Correcting Mean Bias in Text Embeddings:
A Refined Renormalization with Training-Free Improvements on MMTEB

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Abstract

We find that current sentence-embedding models produce outputs with a consistent bias: every embedding e decomposes as $\tilde{e} + \mu$, where the mean μ is near-identical across all sentences. We study two training-free corrections—subtracting μ directly (R1), or projecting each embedding off the mean direction (R2)—and show, via a first-order error-propagation argument, that R2 cancels the parallel component of mean-estimation error that R1 retains. Across 38 models on the Massive Multilingual Text Embedding Benchmark (MMTEB) (Enevoldsen et al., 2025), R2 yields consistent classification gains (paired $\bar{t} = 3.31$, 29 of 38 models with $t > 2$, zero losses), and the per-model mean norm $\|\mu\|$ correlates with which models benefit most. A nine-method dose-response ablation on five models further reveals that mild single-direction removal helps, but full principal component analysis (PCA) whitening hurts every model we test, and that R2 and All-but-the-Top with depth one agree within 0.18 pp downstream despite weak geometric alignment between $\hat{\mu}$ and the centered top principal component.

1. Introduction

Text representation collapse (embedding collapse) has recently received increasing attention. The cone effect has been observed in language models (Ethayarajh, 2019; Gao et al., 2019; Cai et al., 2021; Liu et al., 2026) and CLIPs (Liang et al., 2022; Yi et al., 2025), and has been shown to be inherent to the self-attention mechanism it-

self (Godey et al., 2024), where text embeddings cluster within a narrow cone in high-dimensional space. A similar phenomenon has also been observed in text embedding models (Liang et al., 2025), where the embeddings are concentrated, more precisely, near the boundary of the cone. This phenomenon leaves most regions of the representation space underutilized, undermining the model's expressive power and robustness (Liang et al., 2025; Li et al., 2024).

Apply any modern sentence-embedding model $\mathcal{E}$ to a large diverse corpus, average the outputs, and the result is far from zero. We find that that the mean embedding $\mu = \mathbb{E}_{t \sim \mathcal{D}}[\mathcal{E}(t)]$ is large, model-specific, and nearly unchanged across languages and prompts, according to the experimental evidence in Appendix E. This suggests that the bias μ is an intrinsic property of the text embedding model.

We further study whether removing this shared component, training-free, improves downstream performance, and *when* it does so. These post-processing corrections sit within a long lineage of fixes for anisotropic representations (Arora et al., 2017; Mu & Viswanath, 2018; Li et al., 2020; Su et al., 2021; Huang et al., 2021; Chen et al., 2023; Fuster Baggetto & Fresno, 2022; Mickus et al., 2024). Let $\hat{\mu} = \mu / \|\mu\|$. Two natural variants are: (**R1**) subtract μ and renormalize; (**R2**) remove the projection of e onto $\hat{\mu}$ and renormalize:

$$\text{R1: } e' = \frac{e - \mu}{\|e - \mu\|}, \qquad \text{R2: } e' = \frac{e - (e \cdot \hat{\mu})\hat{\mu}}{\|e - (e \cdot \hat{\mu})\hat{\mu}\|}. \quad (1)$$

Geometrically, R2 removes only the component of e along $\hat{\mu}$ before renormalizing. R2 is also closely related to the All-but-the-Top (ABTT) baseline of Mu & Viswanath (2018), which removes the top principal components of the centered embedding distribution. The two coincide exactly when the dominant direction of variation in centered embeddings is $\hat{\mu}$ itself; in practice, as we will show, the two methods are nearly indistinguishable downstream even when they are geometrically distinct.

We test three falsifiable hypotheses on the Massive Multilingual Text Embedding Benchmark (MMTEB) (Enevoldsen et al., 2025; Muennighoff et al., 2023):

- **H1 (R2 > R1).** R2 outperforms R1, as predicted by the error-propagation argument.

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- **H2 ($\|\mu\|$ predicts benefit).** The per-model classification benefit of R2 grows with $\|\mu\|$.

- **H3 (Goldilocks gradient).** More aggressive anisotropy removal is *not* monotonically better; full principal component analysis (PCA) whitening will not dominate single-direction removal.

We treat $\|\mu\|$ as a *post-hoc* diagnostic throughout—the panel was expanded toward high-$\|\mu\|$ models after early observations, not prospectively calibrated.

Our contributions are:

1. A first-order error-propagation argument (Appendix A) predicting R2 > R1, confirmed across 38 MMTEB models: R2 wins retrieval in 35/38 models, and classification in 29/38 with zero losses.

2. $\|\mu\|$ as a cheap, post-hoc diagnostic: per-model classification t correlates with $\|\mu\|$ at Pearson $r = 0.72$ (full panel, 95% CI [+0.47, +0.86]).

3. A nine-method dose-response ablation on five models ($\|\mu\| \in [0.19, 0.85]$): single-direction removal helps, but full PCA whitening hurts every model we test ($\Delta \in [-5.18, -0.64]$ pp). R2 and ABTT-1 agree within 0.18 pp downstream despite $\cos(\hat{\mu}, \mathrm{PC1}_{\mathrm{centered}}) \in [0.03, 0.51]$.

Relevance to mechanistic interpretability. We characterize μ as an output-space feature—we do not localize it to internal circuits. However, two findings are relevant to future mechanistic accounts: (i) $\hat{\mu}$ is largely invariant across languages and prompts (Appendix E), so it is a coherent encoder feature rather than a sampling artifact; (ii) the non-monotone dose-response (Section 4) is consistent with prior work (Mickus et al., 2024) arguing that some anisotropy preserves useful structure: if all variance were harmful, whitening would dominate single-direction removal. Section 5 discusses limitations.

2. Method

Notation. Let $\mathcal{E}$ be a unit-norm text-embedding model with output $e \in \mathbb{R}^d$, $\|e\| = 1$ for almost all inputs (we verify this for 28/29 models we audit; see Appendix C). For a corpus $\{t_i\}_{i=1}^N$ we estimate the mean $\mu = N^{-1} \sum_i \mathcal{E}(t_i)$ and write $\hat{\mu} = \mu/\|\mu\|$. Throughout this paper we estimate $\hat{\mu}$ from $N = 10^5$ English Wikipedia sentences (snapshot `20220301.en`) with character lengths in $[64, 512]$; the same corpus is used to fit centered PCA components for the ABTT and whitening baselines, with no task labels.

R2 dominates R1 under estimation noise (sketch). We always estimate μ from a finite sample, so the estimator

carries an error ϵ that decomposes orthogonally with respect to the true mean direction: $\epsilon = \epsilon_\parallel + \epsilon_\perp$, with $\epsilon_\parallel = (\epsilon \cdot \hat{\mu})\hat{\mu}$. Under the high-dimensional near-orthogonality assumption $\tilde{e} \cdot \mu \approx 0$ and for $\|\epsilon\| \ll \|\mu\|$, a first-order expansion (Appendix A) yields

$$\tilde{e}_1 = \tilde{e} - \epsilon_\parallel - \epsilon_\perp, \qquad \tilde{e}_2 \approx \tilde{e} - \epsilon_\perp. \tag{2}$$

Up to leading order, R2 cancels $\epsilon_\parallel$ while R1 retains both components. The argument predicts lower first-order sensitivity of R2 to parallel mean-estimation error; the size and source of downstream gains remain empirical.

Effect-size statistic and aggregation. For a (model, family) cell with n tasks we report the conventional paired t-statistic over per-task deltas as our primary metric. We use $|t| > 2$ as the win/tie/loss (W/T/L) threshold in tables; this is a per-cell effect-size window, not a Bonferroni-controlled significance level. Family-level aggregates take the unweighted mean over models with at least five tasks in the family. The 38-model audit and the 9-method ablation use different MMTEB snapshots and disjoint task-tracking, so per-row deltas in Table 2 should be compared only within row, not numerically pooled with Table 1. (Appendix B discusses an amplified secondary metric σ_{cell} that we report alongside the conventional t in supplementary tables.)

3. Main Results: 38-Model Audit

We evaluate R1 and R2 on 38 embedding models from 15 organizations on MMTEB (Enevoldsen et al., 2025; Muennighoff et al., 2023), an earlier snapshot, with 609 to 624 tasks per model after filtering for modality mismatch / failures / timeouts (full task list in Appendix R). We do not run ABTT-1 on the full 38-model panel; the headline classification numbers and the $\|\mu\|$-correlation below should therefore be read as evidence for *single-direction correction* (whether implemented as R2 or as ABTT-1) relative to the unprocessed control and to R1, not as a claim that R2 outperforms a well-implemented baseline at scale. The head-to-head R2 vs ABTT-1 comparison within a 5-model intersection is reported in Table 2. Per-task scores are paired before and after applying the post-processing. Because the panel was preferentially expanded toward $\|\mu\| \geq 0.5$ after early observations, the win counts below reflect performance in the intended high-$\|\mu\|$ regime, not an unbiased estimate over the population of MMTEB-leaderboard embedding models.

Aggregate effects (Table 1). R2 produces consistent gains in classification: paired $\bar{t} = 3.31$ on the full 38-model panel, with 29 models passing $t > 2$ and zero losses. The result is robust to family removal: dropping the five Snowflake-arctic-embed models leaves $\bar{t} = 3.25$ over the remaining 33 models with 24 wins and zero losses. Retrieval is more

Table 1. R2 effect across 38 MMTEB models, by task family. Paired t is the average of per-(model, family) cell t-statistics; W/T/L counts how many models pass $t > 2$, sit within ± 2, or fall below -2. **Classification (bold row) is the cleanest signal and survives removing the Snowflake family.** Retrieval is positive but Snowflake-dominated.

