What if Tomorrow is the World Cup Final? Counterfactual Time Series Forecasting with Textual Conditions

Abstract

Time series forecasting has become increasingly critical in real-world scenarios, where future sequences are influenced not only by historical patterns but also by forthcoming events. In this context, forecasting must dynamically adapt to complex and stochastic future conditions, which introduces fundamental challenges in both forecasting and evaluation. Traditional methods typically rely on historical data or factual future conditions, while overlooking counterfactual scenarios. Furthermore, many existing approaches are restricted to simple structured conditions, limiting their ability to generalize to the real-world complexities. To address these gaps, we introduce the task of counterfactual time series forecasting with textual conditions, enabling more flexible and condition-aware forecasting. We propose a comprehensive evaluation framework that encompasses both factual and counterfactual settings, even in the absence of ground truth time series. Additionally, we present a novel text-attribution mechanism that distinguishes mutable from immutable factors, thereby improving forecast accuracy under sophisticated and stochastic textual conditions.

1. Introduction

Time series forecasting is essential across domains such as energy, climate, healthcare, and finance (Lai et al., 2018; Jing et al., 2024b; 2021; He et al., 2023; Chen et al., 2024; Gao et al., 2024). Despite advances in model architectures (Zeng et al., 2023; Wu et al., 2021; Nie et al., 2022; Yuan & Qiao, 2024) and large-scale learning (Ansari et al., 2024; Woo et al., 2024), performance gains have begun to plateau (Xu et al., 2024), since history-only observations provide limited information for hypothetical future

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Figure 1. Two paradigms of time series forecasting in *traffic volume* with multimodal information are illustrated. Texts in the solid-line box describe the intrinsic features of the time series, whereas texts in the dashed-line box correspond to extrinsic conditions. ① denotes forecasting based on factual conditions, including the deterministic historical and future information. ② denotes forecasting under stochastic counterfactual conditions.

scenarios. Recent multimodal methods enrich forecasting with extrinsic signals such as domain knowledge, news, and expert annotations (Jin et al., 2023; Wang et al., 2024; Liu et al., 2024b;a), while intervention- and counterfactual-based approaches further consider alternative futures (Xu et al., 2024; Melnychuk et al., 2022; Mu et al., 2025). However, these conditions are often factual, deterministic, or coarse categorical treatments, making them insufficient to express complex and stochastic real-world assumptions.

Thus, we study a broader "*what if*" problem: how might time series evolve under complex and stochastic future conditions that may not be realized? We formalize this as *counterfactual conditional time series forecasting*, where future conditions are expressed through textual descriptions beyond categorical attributes (Gu et al., 2025). As shown in Fig. 1, this task requires forecasts to preserve intrinsic characteristics while aligning with counterfactual conditions, raising three challenges: balancing historical and future conditions, adapting models trained on factual observations to counterfactual conditions, and evaluating unobserved counterfactual futures without ground-truth labels.

To address these challenges, we propose the Text-Attributive time series Diffusion model (TADIFF), a multimodal diffusion framework that disentangles text-independent intrinsic temporal features from historical sequences and generates forecasts conditioned on future textual descriptions. To improve counterfactual adaptability and evaluation, we augment training with constructed counterfactual samples and introduce semantic alignment measures that assess consis-

Figure 2. The framework of TADIFF, including the joint optimization of attribution and forecasting, as well as the two-stage inference. TADIFF first attributes the intrinsic features $\mathbf{x}_{h,T}$ of the historical sequence $\mathbf{x}_{h,0}$ given the historical textual condition $\mathbf{c}_h$. Then, conditioned on the historical sequence $\mathbf{x}_{h,0}$ and the future textual condition $\mathbf{c}_f$, TADIFF forecasts the future sequence $\hat{\mathbf{x}}_{f,0}$ by leveraging the intrinsic historical features $\hat{\mathbf{x}}_{f,T} = \mathbf{x}_{h,T}$ as initial noise state of diffusion.

tency with both historical patterns and textual conditions without requiring counterfactual ground truth.

Our main contributions are: (i) We introduce a novel task, counterfactual time series forecasting with textual conditions, enabling accurate, flexible forecasting under stochastic assumptions. (ii) We propose a comprehensive evaluation framework that combines numerical accuracy and semantic alignment measures, allowing systematic benchmarking in both factual and counterfactual settings. (iii) We develop a text-attributive time series diffusion model (TADIFF) that disentangles intrinsic historical patterns from textual context, along with a training strategy that improves the model's adaptability to diverse counterfactual conditions through the constructed counterfactual data.

2. TADIFF: Text-Attributive Time Series Diffusion Model

2.1. Counterfactual Time Series Forecasting

Given a historical sequence $\mathbf{x}_h \in \mathbb{R}^{L_h}$, its historical text $\mathbf{c}_h$, and a future textual condition $\mathbf{c}_f$, the goal is to predict $\hat{\mathbf{x}}_f = G(\mathbf{x}_h, \mathbf{c}_h, \mathbf{c}_f) \in \mathbb{R}^{L_f}$. In the factual setting, $\mathbf{c}_f$ is the condition that actually occurs and ground truth $\mathbf{x}_f$ is available. In the counterfactual setting, $\mathbf{c}_f$ describes an alternative future, so no ground-truth series exists. A useful forecast should therefore satisfy two constraints: it should preserve intrinsic properties implied by $\mathbf{x}_h$ while reflecting the extrinsic effects described by $\mathbf{c}_f$.

2.2. Text-Attribution Mechanism

To achieve balanced forecasting considering the combined effects of history and future, we propose a text-attribution mechanism that attributes historical sequences prior to forecasting, aiming to decouple the intrinsic features of the sequence from the extrinsic conditions. As shown in Fig. 2, the overall process consists of a two-stage inference and a joint training with two optimization objectives. We provide

the details of the model architecture in Appendix F.

