Beyond Static Visual Tokens: Structured Sequential Visual Chain-of-Thought Reasoning

Abstract

Current multimodal LLMs encode images as static visual prefixes and rely on text-based reasoning, lacking goal-driven and adaptive visual access. Inspired by human visual perception—where attention is selectively and sequentially shifted from the most informative regions to secondary cues—we propose Structural Sequential Visual CoT (**SSV-CoT**). First, a question-relevant saliency map identifies and organizes key visual regions, explicitly modeling the spatial distribution of visual importance. Second, reasoning is performed following this discriminative order, inducing a curriculum-like semantic progression from primary to secondary cues. This method is trained end-to-end, using text cot and answer supervision, without relying on region-level annotations or specialized external tools. Experiments on diverse visual reasoning benchmarks show gains, validating structured and sequential visual cognition.

1 Introduction

Despite rapid advances in multimodal LLMs (Alayrac et al., 2022; Liu et al., 2023; Li et al., 2023; Dai et al., 2023), current systems still suffer from a fundamental limitation in how vision is integrated into reasoning. Most architectures encode an image once into visual tokens or a global embedding and inject it into the LLM as static context (Alayrac et al., 2022; Li et al., 2023; Liu et al., 2023). Reasoning then unfolds purely in text space: as the chain-of-thought grows, the model increasingly ignores the image, cannot revisit or operate on visual content, and lacks goal-directed visual actions such as selecting, refocusing, or comparing regions. As a result, visual perception and language reasoning remain largely disentangled, and vision functions as a passive prefix rather than an active part of cognition.

Existing attempts to mitigate this gap face significant drawbacks. External tool pipelines introduce

What can you infer about the current weather conditions?

Figure 1: MLLM lacks visual analysis, while SSV integrates cues through structured sequential reasoning to reach the correct answer.

cropping or detection but require complex orchestration (Wu et al., 2023; Chen et al., 2023). Region-based supervision depends on costly annotations (Lin et al., 2022; Khan et al., 2022). Generative visual-token or image synthesis is inefficient and poorly aligned with reasoning needs (Esser et al., 2021; Ding et al., 2022). Latent-space alignment methods learn global correspondences yet provide no explicit visual access steps (Radford et al., 2021; Li et al., 2023). Interleaved chain-of-thought methods re-inject visual tokens but enable passive re-attention over a large patch space, without modeling where to look next (Zhang et al., 2024b). None of these approaches support internal, sequential, goal-conditioned visual cognition.

As illustrated in Fig. 1, humans rarely solve visual tasks by processing an entire scene uniformly. Instead, they first form a coarse global impression and then sequentially attend to task-relevant regions as reasoning unfolds, a pattern well documented in studies of human visual attention and eye movements (Yarbus, 1967; Itti et al., 1998). In the example, the left approach (MLLM-CoT) fixates on the presence of snow-covered ground and ski equipment, ignores critical cues such as strong sunlight and sharp shadows, and arrives at an incorrect conclusion. In contrast, the right approach (SSV-CoT) explicitly guides visual attention through a structured sequence: it first focuses on salient re-

gions (e.g., ski equipment and shadows) and then integrates additional cues (e.g., lighting conditions) to refine the hypothesis, ultimately reaching the correct answer. This comparison highlights a fundamental limitation of existing multimodal large language models, which typically compress images into a fixed set of visual tokens and perform reasoning purely in text space (Alayrac et al., 2022; Li et al., 2023). While recent work on chain-of-thought reasoning has shown the benefits of explicit intermediate reasoning in language models (Wei et al., 2022), visual perception in current MLLMs remains largely passive and decoupled from the reasoning process. This disconnect between perception and cognition motivates our central question: can a model learn not only *what* to look at, but also *when* and *in which order* to look, driven directly by its ongoing reasoning?

Inspired by human visual cognition, we propose **SSV-CoT**, a multimodal reasoning framework that couples structured visual representation with sequential, goal-conditioned visual access. Given an image–question pair, SSV-CoT performs a single forward pass through a vision encoder and MLLM to construct a structured visual representation: a question-aware saliency map is generated, binarized, and decomposed via connected component analysis, yielding a bank of candidate region embeddings together with a global scene embedding. Conditioned on the evolving reasoning state, a visual cognition policy scores candidate regions and selects one region (or the global embedding) at each step, injecting its embedding into the MLLM, so that reasoning unfolds as an interleaved process of visual querying and textual inference. To reflect human attentional control, SSV-CoT further incorporates an adaptive stopping mechanism that dynamically determines whether to continue visual access, balancing evidence sufficiency against redundant queries.

