Generative Skill Chaining: Long-Horizon Skill Planning with Diffusion Models

Abstract: Long-horizon tasks, usually characterized by complex subtask dependencies, present a significant challenge in manipulation planning. Skill chaining is a practical approach to solving unseen tasks by combining learned skill priors. However, such methods are myopic if sequenced greedily and face scalability issues with search-based planning strategy. To address these challenges, we introduce Generative Skill Chaining (GSC), a probabilistic framework that learns skill-centric diffusion models and composes their learned distributions to generate long-horizon plans during inference. GSC samples from all skill models in parallel to efficiently solve unseen tasks while enforcing geometric constraints. We evaluate the method on various long-horizon tasks and demonstrate its capability in reasoning about action dependencies, constraint handling, and generalization, along with its ability to replan in the face of perturbations. We show results in simulation and on real robot to validate the efficiency and scalability of GSC, highlighting its potential for advancing long-horizon task planning. More details are available at: `sites.google.com/view/generative-skill-chaining`.

Keywords: Manipulation Planning, Diffusion Models, Task and Motion Planning

1 Introduction

Long-horizon reasoning is crucial in solving real-world manipulation tasks that involve complex inter-step dependencies. An illustrative example is shown in Figure 1(bottom), where a robot must reason about the long-term effect of each action choice, such as the placement pose of the object and how to grasp and use the tool, in order to devise a plan that will satisfy various environment constraints and the final task goal (place object under rack). However, finding a valid solution often requires searching in a prohibitively large planning space that expands exponentially with the task length. Task and Motion Planning (TAMP) methods address such problems by jointly searching for a sequence of primitive skills (e.g., `pick`, `place`, and `push`) and their low-level control parameters. While effective, these methods require knowing the underlying system state and the kinodynamic models of the environment, making them less practical in real-world applications. This work seeks to develop a learning-based skill planning approach to tackle long-horizon manipulation problems.

Prior learning approaches that focus on long-horizon tasks often adopt the options framework [1, 2] and train meta-policies with primitive skill policies as their temporally-extended action space [3–8]. However, the resulting meta policies are *task-specific* and have limited generalizability beyond the training tasks. A number of recent works turn to *skill-level models* that can be composed to solve new tasks via test-time optimization [9–15]. Key to their successes are skill-chaining functions that can determine whether each parameterized skill can lead to states that satisfy the preconditions of the next skills in a plan, and eventually the success of the overall task. However, these methods are *discriminative*, meaning that they can only estimate the feasibility of a given plan and requires an exhaustive search process to solve a task. This bottleneck poses a severe scalability issue when dealing with increasingly complex and long skill sequences.

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Figure 1: **(Top)** Generative Skill Chaining (GSC) aims to solve a long-horizon task for a given sequence of skills by using linear probabilistic chains to parallelly sample from a joint distribution of multiple skill-specific transitions $q_\pi(\mathbf{s}, \mathbf{a}, \mathbf{s}')$ learned using diffusion models. The framework implicitly considers transition feasibility and subsequent skill affordability while demonstrating flexible constraint-handling abilities. **(Bottom)** An example of a long-horizon TAMP problem composed of multiple skills. Such a task necessitates reasoning inter-dependencies between actions.

In this paper, we propose a *generative* and *compositional* framework that allows direct sampling of valid skill chains given a plan skeleton. Key to our method is skill-level probabilistic generative models that capture the joint distribution of precondition - skill parameter - effect of each skill. Sampling a valid skill chain boils down to, for each skill in a plan, conditionally generating skill parameters and post-condition states that satisfy the pre-condition of the next skill, constrained by the starting state and the final goal. The critical technical challenge is to ensure that the sequence of skill parameters is achievable from the initial state (*forward flow*) to satisfy the long-horizon goal (*backward flow*) and account for additional constraints.

To this end, we introduce **Generative Skill Chaining (GSC)**, a framework to train individual skill diffusion models and combine them according to given unseen task skeletons with arbitrary constraints at test time. Each skill is trained as an unconditional diffusion model, and the learned distributions are linearly chained to solve for an unseen long-horizon goal during evaluation. Further, we employ classifier-based guidance to satisfy any specified constraints. GSC brings a paradigm shift in the approaches used to solve TAMP problems to date and uses probabilistic models to establish compositionality and reason for long-horizon dependencies without being trained on any such task. We demonstrate the efficiency of GSC on three challenging manipulation task domains, explore its constraint handling advantages, and deploy a closed-loop version on a physical robot hardware to show generalization capabilities and robustness.