Inference Stage 1: Attribution. We believe that the historical sequence $\mathbf{x}_{h,0}$ is the result produced by the joint influence of the extrinsic condition $\mathbf{c}_h$ and the intrinsic feature. The influence of historical extrinsic condition $\mathbf{c}_h$ is gradually eliminated from historical sequence $\mathbf{x}_{h,0}$ through the condition-aware diffusion process:

$$\mathbf{x}_{h,T} = (\psi_{T-1}^{-1} \circ \cdots \circ \psi_0^{-1})(\mathbf{x}_{h,0}, \mathbf{c}_h), \quad (1)$$

where $\circ$ represents the function composition, ψ_t^{-1} is the inverse transition defined in Eq. 10.

Inference Stage 2: Forecasting. As shown in the right half of Fig. 2, we take the intrinsic feature of historical sequence $\mathbf{x}_{h,T}$ as the initial state $\hat{\mathbf{x}}_{f,T}$ for forecasting:

$$\hat{\mathbf{x}}_{f,T} = \mathbf{x}_{h,T},$$
$$\hat{\mathbf{x}}_0 = \mathbf{x}_{h,0} \oplus \hat{\mathbf{x}}_{f,0} = (\psi_1 \circ \cdots \circ \psi_T)(\mathbf{x}_{h,0} \oplus \hat{\mathbf{x}}_{f,T}, \mathbf{c}_f),$$
$$(2)$$

where $\oplus$ is the concatenation operation, ψ_t is the denoising process of diffusion model defined in Eq. 9.

Forecasting Optimization. As illustrated in the left half of Fig. 2, the input for the diffusion noise estimator can be expressed as: $\mathbf{x}_t = \mathbf{x}_{h,0} \oplus \left[\sqrt{\alpha_t}\mathbf{x}_{f,0} + \sqrt{1-\alpha_t}\boldsymbol{\epsilon}\right] \in \mathbb{R}^{L_h+L_f}$, which is the mixed sequence containing the clear history and noisy future sequence, t is the diffusion step. The loss function can be written as:

$$\mathcal{L}_F(\theta) = \mathbb{E}_{\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0},\mathbf{I}), t \sim \mathcal{U}(1,T)} ||\mathbf{m} \times [\epsilon_\theta(\mathbf{x}_t, \mathbf{c}_f, t) - \boldsymbol{\epsilon}]||_2^2, \quad (3)$$

where $\mathbf{m} \in \{0\}^{L_h} \oplus \{1\}^{L_f}$ is the mask to make sure only the future components are supervised.

Attribution Optimization. The attribution is optimized through better noise estimation given the noisy historical sequence $\mathbf{x}_{h,t}$ and its corresponding condition $\mathbf{c}_h$. The loss is defined as the expectation of noise estimation error:

$$\mathcal{L}_A(\theta) = \mathbb{E}_{\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0},\mathbf{I}), t \sim \mathcal{U}(1,T)} ||\epsilon_\theta(\mathbf{x}_{h,t}, \mathbf{c}_h, t) - \boldsymbol{\epsilon}||_2^2, \quad (4)$$

where $\mathbf{x}_{h,t} = \sqrt{\alpha_t}\mathbf{x}_{h,0} + \sqrt{1-\alpha_t}\boldsymbol{\epsilon}$ is the noisy history.

Overall Learning Objective. The final loss function is the weighted sum: $\mathcal{L}(\theta) = \lambda_F \cdot \mathcal{L}_F(\theta) + \lambda_A \cdot \mathcal{L}_A(\theta)$, where the forecasting and attribution share the same parameters θ.

2.3. Evaluate Forecasts without Ground Truth

To evaluate intrinsic and extrinsic consistency, we propose DTTC (**D**isentangled **T**ime Series and **T**ext **C**onsistency), which includes DTTC-I and DTTC-E for measuring alignment with historical intrinsic features and future textual conditions, respectively. DTTC uses a disentangled time series encoder E_{ts} to obtain $\mathbf{I}_h, \mathbf{E}_h = E_{\text{ts}}(\mathbf{x}_h)$ and $\mathbf{I}_f, \mathbf{E}_f = E_{\text{ts}}(\mathbf{x}_f)$, and a text encoder E_{text} to obtain $\tilde{\mathbf{E}}_h = E_{\text{text}}(\mathbf{c}_h)$

Table 1. Averaged forecasting performance under *factual* conditions. The best results are in **bold**, and the second-best results are underlined. Arrows ↑ (↓) indicate that higher (lower) is better.

