then squirrel chase rabbit.
> **Override prompt:** Anne is young. If someone is quiet then they are young.
> **Question:** Squirrel chase rabbit?
> **Base Answer:** *True* **Override Answer:** *Unknown*

We design separate subsets targeting Conditional Rules and Universal Quantification.

4 Methodology

4.1 Interventions

Below we describe our interventions, which we use different terms for, even when they can be seen as special cases of each other.

For each of these interventions, we intervene on the residual blocks. In particular, we intervene on the output from one residual block component, which acts as the input to the next residual block. We do this because the combined effect of attention and MLP components are captured in the block output, and we want to intervene on a "macro" layer behaviour as opposed to smaller subcomponents of the layer.

Zeroing-out Intervention: (McGrath et al., 2023) Here we selectively replace token activations with zero. We perform two versions of this experiment, in one version, which we call *zero* (or necessity) intervention, a token activation z is zeroed out, and all other activations are left untouched. In a second version, which we call *non-zero* (or sufficiency) intervention, we leave a token activation z untouched, and zero out all other activations.

Interchange Intervention (Geiger et al., 2022) involves replacing the internal activation of the *base prompt* with that of the *override prompt* at a specific intervention layer and token position. Formally, let $\mathbf{z}_{\text{base},t}^{(l)}$ denote the output of the transformer block at layer l and token position t for the base prompt. We replace this with $\mathbf{z}_{\text{override},t}^{(l)}$ the corresponding activation from the override prompt and continue the forward pass using this modified representation.

This allows us to examine how information originating from the override prompt influences the model's response when introduced partway through computation on the base prompt. By performing interchange interventions across layers

$l = 0, 1, ..., L$, we identify which parts of the network are most responsible for reasoning over logical structures.

We use the NNsight library (Fiotto-Kaufman et al., 2024) to execute the interchange interventions.

Layer Swap Intervention: (Lad et al., 2025) We take the logit with the highest value, and check if it corresponds to True, False, or Unknown. We only considered datapoints where the model originally answers questions correctly, i.e. the logit for the correct class (True, False, Unknown) was highest. To do a layer swap intervention, we replace the entire layer activation of the intervention layer, with the entire activation of the swap layer.

4.2 Evaluation Metrics

Zeroing Out Accuracy After zeroing out tokens as described in Section 4.1, we obtain a predicted label by applying argmax over the output logits. Accuracy for each layer is computed as a fraction of samples for which predicted label matches the ground-truth label.

Interchange Intervention Accuracy (IIA) measures whether a model's response aligns with the expected outcome after an interchange intervention. For each input, we perform interchange intervention as defined in Section 4.1. The model is then queried with a follow-up question, and its answer is compared to the *expected answer* (i.e., the answer the model would give if it fully adopted the logic from the override prompt).

Let $y^{(i)}$ be the model's answer to the i-th intervened example, and let $\hat{y}^{(i)}$ be the corresponding *override answer*. Then IIA is defined as $\frac{1}{N} \sum_{i=1}^{N} \mathbf{1}_{[y^{(i)} = \hat{y}^{(i)}]}$, where $\mathbf{1}_{[\cdot]}$ is the indicator function and N is the number of examples.

This metric captures whether the interchange intervention successfully transfers logical structure from the override prompt into the base context. By computing IIA across layers, we identify where in the model such logical reasoning is most causally encoded.

Layer Swap Accuracy: We calculate the impact of the layer swap interchange intervention by taking the difference between the logit of the correct class (True, False, Unknown) when using the original layer's activations during inference, and the logit for the correct class when using the swapped activation during inference.

4.3 Intervention Targets

4.3.1 Punctuation Zeroing Out

targets are all the periods in a prompt, and/or the question mark in a prompt.

Punctuation Interchange Interventions targets are:

- **First Sentence**: For a base prompt, consider the first full sentence excluding the period. Swap the activations of that entire base sentence with those of an override.

- **First Period**: For a base prompt, consider the first period. Swap the activations at that period between a base sentence and an override sentence.

Let the base be *"Dave is nice. Fiona is grey. If someone is happy, they are cool."* and the override be *"Ben is purple. Adam is cool. All happy are sad."* In the first-period swap, we exchange the activation at the period following *"Dave is nice"* with that from the period after *"Ben is purple"*. We then ask a question derived from the override context, such as *"Is Ben purple?"* A correct response indicates that the information from the base context has been transferred via the period token — suggesting it acts as a summarization.