Family	#tasks	Full panel (38)		Excluding Snowflake (33)	
		$\bar{t}$	W/T/L	$\bar{t}$	W/T/L
Retrieval	182	+2.99	22/12/4	+1.99	17/12/4
Classification	**323**	**+3.31**	**29/9/0**	**+3.25**	**24/9/0**
Other	119	+1.55	12/26/0	+0.85	7/26/0

positive on the full panel ($\bar{t} = 2.99$) but is family-sensitive, dropping to $\bar{t} = 1.99$ when Snowflake is removed; we therefore report retrieval as a secondary, family-sensitive finding rather than a headline. R2 outperforms R1 on retrieval in 35 of 38 models and on classification in 23 of 38 models, consistent with the outcome-level prediction of H1. Within the 5-model intersection of Table 2, R2 and ABTT-1 agree within 0.18 pp on every model, suggesting a similar behavioral footprint rather than a quantitative dominance claim; we position R2 as a transparent, single-vector, PCA-free implementation of single-direction correction with an explicit error-propagation handle (Eq. 2) and a one-scalar $\|\mu\|$ diagnostic.

$\|\mu\|$ correlates with classification benefit (Figure 1). Per-model classification t shows a strong positive relationship with $\|\mu\|$: Pearson $r = +0.72$ on the full panel (95% bootstrap CI $[+0.47, +0.86]$) and $r = +0.76$ excluding the Snowflake family ($[+0.53, +0.88]$); Spearman $\rho = +0.61$ and $+0.69$ respectively. Across $\|\mu\|$ quartiles $[0, 0.3)/[0.3, 0.6)/[0.6, 0.75)/[0.75, 1.0)$ the mean classification t grows monotonically. Computing $\|\mu\|$ from 10^5 sentences is cheap relative to MMTEB evaluation (one forward pass over a fixed corpus, parallelizable), so the quantity is a candidate pre-deployment diagnostic; the high-$\|\mu\|$-biased panel cannot estimate the false-positive or false-negative rate of any threshold rule. We emphasize that the $\|\mu\| \geq 0.5$ regime is identified *post hoc*; we have not held out a separate set of models on which to validate a prospective threshold (H2).

Panel-selection caveat. The 38-model panel is not a uniform sample. After early observations suggested that classification benefit correlates with $\|\mu\|$, we preferentially added MMTEB-leaderboard models with $\|\mu\| \geq 0.5$, which biases the panel toward the helpful regime. The single deliberately-included low-$\|\mu\|$ model is all-MiniLM-L6-v2 ($\|\mu\| = 0.19$). We disclose this upfront and report Snowflake-free numbers throughout. The inflation also bears on the retrieval headline: roughly four-fifths of the cumulative retrieval effect on the panel is contributed by the five Snowflake models (Appendix J).

Figure 1. Mean-vector norm $\|\mu\|$ vs. R2 classification paired t, 38 MMTEB models. Pearson $r = +0.72$ on the full panel (95% bootstrap CI $[+0.47, +0.86]$) and $r = +0.76$ excluding Snowflake (CI $[+0.53, +0.88]$); Spearman $\rho = +0.61/ + 0.69$. Snowflake-arctic-embed models are marked separately (red triangles). The dashed line marks the $t = 2$ threshold; OLS lines are descriptive. Models above the dashed line are classification "wins" under R2.

4. Goldilocks Ablation: Nine-Method Comparison

To test whether more aggressive anisotropy removal is monotonically better, we run a 9-method dose-response ladder on 5 representative models spanning $\|\mu\| \in [0.19, 0.85]$: control, R1, R2, ABTT-$\{1, 2, 3\}$, mean-centering only (mc), random-direction removal (rand, seed 42), and full-rank PCA whitening (whi). Whitening, the most aggressive entry on the ladder, centers the embeddings, scales each principal component by $1/\sqrt{\lambda_i + \epsilon}$ with $\epsilon = 10^{-6}$, then ℓ_2-renormalizes. All methods estimate the necessary corpus statistics from the same 10^5 Wikipedia sentences with no task labels; per-row task counts in Table 2 are the per-model intersection of tasks where all 9 methods completed (a different MMTEB snapshot from Section 3, so the rows are not numerically pooled with Table 1).

Goldilocks dose-response (H3). Whitening, the most aggressive correction, degrades every model in the ladder, with the largest drop on the highest-$\|\mu\|$ model (e5-large-instruct: -5.18 pp). Mild single-

Table 2. Nine-method dose-response ladder: Δ in percentage points (mean score on the per-model intersection of tasks where all methods completed, vs. control). Methods: R1 (subtract μ, renorm.); R2 (project out $\hat{\mu}$, renorm.); ABTT-D (center, remove top-D centered PCs, renorm.) (Mu & Viswanath, 2018); mc (mean-centering only, no renorm.); rand (project out a single random direction, seed 42); whi (full-rank PCA whitening: center, scale each PC by $1/\sqrt{\lambda_i + \epsilon}$ with $\epsilon = 10^{-6}$, renorm.). All methods estimate the necessary corpus-level statistics from the same 10^5 Wikipedia sentences with no task labels. Per-row task counts are not numerically pooled with Table 1.

Model	$\|\mu\|$	#Tasks	R1	R2	ABTT-1	ABTT-2	ABTT-3	mc	rand	whi
e5-large-instr.	0.85	462	+0.59	+0.62	+0.56	**+0.71**	+0.58	+0.07	+0.00	−5.18
Snowflake-m	0.76	333	+0.40	+0.69	+0.87	**+0.92**	+0.78	−0.14	−0.02	−0.64
bge-base-v1.5	0.59	446	+0.22	+0.23	**+0.26**	+0.10	+0.14	+0.04	−0.01	−1.79
nomic-v1	0.59	402	**+0.08**	+0.08	+0.07	+0.06	−0.04	−0.01	−0.03	−0.70
MiniLM-L6	0.19	443	**+0.03**	−0.05	−0.02	−0.03	−0.12	+0.00	−0.01	−0.64

direction removal (R2 or ABTT-1) instead gives positive effects on the four high-$\|\mu\|$ models (+0.6 to +0.9 pp on `Snowflake-m` and `e5-large`, +0.2 to +0.3 pp on `bge`, near-zero on `nomic`). ABTT-2 marginally beats R2 on the two highest-$\|\mu\|$ models, so R2 is not universally optimal, and we position it as a minimal, transparent baseline rather than a new dominant method. The dose-response is consistent with a narrow correction on the dominant bias direction, not a global isotropization.

R2 and ABTT-1: downstream-equivalent, geometrically distinct. R2 removes $\hat{\mu}$ directly; ABTT-1 removes the top centered PC. The cosines are surprisingly small: 0.07 (`e5`), 0.51 (`Snowflake`), 0.05 (`bge`), 0.03 (`nomic`), 0.27 (`MiniLM`); three of five models below 0.1 (Appendix D). Despite this weak alignment, R2 and ABTT-1 agree within 0.18 pp downstream on every model in Table 2. The improvement is not reproduced by an arbitrary direction (Table 2, `rand` column), but the R2/ABTT-1 similarity leaves open whether $\hat{\mu}$ is uniquely causal or one useful global direction among several, a question we cannot resolve with 5 models and a single random-direction seed for the `rand` control.

Negative-direction controls. Mean-centering only (`mc`, no renormalization) gives $\Delta \in [-0.15, +0.07]$ pp, near-zero across the panel, ruling out the alternative that any centering operation suffices. Random-direction removal (`rand`) gives $\Delta \in [-0.03, +0.00]$ pp. To stress-test the random control we additionally ran three more seeds 2, 3, 4 on `Snowflake-m`; the four-seed mean is $+0.005$ pp (std 0.005), versus $+0.567$ pp for R2 on the same model: random projection captures roughly 1% of R2's effect on this model. The multi-seed extension covers a single model; we leave multi-model multi-seed random control to future work.

5. Discussion and Limitations

The evidence above identifies a coherent feature of the output space: a shared mean direction that is large, largely invariant across language and prompt path, and whose dose-

controlled removal produces a small but reliable classification gain when $\|\mu\|$ is itself large. The dose-response curve is non-monotone: single-direction removal helps in the high-$\|\mu\|$ regime, but full PCA whitening hurts every model we test, consistent with prior reports that some anisotropy preserves useful cluster structure (Mickus et al., 2024). Whether μ corresponds to an identifiable internal mechanism or a training-time inductive bias is an open question we do not address.

Limitations. *(i) Panel-selection bias.* The 38-model panel was preferentially expanded toward $\|\mu\| \geq 0.5$ after early observations and is not a uniform sample. *(ii) Snowflake dominance in retrieval.* Retrieval $\bar{t}$ drops $2.99 \rightarrow 1.99$ when the Snowflake family is removed; we treat retrieval as secondary. *(iii) Post-hoc diagnostic.* The $\|\mu\| \geq 0.5$ regime is identified after observing the data, not prospectively validated on held-out models. *(iv) Staged experimental rollout.* The 38-model audit and the 9-method ablation use different MMTEB snapshots; numbers across studies are not pooled. *(v) Output-space, not circuit-level.* We do not localize μ to internal circuits or training-time causes. *(vi) Single-seed random control on most models.* The four-seed random extension covers only one model. *(vii) One whitening variant.* Task-adaptive whitening is out of scope. *(viii) ABTT-2 optimality at top end and ABTT-1 omission from the 38-model panel.* ABTT-2 beats R2 by 0.09 pp on `e5-large-instruct` and 0.23 pp on `Snowflake-m`; R2 is a minimal baseline. The 38-model audit predates the ABTT comparison; the 5-model evidence (Table 2) shows ABTT-1 is downstream-equivalent within 0.18 pp.

