EAGER: Entropy-Aware GEneRation for Adaptive Inference-Time Scaling

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Abstract

With the rise of reasoning language models and test-time scaling methods as a paradigm for improving model performance, substantial computation is often required to generate multiple candidate sequences from the same prompt. This enables exploration of different reasoning paths toward the correct solution, however, allocates the same compute budget for each prompt. Grounded on the assumption that different prompts carry different degrees of complexity, and thus different computation needs, we propose EAGER, a training-free generation method that leverages model uncertainty through token-wise entropy distribution to reduce redundant computation and concurrently improve overall performance. EAGER allows branching to multiple reasoning paths only in the presence of high-entropy tokens, and reallocates the saved compute budget to instances where exploration of alternative paths is most needed. We validate EAGER across multiple open-source models on complex reasoning benchmarks, with gains specifically demonstrated on AIME 2025. When target labels are accessible – as in RLVR training pipelines – EAGER achieves up to +37% in Pass@k and 59% fewer tokens; in test-time settings it still yields +12% in Pass@k and 64% fewer tokens compared to FULL PARALLEL sampling.

1. Introduction

Recent advances in large language models (LLMs) have led to substantial improvements in complex reasoning tasks, particularly with the adoption of chain-of-thought (CoT) prompting (Wei et al., 2022). Such tasks often admit multiple valid reasoning paths that converge to the same correct solution (Stanovich & West, 2002). Rather than relying on a single greedy decoding path, the single generation can be replaced by multiple sampled candidate sequences, thereby producing a diverse set of reasoning paths and correspond-

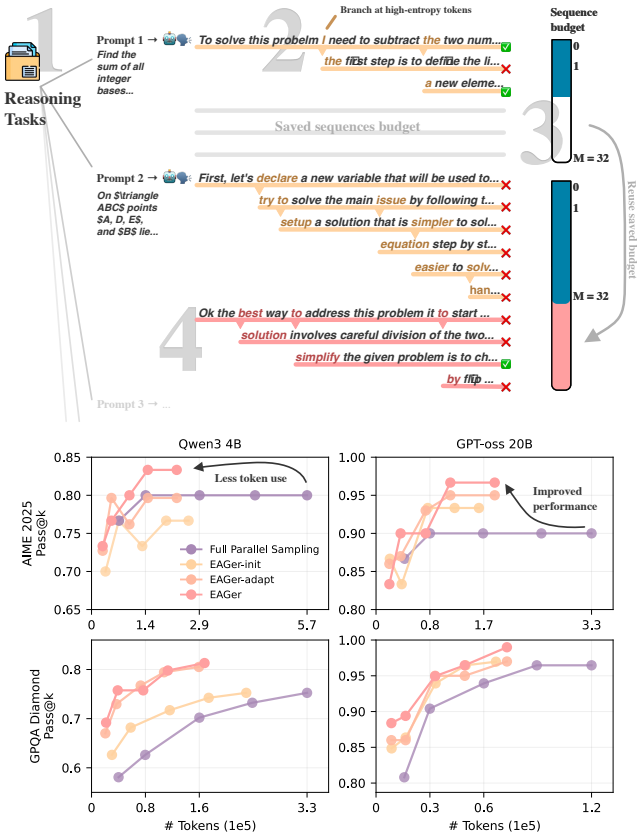

Figure 1. **Top:** We introduce EAGER, a generation method for (1) reasoning benchmarks: (2) decode and branch at high-entropy tokens; (3) cap each prompt at M candidates, yielding EAGER-init; and (4) carry forward unused budget and reallocate it either to prompts that hit the M cap, yielding EAGER-adapt, or, when target labels are available, to prompts that have not yet produced a correct solution (Pass@$k = 0$), yielding our full EAGER. **Bottom:** Our approaches (EAGER -init, -adapt, and full EAGER) consistently reduce token usage compared to the standard FULL PARALLEL sampling baseline when scaling the M limit to $M \in \{4, 8, 16, 24, 32\}$. In addition, EAGER consistently achieves a clear performance advantage over all other decoding methods.

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ing final answers (Wang et al., 2023). This strategy has been shown to enhance performance on challenging reasoning problems: by exploring multiple reasoning paths, the model reduces its reliance on the stochasticity of a single greedy generation and increases the likelihood of arriving at a correct solution.

Despite its success, CoTs introduce an inherent computational inefficiency: reasoning sequences tend to be long, and a large portion of the tokens generated are predictable continuations rather than genuine decision points (Wang et al., 2025). This inefficiency is amplified in approaches that explore multiple reasoning paths in parallel, where each path independently regenerates identical prefixes before diverging. For prompts with simple problems, many of these paths converge to the same solution with little variation, resulting in redundant computation. For more complex prompts, however, the diversity of reasoning paths becomes crucial, and additional generations may be necessary to discover a correct solution (Snell et al., 2025; Muennighoff et al., 2025). This observation suggests that a per-problem decision to let or not let the model explore alternative paths would be desirable. We argue that such decision can be guided by monitoring model uncertainty during generation towards an adaptive allocation of computating budget. Intuitively, when the model's predictions are confident and stable, only a few candidate sequences are needed, while at points of high uncertainty, where multiple reasoning paths are plausible, additional exploration becomes critical.

To address these issues, we introduce **EAGER**, an **Entropy-Aware Generation** method that monitors token-level uncertainty during decoding to guide where new parallel reasoning traces should start. By branching only at high-entropy tokens, we avoid regenerating identical low-entropy continuations, substantially reducing computation overhead without sacrificing coverage of diverse reasoning traces. Furthermore, reducing the parallel samples for *easy* prompts, EAGER dynamically allocates the unused sampling budget towards more challenging ones, maximizing the benefits of inference-time scaling for difficult prompts.[1]

We evaluate EAGER on a diverse set of benchmarks, spanning from complex math problems to science-related questions and code generation tasks. All the tested LMs, from the smallest 3B to the biggest 20B parameter model, show a performance boost of up to 37% when using EAGER compared to our baseline FULL PARALLEL sampling setting.

Our main contributions are as follows:

- We empirically show that token-wise entropy peaks as a form of online (i.e., measured during generation) uncertainty is a good proxy that shows when more exploration is needed during the generation, hence reflecting the difficulty of a prompt for the model used.
- We introduce, *a novel*, training-free decoding method that leverages entropy distribution during generation to dynamically reduce compute cost while maintaining the benefits of inference-time scaling. EAGER generates up to 65% fewer tokens and saves up to 80% of the entire generation budget across all our benchmarks and models.
- To maximize the benefits of inference-time scaling, we show that EAGER enables adaptive use of the given sampling budget, where it spends more compute on the *hard* problems. This yields up to 12% improvements in test-time settings without access to target labels, and up to 37% when labels are available, on the AIME 2025 reasoning benchmark.

2. Preliminaries

In the inference-time scaling paradigm, a language model generates multiple parallel sequences so that it can *explore* various reasoning paths to find a correct solution (Welleck et al., 2024; Snell et al., 2025). This is oftentimes facilitated by sampling completions from the model with a relatively high temperature using methods such as nucleus sampling (Holtzman et al., 2020). We refer to this standard approach as the FULL PARALLEL sampling generation procedure. This approach is useful in various settings, including for the generation of diverse solutions to a problem, or in large-scale reinforcement learning (RL) pipelines such as in RLVR (DeepSeek-AI, 2025), where among the diverse set of generated sequences, only the correct ones are selected to update the policy.

Our objective is to optimize this process by exploiting uncertainty during generation, allowing an efficient allocation of resources (in terms of number of generated sequences) to solve a given prompt.

2.1. Uncertainty in LLMs' Generations

Among the different techniques for uncertainty quantification in LLMs, we focus our attention on top-K token entropy, as token entropy has been shown to be a powerful uncertainty quantification measure (Fomicheva et al., 2020). We define top-K token entropy as:

$$H_t^{(K)} := -\sum_{i \in \mathcal{I}_t^{(K)}} p_{t,i}^{(K)} \log p_{t,i}^{(K)}, \tag{1}$$

where $\mathcal{I}_t^{(K)} \subseteq \{1, \ldots, |V|\}$ is the index set of the K tokens with highest $p_{t,i}$ probability with V denoting the vocabulary of the LM and $t \in \mathbb{N}^+$ indexes the current generation

[1] Code and data are available at https://github.com/DanielSc4/EAGer.

step. Specifically, the quantity $p_{t,i}$ represents the probability assigned by the model to token $i \in V$ at step t after the softmax computation. We denote $\mathcal{I}_t^{(K)} \subseteq \{1, \ldots, |V|\}$ the index set of the K tokens with the highest probability $p_{t,i}$ and $p_{t,i}^{(K)}$ their re-normalized probabilities, given by:

$$p_{t,i}^{(K)} := \frac{p_{t,i}}{\sum_{j \in \mathcal{I}_t^{(K)}} p_{t,j}}, \quad i \in \mathcal{I}_t^{(K)}, \tag{2}$$

where $\sum_{i \in \mathcal{I}_t^{(K)}} p_{t,i}^{(K)} = 1$.