Conditional Statements This rule structure captures logical implication, typically in the form "If A, then B". For example, given the base sentence *"Dave is nice. If Dave is nice then he is happy."* and a override sentence *"Ram is cool. If Ram is cool then he is great."*, we replace the activation of the consequent token *"happy"* in the base with *"great"* from the override. We then query the model with *"Is Dave great?"* to see whether it adopts the altered consequent, effectively testing whether it continues to reason over the modified rule.

Universal Quantification This rule type involves generalized statements about all members of a category, typically structured as *"All [adjective] things are [predicate]"*. These constructions are common in both natural language and formal logic and require the model to generalize from an adjective-noun combination to a property.

To study this, we use a base sentence such as *"All blue things are nice."* and a override sentence like *"All green things are great."* We intervene by replacing the activation of the predicate token *"nice"* in the base with the corresponding token

Figure 1: Selectively either zeroing out period and question mark tokens or non-zeroing out only these tokens for GPT-2, DeepSeek and Gemma.

"great" from the override. We then query the model with "Are all blue things great?" to test whether it adopts the altered predicate and violates or preserves the original generalization.

Layer Swaps   target the activations of an entire prompt.

5   Results

5.1   Punctuation Analysis

Sufficiency of Periods and Question Mark   In Figure 1a, we selectively keep some tokens non-zero and zero out all other tokens for GPT2. Here we see that for later layers (layer 7 to 11) the performance remains high even when almost all tokens are zeroed out, as long as period and question tokens are non-zero. This means that the period and question mark tokens in these layers contain all information that is needed to answer the question, i.e. they are sufficient for answering the question.

Necessity of Periods and Question Mark   We also find in Figure 1d for GPT2, that when period and question mark are both zeroed out (and all other tokens are non-zero), the performance is dramatically low, which means these tokens are necessary for answering the question.

DeepSeek and Gemma.   For DeepSeek punctuation is sufficient in the first and last layer, and

necessary in the first. For Gemma punctuation is sufficient in layer 12, 15 and 17, but never both necessary and sufficient.

We further dissect these results for GPT2 below

Question Mark is Necessary and Sufficient in Some Layers   When question mark is the only non-zero token in layer 4 or in the last five layers (Figure 3b) performance is high, but when it is the only zeroed out token in layer 4 or the last five layers (Figure 3d) the performance is low. In contrast, period is necessary in layers 0 to 4 (Figure 3c), but not sufficient in those layers (Figure 3a).

Tokens Can "Dilute" Question Mark   In Figure 3b we find that if question mark is the only non-zero token in layer 4, then performance is high. However, we also find in Figure 3c that if period tokens are the only zero tokens (so in particular question mark is non-zero) in layer 4 then performance is low. We hypothesize that this is because the many other non-zero tokens in Figure 3c "dilute" the question mark token. We investigate this hypothesis in Figure 2. In this figure question mark is always nonzero, periods are always zero, and we respectively nonzero one in 15, one in 5, one in 2, four in 5 other tokens. We find that performance is high when question mark is one of the few nonzero tokens (see Figure 2a) and gradually

(a) One in 15   (b) One in 5   (c) One in 2   (d) Four in 5

Figure 2: Non-zeroing question mark and different proportions of extra tokens (while keeping periods zero) for GPT-2.

(a) Periods   (b) Question Mark

(c) Periods   (d) Question Mark

Figure 3: Selectively (non-)zeroing out either the period token activations or the question mark activation for GPT-2.

becomes lower as we increase the proportion of nonzero tokens.

Transfer from Period to Question Mark   We find that when period is non-zero in layer 7 (Figure 3a) or if question mark is non-zero in layers 7 to 11 (Figure 3b) then accuracy is high. We hypothesize this is because information can be "transferred" from period to question mark in layer 7.

First Full Sentence Interchange Intervention Accuracy (IIA)   For all three models we find in Figure 4 that when we perform interchange intervention on the first full sentence of the prompt, the IIA starts out high, and then dramatically decreases.