2 Related Work

Task and Motion Planning. Understanding inter-dependencies between sequential actions is a fundamental challenge in solving long-horizon problems. The key idea for solving them is to break the planning problem into a symbolically feasible sequence of smaller subtasks [1–3, 7, 8] and characterize their solutions with primitive actions or skills [4–6]. Such approaches rely on formulating fully-observable conditions and accurate system dynamics forecasting [16, 17] to realize the precondition of applying skill (affordability) and its effect respectively [18–24]. In this direction, logic-geometric programming [25, 26] and hierarchical [27] frameworks have solved for the symbolic feasibility [18, 28, 29] of a sequence of skills sufficient to reach a goal condition from the initial state. While such methods are exhaustive, their strong assumptions limit their practical applications and scalability. To overcome this, we opt for a learning-based framework [11, 30].

Learning to solve long-horizon tasks. Skill-chaining methods model pre- and post-conditions of pre-defined skills to search for feasible goal-reaching plans, but most methods have focused on single-task settings [9–15]. Recent methods have investigated composable skill models to learn multi-task planner [11, 27, 30]. However, such methods are discriminative and require exhaustive searches. Moreover, their auto-regressive nature leads to cascading errors and large exploration spaces as the tasks become long. Recently, Agia et al. [11] proposed a CEM-based skill-chaining strategy that maximizes the success of individual actions in the sequence by training individual skills as RL agents. Their method is still limited to trained policy (deterministic) priors, lack finding multi-modal solutions, and cannot account for additional planning constraints.

Generative models for planning. Generative models have been widely used for planning with Gaussian processes [31] and adversarial networks [32, 33]. With recent advancements in diffusion model-based generative strategies for planning in robotics, such approaches have been adopted for imitation learning [34–38] and offline reinforcement learning [39, 40] settings. Most relevant to this work are `Diffuser` [39], `Decision Diffuser` [40] and `Diffusion Policy` [37]. While they can synthesize sequences of "states" (and/or "actions") as plans and optionally account for constraints [40], such approaches still focus on capturing the distribution of training task solutions and cannot easily solve unseen new tasks. In this work, we introduce a compositional generative planning method that can flexibly combine *skill-level generative model* and generalize to new tasks and constraints introduced during inference time. The proposed framework is inspired by the recent work on generating high-quality extended image chains with parallel diffusion [41] and scalable diffusion models with transformers [42].

3 Preliminaries

Problem formulation. We formulate the skill chaining problem by considering a given symbolically feasible skeleton $\Phi_K = \{(\pi_1, o_1), (\pi_2, o_2), \ldots, (\pi_K, o_K)\}$ of skills from a pre-defined library $\pi_{1:K} \in \Pi$ and the set of objects o on which the skill operates. Each skill $\pi \in \Pi$ is parameterized by a continuous set of feasible skill parameters $\mathbf{a} \in \mathcal{A}_\pi$ governing the desired motion while executing the skill from a state $\mathbf{s}$ in the state space $\mathcal{S}$. The goal is to find optimal skill parameters such that the skeleton is geometrically feasible and the effect of each skill satisfies the precondition of the following skills while the goal condition is satisfied.

Environment setup. We use expert policies to solve individual skills and collect *state-action-state* transitions between current ($\mathbf{s} \in \mathcal{S}$) and next state ($\mathbf{s}' \in \mathcal{S}$) resulting from the execution of a skill π with parameters $\mathbf{a}_\pi \in \mathcal{A}_\pi$ by following the transition model $\mathcal{T}_\pi : \mathcal{S} \times \mathcal{A}_\pi \to \mathcal{S}$. Further, following previous work [11], we consider a selection of basic objects like a hook, a rack, and boxes of various dimensions to construct the environmental setup. The state of the environment consists of fully observable poses and sizes of each of the present objects.