Compared to more precise and computationally intensive uncertainty quantification methods found in the literature (Vashurin et al., 2025; Kuhn et al., 2023; Duan et al., 2024, e.g.,), top-K token entropy provides a strong approximation to the entropy of the full-vocabulary, as it computes the dominant contributions from the most probable tokens with minimal computational overhead [2].

2.2. Entropy in Long Chain-of-Thought Reasoning

For our goal of saving resources in parallel sampling by leveraging model uncertainty, we first need to determine whether and how token entropy values relate to the model's final performance. To this end, we analyze the entropy patterns of the CoT sequences generated by an LLM to solve challenging problems. We monitor the entropy of each token during generation, and rather than analyzing the entire entropy sequence, we focus on identifying significant spikes as signals of higher uncertainty. We hypothesize that this peak-entropy measure can serve as a proxy for the model's perceived difficulty of a problem and thus its (in)ability to solve it: high peaks indicate moments where the model is highly uncertain about the next step in its reasoning chain, low entropy indicates that the model is more confident about what to generate next.

Given the input prompt x, we sample M independent candidate sequences $\{t^{(m)}\}_{m=1}^{M}$ from the language model. During generation, for each token position t in each sequence m, we record the token entropy $H_t^{(K)}(y^{(m)})$, with $K = 20$. For each sequence, we define the peak entropy value $\bar{H}_{\text{peak}}^{(m)}$ as the mean of all entropy values that lie in the pth percentile of the sequence's entropy distribution:

[2]Full-vocabulary entropy computation can be costly due to large vocabulary sizes, often in the tens of thousands. We therefore compute entropy over only the top-$K = 20$ tokens, which provides a favorable trade-off between efficiency and fidelity: the top 20 tokens typically capture the vast majority of the probability mass, while excluding extremely low-probability logits that can introduce numerical noise and instability in entropy estimates.

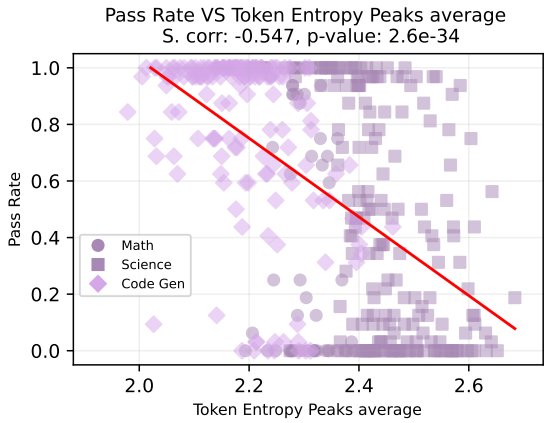

Figure 2. For each sequence generated by Qwen3 4B with FULL PARALLEL sampling ($M = 32$), we report its Pass Rate accuracy and the average entropy peak ($p^{\text{th}} = 99.9$) and plot this against prompt-level Pass Rate. The results reveal a negative correlation ($r = -0.547$) between Pass Rate and the average entropy peak across sequences. Notably, sequences exhibiting higher entropy at any generation step are less likely to yield a correct answer.

$$\bar{H}_{\text{peak}}^{(m)}(p^{\text{th}}) := \frac{1}{|\mathcal{T}_m^{\text{peak}}(p^{\text{th}})|} \sum_{t \in \mathcal{T}_m^{\text{peak}}(p^{\text{th}})} H_t^{(K)}(y^{(m)}), \tag{3}$$

where

$$\mathcal{T}_m^{\text{peak}}(p^{\text{th}}) := \{t : H_t^{(K)}(y^{(m)}) \geq p^{\text{th}}\left(\{H_{t'}^{(K)}(y^{(m)})\}_{t'}\right)\}, \tag{4}$$

and $p^{\text{th}}(\cdot)$ denotes the pth percentile of the entropy sequence.

We run Qwen3 4B[3], a strong open-source LLM with long CoT reasoning capabilities, on five standard reasoning benchmarks for math, science and code generation tasks (see Section 4 for the benchmarks' details), allowing for $M = 32$ parallel sequences to be generated.

Figure 2 shows the Pass Rate accuracy, i.e., the proportion of correct answers out of $M = 32$ generations, for each prompt and the corresponding average peak entropy $\bar{H}_{\text{peak}}^{(m)(p^{\text{th}})}$. We focus on the top percentile, specifically $p^{\text{th}} = 99.9$, to isolate the highest entropy peaks. We observe a statistically significant negative correlation ($\rho \approx -0.55$), between the peak entropy during generation and model Pass Rate accuracy. This suggests that higher entropy peaks, indicative of greater uncertainty during generation, are associated with lower performance. Thus, additional path exploration during these phases may help to improve performance. Conversely, when entropy remains low, the model is more confident on the generated solutions (hence, the long CoT reasoning sequences), suggesting that further exploration may be less

[3]https://huggingface.co/Qwen/Qwen3-4B

likely to yield significant improvements. This observation is in line with recent work which found that high-entropy tokens disproportionately contribute to performance gains during RL training (Wang et al., 2025).

Given this evidence, we ask: *Can token entropy be leveraged to develop a decoding adaptive strategy that allocates more compute to uncertain regions while limiting effort in more confident segments?*

3. Entropy-Aware GEneRation Explained

We introduce **EAGER**, a training-free inference-time scaling approach aimed at optimizing parallel sampling by leveraging token entropy to guide resource allocation. EAGER consists of two stages: in the first one, EAGER-init dynamically adjusts the generation process to focus on sequences where the most effort is needed, while pruning unnecessary generations. In the second stage, the saved computational budget is reallocated to enhance performance on the remaining challenging prompts.

3.1. EAGER-init: Save Compute via Token Entropy

EAGER-init represents the first stage of our approach and operates by identifying potentially *easy* questions during generation. Instead of sampling constant M generations for every prompt, EAGER-init computes token entropy $H_t^{(K)}$ at each step t, and compares it to a predefined threshold θ.[4] If the observed entropy exceeds this threshold, the current sequence is *branched*, creating a new candidate continuation at that position. If the entropy is below the threshold, the generation continues with the existing sequence. During the branching step, we reuse the token distribution from the model but adopt a temporally greedy approach; we select the top two most likely tokens to ensure that the two new sequences always start with different tokens. This process continues until the total number of active sequences reaches a predefined limit M, at which point no further branching occurs. A detailed overview of the EAGER-init algorithm is provided in Algorithm 1.

This process yields a generation tree where the root is the initial sequence, and each branching node corresponds to a high-entropy token (Figure 1); the generation stops when the total number of nodes is equal to M. For implementation efficiency, we restrict the branching procedure to long CoT sequences only, and entropy monitoring is halted if no branching has occurred within the previous 1000 tokens from the last branch.

Reducing test-time compute through EAGER-init. EAGER-init, saves computational budget through two mechanisms. The first arises directly from the branching logic: if a branch occurs at token position t, all preceding tokens $(0, \ldots, t-1)$ are reused across branches rather than being regenerated independently. The second, and more substantial source of savings occurs when the generation process does not saturate the maximum number of sequences M set per prompt. For easy queries, the model's default sampling converges to identical or near-identical completions, so that EAGER-init may terminate with only a single sequence, saving $M-1$ full generations compared to a fixed-budget baseline which would let the model generate M sequences for any given prompt. This surplus capacity can then be reallocated where it is most needed.

[4]We empirically find the best threshold for a model. See Section 4 for a detailed analysis of the threshold.

Algorithm 1 EAGER-init sequence generation

Require: Prompt x, threshold θ, max sequences M, temp. τ, top-K, max steps T
Ensure: Completed sequences $\mathcal{Y}$
  $\mathcal{A} \leftarrow \{y^{(1)}\}$; $\mathcal{Y} \leftarrow \varnothing$
  for $t = 1$ **to** T **do**
    if $\mathcal{A} = \varnothing$ **then**
      break
    end if
    for all $y \in \mathcal{A}$ **do**
      Compute $p(\cdot \mid x, y)$ with temperature τ
      Compute entropy $H_t^{(K)}$ from top-K probs
      if $H_t^{(K)} \geq \theta$ **and** $|\mathcal{A}| < M$ **then**
        $a_1 \leftarrow \arg\max_a p(a \mid x, y)$
        $a_2 \leftarrow$ second-most-likely token
        $y \leftarrow y \circ a_1$; create $y' \leftarrow y \circ a_2$
        Add y' to $\mathcal{A}$
      else
        Sample $a \sim p(\cdot \mid x, y)$; $y \leftarrow y \circ a$
      end if
      if y ends with EOS or length limit **then**
        Move y from $\mathcal{A}$ to $\mathcal{Y}$
      end if
    end for
  end for
  return $\mathcal{Y}$

3.2. EAGER: Dynamically Allocate the Saved Compute

The key challenge is to devise *the best strategy to reallocate the compute which has been saved*. We start by defining an additional budget b, computed as:

$$b_{\text{total}} = \min(M_{\text{theoretical}} - M_{\text{actual}}, 2M) \tag{5}$$

where $M_{\text{theoretical}} = M \times |\mathcal{D}|$ is the maximum possible number of sequences that could be generated for the dataset $\mathcal{D}$, and $M_{\text{actual}} = \sum_{i=1}^{|\mathcal{D}|} \#\,\text{Seq}_i$ is the total number of sequences actually produced under entropy-aware generation.