First Period IIA   The results shown in Figure 4, also indicate that for GPT-2 the IIA peaks in layer 4. DeepSeek shows a similar but more abrupt pattern, starting out at an IIA of just above 20%, remaining constant, suddenly peaking at layer 4 to around 60%, and then dropping to 20% again. Gemma, in contrast, shows negligible sensitivity to interchange interventions for first full period. In line with previous findings (Barbero et al., 2025), we hypothesize that this difference is related to the

context window size of the models: GPT-2 has the smallest window, followed by DeepSeek and then Gemma, or due to Gemma being a distilled model.

First Sentence IIA Drop Coincides with First Period Peak for GPT2 and DeepSeek   For GPT-2 the layer for which the IIA of the first period peaks coincides with the layer for which the IIA of the first sentence finishes its drop. The peak for first period at layer 4 for DeepSeek again coincides with a large drop for first sentence at layer 4. We hypothesize that in the first four layers information from the first sentence is "transferred" to the first period. This is corroborated by Figure 3c, where we find that periods contain important information in the first four layers. However, we would have expected the IIA to either be constantly high, or the zeroing out accuracy to gradually decrease across the first four layers. In Figure 6 in the appendix we find a similar pattern for second sentence and second period, but with a lower final IIA.

5.2   Reasoning Rules

Based on previous work (Sun et al., 2025; Yang et al., 2025) and before starting interchange intervention experiments on reasoning rules we had expected to see the model collecting information in early layers and applying reasoning rules in later layers. However, for GPT-2 our results instead show that similar to first sentence, second sentence, adjective and subject interventions (Figure 4 and Figure 6 in the appendix) intervening on reasoning rules leads to high IIA in the early layers and low IIA in later layers.

Conditional Statements   In Figure 4 we plot the IIA for conditional rules. This means that we take a sentence with "If x, then z" and replace the activations of the consequent z with the activations of z'. We find that GPT-2 has a high IIA in the first layer of around 50%, but this has drastically dropped by layer 6, where the IIA is around 5%, and the IIA remains low for all following layers. We interpret

Figure 4: Layer-wise sensitivity of GPT-2, DeepSeek, and Gemma to interchange interventions applied to different intervention targets (first sentence, first period, conditional statements, universal quantification). Each row represents an intervention target; each column corresponds to a model. When applying interchange intervention we take a sentence and replace a sentence component z with an alternative z' and check whether the model's response aligns with the response we would expect if z' was in the prompt, if so we say the IIA for this datapoint is 1, if not it is 0. See the Evaluation Metrics section for more details on how IIA is calculated and the Intervention Targets section for more details on the intervention targets.

this as the model actively processing information about the consequent (z or z') in the first 5 layers, but after that (from layer 6 onward), the activations in previous layers already determine which conse- quent the model works with. For DeepSeek and Gemma we find a similar pattern, but here the IIA respectively starts around 30% and 25%, and re- spectively drops around layer 4 and layer 7. We

Conditional Statements

(a) GPT-2   (b) DeepSeek   (c) Gemma

Universal Quantification

(d) GPT-2   (e) DeepSeek   (f) Gemma

Figure 5: Comparison of layer swap heatmaps across different language models. Each heatmap shows the correlation between layers when performing layer swapping experiments. Higher correlation values indicate that swapping those layers has minimal impact on model performance, while lower values suggest significant performance degradation.

find that proportionally DeepSeek processes the consequent very quickly, namely in 4 layers (out of 22), whereas GPT-2 has only completed processing the consequent after the middle layer.

Universal Quantification We plot the IIA for universal quantification in Figure 4. In a sentence like "All x are z", we replace the predicate z with z'. The surprising finding here is that for all models, the lowest IIA is still very high, around 40%. This means that for all layers replacing the predicate z with z' leads to the model answering as if the prompt said z' in 40% of the datapoints. In other words, the model does not "stop processing" the predicate after some layer (which is unlike how the models handled conditional rules).

IIA Drop for Conditional Statements Comparing adjective, subject, universal quantification and conditional statements, we find that conditional statements is the only intervention where the IIA drops to a very low point. Out of these universal quantification is the only target where the the IIA is constant for two models (DeepSeek and Gemma). We interpret this as the model revisiting the universal quantification in equal measure in every layer.