The method is trained end-to-end from image–question—text cot-answer without gaze traces, bounding boxes, or external tools: a heuristic supervised stage initializes the policy by imitating a question-conditioned saliency ordering derived from the pretrained MLLM, followed by a GRPO reinforcement learning stage that optimizes visual selection using answer-level rewards with a visual-budget regularizer. Overall, SSV-CoT replaces one-shot visual token injection with a structured, sequential, and adaptive visual reasoning process aligned with human cognitive principles.

Our main contributions are three-fold:

- We model visual access in multimodal reasoning as a *human-inspired, goal-conditioned* process over structured visual units, rather than passive visual token injection.

- We propose a training framework that learns visual selection order from task-level feedback using text-cot and answer supervision, without region-level annotations.

- We introduce an *adaptive, budget-aware* visual reasoning mechanism that decides when to continue or stop visual querying during chain-of-thought reasoning.

2 Related Work

2.1 Visual Reasoning

A broad class of methods augments MLLMs with external visual tools for cropping, detection, or region selection (Schick et al., 2023; Chen et al., 2023; Yang et al., 2023; Aissi et al., 2025), but these rely on complex, non-differentiable pipelines with manually designed actions decoupled from internal reasoning. Another line of work introduces region-level supervision via bounding boxes, captions, or grounding annotations (Li et al., 2022; Yang et al., 2022; Kamath et al., 2021; Liu et al., 2024a), which improves controllability but requires costly labeling and exposes all regions upfront, preventing sequential selection. Related segmentation-based or region-level abstractions, such as SAM-derived masks or region-level ViTs (Kirillov et al., 2023; Chen et al., 2022; Ravi et al., 2024), provide structured features but are typically used as static inputs rather than a decision space. Overall, these approaches treat vision as fixed or externally controlled and do not enable internal, learnable, sequential visual cognition in MLLMs.

2.2 Interleaved Visual Reasoning

Interleaved chain-of-thought methods reintroduce visual tokens during reasoning to alleviate image forgetting (Zhang et al., 2024b; Chen et al., 2025a; Shao et al., 2024; Zhang et al., 2024a; Li and Ma, 2025). While effective for multi-hop visual question answering and chart reasoning, these approaches repeatedly attend to the same static patch set and perform passive re-attention, without modeling where to look next or how visual access should evolve over time. Relatedly, sequential perception models such as glimpse networks and

active-vision agents (Mnih et al., 2014; Ba et al., 2015; Jaegle et al., 2022) demonstrate the benefits of goal-conditioned sequential inspection, but typically rely on small-scale vision architectures or reinforcement learning pipelines that do not scale to LLM-level multimodal reasoning. Overall, although recurrent and interleaved methods improve visual reasoning, they fail to support task-driven, autoregressive visual access that is tightly coupled with the reasoning process, leaving dynamic visual cognition largely unaddressed.

3 Methodology

3.1 Overview

Existing interleaved reasoning methods repeatedly inject dense patch-level visual tokens, often causing redundant signals and unstable reasoning. In contrast (Fig. 2), we first abstract the image into a compact set of question-conditioned visual regions and then perform *sequential visual access* over this region space. We introduce **SSV-CoT**, which decomposes multimodal reasoning into two stages: (1) **Structured Visual Cognition**, constructing salient question-aware region embeddings in a single forward pass; and (2) **Sequential Visual Access**, where a lightweight policy dynamically selects regions at each reasoning step.

3.2 Problem Formulation and Inference Process

Given an image x and question q_{txt}, the model generates an answer by interleaving textual reasoning with selective visual access. Visual reasoning is formulated as a sequence of region-selection actions, where each step selects a region or terminates. At each reasoning step, the model queries a structured region embedding bank based on the current reasoning state until a STOP action produces the final answer.

Formally, while conventional multimodal CoT methods generate purely text-based reasoning steps

$$s^{(1)}, s^{(2)}, \ldots, s^{(K)}, \quad y = \text{LLM}(V, T), \quad (1)$$

where $V = {v_\tau}_{\tau=1}^{N}$ denotes static visual tokens extracted from the image and T is the input question, our approach explicitly models reasoning as an interleaved decision process:

$$a_1, s^{(1)}, a_2, s^{(2)}, \ldots, a_T, s^{(T)}, \quad y = \text{LLM}(\mathcal{E}, T), \quad (2)$$

where each action a_t selects a region embedding from the structured visual space $\mathcal{E}$ (or triggers STOP), grounding each reasoning step in task-relevant visual evidence.