Diffusion models. The diffusion model is a parameterized model $p_\theta(\mathbf{x}_0)$ that estimates an unknown distribution $q(\mathbf{x}_0)$ using the samples $\mathbf{x}_0 \sim q_0(\mathbf{x}_0)$. It consists of two diffusion processes: a forward noising and a reverse denoising process. The forward process progressively injects *i.i.d.* Gaussian noise to samples from $q_0(\mathbf{x}_0)$ and leads to a family of noised distributions $q_t(\mathbf{x}_t)$. The distribution of $\mathbf{x}_t$ conditioned on the clean data $\mathbf{x}_0$ is also a Gaussian: $q_{0t}(\mathbf{x}_t|\mathbf{x}_0) = \mathcal{N}(\mathbf{x}_t; \mathbf{x}_0, \sigma_t^2 \mathbf{I})$, where σ_t defines a fixed series of noise levels monotonically increasing w.r.t. forward diffusion t. The reverse denoising process recovers clean data by iteratively removing the added noise by a process represented as the following stochastic differential equation (SDE) [43–45]:

$$d\mathbf{x} = -2\dot{\sigma}_t\sigma_t\nabla_{\mathbf{x}}\log q_t(\mathbf{x}_t)dt + \sqrt{2\dot{\sigma}_t\sigma_t}d\mathbf{w} \tag{1}$$

where $\nabla_{\mathbf{x}}\log q_t(\mathbf{x}_t)$ is referred to as the score function of the noised distribution and $\mathbf{w}_t$ is a standard Wiener process. We follow DDPM [46] sampling strategy in continuous settings [47]. The score function allows recovery of the minimum mean squared error estimator of $\mathbf{x}_0$ given $\mathbf{x}_t$ [48, 49]:

$$\tilde{\mathbf{x}}_0 := \mathbb{E}[\mathbf{x}_0|\mathbf{x}_t] = \mathbf{x}_t + \sigma_t^2\nabla_{\mathbf{x}_t}\log q_t(\mathbf{x}_t), \tag{2}$$

where we can treat $\tilde{\mathbf{x}}_0$ as a "denoised" version of $\mathbf{x}_t$ at timestep t. In practice, the unknown score function is estimated using a neural network $\epsilon_\theta(\mathbf{x}_t, t)$ by minimizing the denoising score matching [47] objective $\mathbb{E}_{t,\mathbf{x}_0}[\lambda(t)\|\sigma_t \nabla_{\mathbf{x}_t} \log q_{0t}(\mathbf{x}_t|\mathbf{x}_0) - \epsilon_\theta(\mathbf{x}_t, t)\|^2]$ where $\lambda(t)$ is a time-dependent weight. Diffusion models are scalable, and the learned distributions represent all positive samples satisfying the distribution heuristic, thus multi-modal. Further, their simple probabilistic representation allows a wide range of flexible sampling strategies [45, 46, 50, 51] combined with constraint-handling abilities [40, 52–54].

4   Methodology

Generative Skill Chaining (GSC) offers a new paradigm for approaching long-horizon planning with a given skeleton of skills. The primary objective of GSC is to determine the optimal skill parameters for an unseen task skeleton, such that executing the plan achieves a long-horizon goal while satisfying task-specific constraints. It introduces probabilistic chaining of distributions of short-horizon transitions to sample from a long-horizon trajectory distribution. GSC uses skill-level diffusion models to represent each skill's joint distribution of precondition, control parameters, and effect. Further, the framework composes individual skills at inference time to form a sequence-level trajectory distribution, which can be sampled via parallel diffusion to generate feasible skill parameter sequences as planning solutions. This is different from the widely used auto-regressive heuristic-search-based approach [17, 55–57] used in prior works [11, 30].

We consider a given skeleton Φ of skills (and relevant objects) which satisfies the symbolic feasibility of the sequence in the environment. The primary goal is to generate the sequence of states and skill parameters (as shown in Figure 2(a)) such that the final state (here $\mathbf{s}_f \equiv \mathbf{s}^{(2)}$) satisfies a goal condition and leads to the successful execution of the last skill.

(a)

(b)

Figure 2: **(a)** A linear chain graph for a long sequence of transitions and **(b)** adding an additional constraint node.

Action primitives as diffusion models. We characterize the individual skills by the nature of *state-action-state* transitions observed while executing it in the environment. The operation of each skill π can then be represented by an unconditional distribution $q_\pi(\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}'_t)$. Such a representation simultaneously captures the skill policy P_π and the transition dynamics distribution T_π and ensures their consistency. For each skill π in the skill library, we train a diffusion model score function $\epsilon_\pi(\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}'_t, t)$ with transformer backbone as shown in Figure 3 (right) using provided per-skill demonstration data. We represent the set of objects of interest by an order which denotes the relevance of the objects in the scene w.r.t. the skill[1] [11]. We also denote the masked sampling score model for the states and action as $\epsilon_\pi(\mathbf{s}_t, t)$, $\epsilon_\pi(\mathbf{s}'_t, t)$ and $\epsilon_\pi(\mathbf{a}_t, t)$ respectively.