Algorithm 2 Full EAGER algorithm

Require: Dataset $\mathcal{D} = \{(x_i, z_i)\}_{i=1}^{N}$, generations $\{\mathcal{Y}_i\}$ from EAGER-init, max seq. M, threshold θ
Ensure: Augmented generations $\{\mathcal{Y}'_i\}_{i=1}^{N}$
  $M_{\text{theo}} \leftarrow M \cdot |\mathcal{D}|$; $M_{\text{act}} \leftarrow \sum_{i=1}^{N} |\mathcal{Y}_i|$
  $b \leftarrow M_{\text{theo}} - M_{\text{act}}$
  $\mathcal{I} \leftarrow \{i \mid \text{Pass@k}(\mathcal{Y}_i, z_i) = 0\}$
  if $b = 0$ **or** $\mathcal{I} = \varnothing$ **then**
    return $\{\mathcal{Y}_i\}$
  end if
  $b \leftarrow \min(b, 2M)$; distribute uniformly over $\mathcal{I}$
  for all $i \in \mathcal{I}$ **do**
    if $|\mathcal{Y}_i| < M$ **then**
      $\theta' \leftarrow 0.8 \cdot \theta$
    else
      $\theta' \leftarrow \theta$
    end if
    Generate up to $M + b$ seq. via Alg. 1 with θ'
    Append new sequences to $\mathcal{Y}_i$
  end for
  return $\{\mathcal{Y}'_i\}_{i=1}^{N}$

The term $M_{\text{theoretical}} - M_{\text{actual}}$ represents the surplus budget created by early stopping in *easy* prompts. We cap b_{total} at $2M$ to avoid pathological cases where extremely large surpluses would lead to disproportionately high generation budgets for single prompts.[5]

We consider two scenarios: (i) a test-time setting where target labels are unavailable and reallocation must rely solely on model signals, and (ii) a setting where target labels are accessible, as in reinforcement learning pipelines where only correct generations are used for policy updates.

Budget reallocation without target labels. In the absence of target labels, we identify *saturating prompts*, those that hit the maximum branching cap M, as candidates for additional budget. The rationale is that when M serves as a hard limit, promising reasoning paths may remain unexplored. To mitigate this, we reallocate saved budget exclusively to these prompts. We denote this strategy as EAGER-adapt.

Fine-grained budget reallocation with target labels. When target labels are available, we instead focus on *challenging prompts*, defined as those that fail to achieve Pass@k accuracy under EAGER-init (i.e., none of the generated sequences match the correct answer).

[5]Especially in larger datasets, budget savings for easy prompts were large enough to allocate hundreds, if not thousand, of additional sequences to single failing prompts; this cap prevents excessive unbalanced allocation.

For *underutilizing prompts* (fewer than M sequences under EAGER-init), we lower the entropy threshold θ by 20%, encouraging earlier and more frequent branching. For *saturating prompts* (exactly M sequences under EAGER-init), we extend generation up to a new per-prompt limit $M + b_i$ (equally distributed from the b_{total}), thereby deepening exploration where additional sequences may yield correct solutions.

Reallocation in this setting is uniform across all failing prompts, while the generation strategy adapts based on each prompt's prior behavior. By redirecting unused capacity from easier prompts to harder ones, this approach increases coverage without exceeding the global budget $M_{\text{theoretical}}$ (see Algorithm 2). Importantly, savings from branch-based token reuse persist even when $b > 0$, and all additional sequences remain governed by Algorithm 1, ensuring that total token usage stays below an equivalent fixed-budget FULL PARALLEL sampling baseline.

4. Experimental Setting and Results

Models. We evaluate multiple reasoning models from different model families and sizes to test EAGER in comparison to the FULL PARALLEL sampling baseline: SmolLM-3B (HuggingFaceTB, 2025), Qwen3-4B (Team, 2025), DeepSeek-R1-0528-Qwen3-8B (DeepSeek-AI, 2025) and GPT-oss 20B (OpenAI, 2025). Additional generation parameters and EAGER hyper-parameters are available in Appendix E.

Benchmarks. We evaluate our approach saved resources (compute metrics) for generation and performance on a set of diverse reasoning benchmarks on various tasks: AIME 2024 and 2025, and the 2025 Harvard MIT Math Tournament (Balunović et al., 2025) for math, GPQA-Diamond (Rein et al., 2023) for scientific domains, and HumanEval Plus (Liu et al., 2023; 2024) for code generation.

Compute metrics. We evaluate efficiency improvements using two complementary metrics: The first is the average **sequence Count** (#Seq). FULL PARALLEL sampling uses a fixed budget of M sequences, in contrast, EAGER uses a dynamic #Seq that depends on the branching behavior. The second metric is the average **token Count** (#Token) generated. While #Seq provides a general measure of computational efficiency, #Tokens is a more precise indicator since, branching at step t, reuses previously generated tokens $(0, \ldots, t-1)$ as prefix across new branches rather than regenerating them, that can lead to substantial savings even when #Seq is comparable.

Model	Sampling	AIME 2025			GPQA-Diamond			HumanEval Plus		
		p@k	c@k	PR	p@k	c@k	PR	p@k	c@k	PR
SmolLM 3B	FULL PARALLEL	0.53	0.00	0.06	0.49	0.00	0.03	–	–	–
	EAGER-INIT	0.43	0.23	0.26	0.59	0.10	0.15	**0.52**	**0.48**	**0.47**
	EAGER	**0.73**	**0.33**	**0.31**	**0.85**	**0.12**	**0.18**	–	–	–
Qwen3 4B	FULL PARALLEL	0.80	0.70	0.62	0.75	0.51	0.43	0.91	0.82	0.78
	EAGER-INIT	0.77	0.70	0.61	0.79	0.51	0.43	0.86	0.79	0.80
	EAGER	**0.83**	**0.73**	**0.69**	**0.81**	**0.59**	**0.54**	**0.93**	**0.86**	**0.86**
DeepSeek 8B	FULL PARALLEL	**0.80**	0.67	0.65	**0.95**	0.15	0.18	0.95	0.90	0.86
	EAGER-INIT	0.73	0.60	0.59	0.93	0.25	0.24	**0.96**	0.85	0.77
	EAGER	**0.80**	**0.70**	**0.68**	0.94	**0.26**	**0.33**	**0.96**	**0.91**	**0.90**
GPT-Oss 20B	FULL PARALLEL	0.90	**0.83**	0.67	0.96	0.68	0.65	0.95	0.83	0.79
	EAGER-INIT	**0.93**	0.80	0.67	0.97	**0.71**	**0.66**	**0.97**	**0.88**	0.82
	EAGER	**0.93**	**0.83**	**0.69**	**0.98**	0.68	**0.66**	**0.97**	**0.88**	**0.83**

Table 1. Comparison of FULL PARALLEL, EAGER-INIT and EAGER in AIME-2025, GPQA-Diamond and HumanEval Plus. We report pass@k, cons@k and Pass Rate where k is number of samples generated (while always 32 for the baseline, differs per prompt for EAGER-init and EAGER). EAGER consistently achieves the best results and EAGER-init performs very competitive with FULL PARALLEL sampling while saving significant amount of compute as shown in Figure 3.

Performance metrics. We evaluate performance using three complementary metrics. **Pass@k** shows whether the model produces at least one correct final solution, **Cons@k** aggregates responses through majority voting across k generations. Lastly, **Pass Rate** measures the proportion of correct answers over all generated outputs. We report the average metric across each entire benchmark.

Threshold selection trade-off between performance and compute. The entropy threshold θ is the only hyperparameter of EAGER and directly shapes the efficiency-performance trade-off: lower thresholds encourage more frequent branching, increasing both # Seq and # Tokens, while higher thresholds restrict branching, yielding fewer continuations at lower cost. Because top-K entropy peaks concentrate in a narrow band (see Figure 2 and Section 2.2), the effective range is small: we sweep $\theta \in [1.8, 2.7]$ and find consistent efficiency improvements over FULL PARALLEL sampling throughout. To avoid per-benchmark tuning, we adopt a unified protocol: for each model, we select θ using only 10 examples from MATH-500 as a calibration set, and apply the selected value *unchanged* across all benchmarks, including out-of-distribution tasks (HumanEval Plus, GPQA-Diamond). The resulting per-model thresholds are reported in Table 7. We additionally verify that this protocol is robust to the choice of validation set: across 30 runs sampling the 10-example validation set from MATH-500, GSM8K, and ZebraLogic, 27 (90%) recover the identical threshold (see Appendix B). This stability is consistent with entropy distributions being primarily model-dependent rather than task-dependent. The full sweep is reported in Appendix A for transparency.