3.3 Structured Visual Cognition

The first stage builds a compact, question-conditioned, and spatially structured image representation (Fig. 2), aiming to identify a small set of discriminative regions relevant to the question without region-level supervision. Region geometry and base features come from the pretrained vision encoder, while region importance is inferred through question-conditioned multimodal interactions.

Question-conditioned saliency map. Given an image x, we extract patch-level features $h_v = z_{ij}$ using a vision encoder, where z_{ij} denotes patch embeddings on an $H \times W$ grid. We then run the pretrained MLLM on the image–question pair (x, q_{txt}) and obtain the final textual representation q together with multimodal visual tokens $\tilde{z}ij$. Since they lie in a shared embedding space, we compute a question-conditioned saliency score for each patch via

$$Sij = \text{sim}(q, \tilde{z}ij), \quad (3)$$

which reflects the relevance of each spatial location to the question. The saliency map is further normalized to improve robustness:

$$\tilde{S}ij = \frac{S_{ij} - \min(S)}{\max(S) - \min(S)}. \quad (4)$$

Binary masking and connected component analysis. We convert the normalized saliency map $\tilde{S}$ into a binary mask by thresholding:

$$M(i, j) = \mathbb{I}\big[\tilde{S}_{ij} \geq \tau\big], \quad (5)$$

where τ is an adaptive threshold (e.g., Otsu's method) and $\mathbb{I}[\cdot]$ denotes the indicator function.

We then apply connected-component analysis on M under an 8-neighborhood connectivity criterion to obtain a set of candidate regions $\{\mathcal{R}_k\}$. Each region $\mathcal{R}_k$ consists of a connected set of salient patch indices. Small components below a minimum area threshold are discarded to remove spurious noise.

Global complement embedding. To ensure full image coverage and provide robustness against imperfect saliency estimation, all remaining patches not covered by the Top-N regions are aggregated into a single global complement region:

$$e_{\text{global}} = \frac{1}{|\mathcal{I}_{\text{rest}}|} \sum_{(i,j) \in \mathcal{I}_{\text{rest}}} z_{ij}. \quad (6)$$

Figure 2: Overview of the **SSV-CoT** framework. The model first constructs question-aware structured visual regions, then performs sequential visual access during chain-of-thought reasoning to progressively integrate visual evidence and generate the final answer.

Discriminative region construction. Given the connected components $\{\mathcal{R}_k\}$ from the binary saliency mask, we treat each $\mathcal{R}_k$ as a candidate visual region and collect its patch-level visual tokens $\{v_j\}_{j=1}^m$. We adopt an adaptive token compression strategy with a fixed budget $n = 48$. If $m \leq n$, all tokens are preserved and projected individually via a visual projector. Otherwise, we select the top-n tokens by saliency and apply k-means clustering to obtain representative region tokens. Formally, the region representation is a set of projected tokens:

$$E_k = g_{\text{proj}}\big(\{z_{ij} \mid (i,j) \in \mathcal{R}_k\}\big), \quad k = 1, \ldots, N, \tag{7}$$

where $g_{\text{proj}}(\cdot)$ denotes a permutation-invariant region projector that produces a fixed-size set of region tokens.

After obtaining region embeddings, we quantify the discriminativeness of each region by computing a region-level score as the average of the normalized saliency values within the region:

$$\rho_k = \frac{1}{|\mathcal{R}_k|} \sum_{(i,j)\in\mathcal{R}_k} \tilde{S}_{ij}. \tag{8}$$

This score measures the overall saliency consistency of the region with respect to the given question. Regions are then ranked according to ρ_k, and the Top-N highest-scoring regions are selected as discriminative local regions for subsequent sequential visual reasoning. The final output of structured visual cognition is a compact region embedding bank:

$$\mathcal{E} = \{e_1, \ldots, e_N, e_{\text{global}}\}, \tag{9}$$

which provides a structured, question-conditioned abstraction of the image and serves as the candidate visual space for subsequent sequential visual access.

The structured region construction—including Otsu-based thresholding, binary masking, connected-component analysis, and Top-N selection—is treated as a deterministic, non-learnable preprocessing step performed at inference time, while all learnable parameters are confined to the projector, policy module, and the MLLM.

3.4 Sequential Visual Access

The second stage performs task-driven, step-aligned visual reasoning over the structured region space, corresponding to the right part of Figure 2.