Recommendation. On the audited panel, the $\|\mu\| \geq 0.5$ regime was associated with R2 classification gains of $+0.13$ to $+0.76$ pp on the four named models in the dose-response ladder. We do not recommend untuned full-rank PCA whitening as a default.

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A. Error-Propagation Derivation

Let $\tilde{e} = e - \mu$ be the true centered embedding. Decompose the mean-estimation error as $\epsilon = \epsilon_{\parallel} + \epsilon_{\perp}$ with $\epsilon_{\parallel} = \alpha\,\hat{\mu}$ where $\alpha = \epsilon \cdot \hat{\mu}$ is a signed scalar, and $\epsilon_{\perp} \cdot \mu = 0$. Assume $\tilde{e} \cdot \mu \approx 0$ and $\tilde{e} \cdot \epsilon \approx 0$ (high-dimensional near-orthogonality of signal and bias direction). Note that α may be of either sign; the parallel error can over- or under-estimate $\|\mu\|$.

R1. Subtracting the estimated mean gives

$$\tilde{e}_1 = e - (\mu + \epsilon) = \tilde{e} - \alpha\,\hat{\mu} - \epsilon_{\perp}, \tag{3}$$

which retains both the parallel and orthogonal components of ϵ.

R2. Projecting out the estimated mean direction gives

$$\tilde{e}_2 = e - \frac{e \cdot (\mu + \epsilon)}{\|\mu + \epsilon\|^2}\,(\mu + \epsilon). \tag{4}$$

We expand numerator and denominator to first order in $\|\epsilon\|/\|\mu\|$. Using $\tilde{e} \cdot \mu \approx 0$ and $\tilde{e} \cdot \epsilon \approx 0$:

$$e \cdot (\mu + \epsilon) = (\tilde{e} + \mu) \cdot (\mu + \alpha\hat{\mu} + \epsilon_{\perp}) \approx \|\mu\|^2 + \alpha\|\mu\|, \tag{5}$$

$$\|\mu + \epsilon\|^2 = (\|\mu\| + \alpha)^2 + \|\epsilon_{\perp}\|^2 \approx \|\mu\|^2 + 2\alpha\|\mu\| + O(\|\epsilon\|^2). \tag{6}$$

The ratio simplifies to first order as

$$\frac{\|\mu\|^2 + \alpha\|\mu\|}{\|\mu\|^2 + 2\alpha\|\mu\|} \approx 1 - \frac{\alpha}{\|\mu\|} + O\left(\frac{\alpha^2}{\|\mu\|^2}\right). \tag{7}$$

Substituting,

$$\tilde{e}_2 \approx \tilde{e} + \mu - \left(1 - \frac{\alpha}{\|\mu\|}\right)(\mu + \alpha\hat{\mu} + \epsilon_{\perp}). \tag{8}$$

Expanding the product, the leading parallel cancellation reads

$$\mu - \left(1 - \frac{\alpha}{\|\mu\|}\right)\mu = \alpha\,\hat{\mu}, \qquad -\left(1 - \frac{\alpha}{\|\mu\|}\right)\alpha\,\hat{\mu} \approx -\alpha\,\hat{\mu}, \tag{9}$$

so the two parallel contributions cancel to first order, and the orthogonal residual is

$$-\left(1 - \frac{\alpha}{\|\mu\|}\right)\epsilon_{\perp} \approx -\epsilon_{\perp}. \tag{10}$$

Combining,

$$\tilde{e}_2 \approx \tilde{e} - \epsilon_{\perp}. \tag{11}$$

R2 therefore cancels the parallel error $\alpha\,\hat{\mu}$ to leading order, while R1 retains it. The argument characterizes estimation-error propagation only; downstream score gains and their source remain empirical.

Consequence for finite-corpus estimation. If $\hat{\mu}$ is estimated from N Wikipedia sentences, α is itself a random variable with variance scaling like $1/N$. R2 makes the leading-order behaviour insensitive to this parallel component, leaving only the orthogonal residual (which has variance scaling like $(d-1)/(N \cdot \|\mu\|^2)$ in the high-dimensional regime) as the noise that survives renormalization. R1 retains $\alpha\,\hat{\mu}$ regardless of N.

B. Effect-Size Statistic

The body uses two metrics for a (model, family) cell with n tasks. The primary metric is the conventional paired t-statistic $t = \bar{\Delta}/\text{SE}(\Delta)$ over per-task deltas Δ_i; this is what most reviewers expect. The secondary metric, which we call σ_{cell}, is

$$\sigma_{\text{cell}} = \frac{n\,\bar{\Delta}}{s_{\text{baseline}}}, \qquad s_{\text{baseline}} = \sqrt{\frac{1}{n-1}\sum_i (s_i^{\text{ctrl}} - \bar{s}^{\text{ctrl}})^2}. \tag{12}$$

The two are related by $\sigma_{\text{cell}} = \sqrt{n}\,\bar{\Delta}/\sigma^{\text{SE}}$ where $\sigma^{\text{SE}} = s_{\text{baseline}}/\sqrt{n}$ is the standard error of the baseline-score mean. σ_{cell} amplifies effects in cells with many baseline-similar tasks (large n, small s_{baseline}) and is therefore not a paired test. We report it because it is informative about per-cell coherence (it amplifies signals in families with many homogeneous tasks); the W/T/L thresholds at $|\sigma_{\text{cell}}| > 2$ in our tables are an internal effect-size window, not a Bonferroni-controlled significance level. Throughout this paper, the conventional paired t is the primary metric for any claim about whether R2 helps or hurts.

C. Embedding-Norm Audit

Each evaluated model is wrapped via the standard `SentenceTransformer` call path used in evaluation. We re-encoded 200 sentences per model and measured $\|e\|_2$ per output. Of 29 models that loaded successfully on our audit environment, 28 produce unit-norm embeddings ($\|\bar{e}\| = 1.0000$, std $\leq 10^{-3}$). The single non-unit model is `paraphrase-multilingual-MiniLM-L12-v2` (mean ≈ 4.3). The 9 audit failures stem from BFloat16-related dtype issues or custom modeling code that bypasses the audit harness; all 9 models were nonetheless successfully evaluated end-to-end in the primary pipeline. This audit rules out a normalization confound for R1, R2, and ABTT on the remaining 28 models. Raw per-model statistics accompany this submission.

D. PC1 vs Mean Alignment: Centered and Uncentered

There is a folklore observation that "the first principal component of sentence embeddings is essentially the mean direction." This is true for the *uncentered* principal direction (the right singular vector of the raw embedding matrix), because the large mean-norm $\|\mu\|$ makes $\mu\mu^\top$ dominate the uncentered second moment $\mathbb{E}[ee^\top] = \mathbb{E}[\tilde{e}\tilde{e}^\top] + \mu\mu^\top$.

The All-but-the-Top algorithm of Mu & Viswanath (2018) works on *centered* embeddings instead: it subtracts μ first, then removes the top principal component(s) of the residual distribution. After centering, the μ-direction variance is gone, and the centered top PC is whatever direction had the second-largest variance in the raw embeddings. There is no a priori reason for that residual direction to align with $\hat{\mu}$.

Both quantities are well-defined and easy to compute. We report both:

Model	$\|\mu\|$	$\cos(\hat{\mu}, \text{PC1}_{\text{centered}})$	$\cos(\hat{\mu}, \text{PC1}_{\text{uncentered}})$
intfloat/multilingual-e5-large-instruct	0.85	0.0699	1.0000
Snowflake/snowflake-arctic-embed-m	0.76	0.5149	0.9998
BAAI/bge-base-en-v1.5	0.59	0.0477	1.0000
nomic-ai/nomic-embed-text-v1	0.60	0.0280	1.0000
sentence-transformers/all-MiniLM-L6-v2	0.19	0.2663	0.9757

The right column recovers the folklore: on the four high-$\|\mu\|$ models, the uncentered top principal direction is indistinguishable from $\hat{\mu}$ to four decimal places. The exception is the low-$\|\mu\|$ `all-MiniLM-L6-v2`, where $\|\mu\|^2 \approx 1.5 \, \lambda_1^{\text{centered}}$ is no longer dominant over the centered top eigenvalue and $\hat{\mu}$ ceases to be (nearly) the top uncentered direction.

Closed-form computation. The uncentered second-moment matrix is a rank-1 update $C = C_{\text{centered}} + \|\mu\|^2 \, \hat{\mu}\hat{\mu}^\top$ of the centered covariance. Expanding $\hat{\mu} = \sum_i \alpha_i u_i$ in the centered eigenbasis, the largest eigenvalue λ^* of C is the largest root of the secular equation $1 = \|\mu\|^2 \sum_i \alpha_i^2 / (\lambda^* - \lambda_i^{\text{centered}})$, and the corresponding eigenvector is $v_1 \propto \sum_i [\alpha_i / (\lambda^* - \lambda_i^{\text{centered}})] \, u_i$. We solve this in float64 from the saved centered eigenvectors and eigenvalues; the closed-form solver and the resolved cosines accompany this submission, and no additional embedding forward passes were required.

Why this is interesting for ABTT-1 vs R2. On the four high-$\|\mu\|$ models, the centered top PC is nearly orthogonal to $\hat{\mu}$ (cos ≤ 0.07 for three of them). ABTT-1 therefore performs two essentially independent operations: (i) subtract the mean direction, and (ii) remove a separate, almost-orthogonal residual direction. R2 only does step (i). Despite this geometric difference, R2 and ABTT-1 give almost identical downstream effects (Table 2, within 0.18 pp on every model). The simplest reading is that step (ii) of ABTT-1 contributes very little downstream on these models, and the dominant effect comes from removing the $\hat{\mu}$ direction, which both methods do. We phrase this as a hypothesis rather than a proven mechanism. On the low-$\|\mu\|$ MiniLM the picture is different: there is non-trivial $\hat{\mu}$/centered-PC1 alignment (0.27), so step (ii) partially overlaps with step (i); both methods give near-zero downstream effect, consistent with the small $\|\mu\|$ leaving little anisotropy to remove in the first place.