Datasets	Metric	DLinear	PatchTST	Sundial	VerbalTS	TimeCMA	TimeMMD	CT	IATSF	TADIFF (ours)
Synth	↓ MAE	$0.73_{\pm0.03}$	$0.67_{\pm0.00}$	$0.76_{\pm0.00}$	$1.00_{\pm0.00}$	$0.82_{\pm0.00}$	$0.66_{\pm0.00}$	$0.57{\pm}0.00$	$\underline{0.55}_{\pm0.00}$	$\mathbf{0.54}_{\pm0.00}$
	↓ MSE	$0.87_{\pm0.06}$	$0.73_{\pm0.01}$	$1.01_{\pm0.00}$	$1.53_{\pm0.01}$	$1.09_{\pm0.00}$	$0.67_{\pm0.00}$	$\mathbf{0.34}_{\pm0.00}$	$\underline{0.48}_{\pm0.01}$	$0.51_{\pm0.00}$
	↑ DTTC-I	$13.75_{\pm0.18}$	$\underline{14.65}_{\pm0.06}$	$13.73_{\pm0.01}$	$12.42_{\pm0.03}$	$13.64_{\pm0.01}$	$14.30_{\pm0.02}$	$13.43_{\pm0.04}$	$13.08_{\pm0.01}$	$\mathbf{15.37}_{\pm0.03}$
	↑ DTTC-E	$64.68_{\pm0.20}$	$67.06_{\pm0.05}$	$64.25_{\pm0.04}$	$\underline{74.30}_{\pm0.28}$	$64.26_{\pm0.05}$	$68.87_{\pm0.21}$	$67.68_{\pm0.21}$	$63.32_{\pm0.02}$	$\mathbf{78.40}_{\pm0.13}$
ETTm1	↓ MAE	$0.84_{\pm0.01}$	$0.82_{\pm0.02}$	$0.90_{\pm0.00}$	$\underline{0.58}_{\pm0.02}$	$0.88_{\pm0.00}$	$0.79_{\pm0.01}$	$0.79_{\pm0.02}$	$0.82_{\pm0.00}$	$\mathbf{0.57}_{\pm0.04}$
	↓ MSE	$1.52_{\pm0.01}$	$1.55_{\pm0.05}$	$1.90_{\pm0.00}$	$\underline{0.87}_{\pm0.05}$	$1.61_{\pm0.01}$	$1.37_{\pm0.03}$	$1.29_{\pm0.05}$	$1.42_{\pm0.02}$	$\mathbf{0.76}_{\pm0.10}$
	↑ DTTC-I	$8.99_{\pm0.39}$	$\underline{9.97}_{\pm0.12}$	$9.96_{\pm0.00}$	$8.16_{\pm0.04}$	$8.34_{\pm0.09}$	$9.74_{\pm0.19}$	$8.44_{\pm0.09}$	$7.92_{\pm0.04}$	$\mathbf{10.01}_{\pm0.03}$
	↑ DTTC-E	$86.33_{\pm5.97}$	$109.60_{\pm1.63}$	$96.98_{\pm0.14}$	$\underline{141.14}_{\pm1.55}$	$74.17_{\pm1.01}$	$108.14_{\pm0.76}$	$88.22_{\pm1.47}$	$80.65_{\pm0.95}$	$\mathbf{146.91}_{\pm1.78}$
Traffic	↓ MAE	$0.52_{\pm0.00}$	$0.42_{\pm0.02}$	$\underline{0.40}_{\pm0.00}$	$0.80_{\pm0.00}$	$0.93_{\pm0.00}$	$0.41_{\pm0.00}$	$0.45_{\pm0.00}$	$0.91_{\pm0.00}$	$\mathbf{0.35}_{\pm0.01}$
	↓ MSE	$0.43_{\pm0.00}$	$0.29_{\pm0.02}$	$0.34_{\pm0.00}$	$1.07_{\pm0.01}$	$1.07_{\pm0.00}$	$\underline{0.28}_{\pm0.01}$	$0.34_{\pm0.01}$	$1.05_{\pm0.00}$	$\mathbf{0.27}_{\pm0.05}$
	↑ DTTC-I	$11.27_{\pm0.07}$	$12.97_{\pm0.41}$	$\underline{16.36}_{\pm0.01}$	$9.73_{\pm0.05}$	$6.31_{\pm0.02}$	$12.97_{\pm0.36}$	$11.12_{\pm0.16}$	$6.52_{\pm0.02}$	$\mathbf{17.90}_{\pm0.07}$
	↑ DTTC-E	$48.31_{\pm0.14}$	$58.32_{\pm2.02}$	$66.14_{\pm0.09}$	$53.75_{\pm0.30}$	$21.71_{\pm0.12}$	$\underline{58.86}_{\pm1.42}$	$54.10_{\pm1.49}$	$24.21_{\pm0.22}$	$\mathbf{81.38}_{\pm0.15}$
Exchange	↓ MAE	$0.15_{\pm0.00}$	$\underline{0.14}_{\pm0.00}$	$\underline{0.14}_{\pm0.00}$	$0.21_{\pm0.00}$	$0.15_{\pm0.00}$	$0.22_{\pm0.00}$	$0.23_{\pm0.01}$	$\mathbf{0.12}_{\pm0.00}$	$0.15_{\pm0.01}$
	↓ MSE	$\mathbf{0.04}_{\pm0.00}$	$\mathbf{0.04}_{\pm0.00}$	$\mathbf{0.04}_{\pm0.00}$	$0.10_{\pm0.00}$	$\mathbf{0.04}_{\pm0.00}$	$\underline{0.08}_{\pm0.00}$	$0.10_{\pm0.01}$	$\mathbf{0.04}_{\pm0.00}$	$\mathbf{0.04}_{\pm0.00}$
	↑ DTTC-I	$16.62_{\pm0.02}$	$16.78_{\pm0.17}$	$\underline{17.04}_{\pm0.02}$	$15.62_{\pm0.03}$	$16.62_{\pm0.02}$	$16.03_{\pm0.03}$	$15.71_{\pm0.02}$	$16.33_{\pm0.03}$	$\mathbf{17.37}_{\pm0.04}$
	↑ DTTC-E	$204.90_{\pm0.17}$	$208.68_{\pm0.67}$	$206.49_{\pm0.31}$	$\underline{212.13}_{\pm0.12}$	$204.64_{\pm0.10}$	$184.25_{\pm1.58}$	$199.23_{\pm1.38}$	$209.12_{\pm0.33}$	$\mathbf{216.03}_{\pm3.11}$
Weather	↓ MAE	$0.26_{\pm0.00}$	$\underline{0.19}_{\pm0.00}$	$0.24_{\pm0.00}$	$0.51_{\pm0.02}$	$0.30_{\pm0.00}$	$0.27_{\pm0.00}$	$0.31_{\pm0.05}$	$\mathbf{0.18}_{\pm0.00}$	$\mathbf{0.18}_{\pm0.00}$
	↓ MSE	$0.15_{\pm0.00}$	$\underline{0.11}_{\pm0.00}$	$0.14_{\pm0.00}$	$0.46_{\pm0.03}$	$0.19_{\pm0.00}$	$0.13_{\pm0.00}$	$0.17_{\pm0.04}$	$\mathbf{0.09}_{\pm0.00}$	$\underline{0.11}_{\pm0.00}$
	↑ DTTC-I	$26.79_{\pm0.00}$	$\underline{26.83}_{\pm0.02}$	$\underline{26.83}_{\pm0.01}$	$24.85_{\pm0.06}$	$\mathbf{26.84}_{\pm0.00}$	$26.41_{\pm0.02}$	$26.24_{\pm0.32}$	$26.54_{\pm0.00}$	$26.65_{\pm0.04}$
	↑ DTTC-E	$29.60_{\pm0.02}$	$30.25_{\pm0.04}$	$29.44_{\pm0.01}$	$\underline{31.23}_{\pm0.02}$	$29.45_{\pm0.01}$	$29.25_{\pm0.08}$	$29.98_{\pm0.27}$	$29.81_{\pm0.00}$	$\mathbf{31.55}_{\pm0.15}$