Step-aware triggering. During chain-of-thought decoding, we treat the newline character \n as an implicit step boundary. Each time a newline is generated, the model completes a reasoning step and triggers a visual selection decision.

Let $h_t \in \mathbb{R}^{D_L}$ denote the final-layer hidden state of the newline token at step t. This hidden state summarizes the current reasoning context and serves as the query for visual selection.

Similarity-based region scoring. At each reasoning step t, we obtain the hidden state of the signal token $h_t \in \mathbb{R}^{D_L}$, which summarizes the current reasoning context. We first project the signal

token through a signal projector:

$$\tilde{h}_t = W_{\text{sig}} h_t \in \mathbb{R}^{D_L}. \qquad (10)$$

Similarly, each region token embedding $e_k \in \mathbb{R}^{D_v}$ is projected into the language space via a visual projector:

$$\tilde{e}_k = W_{\text{vis}} e_k \in \mathbb{R}^{D_L}. \qquad (11)$$

We then compute similarity scores between the projected signal token and all projected region embeddings:

$$s_{t,k} = \text{sim}(\tilde{h}_t, \tilde{e}_k), \quad k \in \{1, \ldots, K\}. \qquad (12)$$

To enable adaptive termination of visual access, we additionally include a learnable STOP embedding, which is scored in the same manner as region tokens.

Policy and action execution. The policy head g_θ induces a distribution over actions:

$$\pi_\theta(a_t = k \mid s_t) = \text{softmax}(s_t)_k, \qquad (13)$$

where $k \in \{1, \ldots, K, \text{STOP}\}$. If $a_t = k$, the corresponding region embedding is injected to condition subsequent reasoning; if $a_t = \text{STOP}$, the model produces the final answer without further visual input.

3.5 Training Procedure

We train SSV-CoT with a two-stage protocol using image–question–textual CoT–answer data, without any supervision on visual regions or access order. To mitigate noisy early saliency estimates, we adopt a probabilistic curriculum that gradually shifts from random visual access to structured, discriminative region reasoning. The pipeline consists of (1) heuristic supervised fine-tuning to initialize the visual access policy aligned with textual chain-of-thought reasoning, and (2) GRPO-based reinforcement learning to refine the visual cognition order using answer-level rewards.

Stage I: Heuristic Supervised Fine-Tuning with Probabilistic Curriculum The goal of the first stage is to teach the model how to interleave textual reasoning with visual region access, rather than to learn a perfect visual selection strategy. However, saliency maps estimated from a pretrained MLLM are often noisy at early training stages, which may lead to unstable optimization if directly used as supervision.

To stabilize training, we adopt a probabilistic curriculum learning strategy. Specifically, we define a curriculum coefficient $\lambda_e \in [0, 1]$ for epoch e, which linearly increases from 0 to 1 during a warm-up period of E_{warm} epochs:

$$\lambda_e = \min\left(1, \frac{e}{E_{\text{warm}}}\right). \qquad (14)$$

For each training sample $(x, q_{\text{txt}}, a_{\text{gold}})$, we construct a pseudo-expert region ordering as follows: With probability $1 - \lambda_e$, we sample regions using a random region strategy, which selects spatially contiguous image blocks independent of the question. With probability λ_e, we apply the proposed question-conditioned discriminative region selection method described in Section 3.3, and rank the resulting regions by their saliency scores.

The resulting region sequence $(r_1, \ldots, r_T)$ is treated as a heuristic viewing trajectory. During SFT, we perform behavior cloning on the visual access policy by minimizing the cross-entropy loss:

$$\mathcal{L}_{\text{SFT}} = -\sum_{t=1}^{T} \log \pi_\theta(a_t = r_t \mid s_t), \qquad (15)$$

where s_t denotes the policy state at reasoning step t.

This curriculum-guided SFT initializes the policy with stable region–text interleaving behavior while avoiding overfitting to unreliable early saliency signals.

Stage II: GRPO-Based Reinforcement Learning with Mixed Exploration While the heuristic policy learned in Stage I provides a stable initialization, it is not directly optimized for end-task performance. In the second stage, we refine the visual access policy using reinforcement learning with answer-level supervision.

Given a training sample $(x, q_{\text{txt}}, a_{\text{gold}})$, we fix the image and question and sample a group of K trajectories using a mixed sampling policy:

$$\pi_{\text{mix}} = (1 - \lambda_e) \pi_{\text{rand}} + \lambda_e \pi_\theta, \qquad (16)$$

where π_{rand} denotes a random region selection policy and π_θ is the current learned policy. The same curriculum coefficient λ_e is used to gradually shift from exploration to exploitation.