4.1. Results

EAGER-init and EAGER yield significant savings in computation. Figure 3 (top row) illustrates the efficiency advantages of EAGER-init and EAGER across all benchmarks and model scales. Starting with EAGER-init, the total number of generated tokens is typically less than half of that required by FULL PARALLEL sampling. Building on this, EAGER (and EAGER-adapt) leverages a small fraction of the saved budget to further improve accuracy, while still generating substantially fewer sequences than FULL PARALLEL sampling. On the performance side, EAGER consistently achieves higher Pass Rate accuracy than FULL PARALLEL sampling, indicating superior performance per unit of computation. It is worth noting that the performance of SmolLM 3B is nearly 0.0 across all metrics in the parallel-sampling setting. This is caused by the generation of sequences in which the same tokens are repeatedly produced (e.g., "The answer is: The answer is: The ..."). This effect, along with the effect of temperature is discussed in Appendix D.

Saturation is a good proxy for budget reallocation. In the absence of target labels, EAGER-adapt reallocates additional budget to saturating prompts as a proxy for identifying challenging cases. Table 2 reports results across all benchmarks and models. On average, this strategy not only achieves substantial token savings during generation, but also improves exploration, yielding higher Pass@k compared to the FULL PARALLEL sampling baseline. In other words, EAGER-adapt saves a large fraction of compute while at the same time uncovering more successful reasoning paths.

For comparison, Table 2 also reports the full EAGER approach. While it benefits from the unfair advantage of access to target labels, redirecting budget to saturating sequences

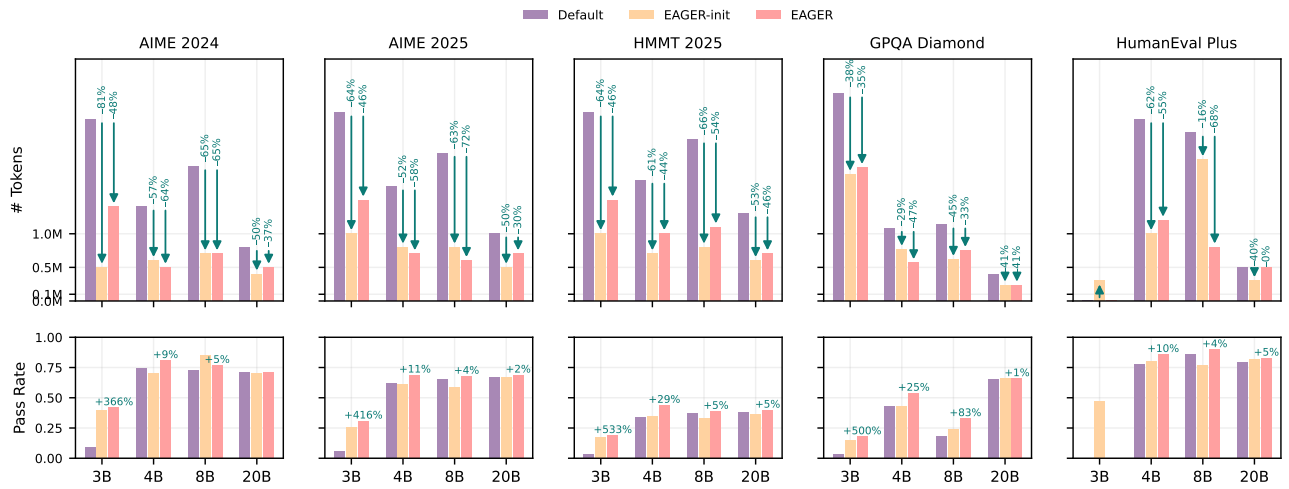

Figure 3. Compute and performance trade-offs of EAGER-init and EAGER. Across all benchmarks and model size, the efficiency of EAGER-init and EAGER consistently outperforms FULL PARALLEL sampling, requiring only half as many tokens in most cases (top). In addition, they achieve higher pass rate accuracy (bottom). For issues specific to the smallest 3B model, see Appendix D.

Data		SmolLM 3B FP	SmolLM 3B EAGER init	SmolLM 3B EAGER adapt	SmolLM 3B EAGER full	Qwen3 4B FP	Qwen3 4B EAGER init	Qwen3 4B EAGER adapt	Qwen3 4B EAGER full	DeepSeek 8B FP	DeepSeek 8B EAGER init	DeepSeek 8B EAGER adapt	DeepSeek 8B EAGER full	GPT-Oss 20B FP	GPT-Oss 20B EAGER init	GPT-Oss 20B EAGER adapt	GPT-Oss 20B EAGER full
AIME 2024	↑ p@k	0.60	0.57	0.63	**0.67**	0.90	0.80	0.85	0.87	**0.93**	0.90	**0.93**	0.90	0.93	0.90	0.95	**1.00**
	↓ # T	27	**5**	18	14	14	**6**	**6**	**6**	20	**7**	8	**7**	8	**4**	5	5
AIME 2025	↑ p@k	0.53	0.43	0.60	**0.73**	0.80	0.77	0.80	**0.83**	**0.80**	0.73	**0.80**	**0.80**	0.90	**0.93**	0.93	**0.93**
	↓ # T	28	10	**15**	**15**	17	8	9	**7**	22	8	9	**6**	10	**5**	6	7
HMMT 2025	↑ p@k	0.23	0.23	0.37	**0.40**	0.50	0.43	0.57	**0.60**	**0.57**	0.43	0.47	0.50	0.63	**0.67**	**0.67**	**0.67**
	↓ # T	28	10	**15**	**15**	18	**7**	13	10	24	**8**	11	11	13	**6**	7	7
GPQA-Dia.	↑ p@k	0.49	0.59	0.76	**0.85**	0.75	0.79	0.79	**0.81**	0.95	0.93	0.93	**0.94**	0.96	0.97	**0.98**	**0.98**
	↓ # T	185	**113**	130	119	65	46	48	**34**	68	**37**	39	45	24	**14**	**14**	**14**
HE-Plus	↑ p@k	0.00	0.52	0.68	**0.75**	0.91	0.86	0.92	**0.93**	0.95	**0.96**	**0.96**	**0.96**	0.95	**0.97**	**0.97**	**0.97**
	↓ # T	161	**3**	24	**20**	27	**10**	12	12	25	21	23	**8**	5	**3**	5	5

Table 2. Reallocation of the additional budget (EAGER-adapt) only on Saturating prompts (i.e., prompts that reach $M = 32$ generated sequences). All experiments use model-dependent thresholds reported in Table 7 found to provide a good balance between number of tokens (# T $\times$ 1e5) used and performance (p@k) on the MATH-500 calibration subset. **Bold** are best results, underline second best.

still achieves the second-best performance in most settings.

EAGER always achieves better performances than FULL PARALLEL sampling. As shown in Figure 3, EAGER consistently outperforms FULL PARALLEL sampling in terms of Pass Rate. Table 1 shows a more comprehensive overview using Pass@k, Cons@k, and Pass Rate. While Pass@k is highest under EAGER, Pass Rate is consistently equal or better even for EAGER-init compared to FULL PARALLEL sampling. This suggests that EAGER-init effectively prunes unproductive generations (higher Pass Rate) at the cost of reduced exploration (lower Pass@k). In general, Pass@k is particularly useful in scenarios where obtaining at least one correct answer is critical, for example, when the user prioritizes correctness and exploration over efficiency as per in Reinforcement Learning applications. In contrast, Pass Rate and Cons@k capture a different dimension of quality: (i) higher values indicate that EAGER focuses computation more effectively on promising generations, and (ii) given the extreme efficiency gains of EAGER-init compared to FULL PARALLEL sampling, the trade-off is often strongly favorable.

EAGER scales effectively under budget constrains. We evaluate the effect of scaling the maximum number of allowed generations, M, on overall performance. As shown in Figure 4, increasing M improves the probability of obtaining at least one correct solution (Pass@k). This trend is expected, as a larger generation budget naturally enables more extensive exploration. Notably, EAGER-init – and even more so EAGER – achieve superior Pass@k under the same constraints, often with significantly fewer tokens. In other words, EAGER not only benefits from larger M but also allocates its computational budget more efficiently, resulting in a consistent shift of the Pareto frontier, where higher accuracy is achieved at lower token cost.