Sequencing skill diffusion models. To solve our objective of finding a sequence of suitable skill transitions which satisfies Φ, an auto-regressive approach primarily used in prior works follows:

$$p_\Phi(\mathbf{s}^{(0:2)}|\mathbf{s}^{(0)}) \equiv P_{\pi_1}(\mathbf{a}^{(0)}|\mathbf{s}^{(0)}) \ T_{\pi_1}(\mathbf{s}^{(1)}|\mathbf{s}^{(0)}, \mathbf{a}^{(0)}) \ P_{\pi_2}(\mathbf{a}^{(1)}|\mathbf{s}^{(1)}) \ T_{\pi_2}(\mathbf{s}^{(2)}|\mathbf{s}^{(1)}, \mathbf{a}^{(1)})$$

However, such formulations are myopic and can only be rolled out in the forward direction without feedback from the final task goal. This limits long-horizon reasoning, and prior methods have leveraged random [30] or CEM-based rollouts [11] to sample from such a distribution. To overcome the above limitations, we transform the unconditional skill diffusion models into a forward and a backward conditional distribution, as

$$p_\Phi(\mathbf{s}^{(0:2)}|\mathbf{s}^{(0)}) \propto q_{\pi_1}(\mathbf{s}^{(0)}, \mathbf{a}^{(0)}, \mathbf{s}^{(1)}) q_{\pi_2}(\mathbf{a}^{(1)}, \mathbf{s}^{(2)}|\mathbf{s}^{(1)}) = \frac{q_{\pi_1}(\mathbf{s}^{(0)}, \mathbf{a}^{(0)}, \mathbf{s}^{(1)}) q_{\pi_2}(\mathbf{s}^{(1)}, \mathbf{a}^{(1)}, \mathbf{s}^{(2)})}{q_{\pi_2}(\mathbf{s}^{(1)})}$$

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[1]For example, if there is a hook (1), a box (2) and a rack (3) in the environment, then the object order corresponding to tasks are: (a) pick the box: $[2, 1, 3]$, (b) Place Box on Rack: $[2, 3, 1]$.

Figure 3: **Left** The primitive skills and their executions are shown with the objects of interest. **Right** Transformer-based skill diffusion model. We use the noisy *state-action-state* distribution $\mathbf{x}_t \sim \{\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}'_t\}$ at diffusion step t to obtain the corresponding ϵ_θ during sampling. The skill object order depends on the objects of interest and is represented as a collection of one-hot vectors.

$$p_\Phi(\mathbf{s}^{(0:2)}|\mathbf{s}^{(2)}) \propto q_{\pi_1}(\mathbf{s}^{(0)}, \mathbf{a}^{(0)}|\mathbf{s}^{(1)}) q_{\pi_2}(\mathbf{s}^{(1)}, \mathbf{a}^{(1)}, \mathbf{s}^{(2)}) = \frac{q_{\pi_1}(\mathbf{s}^{(0)}, \mathbf{a}^{(0)}, \mathbf{s}^{(1)}) q_{\pi_2}(\mathbf{s}^{(1)}, \mathbf{a}^{(1)}, \mathbf{s}^{(2)})}{q_{\pi_1}(\mathbf{s}^{(1)})}$$

In both equations above, the relations implicitly give rise to the notion of skill affordability and transition feasibility, i.e., the resulting state from the one skill must lie in the initial state distribution of the next skill and vice-versa. Now, if we transform the probabilities into their respective score functions ($\nabla_{\mathbf{x}} \log q(\mathbf{x})$) for a particular reverse diffusion sampling step t, we obtain:

$$\epsilon_\Phi(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) = \epsilon_{\pi_1}(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, t) + \epsilon_{\pi_2}(\mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) - \epsilon_{\pi_2}(\mathbf{s}_t^{(1)}, t) \quad (3)$$

$$\epsilon_\Phi(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) = \epsilon_{\pi_1}(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, t) + \epsilon_{\pi_2}(\mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) - \epsilon_{\pi_1}(\mathbf{s}_t^{(1)}, t) \quad (4)$$

respectively. Finally, we linearly combine the score functions from the forward and backward distributions weighted by a dependency factor γ:

$$\epsilon_\Phi(\mathbf{s}_t^{(1)}, t) = \gamma_{\pi_1} \, \epsilon_{\pi_1}(\mathbf{s}_t^{(1)}, t) + (1 - \gamma_{\pi_1}) \, \epsilon_{\pi_2}(\mathbf{s}_t^{(1)}, t), \quad (5)$$