Each trajectory i yields a region access sequence $g^{(i)}$, a generated answer $\hat{a}^{(i)}$, and a scalar reward $R^{(i)}$ computed solely based on answer quality.

Within each group, we compute the group-relative advantage:

$$A^{(i)} = R^{(i)} - \frac{1}{K} \sum_{j=1}^{K} R^{(j)}. \qquad (17)$$

The policy is optimized using the GRPO objective:

$$\mathcal{L}_{\text{RL}} = -\sum_{i=1}^{K} \sum_{t=1}^{T_i} A^{(i)} \log \pi_\theta(a_t^{(i)} \mid s_t^{(i)}). \qquad (18)$$

To prevent large deviations from the SFT-initialized policy, we additionally apply a KL regularization term:

$$\mathcal{L}_{\text{KL}} = \mathbb{E}_s \left[\text{KL}\big(\pi_\theta(\cdot \mid s) \, \| \, \pi_{\text{SFT}}(\cdot \mid s)\big) \right]. \qquad (19)$$

The final optimization objective is:

$$\min_\theta \ \mathcal{L}_{\text{RL}} + \beta \, \mathcal{L}_{\text{KL}}. \qquad (20)$$

The reward is a linear combination of four terms:

$$r = r_{\text{task}} + \lambda_1 \, r_{\text{format}} - \lambda_2 \, r_{\text{length}} - \lambda_3 \, r_{\text{vision}}. \qquad (21)$$

Here, r_{task} is the task reward: for multiple-choice or numeric questions, it is 1 if the answer is exactly correct and 0 otherwise; for open-ended math reasoning, we use exact match with numerical-tolerance checking. The format reward r_{format} encourages compliance with a predefined *reasoning–answer* output template, and invalid formatting or missing a final answer is penalized. The length penalty r_{length} is proportional to the number of generated tokens to discourage overly verbose reasoning. The vision penalty r_{vision} is proportional to the number of visual access steps (or queried regions) to discourage excessive visual reliance and promote discriminative, budget-aware visual usage with adaptive stopping.

4 Experiments

4.1 Experimental Datasets

We evaluate our method on a diverse set of visual reasoning benchmarks. For commonsense visual reasoning, we use M3CoT (Zhang et al., 2024b), ScienceQA (Lu et al., 2022), and LLaVA-Bench In-the-Wild (LLaVA-W) (Liu et al., 2023). M3CoT focuses on multi-domain, multi-step multimodal reasoning, ScienceQA serves as a standard benchmark

for general VLM reasoning, and LLaVA-W evaluates fine-grained visual understanding via long-form answers with GPT-4V references. For mathematical visual reasoning, we adopt MathVista (Lu et al., 2024a) and MathVision (Wang et al., 2024a), which require both fine-grained visual perception and multi-step mathematical reasoning.

For training data, we use the M3CoT training set and the LLaVA-CoT-100k (Xu et al., 2025) training set for commonsense visual reasoning. For mathematical visual reasoning, we adopt MathV360K (Shi et al., 2024), from which we carefully select over 50K diverse samples and generate textual chain-of-thought annotations using GPT-4V. All the above datasets contain textual chain-of-thought annotations and do not include any visual grounding or visual token-level annotations.

4.2 Compared Methods

For **commonsense visual reasoning**, we compare our method with several representative reasoning strategies, all instantiated on the same QWEN2-VL-7B backbone for fairness. **Multi-modal CoT** (Zhang et al., 2024b) generates text-only intermediate reasoning steps before producing the final answer. **CCoT** (Mitra et al., 2024) constructs a scene graph to capture compositional object relations and uses it to guide answer generation. **DDCoT** (Zheng et al., 2023) decomposes the question into sub-questions and answers them using a VLM. **SCAFFOLD** (Lei et al., 2024) overlays coordinate grids onto images to expose fine-grained spatial information and guides reasoning with these coordinates. **ICoT** (Gao et al., 2025) repeatedly re-injects visual tokens during CoT while treating visual patches uniformly.

For **mathematical visual reasoning**, we compare our method against a set of strong recent vision-language models, including MiniCPM-V-2.6 (Yao et al., 2024), VITA-1.5 (Fu et al., 2025), LLaVA-CoT (Xu et al., 2025), Qwen2-VL-7B (Wang et al., 2024b), InternVL2.5 (Chen et al., 2025b), POINTS (Liu et al., 2024b), Ovis (Lu et al., 2024b), and TVC-Qwen2-VL-7B (Sun et al., 2025). TVC-Qwen2-VL-7B mitigates visual forgetting in multimodal long-chain reasoning by periodically reintroducing compressed visual inputs during reasoning.