Table 2. Averaged forecasting performance under *counterfactual* conditions. The best results are in **bold**, and the second-best results are underlined. Arrows ↑ (↓) indicate that higher (lower) is better.

Datasets	Metric	DLinear	PatchTST	Sundial	VerbalTS	TimeCMA	TimeMMD	CT	IATSF	TADIFF (ours)
ETTm1	↑ DTTC-I	$8.96_{\pm0.40}$	$\underline{10.51}_{\pm0.11}$	$9.94_{\pm0.00}$	$8.62_{\pm0.04}$	$9.47_{\pm0.61}$	$10.14_{\pm0.06}$	$8.43_{\pm0.10}$	$7.93_{\pm0.04}$	$\mathbf{10.59}_{\pm0.02}$
	↑ DTTC-E	$96.45_{\pm4.89}$	$113.02_{\pm1.39}$	$107.14_{\pm0.02}$	$\underline{140.95}_{\pm1.57}$	$103.42_{\pm7.89}$	$113.65_{\pm0.49}$	$93.24_{\pm2.09}$	$87.71_{\pm0.62}$	$\mathbf{148.72}_{\pm1.21}$
Traffic	↑ DTTC-I	$11.33_{\pm0.08}$	$12.99_{\pm0.39}$	$\underline{16.32}_{\pm0.01}$	$9.44_{\pm0.05}$	$6.36_{\pm0.03}$	$12.96_{\pm0.43}$	$11.15_{\pm0.14}$	$6.57_{\pm0.08}$	$\mathbf{18.08}_{\pm0.11}$
	↑ DTTC-E	$48.41_{\pm0.18}$	$54.86_{\pm1.70}$	$\underline{64.79}_{\pm0.04}$	$53.69_{\pm0.32}$	$22.71_{\pm0.03}$	$56.10_{\pm1.01}$	$52.67_{\pm1.55}$	$24.62_{\pm0.24}$	$\mathbf{78.58}_{\pm0.06}$
Exchange	↑ DTTC-I	$16.61_{\pm0.02}$	$16.79_{\pm0.17}$	$\underline{17.03}_{\pm0.01}$	$15.29_{\pm0.06}$	$16.79_{\pm0.08}$	$16.25_{\pm0.17}$	$15.67_{\pm0.04}$	$16.31_{\pm0.05}$	$\mathbf{17.30}_{\pm0.04}$
	↑ DTTC-E	$200.45_{\pm0.04}$	$201.30_{\pm1.08}$	$200.57_{\pm0.13}$	$\underline{211.37}_{\pm0.61}$	$201.84_{\pm0.39}$	$196.16_{\pm2.10}$	$194.49_{\pm0.85}$	$199.65_{\pm0.26}$	$\mathbf{213.94}_{\pm2.18}$
Weather	↑ DTTC-I	$26.79_{\pm0.01}$	$26.83_{\pm0.02}$	$26.83_{\pm0.00}$	$24.43_{\pm0.05}$	$\underline{26.84}_{\pm0.00}$	$26.75_{\pm0.11}$	$26.25_{\pm0.29}$	$26.53_{\pm0.01}$	$\mathbf{26.93}_{\pm0.04}$
	↑ DTTC-E	$29.04_{\pm0.03}$	$29.25_{\pm0.05}$	$28.91_{\pm0.01}$	$\underline{30.16}_{\pm0.05}$	$29.00_{\pm0.01}$	$29.30_{\pm0.18}$	$29.23_{\pm0.18}$	$29.18_{\pm0.01}$	$\mathbf{30.99}_{\pm0.14}$

and $\tilde{\mathbf{E}}_f = E_{\text{text}}(\mathbf{c}_f)$. The encoders are trained with contrastive learning (Radford et al., 2021) to align intrinsic features across historical and future sequences and extrinsic features across sequences and texts. We compute:

$$\text{DTTC-I} = \frac{1}{N} \sum_{i=1}^{N} \langle \mathbf{I}_f[i], \mathbf{I}_h[i] \rangle;$$

$$\text{DTTC-E} = \frac{1}{N} \sum_{i=1}^{N} \langle \mathbf{E}_f[i], \tilde{\mathbf{E}}_f[i] \rangle, \tag{5}$$

where $\langle \cdot, \cdot \rangle$ denotes the inner product. DTTC-I measures intrinsic consistency with historical patterns, while DTTC-E measures extrinsic consistency with future conditions.