Here, $\gamma \in [0, 1]$ is a decision variable that balances the influence of the state in the transition of the skill w.r.t. the subsequent skill and the goal condition. This is an important aspect that governs the behavior of the skills in the sequence and the choice of their respective parameters.

Classifier-based guidance for constraint satisfaction. Besides the final task goal, constraints play an important role in governing the feasibility of actions in the environment and specifying task-specific conditions, such as maximizing/minimizing the distance between two objects in an intermediate or final state. Our diffusion model-based formation allows GSC to easily incorporate additional constraints as implicit (in-painting) or explicit (classifier-based) guidance. Here we present a flexible sampling strategy in the presence of several planning constraints. In principle, the additional constraints Ψ can be appended as additional terms in the target sampling distribution:

$$p_{\Phi, \Psi}(\mathbf{s}^{(0:2)}) \propto p_\Phi(\mathbf{s}^{(0:2)}|\mathbf{s}^{(0)}) \; h(\{\mathbf{s}, \mathbf{a}\}_\Psi)$$

where $h(\cdot)$ is the likelihood of the constraint acting on a set of state-action nodes given by $\{\mathbf{s}, \mathbf{a}\}_\Psi$. The corresponding diffusion score function with the added constraints becomes

$$\epsilon_{\Phi, \Psi}(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) = \epsilon_\Phi(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) + \epsilon_\Psi(\{\mathbf{s}_t, \mathbf{a}_t\}, t) \quad (6)$$

where $\epsilon_\Psi(\{\mathbf{s}_t, \mathbf{a}_t\}, t) \propto \nabla_{\{\mathbf{s}_t, \mathbf{a}_t\}} \log h(\{\mathbf{s}_t, \mathbf{a}_t\}_\Psi)$. Consider the example shown in Figure 2(b) where the constraint depends on the nodes $\mathbf{a}^{(0)}, \mathbf{a}^{(1)}$ and $\mathbf{s}^{(2)}$. Suppose the constraint is chosen to be a binary indicator (i.e. success $= 1$) of satisfaction and is defined for the denoised samples $(\mathbf{a}_0^{(0)}, \mathbf{a}_0^{(1)}$

and $\mathbf{s}_0^{(2)}$) at $t = 0$. In such a situation, the likelihood is defined as the exponential of the constraint satisfaction such that

$$h_\Psi(\mathbf{a}_0^{(0)}, \mathbf{a}_0^{(1)}, \mathbf{s}_0^{(2)}) = \exp\left[-\alpha\left(1 - \Psi(\mathbf{a}_0^{(0)}, \mathbf{a}_0^{(1)}, \mathbf{s}_0^{(2)})\right)\right] \tag{7}$$

It is worth noting that while the constraint is a function of the denoised samples, the gradients must be calculated w.r.t. the noised samples. We calculate this by first obtaining the denoised sample $\tilde{\mathbf{x}}$ for the diffusion step t from Equation 2 and then modifying the corresponding nodes in $\epsilon_\Phi(\mathbf{s}_t^{(0)}, \mathbf{a}_t^{(0)}, \mathbf{s}_t^{(1)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t)$ based on the weight factor α, as

$$\tilde{\epsilon}_\Phi(\mathbf{a}_t^{(0)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) = \epsilon_\Phi(\mathbf{a}_t^{(0)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}, t) - \alpha\nabla_{\mathbf{a}_t^{(0)}, \mathbf{a}_t^{(1)}, \mathbf{s}_t^{(2)}}\left(1 - \Psi(\tilde{\mathbf{a}}_0^{(0)}, \tilde{\mathbf{a}}_0^{(1)}, \tilde{\mathbf{s}}_0^{(2)})\right) \tag{8}$$