4.3 Model Implementation

We use Qwen2-VL-7B as the base model in our experiments. Both projectors are implemented as

Methods	M3CoT ACC.↑	ScienceQA ACC.↑	LLaVA-W ROUGE-L↑
Qwen2-VL-7B	43.6	56.3	32.7
MultimodalCoT	40.1	51.3	30.7
CCoT	43.3	56.4	29.4
DDCoT	42.6	55.2	31.2
SCAFFOLD	41.7	53.7	31.8
ICoT	44.1	56.8	34.2
SSV-CoT (Ours)	**44.9**	**57.3**	**35.7**

Table 1: **Commonsense visual reasoning results.** Comparison of SSV-CoT applied to Qwen2-VL-7B with CoT-based methods (including No-CoT, MultimodalCoT, CCoT, DDCoT, SCAFFOLD, and ICoT) on M3CoT (Accuracy), ScienceQA (Accuracy), and LLaVA-W (ROUGE-L). The best result for each benchmark is highlighted in bold.

Model	MathVista Acc. ↑	MathVision Acc. ↑	Average Acc. ↑
MiniCPM-V-2.6	60.8	18.4	39.6
VITA-1.5	66.2	19.5	42.9
LLaVA-CoT	52.5	19.9	36.2
Qwen2-VL-7B	60.9	16.3	38.6
InternVL2.5	64.5	17.0	40.8
POINTS 1.5	66.4	22.0	44.2
Ovis1.6-Gemma2	70.2	20.6	45.4
TVC-Qwen2-VL-7B	68.1	22.7	45.4
SSV-CoT (Ours)	**72.2**	**23.5**	**47.9**

Table 2: **Mathematical visual reasoning results.** Comparison of SSV-CoT applied to Qwen2-VL-7B with vision-language models on MathVista (Accuracy) and MathVision (Accuracy). The best results are highlighted in bold.

Methods	M3CoT ACC.↑	ScienceQA ACC.↑	LLaVA-W ROUGE-L↑
SSV-CoT	44.9	57.3	35.7
w/o SR	43.5 (-1.4)	56.1 (-1.2)	33.9 (-1.8)
w/o SS	43.8 (-1.1)	56.4 (-0.9)	34.2 (-1.5)
w/o AS	44.3 (-0.6)	56.9 (-0.4)	35.0 (-0.7)

Table 3: Ablation study of SSV-CoT on commonsense visual reasoning benchmarks. SR denotes Structured Regions, SS denotes Sequential Selection, and AS denotes Adaptive Stopping. Numbers in parentheses denote performance degradation compared with the full model.

4.4 Overall Performance

Overall, the experimental results indicate that SSV-CoT leads to consistent improvements in long-context multimodal reasoning across both commonsense and mathematical tasks.

For commonsense visual reasoning (Table 1), SSV-CoT shows moderate gains over the Qwen2-VL-7B backbone, with improvements of +1.3 Accuracy on M3CoT, +1.0 Accuracy on ScienceQA, and +3.0 ROUGE-L on LLaVA-W. Compared with ICoT, which interleaves visual tokens while treating image patches uniformly, SSV-CoT better preserves task-relevant visual information through goal-conditioned and sequential visual selection, resulting in more stable performance across benchmarks.

For mathematical visual reasoning (Table 2), SSV-CoT also improves upon the Qwen2-VL-7B baseline, increasing the average score from 38.6 to 47.9. In comparison to TVC, which alleviates

visual forgetting by periodically reintroducing compressed visual inputs, SSV-CoT further aligns visual selection with reasoning objectives, supporting more effective use of visual information in multi-step mathematical reasoning.

Overall, these results suggest that SSV-CoT helps mitigate visual forgetting and supports task-aware visual grounding, contributing to improved performance across diverse visual reasoning scenarios.

5 Discussion

5.1 Ablation Experiment

We ablate SSV-CoT to assess the contribution of its core components across three commonsense visual reasoning benchmarks (Table 3), with the following settings: (1) *w/o Structured Regions*: the model does not construct question-conditioned structured regions and directly injects raw visual tokens, resembling patch-level interleaved reasoning; (2) *w/o Sequential Selection*: all region embeddings are injected at once, removing the sequential visual access order; (3) *w/o Adaptive Stopping*: the model is forced to attend to a fixed number of regions without dynamically deciding when to stop visual querying.