2.4. Adapt to diverse future conditions

Since we lack the ground truth of future $\mathbf{x}_f$ for counterfactual data, we sample a Gaussian noise $\hat{\mathbf{x}}_{f,T} \sim \mathcal{N}(0, \mathbf{I})$ as the initial state, and gradually denoise it for diffusion training. For each denoising step t, we have noisy data $\hat{\mathbf{x}}_{f,t}$ to estimate the clear data $\hat{\mathbf{x}}_{f,0}$, and finetune the model to

increase the DTTC scores with λ_I, λ_E as loss weight:

$$\mathbf{I}_h, \mathbf{E}_h = E_{\text{ts}}(\mathbf{x}_h); \hat{\mathbf{I}}_f, \hat{\mathbf{E}}_f = E_{\text{ts}}(\hat{\mathbf{x}}_{f,0}); \tilde{\mathbf{E}}_f = E_{\text{text}}(\mathbf{c}_f),$$
$$\mathcal{L}_{\text{DTTC}}(\theta) = -\mathbb{E}\left(\lambda_I \cdot <\mathbf{I}_h, \hat{\mathbf{I}}_f> + \lambda_E \cdot <\hat{\mathbf{E}}_f, \tilde{\mathbf{E}}_f> \right). \tag{6}$$

3. Experiment

In this section, we describe the experimental setup and report results, structured around the following research questions (RQs): **RQ1**: Can TADIFF preserve the intrinsic features of the historical sequence while simultaneously satisfying the specified future conditions? **RQ2**: Can TADIFF adapt to diverse counterfactual conditions given the same historical sequence? **RQ3**: Does the DTTC metric enable providing reasonable and intuitive evaluations?

3.1. Experiment Setup

We evaluate on one synthetic dataset with counterfactual ground truth and four real-world datasets: Weather (Xu et al., 2024), ETTm1 (Zhou et al., 2021), Exchange (Lai

Table 3. The ablation study of CF and TA on **ETTm1** and **Traffic** datasets. CF represents the fine-tuning on the counterfactual data. TA represents the text-attribution mechanism.

Datasets			ETTm1							Traffic			
Setting			Factual			Counterfactual			Factual			Counterfactual	
Metric	↓ MAE	↓ MSE	↑ DTTC-I	↑ DTTC-E	↑ DTTC-I	↑ DTTC-E	↓ MAE	↓ MSE	↑ DTTC-I	↑ DTTC-E	↑ DTTC-I	↑ DTTC-E
TADIFF	$\mathbf{0.57}_{\pm0.04}$	$\mathbf{0.76}_{\pm0.10}$	$\mathbf{10.01}_{\pm0.03}$	$\mathbf{146.91}_{\pm1.78}$	$\mathbf{10.59}_{\pm0.02}$	$\mathbf{148.72}_{\pm1.21}$	$0.35_{\pm0.03}$	$0.27_{\pm0.05}$	$\mathbf{17.90}_{\pm0.07}$	$\mathbf{81.38}_{\pm0.15}$	$\mathbf{18.08}_{\pm0.11}$	$\mathbf{78.58}_{\pm0.06}$
w/o CF	$0.58_{\pm0.05}$	$0.82_{\pm0.17}$	$9.48_{\pm0.06}$	$144.74_{\pm1.65}$	$10.06_{\pm0.04}$	$146.73_{\pm1.12}$	$\mathbf{0.31}_{\pm0.01}$	$\mathbf{0.24}_{\pm0.01}$	$17.57_{\pm0.03}$	$80.84_{\pm0.21}$	$17.31_{\pm0.03}$	$78.11_{\pm0.22}$
w/o TA	$0.59_{\pm0.04}$	$0.77_{\pm0.04}$	$9.05_{\pm0.04}$	$142.36_{\pm1.50}$	$9.35_{\pm0.07}$	$141.01_{\pm1.75}$	$0.49_{\pm0.01}$	$0.78_{\pm0.16}$	$15.41_{\pm0.11}$	$76.34_{\pm0.22}$	$15.28_{\pm0.04}$	$73.52_{\pm0.25}$

Figure 3. The initial noise distribution between the TADIFF (green) and TADIFF without text-attribution (red) on **Synth** (left) and **Exchange** (right) datasets.

et al., 2018), and Traffic (Leo, 2024). Baselines include unimodal forecasters DLinear, PatchTST, and Sundial (Zeng et al., 2023; Nie et al., 2022; Liu et al., 2025), text-based or multimodal models VerbalTS, TimeMMD, TimeCMA, and IATSF (Gu et al., 2025; Liu et al., 2024b;a; Xu et al., 2024), and the counterfactual treatment model CT (Melnychuk et al., 2022). We report MAE/MSE for numerical accuracy when ground truth exists and DTTC-I/DTTC-E for semantic consistency when the ground truth is absent. More details on dataset construction and the DTTC model are provided in Appendices D and E, respectively.

3.2. Main Results

Finding 1: TADIFF *achieves superior numerical accuracy and semantic consistency.* As shown in Tab. 1, unlike generation baselines that neglect historical patterns and forecasting baselines that underuse future conditions, TADIFF consistently balances both information sources, answering **RQ1** with accurate and semantically consistent forecasts.

Finding 2: TADIFF *generalizes well to diverse counterfactual future conditions.* As shown in Tabs. 1 and 2, TADIFF consistently improves semantic consistency under diverse and unseen condition combinations, answering **RQ2** with stronger adaptability to varying future scenarios.