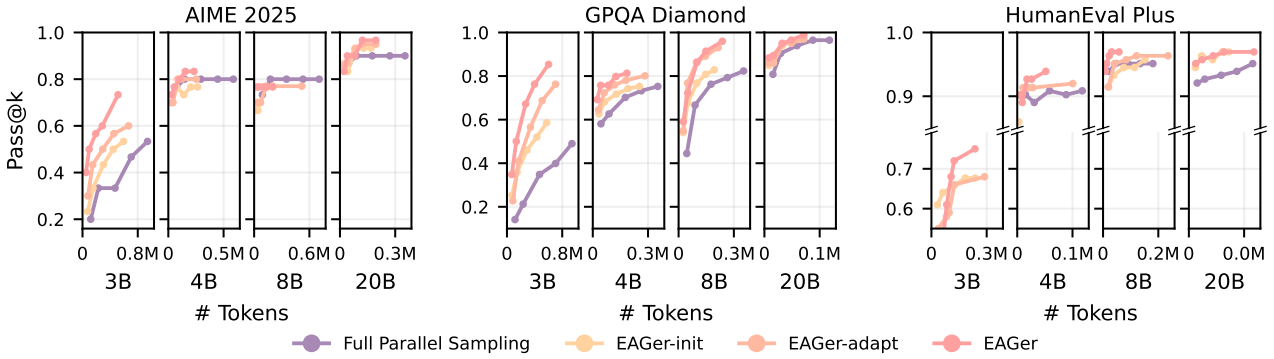

Figure 4. Performance comparison with scaling the total allowed sequences for generating ($M \in \{1, 4, 8, 16, 24, 32\}$). As M increases (line's markers), EAGER consistently improves Pass@k (y-axis) while reducing the number of tokens needed to find the correct solution (x-axis), further shifting the Pareto frontier of the performance–efficiency trade-off.

5. Related Works

Since the recent introduction of test-time scaling (Snell et al., 2025; Welleck et al., 2024), multiple approaches have been proposed to improve its efficiency and performance. (Wu et al., 2025) propose REBASE (REward BAlanced SEarch) a branching method that expands reasoning trajectories that are evaluated as being of high quality by a reward model. While powerful, REBASE is significantly more computationally expensive compared to directly computing token entropy at test-time. DeepConf (Deep Think with Confidence, Fu et al., 2025) is a method that also leverages local confidence measures to increase performance and efficiency during generation. DeepConf uses this confidence measure to truncate sequences where it is lower than a predefined threshold (determined during a warm-up stage). The combination of this warm-up stage and the truncation of non-promising sequences results in a theoretical token usage that is greater than in our proposed approach, where the certainty measure drives branching instead of truncation.

In Appendix C, we provide a detailed empirical comparison between our approach, DeepConf, and the ESC method (Li et al., 2024). ESC adopts a token-saving strategy based on generating in small sequential windows and halting early when all trajectories converge to the same final answer, thereby reducing unnecessary continuation.

We note additional works on uncertainty estimation such as Kang et al. (2025) which introduces *self-certainty*, a sequence-level measure closely related to cross-entropy. The authors demonstrate that self-certainty discriminates well between correct and incorrect answers and is robust to reasoning length. The authors additionally illustrate that self-certainty driven answer selection (through a voting mechanism) leads to improvements in reasoning benchmarks. While the the current work is closely related to the work by Kang et al., we demonstrate that token-level certainty (in contrast to sequence-level) can function as a useful tool to modulate performance and efficiency in reasoning LLMs.

6. Conclusion and Future Directions

By leveraging token-level entropy, EAGER-init proves to be a highly performant training-free generation method with significantly higher efficiency compared to FULL PARALLEL sampling. In applications such as RLVR, where the correct answer is known, EAGER surpasses the Pass@k performance by up to 37% compared to FULL PARALLEL sampling while using up to 65% fewer tokens. Even without a verifier at test time, EAGER-adapt improves exploration, surpassing FULL PARALLEL sampling performance while generating up to 40% fewer tokens. In both cases, the methods demonstrate the ability to *save large amounts of compute and simultaneously enhance exploration*. Finally, we show that the approaches are domain (math, science and coding) and temperature (see Appendix D) agnostic.

While our current work uses token-level entropy to create branching reasoning streams, future research could explore other methods for quantifying uncertainty. For example, using Kullback-Leibler (KL) Divergence to measure token uncertainty is a promising direction, inspired by the work of (Kang et al., 2025). At the same time, a key consideration is that the uncertainty quantification method must be lightweight, as a computationally expensive approach would undermine the goal of improving generation efficiency.

Limitations

While EAGer delivers consistent gains in efficiency and performance, several limitations should be acknowledged. First, the full EAGer variant relies on the availability of target labels to identify failing prompts for budget reallocation. This restricts its direct applicability to settings with verifiable answers, such as math, code, and RLVR pipelines,

while open-ended reasoning tasks would require an external verifier or reward model to enable the same fine-grained reallocation. The label-free variants (EAGer-init and EAGer-adapt) do not suffer from this constraint.

Second, EAGer introduces one hyperparameter, the entropy threshold θ, which must be selected per model. While our protocol shows that this can be done robustly using only 10 validation examples and transfers across in-distribution and OOD benchmarks (§4), it still represents a small upfront cost that fully training-free baselines such as FULL PARALLEL sampling do not incur. We note, however, that the selected thresholds are highly consistent across the models we tested (Table 7), although further testing is needed to verify whether this consistency holds for much larger models.

Along the same line, our evaluation focuses on verifiable reasoning tasks across math, science, and code generation, spanning models from 3B to 20B parameters. Whether the entropy-guided branching principle generalizes to substantially larger models, agentic settings, or non-verifiable open-ended generation remains an open question that we leave to future work.

Impact Statement

This paper presents work whose goal is to advance the field of Machine Learning, specifically improving the efficiency of inference-time scaling for reasoning language models. By reducing the computational cost of generating high-quality reasoning traces, EAGER lowers the resource barrier for running large language models on complex tasks, potentially making capable AI reasoning more accessible to researchers and practitioners with limited compute budgets. The primary societal benefit is therefore a reduction in the energy and infrastructure costs associated with test-time scaling workloads. We note that EAGER is a general-purpose generation method and does not introduce new capabilities beyond those of the underlying models it is applied to; any ethical considerations associated with reasoning language models themselves apply equally here. We see no additional ethical concerns specific to this work that must be highlighted.

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A. Complete Results

Table 3 presents a complete overview of the results of our experiments.

B. Threshold Selection Robustness

The unified threshold protocol described in Section 4 selects θ for each model using a small validation set of 10 examples drawn from MATH-500, and applies the resulting value unchanged across all benchmarks. A natural concern is whether this protocol is robust to the choice of validation source: if a different validation benchmark would yield a substantially different threshold, then the method would still implicitly require choosing a suitable validation set, partially negating its practicality.

To test this, we run the threshold-selection procedure under three different validation sources, chosen to span a wide range of task characteristics:

- **MATH-500**: difficult competition-style math problems, in-domain with respect to our math benchmarks.
- **GSM8K**: grade-school math problems, considerably easier than MATH-500.
- **ZebraLogic**: logic-puzzle reasoning, completely out-of-domain with respect to the benchmarks used in the main paper.

For each source, we randomly sample five different 10-example validation sets and run threshold selection on Qwen3-4B for both EAGer-init and the full EAGer variant. This yields $3 \times 5 \times 2 = 30$ independent selection runs.

Table 4 reports the selected thresholds across all 30 runs. In 27 out of 30 runs (90%), the selection procedure recovers the identical threshold to the one used in our main experiments, regardless of validation source. The only deviations are a single GSM8K run for EAGer-init (selecting $\theta = 2.1$ instead of 2.0) and a single MATH-500 run for full EAGer (selecting $\theta = 2.1$ instead of 2.5).

C. Related Approaches

We include results for the AIME 2025 benchmark comparing several approaches: ESC (Li et al., 2024), a sampling method designed to reduce token usage relative to FULL PARALLEL sampling; and DeepConf, the concurrent work of Fu et al. (2025), which estimates the model's confidence in its generated sequence and terminating generation when that confidence falls below a threshold. We report these results in Table 5.

We also include an additional metric, wall-clock time, to highlight the practical impact of these approaches. This metric serves only as a broad overall comparison within the context of these experiments, as wall-clock time is highly sensitive to system configuration and environmental conditions and is not fully isolated from external factors.

Implementation-wise, we adopt ESC using the original authors' default parameters. We set the number of windows per generation to 8 and the maximum budget to $M = 32$. For DeepConf, we use its online variant, which provides the best performance and is the closest to the intended use cases of both their and our proposed sampling approaches. The online variant includes a per-prompt warm-up stage, which we count toward the reported Pass Rante and the total number of generated tokens. We also set its maximum budget to $M = 32$, matching our setup and the other baselines.

Table 5 clearly shows that our strongest method (full EAGER) outperforms every baseline and related approach. However, we exclude full EAGER from direct comparison and instead highlight the best results among all other methods in **bold**. This exclusion is necessary because full EAGER has an inherent and unfair advantage having access to target labels. Under fair comparison, EAGER-adapt emerges as the strongest overall approach, striking a near-optimal balance between performance (Pass@k and Pass Rate) and efficiency (number of tokens generated, # T) across all models.

We also note that ESC exhibits significantly higher wall-clock times compared not only to both our approach and DeepConf but also FULL PARALLEL sampling. This is a direct consequence of its design: ESC relies on small sequential windows and repeatedly evaluates intermediate results to decide whether to continue to the next window, up to the full budget M. While this approach does reduce token usage relative to FULL PARALLEL sampling, it severely restricts parallelization, resulting in considerably slower overall execution.