Layer Swaps In Figure 5 each entry represents the impact of a layer swap, where the x-axis represents the the layer we intervene on, and the y-axis represents layer we swap it with. The swap layer plot, see Figure 5, indicates that for conditional statements layers have specific functions, and can not replace each other, whereas for universal quantification layers are more replaceable. We speculate this may indicate that conditional statements are more difficult for the model to solve as compared to universal quantification.

6 Conclusion

We analyzed the importance of punctuation tokens ('.' and '?') through the lens of necessity and sufficiency for model performance. Our findings reveal stark model-specific differences: for GPT-2, punctuation is both necessary and sufficient in multiple layers, while this holds far less in DeepSeek and not at all in Gemma. We found that conditional statements and universal quantification are processed very differently across layers, suggesting distinct underlying inductive biases in how models learn to represent and perform reasoning.

7 Limitations and Future Work

We only do necessity and sufficiency investigations for punctuation. Future work could expand this investigation to other tokens and to a wider variety of models beyond GPT-2.

In intervention analysis we only did token level interventions per layer; more fine-grained intervention and subspace analysis would be valuable.

In our reasoning investigation we did part-of-sentence interventions, where we targeted the consequent or predicate in a prompt. Although we did find differences in IIA between different part-of-sentence targets, it is hard to know to what extent our results apply to syntactic processing of tokens in general, or to reasoning specifically. Future work could investigate swapping entire rules (for example "if then" statements with "if and only if then" statements).

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A Appendix

Feature	GPT2-small	DeepSeek	Gemma
Architecture	Decoder-only	Decoder-only	Decoder-only
LayerNorm position	Post-LN	Pre-LN	Pre-LN
Positional embeddings	Absolute	RoPE	RoPE
Attention mechanism	MHA	GQA/MQA	MHA
Residual connection	Sequential	Parallel	Parallel
Activation function	GeLU	SwiGLU	GeLU
Model size	124M	1.3B	2B
Context length	1k	16k	8k
Training objective	Next-token prediction	Next-token + multi-token	Knowledge distillation
Memory optimization	Standard	Speed + memory efficient	Knowledge distill. + memory

Table 1: Architectural comparison of language models used in our experiments. All models follow the decoder-only transformer architecture with key differences in normalization, attention mechanisms, and optimization strategies.

A.1 Reproducibility Statement

Our experiments were conducted using NVIDIA RTX 4090 GPUs. We evaluated a range of models across different families and sizes:

- **GPT-2 Small** (124M parameters) A fine-tuned version of OpenAI's GPT-2 model for patent claim generation, available under the MIT License: https://github.com/openai/gpt-2.

- **Gemma-2** (2B parameters) We used Gemma-2 2B released by Google DeepMind under the Gemma License: https://ai.google.dev/gemma/terms.

- **DeepSeek-Coder** (1.3B parameters) We used DeepSeek Coder 1.3B released by Hugging Face under the Apache 2.0 License: https://github.com/deepseek-ai/DeepSeek-Coder.

Approx. Hours	GPU	Model	Memory
25 h	NVIDIA RTX 4090	Various	200GB

Table 2: Approximate compute resources used for experiments.

Our datasets and model configurations are described throughout this paper and in the Appendix to support reproducibility.

Figure 6: Layer-wise sensitivity to logical rule and period token interchange interventions across GPT-2, DeepSeek, and Gemma. Each row represents a rule type; each column corresponds to a model.

B   Usage of AI

This work made limited use of AI-assisted tools for secondary support tasks in writing and code review. Perplexity was occasionally used to obtain stylistic or organizational suggestions when revising the paper, such as rephrasing sentences for clarity or improving paragraph flow. All conceptual framing, argumentation, and interpretation of results were developed and written by the authors. Claude was used as a code-review assistant to identify potential implementation issues and improve code readability in experimental scripts. All experimental design choices, data processing steps, and final implementations were authored, verified, and executed solely by the research team. No text, analysis, or data generated by AI systems was included without human verification, and no AI system contributed original research ideas or interpretations. The use of AI assistants in this project conforms to standard publication ethics and authorship policies, which state that AI tools may aid researchers but cannot be listed as authors or credited with intellectual contributions.

C   ACL Paper Checklist

C.1   For every submission

C.1.1   Did you discuss the *limitations* of your work?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section 6.1

C.1.2   Did you discuss any potential *risks* of your work?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: No

Justification: Our work does not shed light upon the adversarial usage of AI models for harm nor do our findings help adversarial users. Hence, we do not provide any potential risks.