3.3. Ablation Study and Extended Analysis

Finding 3: *Finetuning with counterfactual data preserves numerical accuracy while enhancing semantic consistency.* As shown in Tab. 3, fine-tuning improves leads to higher semantic consistency in both factual and counterfactual forecasting, while maintains strong numerical accuracy.

Finding 4: *Text-attribution improves both historical and conditional consistency.* As shown in Tab. 3, adding text-attribution improves semantic consistency and numerical accuracy, with especially notable gains under counterfactual

Table 4. Evaluation of DTTC models on different datasets. Given a future sequence, DTTC-I and DTTC-E report the accuracy of retrieving the most similar historical sequence and future condition, respectively, from three candidates.

Dataset	Synth	ETTm1	Traffic	Exchange	Weather
DTTC-I	84.57%	55.06%	91.90%	84.60%	79.96%
DTTC-E	96.36%	95.93%	97.69%	98.44%	77.91%

settings. We further show its ability to decouple intrinsic sequence features from extrinsic conditions in Appendix G.4.

Finding 5: *Text-attribution optimizes the diffusion initial noise space.* As shown in Fig. 3, text-attribution produces more compact initial noise clusters than the attribution-free setting. This indicates that it preserves intrinsic historical features and facilitates more effective conditional denoising, leading to more accurate forecasts.

Figure 4. Qualitative comparison of forecasting on Synth dataset. Column 1: the forecasting of TADiff without text-attribution; Column 2: the forecasting of TADiff with text-attribution; Column 3: the future textual condition.

Finding 6: *Text-attribution helps preserve intrinsic trends while incorporating future text.* As shown in Fig. 4, TADIFF with text-attribution better captures the invariant trend type shared by historical and future sequences in Synth, while aligning more closely with future textual semantics. This yields more accurate and reasonable forecasts.

Finding 7: *DTTC effectively captures intrinsic time-series features and extrinsic semantics.* Given a future sequence, DTTC retrieves its paired historical sequence and future textual condition from three candidates. As shown in Tab. 4, both DTTC-I and DTTC-E achieve high retrieval accuracy, demonstrating that DTTC can align the intrinsic features of historical and future series, as well as the semantics between future series and extrinsic conditions. This supports the reliability of the proposed metrics and addresses **RQ3**.

References

Achiam, J., Adler, S., Agarwal, S., Ahmad, L., Akkaya, I., Aleman, F. L., Almeida, D., Altenschmidt, J., Altman, S., Anadkat, S., et al. Gpt-4 technical report. *arXiv preprint arXiv:2303.08774*, 2023.

Ansari, A. F., Stella, L., Turkmen, C., Zhang, X., Mercado, P., Shen, H., Shchur, O., Rangapuram, S. S., Pineda Arango, S., Kapoor, S., Zschiegner, J., Maddix, D. C., Mahoney, M. W., Torkkola, K., Gordon Wilson, A., Bohlke-Schneider, M., and Wang, Y. Chronos: Learning the language of time series. *Transactions on Machine Learning Research*, 2024. ISSN 2835-8856. URL https://openreview.net/forum?id=gerNCVqqtR.

Ashok, A., Williams, A. R., Zheng, V. Z., Rish, I., Chapados, N., Marcotte, É., Zantedeschi, V., and Drouin, A. Beyond naïve prompting: Strategies for improved zero-shot context-aided forecasting with llms. *arXiv preprint arXiv:2508.09904*, 2025.

Chen, Y., Ren, K., Wang, Y., Fang, Y., Sun, W., and Li, D. Contiformer: Continuous-time transformer for irregular time series modeling. *Advances in Neural Information Processing Systems*, 36, 2024.

Christ, M., Braun, N., Neuffer, J., and Kempa-Liehr, A. W. Time series feature extraction on basis of scalable hypothesis tests (tsfresh–a python package). *Neurocomputing*, 307:72–77, 2018.

Gao, Y., Chen, H., Wang, X., Wang, Z., Wang, X., Gao, J., and Ding, B. Diffsformer: A diffusion transformer on stock factor augmentation. *arXiv preprint arXiv:2402.06656*, 2024.

Gendron, G., Rožanec, J. M., Witbrock, M., and Dobbie, G. Counterfactual causal inference in natural language with large language models. *arXiv preprint arXiv:2410.06392*, 2024.

Gu, S., Li, C., Jing, B., and Ren, K. Verbalts: Generating time series from texts. *International Conference on Machine Learning*, 2025.

He, H., Zhao, S., Xi, Y., and Ho, J. C. Meddiff: Generating electronic health records using accelerated denoising diffusion model. *arXiv preprint arXiv:2302.04355*, 2023.

Jin, M., Wang, S., Ma, L., Chu, Z., Zhang, J. Y., Shi, X., Chen, P.-Y., Liang, Y., Li, Y.-F., Pan, S., et al. Time-llm: Time series forecasting by reprogramming large language models. *arXiv preprint arXiv:2310.01728*, 2023.

Jing, B., Tong, H., and Zhu, Y. Network of tensor time series. In *Proceedings of the Web Conference 2021*, pp. 2425–2437, 2021.

Jing, B., Gu, S., Chen, T., Yang, Z., Li, D., He, J., and Ren, K. Towards editing time series. *Advances in Neural Information Processing Systems*, 2024a.

Jing, B., Wang, Y., Sui, G., Hong, J., He, J., Yang, Y., Li, D., and Ren, K. Automated contrastive learning strategy search for time series. In *Proceedings of the 33rd ACM International Conference on Information and Knowledge Management*, pp. 4612–4620, 2024b.