E. Multilingual and Prompt-Path Probes

Multilingual μ. For `multilingual-e5-large-instruct`, we recomputed μ using 10 Wikipedia language editions (10 000 sentences each: en, de, fr, es, zh, ja, ru, ar, ko, pt). The running mean stabilizes after the first few languages:

After language	running $\|\mu\|$	cumulative samples
english (en, init.)	0.8496	10 000
+ german (de)	0.8507	20 000
+ french (fr)	0.8508	30 000
+ spanish (es)	0.8497	40 000
+ chinese (zh)	0.8463	50 000
+ japanese (ja)	0.8453	60 000
+ russian (ru)	0.8445	70 000
+ arabic (ar)	0.8427	80 000
+ korean (ko)	0.8424	90 000
+ portuguese (pt, final)	0.8431	100 000

Final norms: $\|\mu_{\text{en}}\| = 0.849$, $\|\mu_{\text{multi}}\| = 0.843$; $\cos(\mu_{\text{en}}, \mu_{\text{multi}}) = 0.973$ (angle $13.2°$). The bias direction is largely model-intrinsic rather than language-specific. This does *not* constitute a downstream multilingual re-evaluation, which we leave to future work.

Prompt-path probe. For the same instruct model we recomputed μ on 10^5 sentences using two representative prompts:

- *Retrieval prompt*: "Instruct: Given a web search query, retrieve relevant passages that answer the query\nQuery: "

- *Classification prompt*: "Instruct: Classify the following text\nQuery: "

Norms and inter-prompt cosines:

	plain	retrieval prompt	classification prompt
$\|\mu\|$	0.849	0.861	0.926
plain		0.991 (7.8°)	0.868 (29.7°)
retrieval prompt			0.840 (32.9°)

Prompt mismatch is minor for retrieval-style prompts and moderate for classification-style prompts. We did not re-run R2 with prompted $\hat{\mu}$.

F. Multi-Seed Random-Direction Control

On `Snowflake-arctic-embed-m` we ran three additional random-direction seeds beyond the seed-42 `random` column of Table 2.

Seed	Δ (pp) on per-task intersection	ratio to R2
42	+0.0015	0.3%
2	+0.0009	0.2%
3	+0.0072	1.3%
4	+0.0106	1.9%
mean	+0.005 (std 0.005)	0.9%
R2 (reference)	+0.567	

The mean random-direction effect captures roughly 1% of the R2 effect on this model. Multi-model multi-seed extension is left to future work.

Figure 1. R2 Transformation of Embedding Distribution

R2: $\mathbf{e}' = (\mathbf{e} - (\mathbf{e}\cdot\hat{\mu})\,\hat{\mu})/\|\cdot\|$. The shared μ component is removed; only $\tilde{\mathbf{e}} \perp \hat{\mu}$ remains and is renormalized.

Figure 2. Geometric intuition for R2. *Left*: each embedding decomposes as $e = \tilde{e} + \mu$, and embeddings concentrate around the mean direction $\hat{\mu}$. *Right*: R2 projects e off $\hat{\mu}$ and renormalizes to unit length, leaving $\tilde{e}_2 \approx \tilde{e} - \epsilon_\perp$ to first order in the mean-estimation error.

Table 3. Mean R2 paired t-statistic per family, stratified by $\|\mu\|$ quartile.

$\|\mu\|$ bin	#	Retrieval	Classif.	Other
[0.00,0.30)	2	+2.34	−0.25	+0.05
[0.30,0.60)	6	+1.36	+2.46	+1.23
[0.60,0.75)	10	+2.15	+3.31	+1.39
[0.75,1.05)	20	+3.95	+3.91	+1.88

G. μ-Decomposition Schematic

H. $\|\mu\|$ Quartile Stratification

The classification effect grows monotonically across $\|\mu\|$ quartiles. The retrieval effect grows from quartile 1 to quartiles 3-4 but is bin-sensitive: the upper retrieval quartile is dominated by the Snowflake family (see Appendix J). The Other family stays small and noisy throughout, consistent with the body's positioning of retrieval as a family-sensitive secondary finding.

I. R2 vs R1 Retrieval Head-to-Head

Across the full 38-model panel, R2's retrieval paired t-statistic exceeds R1's on 35 of 38 models, and R2's σ_{cell} exceeds R1's on 36 of 38 models. The exceptions are flagged with † in the table. This pattern is consistent with the first-order error-propagation prediction (Appendix A) but does not isolate the mechanism, since MMTEB scores cannot independently vary the parallel-vs-orthogonal split of the mean-estimation error.

J. Snowflake Share Decomposition for Retrieval

The five Snowflake-arctic-embed models contribute roughly 80% of the cumulative R2 retrieval σ_{cell} on the 38-model panel. This concentration is the underlying reason that retrieval is treated as a family-sensitive secondary finding throughout the body, and why we report Snowflake-free numbers in Table 1.

Table 4. Retrieval R1-vs-R2 head-to-head on the 38-model panel, sorted by $\|\mu\|$. R2 wins 35/38 on paired t and 36/38 on σ_{cell}; the three exceptions are highlighted with a dagger.

Model	$\|\mu\|$	#T	t_{R_1}	t_{R_2}	σ_{R_1}	σ_{R_2}	$t_{R_2} > t_{R_1}$	$\sigma_{R_2} > \sigma_{R_1}$
e5-small	0.86	182	−1.02	−1.15	−1.1	−1.2	†	†
rubert-tiny-turbo	0.86	179	+6.09	+6.05	+15.6	+16.1	†	✓
multilingual-e5-small	0.85	181	+2.87	+2.90	+2.6	+2.6	✓	✓
multilingual-e5-large-inst..	0.85	182	+7.94	+8.01	+12.5	+12.7	✓	✓
e5-small-v2	0.85	182	+0.12	+0.15	+0.1	+0.2	✓	✓
sentence-t5-base	0.84	182	−4.00	−3.77	−2.3	−2.1	✓	✓
e5-base	0.84	182	+4.80	+4.98	+5.9	+6.1	✓	✓
e5-base-v2	0.83	174	+1.72	+1.74	+1.5	+1.5	✓	†
granite-embedding-125m-eng..	0.82	181	+2.17	+2.27	+0.5	+0.6	✓	✓
bge-base-en	0.82	180	+9.34	+9.55	+8.3	+8.4	✓	✓
GIST-all-MiniLM-L6-v2	0.82	180	+6.02	+6.10	+4.1	+4.1	✓	✓
sentence-t5-large	0.81	178	−5.08	−4.44	−3.1	−2.5	✓	✓
LaBSE-ru-turbo	0.80	181	+4.79	+4.86	+10.6	+10.8	✓	✓
snowflake-arctic-embed-xs	0.80	182	+9.18	+9.32	+37.0	+38.9	✓	✓
rubert-tiny2	0.80	181	+2.46	+2.87	+5.2	+6.1	✓	✓
jina-embeddings-v2-base-en	0.80	173	−0.29	−0.29	−0.2	−0.2	†	✓
snowflake-arctic-embed-m-1..	0.79	175	+8.09	+8.17	+43.6	+46.9	✓	✓
snowflake-arctic-embed-s	0.78	182	+10.16	+10.39	+47.6	+51.5	✓	✓
GIST-small-Embedding-v0	0.77	182	+1.57	+1.82	+0.9	+1.0	✓	✓
snowflake-arctic-embed-m	0.76	182	+9.10	+9.54	+74.2	+90.1	✓	✓
GIST-Embedding-v0	0.74	182	+1.52	+1.63	+0.6	+0.7	✓	✓
MedEmbed-small-v0.1	0.72	181	+2.59	+3.24	+1.4	+1.7	✓	✓
granite-embedding-107m-mul..	0.71	181	−4.26	−4.11	−1.6	−1.5	✓	✓
granite-embedding-30m-engl..	0.69	181	+1.63	+1.65	+0.7	+0.8	✓	✓
granite-embedding-278m-mul..	0.69	181	−3.21	−2.35	−1.1	−0.9	✓	✓
gte-multilingual-base	0.63	181	+3.25	+3.59	+1.7	+1.9	✓	✓
bge-small-en-v1.5	0.62	182	+5.32	+5.86	+2.7	+2.9	✓	✓
snowflake-arctic-embed-m-v..	0.62	181	+10.00	+10.44	+52.8	+69.8	✓	✓
Wartortle	0.62	182	−2.21	−1.99	−1.0	−0.9	✓	✓
paraphrase-multilingual-Mi..	0.60	181	+1.62	+3.56	+0.3	+0.9	✓	✓
Squirtle	0.60	182	−1.74	−1.16	−1.0	−0.6	✓	✓
nomic-embed-text-v1	0.59	174	−2.00	−1.06	−1.9	−0.9	✓	✓
bge-base-en-v1.5	0.59	181	+5.00	+5.52	+3.2	+3.5	✓	✓
USER-base	0.50	179	−1.49	−0.42	−1.1	−0.3	✓	✓
LaBSE-en-ru	0.41	182	−1.51	+2.59	−1.3	+1.8	✓	✓
potion-multilingual-128M	0.34	182	−8.90	+2.70	−4.8	+1.2	✓	✓
potion-base-8M	0.23	180	−3.20	+1.04	−1.5	+0.4	✓	✓
all-MiniLM-L6-v2	0.19	169	+3.00	+3.64	+0.6	+0.9	✓	✓

Total: $t_{R_2} > t_{R_1}$ in 35/38 models; $\sigma_{R_2} > \sigma_{R_1}$ in 36/38 models.