Summary. To summarize, the proposed framework GSC is divided into three segments: (1) train individual skill diffusion models with the proposed architecture without any knowledge about other skills, (2) chain skill diffusion models according to an unseen task skeleton during inference using probabilistic linear chaining of the individually learned distributions with a dependency factor, and (3) incorporate classifier-based guidance for any unseen planning constraint added while inference. Following standard reverse denoising, we consider parallelly sampling from all individual models instead of one and hence our proposed approach is both task-skeleton and skeleton-length agnostic. Further, the dependency factor helps in making flexible design choices for satisfying the desired goal condition. While a constant value of $\gamma = 0.5$ is sufficient, it can be fine-tuned for every skill. In addition to the above, we also collect failure data to train a success probability prediction module $Q(\mathbf{s}, \mathbf{s}') : \mathcal{S} \times \mathcal{S} \rightarrow [0, 1]$ for each skill which is a measure of the successful execution of the skill given the current and the transitioned state. Such a model is used to consider the best parameter sequence from the sampled candidate solutions. We illustrate the overall algorithm in Appendix A.

5 Results

We conduct experiments to validate the efficacy of GSC in (1) long-horizon planning for unseen tasks of arbitrary lengths, (2) constraint handling and satisfaction, and (3) maximizing action-dependency horizon and finally (4) generalization to perturbations. First, we show the compositional and constraint-handling performance of GSC in a toy domain. Second, we evaluate the performance of the chaining trained skill diffusion models on nine standard TAMP tasks introduced by previous work [11]. These tasks encompass a wide range of skeleton lengths and challenge the method on various levels of long-horizon dependency. Finally, we discuss the response of GSC to perturbations, followed by the importance of dependency factor γ in the success of GSC.

Baselines and metrics. In the context of skill chaining, we primarily consider search-based methods with CEM optimization strategy. Our main baselines are CEM methods with uniform priors (**Random CEM**) and learned policy priors (**STAP**). Further, to show improvement in performance as compared to training on task sequences and expecting generalization to new ones, we add **DAF**'s [30] performance following Agia et al. [11]. Another potential

Figure 4: **Toy Domain:** We model four distributions of states and segment one of them into left and right segments. The above figure illustrates diffusion model composition using GSC with fixed start state and unit actions followed by the addition of soft and hard constraint guidance.

baseline is using diffusion for states only and inverse dynamics model for actions based on **Decision Diffuser** [40]. However, due to considerable distribution shift and cascading error from state predictions, such a method does not perform well (refer to Appendix B). The success rate of satisfying the goal condition in 100 random environment executions is used as the comparison metric[2].

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[2]We consider the same results for baselines as demonstrated in previous work [11].

Toy domain. The 2D domain consists of states as the $\mathbf{s} \triangleq (x, y)$ position of a point sample and the action, $\mathbf{a} = [u, v, a] \in \mathbb{R}^3$, as the direction of the unit vector (u, v) and magnitude (a). A transition is defined by $\mathbf{s}' = \mathbf{s} + [au, av]$. To replicate the skill distributions, we create multiple state distributions Figure 4(a) and collect transition data between them to represent individual skills. We illustrate the performance of GSC in chaining trained skill models Figure 4(b) to sample transitions between sequence of distributions Figure 4(c) with fixed initial state and unit action. Finally, we validate the constraint satisfaction performance by first constraining final states to the left segment and second, keeping the goal state fixed Figure 4(d)(e), respectively. The success in the above tasks validates the framework's ability to compose skills and handle arbitrary constraints directly while evaluation.

Long-horizon manipulation. We consider TAMP problems in a PyBullet [58] environment and follow the tasks proposed by STAP [11], namely: **(i) Hook Reach:** The hook is used to pull a box followed by executing other skills on the box. **(ii) Constrained Packing:** Multiple boxes should be placed on the rack so that all of them can be accommodated without interference. **(iii) Rearrangement Push:** A sequence of placement and push using a hook is executed to bring a box below the rack. The proposed three skeletons for each category above are solved using our method and compared against the previous work and their baselines w.r.t. the success rate is shown in Table 1. These tasks are unseen while training, have varying skeleton lengths, and demand reasoning long-horizon action dependencies. The performance of GSC implies that it is better than (or as good as) search-based methods, along with other advantageous abilities. The details about the target skeletons and the desired transitions are further explained in Appendix C.