More broadly, our *branch-and-reuse* strategy provides consistent advantages for several reasons: (i) it reuses previously generated tokens, (ii) avoids producing multiple sequences when the model is already *confident*, (iii) requires no warm-up

stage (unlike DeepConf-online) and (iv) KV-cache reloading has negligible overhead at the scale of our long generations, as evidenced by the wall-clock results. Empirically, we achieve comparable or superior performance across similar settings. We also observe that for easier prompts (where Pass Rate ≈ 1, i.e., all generated answers are identical and correct), our method saves substantial tokens by generating only one or two branches. In contrast, DeepConf – relying solely on confidence estimates – often judges the model confident enough to generate all 32 sequences, leading to fully redundant token generation.

D. Effect of Temperature

The temperature hyperparameter, τ, plays a critical role during autoregressive decoding by scaling the logits used by the sampling method (decoding becomes more greedy as $\tau \to 0$). In this section, we conduct a short exploration on the effect of temperature on EAGER. This is especially important in the current context, where a higher diversity among the generated sequences can intuitively have an effect on the performance metrics. For this exploration, we focus on two LLMs, SmolLM 3B & DeepSeek 8B, two temperature settings, $\tau \in \{0.6, 0.9\}$ and AIME 2025 as the evaluation dataset. Furthermore, we conduct the analysis for varying entropy threshold levels $\theta \in \{2.0, 2.2, 2.3, 2.4, 2.4, 2.5\}$.

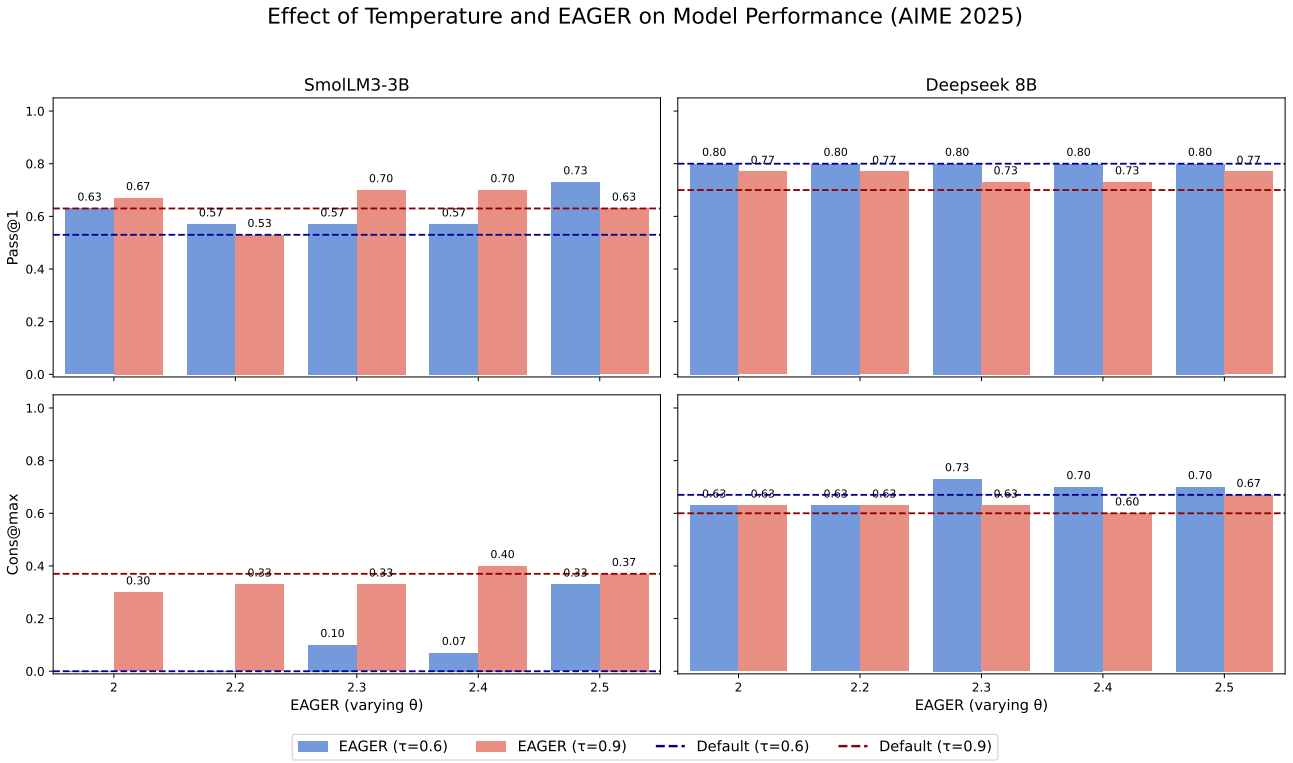

Figure 5. Pass@k and Cons@k at low ($\tau = 0.6$) and high($\tau = 0.6$) temperature settings. Horizontal lines show the performance for the default sampling method, while the bars show EAGER's performance for varying entropy threshold levels θ.

As shown in Figure 5, SmolLM 3B generally performs best at the high temperature setting while the opposite is true for DeepSeek 8B. Importantly, at both temperature levels, EAGER is competitive with the corresponding default baselines, often surpassing them. A direct comparison between the low and high temperature setting including all metrics for default, EAGER and EAGER-init generations is presented in Table 6.

Notably, the performance of SmolLM 3B is particularly higher in the high temperature setting when measured by the Cons@max rate. We find that this is a result of the reduction of generations in which the same tokens are repeatedly produced (e.g., "The answer is: The answer is: The ..."). Specifically, in the high temperature setting, this phenomenon occurs, on average, 59.1% less compared to the low temperature setting. This behaviour was only observed with SmolLM 3B, suggesting it results from the smaller model size. An exception arises with the HumanEval Plus benchmark, where SmolLM 3B failed to solve any tasks, resulting in all metrics being zero under the FULL PARALLEL sampling setting. In

contrast, EAGER-init and EAGER appeared to partially mitigate this issue.

Lastly, we also find that the temperature has an effect on the number of tokens generated which, by extension, impact performance. For example, when EAGER is used at the high temperature setting, Deepseek 8B generates, on average, less than half the number of tokens compared to the low temperature setting. In contrast, SmolLM3-3B generates more tokens at the high-temperature setting. In both cases, and in line with the test-time scaling paradigm, we find that higher performance is achieved in whichever temperature setting more tokens are generated.

E. Generation Parameters

All models are used with their longest thinking configuration to get their best performances. Furthermore we limit their context window to 32k tokens. All sequences are generated with a temperature of $\tau = 0.60$ and a top-p of 95%. The effect of temperature is discussed in Appendix D. Table 7 reports the thresholds used for each benchmark and model. Following the discussion in Section 4, we select thresholds independently based on their intended use. The EAGER-init sampling method is designed to save budget without significantly compromising performance (lower threshold), whereas EAGER aims to preserve as much performance as possible for later reuse, higher threshold are preferred in such scenario.