K. Per-Model Effect Distribution

L. $\|\mu\|$ vs Per-Model Mean $\triangle$, Both Methods

M. Per-Model Significance Profile under R2

Each row reports, for one of the 28 audited models with sufficient per-task σ data, the proportion of tasks for which R2 yields a significant improvement ($> 2\sigma_{\text{cell}}$) and the proportion for which it yields a significant degradation. Highest-$\|\mu\|$ Snowflake-family models top the list; the $\|\mu\| \leq 0.3$ tail (`all-MiniLM-L6-v2`, `potion-base-8M`) is at the bottom.

N. Per-Task Significance Profile under R2

Each row reports, for one MMTEB task, the proportion of audited models for which R2 yields a significant improvement or degradation on that task. Retrieval and clustering tasks dominate the top of the list; a small tail of pair-classification, summarization, and reranking tasks shows mixed effects.

O. Large-Effect Tasks: Per-Model Breakdown

Filter: $|\Delta| > 0.1$ score units AND relative change $|\delta| > 2\%$. The first numeric column is the count of tasks with significant improvement; the columns to its right are the average, max, and min improvement deltas. The columns starting with # ↓ are the analogous degradation statistics. Models not listed had no tasks meeting the filter.

Table 5. Per-model R2 retrieval σ_{cell} contribution to the panel aggregate. Total = 372.7; Snowflake family contributes 297.2 (79.7%) of the cumulative σ_{cell}. The remaining 33 models contribute the balance. Models sorted by individual contribution.

Model	$\|\mu\|$	$\sigma_{\text{cell}}^{R_2}$	% of total
snowflake-arctic-embed-m ♠	0.76	+90.09	+24.2
snowflake-arctic-embed-m-v.. ♠	0.62	+69.81	+18.7
snowflake-arctic-embed-s ♠	0.78	+51.48	+13.8
snowflake-arctic-embed-m-l.. ♠	0.79	+46.88	+12.6
snowflake-arctic-embed-xs ♠	0.80	+38.94	+10.4
rubert-tiny-turbo	0.86	+16.06	+4.3
multilingual-e5-large-inst..	0.85	+12.65	+3.4
LaBSE-ru-turbo	0.80	+10.82	+2.9
bge-base-en	0.82	+8.44	+2.3
rubert-tiny2	0.80	+6.11	+1.6
e5-base	0.84	+6.06	+1.6
GIST-all-MiniLM-L6-v2	0.82	+4.14	+1.1
bge-base-en-v1.5	0.59	+3.53	+0.9
bge-small-en-v1.5	0.62	+2.93	+0.8
multilingual-e5-small	0.85	+2.60	+0.7
gte-multilingual-base	0.63	+1.86	+0.5
LaBSE-en-ru	0.41	+1.80	+0.5
MedEmbed-small-v0.1	0.72	+1.69	+0.5
e5-base-v2	0.83	+1.45	+0.4
potion-multilingual-128M	0.34	+1.24	+0.3
GIST-small-Embedding-v0	0.77	+1.03	+0.3
all-MiniLM-L6-v2	0.19	+0.89	+0.2
paraphrase-multilingual-Mi..	0.60	+0.85	+0.2
granite-embedding-30m-engl..	0.69	+0.75	+0.2
GIST-Embedding-v0	0.74	+0.66	+0.2
granite-embedding-125m-eng..	0.82	+0.56	+0.2
potion-base-8M	0.23	+0.42	+0.1
e5-small-v2	0.85	+0.16	+0.0
jina-embeddings-v2-base-en	0.80	−0.22	-0.1
USER-base	0.50	−0.28	-0.1
Squirtle	0.60	−0.60	-0.2
granite-embedding-278m-mul..	0.69	−0.87	-0.2
nomic-embed-text-v1	0.59	−0.90	-0.2
Wartortle	0.62	−0.93	-0.2
e5-small	0.86	−1.24	-0.3
granite-embedding-107m-mul..	0.71	−1.51	-0.4
sentence-t5-base	0.84	−2.12	-0.6
sentence-t5-large	0.81	−2.53	-0.7

♠ Snowflake family. Family total 297.2 = 79.7% of cumulative σ_{cell}.

P. Large-Effect Tasks: Per-Task Breakdown

Same filter as Appendix O, but indexed by task rather than model. `WinoGrande` is uniformly improved across all 10 models for which it is in the test grid; `ChemHotpotQARetrieval`, the `CQADupstack*` family, and `HotpotQAHardNegatives` also show broad gains.

Q. Per-Model 9-Method Task Counts

The right-most column is the per-model intersection used as the basis for the Δ values in Table 2. Per-method counts vary because some methods experience occasional task-level failures (timeouts, OOMs, or numerical errors specific to the post-processing step); in particular, the `whiten` column has the smallest task count for every model because full-rank PCA on the largest tasks intermittently exceeded our memory budget.

R. MMTEB Task Filtering: Full 192-Task List

The 5-model nine-method ablation uses MMTEB v1.38.18 (929 tasks total) and excludes 192 tasks falling into three disjoint categories:

1. *Failures* (115): tasks that consistently crash or produce invalid outputs across multiple runs.

2. *Timeouts* (28): tasks that exceed the wall-clock budget (default 1 h, sometimes extended to 3 h) even after retries.

3. *Unsupported modality* (49): image-based or multimodal benchmarks incompatible with text-only embedding models.

Table 6. Per-model proportion of tasks where R2 produces a large effect, measured as per-model-internal $|z| > 2$ (Δ deviates from the model's own mean Δ by more than 2 within-model standard deviations). This is a model-internal effect-size, not the per-family σ_{cell} used elsewhere; computed directly from per-task Δ in `RESULTS_38MODEL.json`. Models sorted by improvement proportion.

Model	$\|\mu\|$	$> 2\sigma_\Delta$ (%)	$< -2\sigma_\Delta$ (%)
snowflake-arctic-embed-xs	0.80	5	0
snowflake-arctic-embed-m	0.76	5	0
snowflake-arctic-embed-m-v..	0.62	5	0
snowflake-arctic-embed-s	0.78	5	0
snowflake-arctic-embed-m-l..	0.79	5	0
multilingual-e5-large-inst..	0.85	4	1
bge-base-en	0.82	4	2
Wartortle	0.62	4	3
sentence-t5-large	0.81	3	2
rubert-tiny-turbo	0.86	3	2
bge-base-en-v1.5	0.59	3	2
bge-small-en-v1.5	0.62	3	3
Squirtle	0.60	3	2
multilingual-e5-small	0.85	3	1
LaBSE-ru-turbo	0.80	3	1
GIST-small-Embedding-v0	0.77	3	2
e5-base	0.84	3	1
potion-multilingual-128M	0.34	3	2
GIST-all-MiniLM-L6-v2	0.82	3	1
sentence-t5-base	0.84	3	2
granite-embedding-125m-eng..	0.82	3	2
paraphrase-multilingual-Mi..	0.60	3	2
GIST-Embedding-v0	0.74	3	2
all-MiniLM-L6-v2	0.19	3	3
jina-embeddings-v2-base-en	0.80	3	2
nomic-embed-text-v1	0.59	3	2
MedEmbed-small-v0.1	0.72	3	2
e5-base-v2	0.83	3	1
e5-small-v2	0.85	3	2
LaBSE-en-ru	0.41	2	3
granite-embedding-278m-mul..	0.69	2	1
gte-multilingual-base	0.63	2	3
granite-embedding-30m-engl..	0.69	2	2
granite-embedding-107m-mul..	0.71	2	0
e5-small	0.86	2	3
potion-base-8M	0.23	2	2
USER-base	0.50	2	3
rubert-tiny2	0.80	2	2

Table 7. Per-task proportion of the 38 audited models for which R2 produces a large improvement or degradation, using the same per-model-internal $|z| > 2$ metric as Table 6. Tasks with no models meeting the threshold are omitted.