Imposing additional constraints. In addition to the skeletons evaluated for the long-horizon problems and extending the experiments conducted for the toy domain, we impose certain planning constraints on the final state, intermediate states, and actions. This is done by adding an objective of maximizing the distance between all the "place" skill action parameters in the skeleton (this addition is still task agnostic) for the `constrained packing` task. The resulting sequence of states is shown in Figure 5. Further, we compare cumulative task completion and constraint satisfaction success rate with previous approaches in Table 2. This qualitatively and quantitatively demonstrates that the framework can handle such unseen constraints in test time.

Table 1: The success rate of the proposed GSC algorithm is shown and compared with relevant search-based baselines (CEM strategy). All results are calculated from 100 trials for each task.

Methods	Hook Reach			Rearrangement Push		
	Task 1	Task 2	Task 3	Task 1	Task 2	Task 3
Random CEM	0.54	0.40	0.30	0.30	0.10	0.02
DAF (Generalization)	0.32	0.05	0.0	0.0	0.08	0.0
STAP (Policy CEM)	0.88	0.82	0.76	0.40	0.52	0.18
GSC (Ours)	0.84	0.84	0.76	0.68	0.60	0.18

Figure 5: For a `constrained packing` task of picking-and-placing all the boxes on the rack: Task agnostic secondary placement objectives help in realizing accurate and consistent state-action sequences in **Top** Simulation and **Bottom** open loop hardware rollouts.

Generalizing to unseen sequences. We next highlight the generalization ability of GSC by evaluating it on more complex unseen task plans. First, we increase the maximum horizon dependency of action by changing the goal to position not only the box but also the hook in such a fashion which

Table 2: The success rate of GSC algorithm with and without task-agnostic constraint handling is shown for `Constrained Packing` task and compared with relevant baselines.

Methods	Constrained Packing		
	Task 1	Task 2	Task 3
Random CEM	0.45	0.45	0.10
DAF (Generalization)	0.45	0.70	0.0
STAP (Policy CEM)	0.65	0.68	0.20
GSC (Ours w/o constraint guidance)	0.70	0.80	0.50
GSC (Ours w/ constraint guidance)	0.75	1.0	1.0

complies with the success of the "push" skill in the `rearrangement push` domain. The resulting state sequence is shown in Figure 1 (bottom). Secondly, we execute our algorithm in a closed-loop fashion and use the skill success classifier to indicate sub-task completion. The sampled plan is executed and the resulting state is checked for subsequent skill feasibility. In case, the state satisfies the pre-condition for a future or previous skill, the plan is resampled from that skill to complete the task. We demonstrate this perturbation experiment on a Franka Panda arm (video attached to supplementary, hardware execution details in Figure E).

Importance of the forward and backward dependency. The dependency variable γ governs the flow of information from the initial state (forward) and the goal (backward) during the diffusion process. We provide a qualitative study of this feature in Figure 6. In the case where the forward flow information is weak ($\gamma = 0$), the model tends to hallucinate and predict states that are inconsistent with the initial state. When the backward flow is weak ($\gamma = 1$), the model becomes myopic and fails to solve the task. We empirically found that $\gamma = 0.5$ achieves a balanced performance.

Figure 6: Example of `rearrangement push` task rollout with different dependency factor γ: **Top: Hallucination** ($\gamma = 0$) With a weak forward signal, the framework fails to realize correct position of objects at the final stage. **Bottom: Myopic** ($\gamma = 1$) A weak backward information behaves like policy shooting and fails to understand long-horizon dependency.

6 Limitations

The proposed framework is only validated on a fully observable environment setup with no degree of partial observability and operates on low-dimensional state space of the system i.e. 6-DoF poses of the objects. While high-dimensional observations and stochastic dynamics is out of scope, we consider them as future extensions. We use a fixed set of primitive skills and thus the framework requires either expert policy / data to train models or the pre-trained models to perform compositional planning. This can be extended by incorporating skill discovery frameworks.

7 Conclusion

We introduced GSC, a new paradigm to solve TAMP tasks with given skeletons using skill-centric diffusion models. GSC trains high-quality skill diffusion models using a transformer backbone and composes skeleton-specific distributions for unseen skeletons by chaining trained individual skill distribution. Such skeleton-specific distributions are then used to generate long-horizon parameterized skill plan sequences. The framework is scalable and flexible and shows better constraint-handling capacities, and generalizes well to new scenarios, including perturbations and replanning.

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