Lai, G., Chang, W.-C., Yang, Y., and Liu, H. Modeling long-and short-term temporal patterns with deep neural networks. In *The 41st international ACM SIGIR conference on research & development in information retrieval*, pp. 95–104, 2018.

Leo. Istanbul traffic index. Kaggle, 2024. URL https://www.kaggle.com/datasets/leonardo00/istanbul-traffic-index/data.

Li, Z., Tan, Y., Cheng, X., and Qin, Y. Ftmixer: Frequency and time domain representations fusion for time series forecasting. *IEEE Signal Processing Letters*, 2025.

Liu, C., Xu, Q., Miao, H., Yang, S., Zhang, L., Long, C., Li, Z., and Zhao, R. Timecma: Towards llm-empowered time series forecasting via cross-modality alignment. *arXiv preprint arXiv:2406.01638*, 2024a.

Liu, H., Xu, S., Zhao, Z., Kong, L., Kamarthi, H., Sasanur, A. B., Sharma, M., Cui, J., Wen, Q., Zhang, C., et al. Time-mmd: A new multi-domain multimodal dataset for time series analysis. *arXiv preprint arXiv:2406.08627*, 2024b.

Liu, Y., Qin, G., Shi, Z., Chen, Z., Yang, C., Huang, X., Wang, J., and Long, M. Sundial: A family of highly capable time series foundation models. *arXiv preprint arXiv:2502.00816*, 2025.

Melnychuk, V., Frauen, D., and Feuerriegel, S. Causal transformer for estimating counterfactual outcomes. In *International conference on machine learning*, pp. 15293–15329. PMLR, 2022.

Mu, W., Cao, Z., Uludag, M., and Rodríguez, A. Counterfactual probabilistic diffusion with expert models. *arXiv preprint arXiv:2508.13355*, 2025.

Nie, Y., Nguyen, N. H., Sinthong, P., and Kalagnanam, J. A time series is worth 64 words: Long-term forecasting with transformers. *arXiv preprint arXiv:2211.14730*, 2022.

Peebles, W. and Xie, S. Scalable diffusion models with transformers. In *Proceedings of the IEEE/CVF international conference on computer vision*, pp. 4195–4205, 2023.

Radford, A., Kim, J. W., Hallacy, C., Ramesh, A., Goh, G., Agarwal, S., Sastry, G., Askell, A., Mishkin, P., Clark, J., et al. Learning transferable visual models from natural language supervision. In *International conference on machine learning*, pp. 8748–8763. PmLR, 2021.

Rasal, R., Kori, A., Ribeiro, F. D. S., Xia, T., and Glocker, B. Diffusion counterfactual generation with semantic abduction. *arXiv preprint arXiv:2506.07883*, 2025.

Song, J., Meng, C., and Ermon, S. Denoising diffusion implicit models. *arXiv preprint arXiv:2010.02502*, 2020.

Wang, X., Feng, M., Qiu, J., Gu, J., and Zhao, J. From news to forecast: Integrating event analysis in LLM-based time series forecasting with reflection. In *The Thirty-eighth Annual Conference on Neural Information Processing Systems*, 2024. URL https://openreview.net/forum?id=tj8nsfxi5r.

Williams, A. R., Ashok, A., Marcotte, É., Zantedeschi, V., Subramanian, J., Riachi, R., Requeima, J., Lacoste, A., Rish, I., Chapados, N., and Drouin, A. Context is key: A benchmark for forecasting with essential textual information. In *Forty-second International Conference on Machine Learning*, 2025. URL https://openreview.net/forum?id=ih2WuBT1Fn.

Woo, G., Liu, C., Kumar, A., Xiong, C., Savarese, S., and Sahoo, D. Unified training of universal time series forecasting transformers. In *Forty-first International Conference on Machine Learning*, 2024.

Wu, H., Xu, J., Wang, J., and Long, M. Autoformer: Decomposition transformers with auto-correlation for long-term series forecasting. *Advances in neural information processing systems*, 34:22419–22430, 2021.

Wu, H., Hu, T., Liu, Y., Zhou, H., Wang, J., and Long, M. Timesnet: Temporal 2d-variation modeling for general time series analysis. *arXiv preprint arXiv:2210.02186*, 2022.

Wu, S., Zhou, W., Chen, M., and Zhu, S. Counterfactual generative models for time-varying treatments. In *Proceedings of the 30th ACM SIGKDD Conference on Knowledge Discovery and Data Mining*, pp. 3402–3413, 2024.

Xu, Z., Wang, H., and Xu, Q. Intervention-aware forecasting: Breaking historical limits from a system perspective. *arXiv preprint arXiv:2405.13522*, 2024.

Yuan, X. and Qiao, Y. Diffusion-ts: Interpretable diffusion for general time series generation. *arXiv preprint arXiv:2403.01742*, 2024.

Zeng, A., Chen, M., Zhang, L., and Xu, Q. Are transformers effective for time series forecasting? In *Proceedings of the AAAI conference on artificial intelligence*, volume 37, pp. 11121–11128, 2023.

Zhang, B., Zhang, P., Dong, X., Zang, Y., and Wang, J. Long-clip: Unlocking the long-text capability of clip. In *European conference on computer vision*, pp. 310–325. Springer, 2024.

Zhong, S., Ruan, W., Jin, M., Li, H., Wen, Q., and Liang, Y. Time-vlm: Exploring multimodal vision-language models for augmented time series forecasting. *arXiv preprint arXiv:2502.04395*, 2025.

Zhou, H., Zhang, S., Peng, J., Zhang, S., Li, J., Xiong, H., and Zhang, W. Informer: Beyond efficient transformer for long sequence time-series forecasting. In *The Thirty-Fifth AAAI Conference on Artificial Intelligence, AAAI 2021, Virtual Conference*, volume 35, pp. 11106–11115. AAAI Press, 2021.