Task	Type	$> 2\sigma_\Delta$ (%)	$< -2\sigma_\Delta$ (%)
STS17	Other	50	0
ItaCaseholdClassificatio	Classification	45	3
CUADAffiliateLicenseLice	Classification	42	11
MTOPIntentClassification	Classification	42	3
WinoGrande	Retrieval	42	13
SyntecRetrieval	Retrieval	39	0
CUADUnlimitedAllYouCanEa	Classification	29	11
ChemNQRetrieval	Retrieval	29	8
LegalReasoningCausalityL	Classification	29	13
ChemHotpotQARetrieval	Retrieval	26	32
SynPerChatbotConvSAToneU	Classification	26	0
FQuADRetrieval	Retrieval	26	0
WikipediaSpecialtiesInCh	Other	26	13
Touche2020Retrieval.v3	Retrieval	24	0
NLPTwitterAnalysisClassi	Classification	24	0
WikipediaChemistryTopics	Classification	24	26
SyntecReranking	Other	21	3
HotpotQAHardNegatives	Retrieval	21	0
LEMBWikimQARetrieval	Retrieval	21	0
BigPatentClustering.v2	Other	21	3
NQHardNegatives	Retrieval	18	3
SKQuadRetrieval	Retrieval	18	11
AlloprofRetrieval	Retrieval	18	0
ContractNLIInclusionOfVe	Classification	18	0
CUADExclusivityLegalBenc	Classification	18	0
GermanDPR	Retrieval	18	3
TextualismToolDictionari	Classification	18	53
FEVERHardNegatives	Retrieval	18	18
EstQA	Retrieval	18	0
CanadaTaxCourtOutcomesLe	Classification	16	5
KlueMrcDomainClustering	Other	16	13
SlovakSumRetrieval	Retrieval	16	0
MedicalQARetrieval	Retrieval	16	0
SpanishNewsClusteringP2P	Other	16	29
ContractNLIPermissibleCo	Classification	16	13
SyntheticText2SQL	Retrieval	16	11
BuiltBenchClusteringP2P	Other	16	26
LitSearchRetrieval	Retrieval	16	0
Banking77Classification	Classification	16	3
HotpotQA-PLHardNegatives	Retrieval	16	3
CUADWarrantyDurationLega	Classification	13	0
CUADSourceCodeEscrowLega	Classification	13	11
SCDBPTrainingLegalBenchC	Classification	13	5
SynPerChatbotToneUserCla	Classification	13	0
CQADupstackGamingRetriev	Retrieval	13	0
FeedbackQARetrieval	Retrieval	13	0
DBPediaHardNegatives	Retrieval	13	0
TV2Nordretrieval	Retrieval	13	3
KlueYnatMrcCategoryClust	Other	13	16
BSARDRetrieval	Retrieval	13	8
SynPerChatbotRAGToneUser	Classification	13	0
CUADThirdPartyBeneficiar	Classification	13	11
SCDDAccountabilityLegalB	Classification	13	0
CQADupstackPhysicsRetrie	Retrieval	13	0
ContractNLISurvivalOfObl	Classification	13	5
GermanGovServiceRetrieva	Retrieval	13	0
JCrewBlockerLegalBenchCl	Classification	13	0
LegalBenchCorporateLobby	Retrieval	13	0
CQADupstackGisRetrieval	Retrieval	11	0
MSMARCOHardNegatives	Retrieval	11	0

Table 8. Per-model large-effect tasks under R2 (filter: $|\Delta| > 0.1$ score units AND $|\delta| > 2\%$ relative change). Computed from `RESULTS_38MODEL.json`. Only models with at least one task meeting the filter are shown.

Model	# ↑	$\bar{\Delta}_\uparrow$	$\Delta_{\max,\uparrow}$	$\Delta_{\min,\uparrow}$	# ↓	$\bar{\Delta}_\downarrow$	$\Delta_{\max,\downarrow}$	$\Delta_{\min,\downarrow}$
snowflake-arctic-embed-m	59	0.2346	0.5849	0.1019	3	-0.1462	-0.1264	-0.1589
snowflake-arctic-embed-m-v..	53	0.1908	0.5338	0.1011	2	-0.1058	-0.1034	-0.1081
snowflake-arctic-embed-s	43	0.1625	0.5559	0.1021	0	–	–	–
snowflake-arctic-embed-m-l..	39	0.1905	0.3992	0.1022	2	-0.1341	-0.1149	-0.1532
snowflake-arctic-embed-xs	29	0.1536	0.3092	0.1011	1	-0.1682	-0.1682	-0.1682
multilingual-e5-large-inst..	4	0.1192	0.1407	0.1082	1	-0.1308	-0.1308	-0.1308
LaBSE-ru-turbo	3	0.1982	0.3586	0.1150	1	-0.1589	-0.1589	-0.1589
rubert-tiny-turbo	3	0.1573	0.2028	0.1102	1	-0.1215	-0.1215	-0.1215
rubert-tiny2	2	0.1362	0.1553	0.1171	1	-0.1192	-0.1192	-0.1192
e5-base	2	0.1489	0.1871	0.1108	0	–	–	–
e5-base-v2	2	0.1740	0.2289	0.1191	0	–	–	–
nomic-embed-text-v1	2	0.1148	0.1271	0.1025	0	–	–	–
paraphrase-multilingual-Mi..	2	0.1034	0.1040	0.1028	1	-0.2316	-0.2316	-0.2316
bge-small-en-v1.5	1	0.1130	0.1130	0.1130	0	–	–	–
granite-embedding-107m-mul..	1	0.1723	0.1723	0.1723	0	–	–	–
e5-small	1	0.1709	0.1709	0.1709	0	–	–	–
e5-small-v2	1	0.1729	0.1729	0.1729	0	–	–	–
sentence-t5-large	1	0.1227	0.1227	0.1227	0	–	–	–
bge-base-en	0	–	–	–	1	-0.1669	-0.1669	-0.1669
granite-embedding-125m-eng..	0	–	–	–	1	-0.1101	-0.1101	-0.1101
multilingual-e5-small	0	–	–	–	1	-0.1215	-0.1215	-0.1215
jina-embeddings-v2-base-en	0	–	–	–	1	-0.1028	-0.1028	-0.1028

The 38-model R1/R2 audit was run on an earlier MMTEB snapshot; per-model R2 task counts are 609 to 624 after the same three filtering categories. Per-study task-tracker metadata accompanies the submission.

S. MMTEB Models Evaluated: Full Panel

The 38-model panel was built by sweeping the public MMTEB leaderboard, then preferentially adding models with $\|\mu\| \geq 0.5$ after early observations that benefit correlates with the mean-vector norm. `all-MiniLM-L6-v2` is the only deliberately-included low-$\|\mu\|$ model. The selection bias is disclosed in the body and quantified in Appendix J for retrieval.

T. Related Work

Pre-trained sentence embeddings exhibit *anisotropy*: representations concentrate in a narrow cone whose dominant axis carries most of the variance. This was diagnosed early for word embeddings (a representation-degeneration problem during language-model training) by Gao et al. (2019), mapped explicitly for contextual embeddings by Ethayarajh (2019), and re-examined at the cluster-versus-isotropy level by Cai et al. (2021). Whether the resulting cone is the cause of poor semantic similarity, or merely a symptom of other systematic biases (token frequency, punctuation, etc.), has been debated by Fuster Baggetto & Fresno (2022) and revisited by Mickus et al. (2024), who argue that some anisotropy preserves cluster structure that downstream classifiers exploit. More recently, Nastase & Merlo (2025) showed that cosine similarity in sentence embedding spaces captures only shallow commonalities and does not reliably reflect how linguistic information is encoded, further motivating a careful, task-driven evaluation of any post-processing intervention rather than relying on cosine-based diagnostics alone. Our nine-method dose-response ablation is consistent with the latter view: removing *all* anisotropy via full PCA whitening hurts every model we test, while a single-direction correction is small and reliably positive in the high-$\|\mu\|$ regime.

Several training-free or near-training-free post-processing techniques have been proposed to alleviate the cone. The closest ancestors of R1 and R2 are the smoothed-inverse-frequency baseline of Arora et al. (2017), which removes the first principal component of an aggregated word-embedding average, and the All-but-the-Top algorithm of Mu & Viswanath (2018), which centers the embedding distribution and removes its top principal components. ABTT-1 in particular is the dominant baseline for our R2 method: as we report in Section 4, R2 and ABTT-1 are downstream-equivalent within 0.18 pp on every model in our ablation despite weak geometric alignment between $\hat{\mu}$ and the centered top principal component (Appendix D). We accordingly position R2 as a transparent, single-vector implementation of the same intervention rather than a new algorithm, with the additional contributions of an explicit error-propagation handle (Appendix A) and the $\|\mu\|$ pre-deployment diagnostic (Section 3).

Whitening-style methods sit further along the dose-response axis. Li et al. (2020) apply a normalizing flow to push BERT

embeddings toward a Gaussian; Su et al. (2021) and Huang et al. (2021) apply explicit decorrelation transforms. These are reported to improve sentence-similarity tasks in their original settings; on our ablation panel the most aggressive limit (full-rank PCA whitening on a corpus mean) hurts every tested model. We do not interpret this as a global refutation of all whitening-style approaches; rather, it documents a regime (modern multilingual sentence encoders with already-large $\|\mu\|$) in which untuned full-rank whitening is the wrong dose.

Beyond whitening, recent post-processing approaches include subspace manifold projection for anisotropy reduction (Wren et al., 2025), attention-weighted re-projection (`Ditto`; Chen et al., 2023), large-scale dimension-drop ablations (Takeshita et al., 2025), and LLM-driven embedding aggregation (`GenEOL`; Thirukovalluru & Dhingra, 2025). These act on different parts of the representation pipeline (token weighting, dimension subset, ensemble of paraphrases) than R2, which only edits the corpus-mean direction. Contrastive sentence-embedding training such as SimCSE (Gao et al., 2021) also addresses anisotropy but at training time rather than as a plug-in correction. The Sentence-BERT framework of Reimers & Gurevych (2019) gave the broader infrastructure on which most of the encoders we audit are built; the `e5` family of contrastively pre-trained encoders (Wang et al., 2022) is a representative recent backbone, and members of this family appear among our highest-$\|\mu\|$ audit subjects.

Finally, two recent papers use the shared mean direction *as an attack surface* rather than as a quantity to remove: Liang et al. (2025) construct universal magic-word attacks against text-embedding safeguards, and Li et al. (2024) use language-driven anchors as zero-shot adversarial directions on vision-language encoders. These works support the present paper's framing of μ as a coherent, model-intrinsic, transferable direction in the output space.

U. Reproducibility Notes

Mean-vector estimation. For every model, μ is estimated from the same 10^5 sentences sampled from English Wikipedia (snapshot `20220301.en`), filtered to lengths in $[64, 512]$ characters. Sentences are pre-tokenized with NLTK; no task labels are used. The same corpus is used to fit centered PCA components for the All-but-the-Top and full-rank whitening baselines.

Whitening protocol. For each model and task, full-rank whitening (a) centers all embeddings by subtracting μ, (b) computes the SVD of the centered matrix, (c) scales each principal direction by $1/\sqrt{\lambda_i + \epsilon}$ with $\epsilon = 10^{-6}$, and (d) ℓ_2-renormalizes. PCA is fit once per model on the corpus described above and frozen across tasks.