The results show that all components contribute to SSV-CoT. Removing structured regions causes the largest performance drop, while disabling sequential selection also consistently degrades performance. In contrast, removing adaptive stopping leads to smaller but stable declines. Performance drops are more pronounced on M3CoT and LLaVA-W than on ScienceQA, reflecting their stronger reliance on fine-grained visual information.

5.2 In-depth Analysis

Structure and order are mutually reinforcing. Table 4 jointly ablates visual structure and cog-

4.3 (continued)

single-layer linear modules, and we uniformly set the similarity filtering threshold to $\theta = 0.7$. See the appendix for detailed settings.

Figure 3: Comparison of Text-CoT and SSV-CoT on Qwen2-VL-7B for visual reasoning. Errors are shown in red. Only selected regions are displayed, and numbers indicate the token injection order.

Visual repr.	Order (Acc@1 %)	
	Random	Cognition
Patch subset	63.1	65.4
Saliency regions	68.0	72.2

Table 4: 2×2 ablation of visual structure and cognition order on MathVista. Each cell reports Acc@1 (%). All variants share the same visual token budget and maximum steps K.

Strategy	Acc@1 (%)	Avg #regions
Fixed-K=2 (Seq)	68.5	2.0
Fixed-K=3 (Seq)	71.0	3.0
Fixed-K=4 (Seq)	71.3	4.0
Adaptive-K (Ours)	72.2	2.7

Table 5: Visual budget analysis on MathVista. Fixed-K variants always query exactly K regions. Our adaptive-K policy learns when to stop via a <STOP> action, achieving comparable or better accuracy with fewer region queries on average.

nition order on MathVista. Using unstructured patch subsets with a random schedule (*Patch subset, Random*) gives the weakest performance. Introducing a learned access order on top of the same patches (*Patch subset, Cognition*) yields a modest gain (63.1→65.4), suggesting that sequential, goal-conditioned access helps even with weak visual units. Replacing patches with saliency-based regions under a random order (*Saliency regions, Random*) brings a larger improvement (63.1→68.0), showing that structured, semantically coherent regions are crucial on their own. Our full model (*Saliency regions, Cognition*) combines both ingredients and achieves the best accuracy (72.2), with gains that exceed either modification in isolation. This pattern indicates that region structure and cognition order are complementary: the policy needs good regions to reason over, and good regions are used most effectively when queried in a learned sequence.

Adaptive visual budget. Table 5 analyzes how the visual budget interacts with the sequential policy. Increasing the fixed number of region queries from K=2 to K=3 substantially improves performance (68.5→71.0), but further raising the budget to K=4 yields only marginal gains (71.3) while forcing the model to inspect more regions. In contrast, our adaptive-K variant, equipped with a learned <STOP> action, reaches the highest accuracy (72.2) while using 2.7 regions on average. This shows that the model not only learns *where* and *in which order* to look, but also *how much* visual evidence is needed for a given question, yielding more accurate reasoning with a tighter and automatically controlled visual budget.

5.3 Case Study

This Fig. 3 compares the performance of Text-CoT and Structured Visual Reasoning (SSV-CoT) in two typical cases: common-sense visual reasoning (top) and mathematical visual reasoning (bottom). In the common-sense case, Text-CoT focuses on salient but incomplete clues (e.g., multiple ATVs) while ignoring finer contextual details, leading to incorrect conclusions. In contrast, SSV-CoT sequentially focuses on task-relevant areas (boat, trailer, background), progressively integrating evidence to arrive at the correct answer. In the mathematical case, Text-CoT relies on a holistic description of the structure, misinterpreting the spatial layout. However, SSV-CoT explicitly selects and infers key areas (projection, column continuity, extension, and height), enabling accurate spatial reasoning.

6 Conclusion

We introduce SSV-CoT, which frames visual cognition in multimodal reasoning as a structured, sequential process instead of static token injection. Trained with chain-of-thought supervision and answer-level rewards, SSV-CoT learns visual selection and stopping without region annotations or external tools. Empirical results across common-sense and math benchmarks demonstrate consistent improvements and highlight the importance of structured regions and adaptive visual access.

Limitations

SSV-CoT introduces additional computation due to sequential visual access compared with one-shot visual token injection. Moreover, its effectiveness depends on the quality of question-conditioned saliency, which may be less reliable in visually ambiguous scenes. Extending the method to more complex settings such as videos remains future work.