θ	SmolLM3-3B ↑p@1	SmolLM3-3B ↑c@32	SmolLM3-3B ↑PR	SmolLM3-3B ↓# T	SmolLM3-3B ↓# S	Qwen3-4B ↑p@1	Qwen3-4B ↑c@32	Qwen3-4B ↑PR	Qwen3-4B ↓# T	Qwen3-4B ↓# S	Deepseek 8B ↑p@1	Deepseek 8B ↑c@32	Deepseek 8B ↑PR	Deepseek 8B ↓# T	Deepseek 8B ↓# S	GPT-oss 20B ↑p@1	GPT-oss 20B ↑c@32	GPT-oss 20B ↑PR	GPT-oss 20B ↓# T	GPT-oss 20B ↓# S
AIME 2024 (math)																				
—	0.60	0.03	0.09	27	32.0	**0.90**	**0.80**	0.74	14	32.0	**0.93**	0.80	0.73	20	32.0	0.93	0.80	0.71	8	32.0
2.0	0.53	0.03	0.10	18	28.8	0.80	0.73	0.70	6	15.3	0.90	**0.87**	**0.85**	7	15.8	0.93	0.77	0.70	**4**	30.7
2.2	0.53	0.10	0.15	18	28.4	0.70	0.67	0.68	1	1.7	0.80	0.80	0.79	2	4.5	0.90	0.80	0.70	**4**	29.7
2.3	0.52	0.10	0.18	17	26.8	0.67	0.67	0.65	0.3	**1.0**	0.77	0.77	0.76	0.4	1.3	0.90	0.80	0.68	**4**	30.2
2.4	0.67	0.20	0.25	14	22.7	0.77	0.77	0.77	1	**1.0**	0.70	0.70	0.70	**0.3**	**1.0**	0.93	0.83	**0.75**	**4**	27.6
2.5	0.57	**0.50**	0.40	**5**	**16.5**	0.73	0.73	0.73	**0.2**	**1.0**	0.73	0.73	0.73	**0.3**	**1.0**	0.90	0.83	0.69	**4**	**28.0**
2.0	0.73	0.10	0.13	19	32.0	**0.90**	**0.80**	0.74	9	23.4	**0.93**	**0.87**	**0.85**	9	20.0	0.93	0.77	0.70	5	32.0
2.2	0.73	0.10	0.16	19	32	0.87	0.77	0.76	5	11.3	0.90	0.80	0.80	5	12.0	0.93	0.83	0.71	5	32.2
2.3	**0.83**	0.17	0.18	19	33.0	**0.90**	**0.80**	0.75	5	12.4	0.87	0.83	0.81	5	10.1	0.93	0.80	0.68	5	32.1
2.4	0.77	0.20	0.28	19	32.8	0.83	**0.80**	0.79	5	10.5	0.90	0.80	0.78	6	13.0	0.97	0.83	**0.75**	5	32.0
2.5	0.67	**0.50**	**0.42**	14	31.3	0.87	0.83	**0.81**	5	10.7	0.90	0.77	0.77	7	14.0	**1.00**	**0.87**	0.71	5	32.0
AIME 2025 (math)																				
—	0.53	0.00	0.06	28	32.0	0.80	0.70	0.62	17	32.0	**0.80**	0.67	0.65	22	32.0	0.90	**0.83**	0.67	10	32.0
1.8	-	-	-	-	-	0.77	0.70	0.60	0.90	24.5	-	-	-	-	-	-	-	-	-	-
2.0	0.53	0.00	0.05	19	28.8	0.77	0.70	0.61	8	18.4	0.73	0.60	0.59	8	17.4	0.90	**0.83**	0.66	5	31.1
2.2	0.43	0.00	0.07	19	29.9	0.67	0.63	0.64	1	3.1	0.70	0.63	0.64	2	4.9	0.93	0.80	0.67	5	30
2.3	0.37	0.10	0.14	17	27.8	0.60	0.60	0.60	**0.3**	1.1	0.70	0.67	0.66	1	2.2	0.93	0.73	0.64	5	31.4
2.4	0.53	0.07	0.11	17	27.6	0.70	0.70	0.70	**0.3**	1.1	0.63	0.60	0.61	0.5	**1.2**	0.93	0.80	0.66	5	29.8
2.5	0.43	0.23	0.26	**10**	**17.5**	0.60	0.60	0.60	**0.3**	**1.0**	0.63	0.60	0.61	**0.4**	**1.2**	0.90	**0.83**	**0.69**	5	26.1
2.0	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
1.8	-	-	-	-	-	0.80	0.70	0.63	13	32.8	-	-	-	-	-	-	-	-	-	-
2.0	0.63	0.00	0.06	20	32.0	0.83	0.73	0.63	12	30.0	**0.80**	0.63	0.63	12	28.0	0.90	**0.83**	0.66	5	32.0
2.2	0.57	0.00	0.08	20	32.0	0.80	0.70	0.70	6	14.7	**0.80**	0.63	0.68	7	16.1	**0.97**	0.80	0.68	5	32.9
2.3	0.57	0.10	0.15	19	32.1	0.80	**0.77**	0.71	8	17.5	**0.80**	0.73	**0.71**	6	13.1	0.93	0.73	0.64	5	32.2
2.4	0.67	0.07	0.13	19	32.2	0.80	0.73	0.71	5	10.7	**0.80**	**0.70**	0.68	7	15.3	0.93	0.80	0.66	6	33.0
2.5	**0.73**	**0.33**	**0.31**	15	33.6	**0.83**	0.73	**0.69**	7	15.0	**0.80**	**0.70**	0.68	6	14.0	0.93	**0.83**	**0.69**	7	32.0
HMMT (math)																				
—	0.23	0.00	0.03	28	32.0	0.50	0.37	0.34	18	32.0	**0.57**	**0.43**	0.37	24	32.0	0.63	0.53	0.38	13	32.0
1.8	0.23	0.03	0.06	20	31.7	0.43	0.37	0.33	10	22.7	-	-	-	-	-	-	-	-	-	-
2.0	0.33	0.03	0.07	20	30.8	0.43	0.37	0.35	7	15.5	0.43	0.37	0.33	8	18.1	**0.70**	0.43	0.37	**6**	31.9
2.2	0.23	0.00	0.06	18	28.5	0.37	0.37	0.36	1	3.3	0.40	0.37	0.38	3	6.2	0.67	0.43	0.36	**6**	32.0
2.3	0.27	0.10	0.12	17	27.5	0.40	0.40	0.40	1	2.3	0.40	0.40	0.35	2	4.7	0.63	0.47	**0.40**	**6**	30.9
2.4	0.27	**0.17**	0.18	14	23.8	0.33	0.33	0.33	0.4	1.1	0.37	0.37	0.35	1	1.5	0.63	0.43	0.38	**6**	30.8
2.5	0.23	**0.17**	0.17	**10**	**17.4**	0.43	**0.43**	0.43	**0.3**	**1.0**	0.37	0.37	0.37	**0.4**	**1.1**	0.67	**0.53**	**0.40**	**6**	30.5
2.0	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
1.8	0.27	0.03	0.06	20	32.0	0.47	0.37	0.33	15	32.9	-	-	-	-	-	-	-	-	-	-
2.0	**0.40**	0.03	0.09	20	32.0	0.53	0.37	0.36	14	32.0	**0.57**	0.40	0.35	15	32.1	**0.70**	0.43	0.37	**6**	32.0
2.2	0.33	0.00	0.06	19	32.0	0.53	0.37	0.37	11	24.5	**0.57**	**0.43**	**0.43**	13	27.5	n/a	n/a	n/a	n/a	n/a
2.3	0.33	0.10	0.13	19	32.0	0.57	0.40	0.41	10	22.6	0.53	**0.43**	0.38	11	24.0	0.67	0.47	**0.40**	7	32.0
2.4	**0.40**	**0.17**	**0.19**	17	32.2	0.50	0.40	0.37	11	25.2	**0.57**	**0.43**	0.39	11	24.0	0.63	0.43	0.38	7	32.0
2.5	**0.40**	**0.17**	**0.19**	15	32.7	**0.60**	**0.43**	**0.44**	10	21.9	0.50	0.37	0.39	11	23.5	0.67	**0.53**	**0.40**	7	32.0
GPQA-Diamond (science)																				
—	0.49	0.00	0.03	185	32.0	0.75	0.51	0.43	65	32.0	0.95	0.15	0.18	68	32.0	0.96	0.68	0.65	24	32.0
2.0	0.68	0.04	0.09	137	30.8	0.79	0.51	0.43	46	26.8	0.93	0.25	0.24	37	28.5	0.93	**0.72**	**0.66**	**13**	29.7
2.2	0.62	0.07	0.11	130	30.0	0.71	0.47	0.43	38	22.1	0.91	0.18	0.22	33	25.0	0.97	0.71	**0.66**	14	27.6
2.3	0.61	0.02	0.07	133	30.7	0.64	0.49	0.43	23	14.7	0.81	0.21	0.18	23	17.4	0.95	0.66	0.65	14	30.9
2.4	0.61	0.06	0.10	126	29.8	0.56	0.45	0.44	12	7.4	-	-	-	-	-	0.94	0.70	**0.66**	14	25.8
2.5	0.59	0.10	0.15	**113**	**27.6**	0.49	0.46	0.45	**3**	**2.5**	0.66	0.20	0.21	**4**	**3.1**	0.95	0.68	0.65	**13**	**24.0**
2.0	0.79	0.04	0.09	137	32.0	**0.85**	0.51	0.43	59	32.4	0.96	0.25	0.26	43	32.5	**0.99**	**0.72**	**0.66**	15	32.3
2.2	0.81	0.07	0.12	132	32.0	0.81	0.50	0.45	55	32.4	**0.97**	0.18	0.25	43	33.8	0.98	0.71	**0.66**	15	29.9
2.3	0.75	0.03	0.09	135	32.0	0.81	0.53	0.47	44	27.3	**0.97**	0.25	0.25	46	35.4	0.97	0.66	0.65	14	30.9
2.4	0.79	0.08	0.12	128	32.0	0.81	0.51	0.50	37	22.4	-	-	-	-	-	**0.99**	0.70	**0.66**	15	29.9
2.5	**0.85**	**0.12**	**0.18**	**119**	32.1	0.81	**0.59**	**0.54**	34	19.9	0.94	**0.26**	**0.33**	45	35.6	0.98	0.68	**0.66**	14	27.3
HumanEval Plus (code)																				
—	0.00	0.00	0.00	161	32.0	0.91	0.82	0.78	27	32.0	0.95	0.90	0.86	25	32.0	0.95	0.83	0.79	5	32.0
1.8	-	-	-	-	-	0.87	0.76	0.76	16	9.9	0.95	0.82	0.79	18	25.0	-	-	-	-	-
2.0	0.04	0.01	0.01	94	30.7	0.86	0.79	0.80	10	6.20	0.96	0.85	0.77	21	23.0	0.96	0.88	0.83	4	24.7
2.2	0.04	0.01	0.01	65	26.3	0.86	0.86	0.86	1	1.1	0.94	0.86	0.83	13	14.0	**0.97**	0.88	0.82	**3**	23.3
2.3	0.68	0.46	0.44	33	17.3	0.84	0.82	0.82	0.5	1.1	0.87	0.82	0.80	6	7.4	0.93	0.81	0.74	**3**	22.8
2.4	0.52	0.37	0.38	13	9.0	0.81	0.81	0.81	0.5	1.1	0.92	0.88	0.88	3	3.5	**0.97**	0.88	**0.85**	**3**	20.3
2.5	0.52	0.48	0.47	**3**	**2.6**	0.82	0.82	0.82	**0.4**	**1.0**	0.88	0.87	0.86	**1**	**1.5**	0.95	0.86	0.82	**3**	**18.6**
1.8	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
2.0	-	-	-	-	-	**0.94**	0.79	0.82	17	11.2	0.97	0.77	0.74	22	24.7	**0.97**	0.89	0.84	5	29.3
2.2	-	-	-	-	-	0.92	0.86	**0.87**	9	5.7	0.96	0.87	0.83	15	15.9	**0.97**	0.88	0.82	5	29.0
2.3	-	-	-	-	-	0.92	**0.87**	0.86	11	9.9	**0.98**	0.88	0.86	13	16.9	**0.97**	**0.90**	0.84	5	28.8
2.4	**0.75**	**0.52**	**0.56**	20	19.3	**0.94**	**0.87**	0.86	12	10.9	0.97	0.90	0.89	8	8.5	**0.97**	0.89	**0.85**	5	26.4
2.5	-	-	-	-	-	0.93	0.86	0.86	12	11.8	0.96	**0.91**	**0.90**	8	9.3	**0.97**	0.88	0.83	5	27.2