Random-direction control. The seed-42 random direction is sampled from $\mathcal{N}(0, I_d)$ then ℓ_2-normalized. Multi-seed extensions on Snowflake-arctic-embed-m use seeds $\{2, 3, 4\}$ in addition. All seeds are documented in the supplementary release.

Effect-size and W/T/L thresholds. The paired t-statistic is $\bar{\Delta}/\text{SE}(\Delta)$ over per-task deltas within a (model, family) cell with at least 5 tasks. Win/tie/loss counts use $|t| > 2$ or $|\sigma_{\text{cell}}| > 2$ as the threshold; this is an effect-size window, not a Bonferroni-controlled significance level. Bootstrap confidence intervals for Pearson correlations use $10\,000$ resamples with replacement.

Two MMTEB snapshots. The 38-model R1/R2 study was run on an earlier MMTEB snapshot (per-model task counts 609 to 624). The 5-model nine-method ablation was run on MMTEB v1.38.18 (per-model intersections 333 to 462 across all nine methods). Per-row deltas in Table 2 are not numerically pooled with Table 1.

Released artifacts. Every paired per-task delta, every per-method per-task score, the per-model mean vectors, the multilingual-μ trajectory, the prompt-path probe outputs, the embedding-norm audit, the PC1-mean alignment files, the multi-seed random control output, and the per-study task-tracker metadata accompany this submission. Each main-body table, the headline figure, and every supplementary appendix table is regenerated by a corresponding script in the released supplementary materials.

V. Compute

The 38-model R1/R2 audit was run on a single Linux host with several A6000-class GPUs. A typical model of size $\sim 100\,\text{MB}$ requires roughly 24 GPU-hours on one such GPU to complete the filtered MMTEB suite end-to-end. The

5-model nine-method ablation was distributed across an H100-class cloud-GPU cluster. The cumulative GPU budget across the audit and the nine-method ablation is in the low single-digit thousand GPU-hours.

Figure 3. Comparison of two renormalization methods across 38 models, sorted by mean vector norm. Each pair of half-violins shows the per-task score-difference distribution under R1 vs R2 for one model. The median (red bar), quartiles, and adjacent values are marked. The y-axis is logarithm-scaled to better show distributional shape. Models from the same organization share a colour; different organizations use different colours.

Figure 4. Per-model mean task-score change Δ (log-scaled) under R1 (left) and R2 (right) versus $\|\mu\|$. Error bars use the per-model dispersion derived from per-task variability. Fitted lines are descriptive only; the per-method correlations r are reported in the body.

Figure 5. Proportion of tasks with $|\sigma_{\text{cell}}| > 2$ improvement under R2 versus $\|\mu\|$ on the 38-model panel. The body's Figure 1 reports the same data using paired t on the y-axis; this version uses the secondary σ_{cell} metric (see Appendix B).

Table 9. Per-task large-effect breakdown under R2 (filter: $|\Delta| > 0.1$ score units AND $|\delta| > 2\%$ relative change). Computed from `RESULTS_38MODEL.json`.

Task	N	$\#\uparrow$	$\bar{\Delta}_\uparrow$	$\Delta_{\max,\uparrow}$	$\Delta_{\min,\uparrow}$	$\#\downarrow$	$\bar{\Delta}_\downarrow$	$\Delta_{\max,\downarrow}$	$\Delta_{\min,\downarrow}$
WinoGrande	10	10	0.2121	0.5559	0.1150	0	–	–	–
NQHardNegatives	5	5	0.2532	0.3002	0.1909	0	–	–	–
CQADupstackTexRetrieval	5	5	0.1320	0.1772	0.1059	0	–	–	–
MSMARCOHardNegatives	5	5	0.1435	0.1830	0.1223	0	–	–	–
ChemNQRetrieval	5	5	0.2360	0.2884	0.1785	0	–	–	–
CQADupstackGamingRetriev	5	5	0.1963	0.3450	0.1295	0	–	–	–
FeedbackQARetrieval	5	5	0.2353	0.3549	0.1270	0	–	–	–
HotpotQAHardNegatives	5	5	0.3459	0.4562	0.2573	0	–	–	–
FiQA2018	5	5	0.1620	0.1944	0.1315	0	–	–	–
ChemHotpotQARetrieval	6	5	0.4234	0.5849	0.2728	1	-0.1192	-0.1192	-0.1192
CQADupstackEnglishRetrie	5	5	0.1562	0.2108	0.1240	0	–	–	–
CQADupstackProgrammersRe	5	5	0.1544	0.2198	0.1321	0	–	–	–
SyntheticText2SQL	5	5	0.1834	0.2605	0.1254	0	–	–	–
CQADupstackPhysicsRetrie	5	5	0.1772	0.2824	0.1180	0	–	–	–
Touche2020Retrieval.v3	5	5	0.2245	0.2698	0.1903	0	–	–	–
CQADupstackWordpressRetr	5	5	0.1491	0.2460	0.1093	0	–	–	–
CQADupstackRetrieval	5	5	0.1508	0.2450	0.1099	0	–	–	–
LitSearchRetrieval	5	5	0.3329	0.3992	0.2690	0	–	–	–
CQADupstackUnixRetrieval	5	5	0.1448	0.2557	0.1080	0	–	–	–
HotpotQA-PLHardNegatives	5	5	0.1436	0.1743	0.1011	0	–	–	–
WikipediaSpecialtiesInCh	6	5	0.1525	0.2289	0.1130	1	-0.1669	-0.1669	-0.1669
SyntecRetrieval	5	5	0.2100	0.3544	0.1046	0	–	–	–
FEVERHardNegatives	5	5	0.3113	0.5009	0.1407	0	–	–	–
CQADupstackGisRetrieval	4	4	0.1655	0.2725	0.1039	0	–	–	–
MedicalQARetrieval	4	4	0.2924	0.3584	0.1618	0	–	–	–
MLQuestions	4	4	0.1694	0.2086	0.1163	0	–	–	–
NFCorpus	4	4	0.2106	0.2569	0.1299	0	–	–	–
DBPediaHardNegatives	4	4	0.1995	0.2422	0.1471	0	–	–	–
SCIDOCS	4	4	0.1327	0.1471	0.1154	0	–	–	–
CUADThirdPartyBeneficiar	4	4	0.1434	0.1618	0.1029	0	–	–	–
SciFact	4	4	0.3423	0.5767	0.1504	0	–	–	–
CQADupstackMathematicaRe	4	4	0.1384	0.1854	0.1154	0	–	–	–
LEMBWikimQARetrieval	4	4	0.1961	0.3208	0.1479	0	–	–	–
CQADupstackStatsRetrieva	4	4	0.1485	0.1972	0.1244	0	–	–	–
LegalBenchCorporateLobby	4	4	0.2605	0.5331	0.1023	0	–	–	–
SKQuadRetrieval	3	3	0.1651	0.1768	0.1424	0	–	–	–
SweFaqRetrieval	3	3	0.1139	0.1277	0.1011	0	–	–	–
SlovakSumRetrieval	3	3	0.1336	0.1577	0.1019	0	–	–	–
TV2Nordretrieval	3	3	0.1474	0.1705	0.1134	0	–	–	–
BSARDRetrieval	3	3	0.1276	0.1441	0.1036	0	–	–	–
SwednRetrieval	3	3	0.1342	0.1522	0.1202	0	–	–	–
BuiltBenchRetrieval	3	3	0.2456	0.4602	0.1104	0	–	–	–
CQADupstackWebmastersRet	3	3	0.1689	0.2543	0.1090	0	–	–	–
GermanDPR	3	3	0.1210	0.1442	0.1093	0	–	–	–
FQuADRetrieval	3	3	0.2077	0.2391	0.1705	0	–	–	–
CQADupstackAndroidRetrie	3	3	0.1811	0.2940	0.1022	0	–	–	–
ClimateFEVERHardNegative	3	3	0.1654	0.2016	0.1128	0	–	–	–
PubChemWikiPairClassific	3	3	0.1681	0.2348	0.1213	0	–	–	–
GermanGovServiceRetrieva	3	3	0.1582	0.2028	0.1040	0	–	–	–
WikipediaRetrievalMultil	2	2	0.1333	0.1490	0.1177	0	–	–	–
ZacLegalTextRetrieval	2	2	0.1273	0.1464	0.1082	0	–	–	–
SyntecReranking	2	2	0.1537	0.2028	0.1045	0	–	–	–
NarrativeQARetrieval	2	2	0.1137	0.1138	0.1136	0	–	–	–
LEMBNarrativeQARetrieval	2	2	0.1135	0.1138	0.1132	0	–	–	–
GermanQuAD-Retrieval	2	2	0.1883	0.2039	0.1727	0	–	–	–
CUADJointIPOwnershipLega	2	2	0.1849	0.2448	0.1250	0	–	–	–
SciFact-NL	2	2	0.1417	0.1558	0.1277	0	–	–	–
WikipediaChemistryTopics	2	2	0.1074	0.1108	0.1040	0	–	–	–
LegalBenchConsumerContra	1	1	0.1823	0.1823	0.1823	0	–	–	–
LEMBQMSumRetrieval	1	1	0.1030	0.1030	0.1030	0	–	–	–
AlloprofRetrieval	1	1	0.1379	0.1379	0.1379	0	–	–	–
MLQARetrieval	1	1	0.1135	0.1135	0.1135	0	–	–	–
SynPerChatbotConvSAHappi	1	1	0.1025	0.1025	0.1025	0	–	–	–
ToxicChatClassification	1	1	0.1040	0.1040	0.1040	0	–	–	–
TurHistQuadRetrieval	1	1	0.1021	0.1021	0.1021	0	–	–	–
CUADNoSolicitOfCustomers	1	1	0.1071	0.1071	0.1071	0	–	–	–
CodeSearchNetRetrieval	1	1	0.1441	0.1441	0.1441	0	–	–	–
BelebeleRetrieval	1	1	0.1057	0.1057	0.1057	0	–	–	–

Table 10. Per-model task completion across the 9-method ladder. The body of Table 2 reports Δ on the per-model intersection (right-most column).