C.1.3   Do the abstract and introduction summarize the paper's main claims?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Abstract and Section 1

C.2   Did you use or create *scientific artifacts*?

If you answer **Yes**, provide the section number; if you answer **No**, you can skip the rest of this section.

Answer: Yes

Justification: Section 3

If yes:

C.2.1   Did you cite the creators of artifacts you used?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section 3

C.2.2   Did you discuss the *license or terms* for use and/or distribution of any artifacts?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Appendix A.1

C.2.3   Did you discuss if your use of existing artifact(s) was consistent with their *intended use*, provided that it was specified? For the artifacts you create, do you specify intended use and whether that is compatible with the original access conditions (in particular, derivatives of data accessed for research purposes should not be used outside of research contexts)?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section 3

C.2.4 Did you discuss the steps taken to check whether the data that was collected/used contains any *information that names or uniquely identifies individual people* or *offensive content*, and the steps taken to protect / anonymize it?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: No

Justification: We reviewed the dataset details to check for offensive content. Our paper does not contain any offensive material, nor did we generate or use any such content. Additionally, no data used or presented reveals the identity of any individual.

C.2.5 Did you provide documentation of the artifacts, e.g., coverage of domains, languages, and linguistic phenomena, demographic groups represented, etc.?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: No

Justification: The datasets used are synthetic and focused on logical reasoning tasks. They do not involve human subjects or demographic information, so coverage of demographics, ethnicities, or other personal attributes is not applicable.

C.2.6 Did you report relevant statistics like the number of examples, details of train/test/dev splits, etc. for the data that you used/created?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section 3

C.3 Did you run *computational experiments*?

If you answer **Yes**, provide the section number; if you answer **No**, you can skip the rest of this section.

Answer: Yes
If yes:

C.3.1 Did you report the *number of parameters* in the models used, the *total computational budget* (e.g., GPU hours), and *computing infrastructure* used?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Appendix

C.3.2 Did you discuss the experimental setup, including *hyperparameter search* and *best-found hyperparameter* values?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section 3,4,5

C.3.3 Did you report *descriptive statistics* about your results (e.g., error bars around results, summary statistics from sets of experiments), and is it transparent whether you are reporting the max, mean, etc. or just a single run?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: No

Justification: Experiments for each model are deterministic given the same checkpoint and dataset so, reporting summary statistics such as error bars across runs is not applicable.

C.3.4 If you used existing packages (e.g., for preprocessing, for normalization, or for evaluation), did you report the implementation, model, and parameter settings used (e.g., NLTK, Spacy, ROUGE, etc.)?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section 3

C.4 Did you use *human annotators* (e.g., crowdworkers) or *research with human subjects*?

If you answer **Yes**, provide the section number; if you answer **No**, you can skip the rest of this section.

Answer: No
If yes:

C.4.1 Did you report the full text of instructions given to participants, including e.g., screenshots, disclaimers of any risks to participants or annotators, etc.?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: N/A

Justification: N/A

C.4.2 Did you report information about how you recruited (e.g., crowdsourcing platform, students) and paid participants, and discuss if such *payment is adequate* given the participants' demographic (e.g., country of residence)?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: N/A

Justification: N/A

C.4.3 Did you discuss whether and how *consent* was obtained from people whose data you're using/curating (e.g., did your instructions explain how the data would be used)?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: N/A

Justification: N/A

C.4.4 Was the data collection protocol *approved (or determined exempt)* by an ethics review board?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: N/A

Justification: N/A

C.4.5 Did you report the basic demographic and geographic characteristics of the *annotator* population that is the source of the data?

If you answer **Yes**, provide the section number; if you answer **No**, provide a justification.

Answer: N/A

Justification: N/A

C.5 Did you use *AI assistants* (e.g., ChatGPT, Copilot) in your research, coding, or writing?

If you answer **Yes**, provide the section number; if you answer **No**, you can skip the rest of this section.

Answer: Yes
If yes:

C.5.1

sectionIf you used any AI assistants, did you include information about your use? If you answer **Yes**, provide the section number or include your elaboration directly in the checklist response; if you answer **No**, provide a justification.

Answer: Yes

Justification: Section C