Ethical Considerations

SSV-CoT is trained on existing vision-language datasets and does not require additional annotations or external tools. Like other vision-language models, it may inherit biases from the training data. Care should be taken when applying the method in real-world or high-stakes scenarios.

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A Algorithm

Algorithm 1 Question-aware Discriminative Region Selection with Adaptive Token Compression

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Require: Image x, text query q, multimodal model $\mathcal{M}$, number of regions N, token budget n
Ensure: Region set $\mathcal{R} = \{R_1, \ldots, R_N\}$ and region tokens $\{E_k\}_{k=1}^N$

$V \leftarrow \text{VisionEncoder}_{\mathcal{M}}(x), \ t \leftarrow \text{TextEncoder}_{\mathcal{M}}(q)$

$A(i,j) \leftarrow \text{sim}(v_{i,j}, t), \ \tilde{A} \leftarrow \text{Normalize}(A)$

$M \leftarrow \tilde{A} \geq \text{OtsuThreshold}(\tilde{A})$
$\{R_k\} \leftarrow \text{ConnectedComponents}(M)$

Compute $\rho_k = \frac{1}{|R_k|} \sum_{(i,j) \in R_k} \tilde{A}(i,j)$
Select top $(N-1)$ regions by ρ_k
$R_N \leftarrow \Omega \setminus \bigcup_{k=1}^{N-1} R_k$

for each region R_k **do**
  Collect region tokens $\{v_j\}_{j=1}^m$
  if $m \leq n$ **then**
    $E_k \leftarrow \{\text{Proj}(v_j)\}_{j=1}^m$
  else
    Select top-n tokens by saliency
    Cluster selected tokens with k-means
    $E_k \leftarrow \{\text{Proj}(\bar{v}_i)\}_{i=1}^n$

return $\{\mathcal{R}, E_k\}_{k=1}^N$

Algorithm 1 describes the question-aware region selection process. We compute a query-conditioned saliency map over visual patches, apply adaptive thresholding and connected-component analysis to obtain candidate regions, and select the top $N-1$ regions by average saliency, with the remaining area treated as background.

B Key Implementation Details

Region Embedding Injection. Given an input image x and question q, we first obtain N discriminative regions $\{\mathcal{R}_k\}_{k=1}^N$ and compute a region embedding $e_k \in \mathbb{R}^{d_v}$ for each region. Each region embedding is projected to the LLM hidden dimension via a linear projector:

$$\hat{e}_k = \text{Proj}(e_k) \in \mathbb{R}^{d_{\text{LM}}}.$$

The projected region embeddings are concatenated as additional visual prefix tokens and prepended to the original multimodal input. The final input sequence is:

$$[\hat{e}_1, \ldots, \hat{e}_N, \ <\text{image tokens}>, \ <\text{text tokens}>].$$

Region tokens are injected only at the input stage as fixed prefixes; they neither replace nor accumulate over the original visual tokens, and the number of region tokens is fixed to N during inference.

Region Selection and Hyperparameters. We set the default number of regions to $N = 5$, consisting of $N-1$ discriminative regions and one background region. Regions are generated via Otsu-based adaptive thresholding over a similarity heatmap, followed by connected-component analysis. Components with area smaller than $\alpha = 0.01 \times HW$ (where H, W denote the feature map resolution) are discarded. The remaining regions are ranked by their average activation score ρ_k, and the top $N-1$ regions are selected.

GRPO Reward Design. We train the model using GRPO, where the reward is defined as a weighted sum:

$$r = r_{\text{task}} + \lambda_1 r_{\text{format}} - \lambda_2 r_{\text{length}} - \lambda_3 r_{\text{vision}}.$$

Here, r_{task} measures answer correctness, r_{format} enforces valid output structure, r_{length} penalizes overly long generations, and r_{vision} penalizes excessive visual access. We set the weights to

$$\lambda_1 = 0.2, \quad \lambda_2 = 0.01, \quad \lambda_3 = 0.05.$$

Training Configuration. We use Qwen2-VL-7B as the base multimodal large language model (MLLM) in our experiments. Both projectors are implemented as single-layer linear modules. The training procedure consists of two stages: (1) Supervised Fine-Tuning (SFT), where we train for 3 epochs with a learning rate of 1×10^{-6} and a batch size of 64; and (2) Reinforcement Learning (RL), where we train for 700 steps with group size $G = 4$, a weighting factor $\lambda = 0.02$, a learning rate of 1×10^{-6}, and a batch size of 16. During training, the vision encoder is kept frozen, while all remaining model parameters (including the projector layers) are unfrozen and optimized.