Model	‖μ‖	control	R1	R2	ABTT-1	ABTT-2	ABTT-3	mc	rand	whi	intersection
`multilingual-e5-large-inst..`	0.85	603	725	516	649	572	559	615	650	473	462
`snowflake-arctic-embed-m`	0.76	555	569	589	593	561	555	579	553	444	333
`bge-base-en-v1.5`	0.59	667	648	649	582	593	649	557	474	447	446
`nomic-embed-text-v1`	0.59	608	582	596	596	569	491	564	569	402	402
`all-MiniLM-L6-v2`	0.19	452	597	623	600	608	601	597	579	603	443

Table 11. Tasks filtered from MMTEB evaluation (static metadata, identical for all runs). Three disjoint categories: reproducible failures, wall-clock timeouts, and unsupported (image/multimodal) modalities. This list is for the MMTEB v1.38.18 snapshot used by the 5-model nine-method ablation; the 38-model audit used an earlier snapshot with a similar but not identical filter set (per-study task-tracker JSONs accompany the submission).

Category	Count	Tasks
Failures	115	VisualSTS17Eng, VisualSTS17Multilingual, VisualSTS-b-Eng, VisualSTS-b-Multilingual, CodeEditSearchRetrieval, CodeRAGProgrammingSolutions, CodeRAGOnlineTutorials, CodeRAGLibraryDocumentationSolutions, DanFeverRetrieval, TwitterHjerneRetrieval, GreekCivicsQA, BrightRetrieval, BrightLongRetrieval, ClimateFEVER.v2, HagridRetrieval, LEMBNeedleRetrieval, LEMBPasskeyRetrieval, LEMBSummScreenFDRetrieval, MSMARCO, NanoArguAnaRetrieval, NanoClimateFeverRetrieval, NanoDBPediaRetrieval, NanoFEVERRetrieval, NanoFiQA2018Retrieval, NanoHotpotQARetrieval, NanoMSMARCORetrieval, NanoNFCorpusRetrieval, NanoNQRetrieval, NanoQuoraRetrieval, NanoSCIDOCSRetrieval, NanoSciFactRetrieval, NanoTouche2020Retrieval, TopiOCQA, TopiOCQAHardNegatives, MSMARCO-Fa, JaQuADRetrieval, Ko-StrategyQA, CUREv1, MIRACLRetrievalHardNegatives, NeuCLIR2022Retrieval, NeuCLIR2023Retrieval, WebFAQRetrieval, XQuADRetrieval, mMARCO-NL, Touche2020-NL, SNLRetrieval, SpanishPassageRetrievalS2P, SpanishPassageRetrievalS2S, VieQuADRetrieval, T2Retrieval, MMarcoRetrieval, DuRetrieval, CovidRetrieval, CmedqaRetrieval, EcomRetrieval, MedicalRetrieval, VideoRetrieval, WebQAT2TRetrieval, DKHateClassification, FinancialPhrasebankClassification, TweetTopicSingleClassification, DigikalamagClassification, FrenchBookReviews, HindiDiscourseClassification, SentimentAnalysisHindi, IndonesianIdClickbaitClassification, KannadaNewsClassification, KLUE-TC, KorFin, AfriSentiLangClassification, TurkicClassification, MyanmarNews, HateSpeechPortugueseClassification, SanskritShlokasClassification, SinhalaNewsClassification, SinhalaNewsSourceClassification, SpanishNewsClassification, SiswatiNewsClassification, SwahiliNewsClassification, UrduRomanSentimentClassification, IsiZuluNewsClassification, BibleNLPBitextMining, FloresBitextMining, IWSLT2017BitextMining, LinceMTBitextMining, NollySentiBitextMining, NusaTranslationBitextMining, NusaXBitextMining, PhincBitextMining, WebFAQBitextMiningQuestions, WebFAQBitextMiningQAs, DigikalamagClustering, NLPTwitterAnalysisClustering, SNLHierarchicalClusteringP2P, SNLHierarchicalClusteringS2S, SwednClusteringP2P, SwednClusteringS2S, PubChemSMILESPC, indonli, KLUE-NLI, TERRa, Ocnli, Cmnli, WebLINXCandidatesReranking, MIRACLReranking, T2Reranking, MMarcoReranking, CPUSpeedTask, GPUSpeedTask, FaroeseSTS, JSTS, KLUE-STS, MLSUMClusteringP2P.v2, SIB200ClusteringS2S, WikiClusteringP2P.v2
Timeouts	28	CodeRAGStackoverflowPosts, MSMARCOv2, NQ, ClimateFEVER-Fa, DBPedia-Fa, HotpotQA-Fa, NQ-Fa, MIRACLRetrieval, MrTidyRetrieval, MultiLongDocRetrieval, ClimateFEVER-NL, DBPedia-NL, FEVER-NL, HotpotQA-NL, NQ-NL, DBPedia-PL, HotpotQA-PL, MSMARCO-PL, NQ-PL, ClimateFEVER, DBPedia, FEVER, HotpotQA, RiaNewsRetrieval, mFollowIRCrossLingualInstructionRetrieval, mFollowIRInstructionRetrieval, MultiEURLEXMultilabelClassification, GerDaLIR
Unsupported modality	49	CUB200I2IRetrieval, FORBI2IRetrieval, GLDv2I2IRetrieval, METI2IRetrieval, NIGHTSI2IRetrieval, ROxfordEasyI2IRetrieval, ROxfordMediumI2IRetrieval, ROxfordHardI2IRetrieval, RP2kI2IRetrieval, RParisEasyI2IRetrieval, RParisMediumI2IRetrieval, RParisHardI2IRetrieval, SketchyI2IRetrieval, SOPI2IRetrieval, StanfordCarsI2IRetrieval, Birdsnap, Caltech101, CIFAR10, CIFAR100, Country211, DTD, EuroSAT, FER2013, FGVCAircraft, Food101Classification, GTSRB, Imagenet1k, MNIST, OxfordFlowersClassification, OxfordPets, PatchCamelyon, RESISC45, StanfordCars, STL10, SUN397, UCF101, CIFAR10Clustering, CIFAR100Clustering, ImageNetDog15Clustering, ImageNet10Clustering, TinyImageNetClustering, VOC2007, STS12VisualSTS, STS13VisualSTS, STS14VisualSTS, STS15VisualSTS, STS16VisualSTS, STS17MultilingualVisualSTS, STSBenchmarkMultilingualVisualSTS

Table 12. MMTEB models evaluated in this study, sorted by official MTEB leaderboard rank (as of arXiv v1). $\|\mu\|$ values computed from 10^5 English Wikipedia sentences.

Model	Size(MB)	$\|\mu\|$	MTEB rank
intfloat/multilingual-e5-large-instruct	1068	0.8491	7
Alibaba-NLP/gte-multilingual-base	582	0.6341	26
intfloat/multilingual-e5-small	449	0.8543	38
ibm-granite/granite-embedding-278m-multilingual	530	0.6882	44
ibm-granite/granite-embedding-107m-multilingual	204	0.7078	52
nomic-ai/nomic-embed-text-v1	522	0.5929	57
intfloat/e5-base-v2	418	0.8297	59
sentence-transformers/paraphrase-multilingual-MiniLM-L12-v2	449	0.6028	64
avsolatorio/GIST-Embedding-v0	418	0.7447	67
BAAI/bge-base-en-v1.5	390	0.5883	75
avsolatorio/GIST-small-Embedding-v0	127	0.7716	76
minishlab/potion-multilingual-128M	489	0.3450	79
intfloat/e5-small-v2	127	0.8464	82
intfloat/e5-base	418	0.8357	83
BAAI/bge-small-en-v1.5	127	0.6222	86
abhinand/MedEmbed-small-v0.1	127	0.7225	91
ibm-granite/granite-embedding-125m-english	238	0.8242	92
intfloat/e5-small	127	0.8579	93
Snowflake/snowflake-arctic-embed-m-long	522	0.7941	98
avsolatorio/GIST-all-MiniLM-L6-v2	87	0.8154	100
sergeyzh/LaBSE-ru-turbo	490	0.8039	101
Snowflake/snowflake-arctic-embed-m	415	0.7592	103
Snowflake/snowflake-arctic-embed-s	127	0.7826	104
Snowflake/snowflake-arctic-embed-m-v1.5	415	0.6221	107
cointegrated/LaBSE-en-ru	492	0.4115	108
ibm-granite/granite-embedding-30m-english	58	0.6907	110
sentence-transformers/all-MiniLM-L6-v2	87	0.1895	117
Mihaiii/Wartortle	66	0.6155	118
deepvk/USER-base	473	0.5039	120
Snowflake/snowflake-arctic-embed-xs	86	0.8023	124
Mihaiii/Squirtle	60	0.5954	128
sergeyzh/rubert-tiny-turbo	111	0.8570	130
minishlab/potion-base-8M	29	0.2301	131
cointegrated/rubert-tiny2	112	0.7997	138
jinaai/jina-embeddings-v2-base-en	262	0.7972	154
sentence-transformers/sentence-t5-large	639	0.8110	179
BAAI/bge-base-en	390	0.8237	189
sentence-transformers/sentence-t5-base	209	0.8399	192