Table 3. All models, benchmarks and entropy-thresholds θ configurations. Higher is better for Pass@k (p@k), Cons@k (c@32) and Pass Rate (PR); lower is better for # Token. # Token are in 1e5 unit. Results for FULL PARALLEL sampling generations, EAGER-init generations, and full EAGER. **Bold** is best overall, underline is best within each category always including the FULL PARALLEL sampling one.

Table 4. Robustness of threshold selection on Qwen3-4B across three validation sources. For each (source, variant) pair, the 10-example validation set is sampled 5 times. We report the selected threshold and the number of runs (out of 5) that produced it.

Validation source	EAGer variant	Selected threshold (across 5 runs)
MATH-500	init / adapt	5/5 $\rightarrow \theta = 2.0$
MATH-500	full	4/5 $\rightarrow \theta = 2.5$, 1/5 $\rightarrow \theta = 2.1$
GSM8K	init / adapt	3/5 $\rightarrow \theta = 2.0$, 2/5 $\rightarrow \theta = 2.1$
GSM8K	full	5/5 $\rightarrow \theta = 2.5$
ZebraLogic	init / adapt	5/5 $\rightarrow \theta = 2.0$
ZebraLogic	full	5/5 $\rightarrow \theta = 2.5$

Model	AIME 2025 metric	Baseline	Related Works		Our		
		FULL PARALLEL	ESC	DeepConf	EAGER-INIT	EAGER-adapt	EAGER
SmolLM 3B	↑ Pass@k	0.53	0.53	**0.63**	0.53	**0.63**	0.73
	↑ Pass Rate	0.06	0.05	0.26	0.26	**0.28**	0.31
	↓ # Tokens (1e5)	28	28	22	19	**15**	15
	↓ Wall-clock time	∼11h	∼60h	∼8h	∼**4.5h**	∼6h	∼8h
Qwen3 4B	↑ Pass@k	**0.80**	**0.80**	**0.80**	0.77	0.80	0.83
	↑ Pass Rate	0.62	0.63	**0.68**	0.60	**0.68**	0.69
	↓ # Tokens (1e5)	17	11	15	**8**	12	12
	↓ Wall-clock time	∼12h	∼25h	∼10h	∼**5h**	∼8h	∼9h
DeepSeek 8B	↑ Pass@k	**0.80**	**0.80**	**0.80**	0.73	0.77	0.80
	↑ Pass Rate	0.65	0.66	**0.70**	0.59	0.68	0.71
	↓ # Tokens (1e5)	22	13	19	**8**	13	12
	↓ Wall-clock time	∼27h	∼40h	∼24h	∼**10h**	∼15h	∼16h
GPT-Oss 20B	↑ Pass@k	0.90	0.90	0.93	0.90	**0.95**	0.97
	↑ Pass Rate	0.67	**0.69**	0.68	0.66	0.68	0.68
	↓ # Tokens (1e5)	10	7	7	5	**5**	5
	↓ Wall-clock time	∼29h	∼30h	∼20h	∼**13.5h**	∼**13.5h**	∼17h

Table 5. Results on the AIME 2025 benchmark comparing the baseline, related approaches (ESC and DeepConf), and our proposed variants. We report Pass@k, Pass Rate, number of generated tokens, and wall-clock time. **Bold** values indicate the best performance among all fair-comparison methods, excluding full EAGER, which has access to ground-truth labels at test time.

	SmolLM3-3B										Deepseek 8B									
θ	Low Temperature ($\tau = 0.6$)					High Temperature ($\tau = 0.9$)					Low Temperature ($\tau = 0.6$)					High Temperature ($\tau = 0.9$)				
	↑ p@1	↑ c@32	↑ PR	↓ # T	↓ # S	↑ p@1	↑ c@32	↑ PR	↓ # T	↓ # S	↑ p@1	↑ c@32	↑ PR	↓ # T	↓ # S	↑ p@1	↑ c@32	↑ PR	↓ # T	↓ # S
-	0.53	0.00	0.06	**28**	32.0	**0.63**	**0.37**	**0.25**	44	32.0	**0.80**	**0.67**	**0.65**	22.0	32.0	0.70	0.60	0.57	**7.8**	32.0
2.0	0.53	0.00	0.05	**19**	**28.8**	**0.67**	**0.30**	**0.25**	26	31.0	0.73	0.60	**0.59**	8.0	**17.4**	**0.77**	**0.63**	0.58	**3.2**	22.7
2.2	0.43	0.00	0.07	**19**	**29.9**	**0.53**	**0.37**	**0.25**	27	30.9	0.70	**0.63**	**0.64**	2.0	**4.9**	0.70	0.60	0.58	**1.9**	11.3
2.3	0.37	0.10	0.14	**17**	**27.8**	**0.57**	**0.33**	**0.26**	26	29.9	**0.70**	**0.67**	**0.66**	1.0	**2.2**	0.57	0.53	0.53	**0.7**	4.4
2.4	0.53	0.07	0.11	**17**	27.6	**0.60**	**0.40**	**0.32**	22	**25.8**	**0.63**	**0.60**	**0.61**	**0.5**	**1.2**	0.57	0.53	0.53	0.7	4.0
2.5	0.43	0.23	0.26	**10**	**17.5**	**0.50**	**0.37**	0.26	21	24.7	0.63	0.60	0.61	0.4	**1.2**	0.63	0.60	0.61	**0.3**	2.0
2.0	0.63	0.00	0.06	**20**	32.0	**0.67**	**0.30**	**0.25**	27	32.0	**0.80**	0.63	**0.63**	12.0	**28.0**	0.77	0.63	0.58	**4.4**	30.2
2.2	**0.57**	0.00	0.08	**20**	32.0	0.53	**0.33**	**0.25**	28	32.0	**0.80**	0.63	**0.68**	7.0	**16.1**	0.77	0.63	0.62	**3.5**	21.0
2.3	0.57	0.10	0.15	**19**	32.1	**0.70**	**0.33**	**0.27**	28	32.1	**0.80**	**0.73**	**0.71**	6.0	**13.1**	0.73	0.63	0.63	**3.2**	21.1
2.4	0.67	0.07	0.13	**19**	32.2	**0.70**	**0.40**	**0.33**	29	**32.0**	**0.80**	**0.70**	**0.68**	7.0	**15.3**	0.73	0.60	0.59	**3.1**	18.9
2.5	**0.73**	0.33	**0.31**	**15**	33.6	0.63	**0.37**	0.29	29	**32.4**	**0.80**	**0.70**	**0.68**	6.0	**14.0**	0.77	0.67	0.66	**2.4**	**14.9**

Table 6. AIME 2025 results for default, EAGER-init, and EAGER generations for low and high temperature τ and varying entropy threshold θ. Best results per temperature and threshold setting are marked in **boldface**.

Model	EAGER-init	EAGER
SmoLM 3B	2.5	2.5
Qwen3 4B	2.0	2.5
DeepSeek 8B	2.0	2.5
GPT-oss 20B	2.2	2.5

Table 7. Best thresholds selected per model using 10 questions from the held-out calibration set from MATH-500.