A. Impact Statement

This work introduces a novel task of counterfactual time series forecasting under textual conditions. We anticipate several positive societal impacts: (i) assisting humans in forecasting future events and making decisions under complex, stochastic assumptions; (ii) offering innovative and reliable evaluation methods for time series forecasting; and (iii) inspiring approaches of better leveraging multimodal information in time series forecasting.

While we do not foresee immediate or direct negative societal consequences stemming from this work, we recognize that, like other generative technologies, it may be susceptible to misuse. Therefore, responsible use, ethical oversight, and ongoing monitoring are crucial to ensure that the technology is applied for the greater good.

B. Related Work

B.1. Unimodal and Multimodal Time Series Forecasting

Time series forecasting typically involves predicting future values based on historical data. Research has focused on improving this by developing model architectures that better capture temporal patterns, including linear models (Zeng et al., 2023), CNNs (Wu et al., 2022), and transformer-based approaches (Wu et al., 2021; Nie et al., 2022). Recently, foundation models (Ansari et al., 2024; Woo et al., 2024) have emerged to learn universal time series representations from large datasets and model capacity. However, these methods still mainly rely on numerical historical sequences, overlooking the crucial impact of extrinsic conditions.

To address this limitation, recent studies have explored incorporating multimodal extrinsic information into forecasting. Among various modalities, text has become the most prevalent, appearing as domain knowledge (Jin et al., 2023), news (Liu et al., 2024b; Wang et al., 2024), or expert annotations (Liu et al., 2024a), providing complementary signals for prediction. Other approaches transform time series into alternative modalities, such as frequencies (Li et al., 2025) or images (Zhong et al., 2025), to enhance model expressiveness. Nonetheless, these methods predominantly derive multimodal inputs from historical data, limiting their capacity to address scenarios where future dynamics diverge substantially from past observations.

More recent works (Xu et al., 2024; Ashok et al., 2025) have begun to incorporate future interventions into forecasting, with Williams et al. (2025) introducing a benchmark for evaluating time series forecasting conditioned on future events. While these studies recognize the importance of modeling future conditions, they fail to consider the counterfactual setting, where interventions and events are described deterministically, failing to capture the inherent uncertainty of the future. Consequently, these forecasting methods tend to lack robustness and struggle to adapt to diverse counterfactual futures, as empirically demonstrated in Sec. 3.2.

B.2. Counterfactual Modeling

Since the real world is inherently uncertain, researchers are not satisfied with modeling only observed events; instead, they strive to uncover the underlying principles governing system behavior under counterfactual conditions. Such conditions manifest differently across domains. In reasoning tasks, prior work (Gendron et al., 2024) attempts counterfactual logical reasoning in natural language, while Wu et al. (2024) studies how events evolve under different treatments regarding the same time period. In generation and editing tasks, Rasal et al. (2025) generates non-existent images by altering specific features, whereas Jing et al. (2024a) modifies attributes of source time series to produce a target one.

In this work, we focus on forecasting, which presents unique challenges compared to reasoning and generation due to the temporal dependencies involved. In forecasting, the joint influence of historical patterns and future extrinsic conditions should be considered organically. Most existing counterfactual forecasting approaches (Wu et al., 2024; Melnychuk et al., 2022; Mu et al., 2025) attempt to forecast multiple plausible futures under alternative treatments. However, they rely on structured attribute conditions, where possible futures are represented as fixed categories. In contrast, our work leverages unstructured textual conditions, enabling richer and more flexible conditional modeling with broader applicability to real-world scenarios. Furthermore, prior evaluation practices are constrained to synthetic datasets or limited to the observed conditions in real datasets, since counterfactual settings lack ground-truth futures. To address this gap, we propose a novel evaluation metric that assesses the consistency of forecasts with both historical sequences and counterfactual textual conditions, while remaining robust to the absence of ground truth.

Figure 5. The visualization of the initial noise issue and our solution through text-attribution. The distribution plots represent the distribution of the time series under *specific influences*.

C. Preliminary Study: Diffusion Model

Time series forecasting is inherently uncertain. This uncertainty arises from two sources: (i) the variability of future conditions, and (ii) the stochastic nature of time series evolution even under given conditions. To better capture this uncertainty, we adopt a generative modeling approach as the foundation of our forecasting framework. In particular, we employ diffusion models due to training stability and strong capacity for distributional modeling. Our forecasting model is built upon denoising diffusion implicit models (Song et al., 2020). Below, we provide a brief overview of the training and inference procedures of the diffusion model.

During training, noise is gradually added to the original data distribution $q(\mathbf{x}_0)$[1] via a Gaussian Markov transition:

$$q(\mathbf{x}_{1:T}|\mathbf{x}_0) = \prod_{t=1}^{T} q(\mathbf{x}_t|\mathbf{x}_{t-1}),$$

$$q(\mathbf{x}_t|\mathbf{x}_{t-1}) = \mathcal{N}(\sqrt{1-\beta_t}\mathbf{x}_{t-1}, \beta_t \mathbf{I}),$$

(7)

and produces the noisy sample $\mathbf{x}_t$ at each diffusion step $t \in [1, T]$. Here $\{\beta_t\}_{t=1}^{T}$ are the predetermined variance schedule. $\mathbf{x}_t$ can be expressed as $\mathbf{x}_t = \sqrt{\alpha_t}\mathbf{x}_0 + \sqrt{1-\alpha_t}\epsilon$, where $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ and $\alpha_t := \prod_{s=1}^{t}(1-\beta_s)$. Then, a learnable noise estimation network $\epsilon_\theta(\mathbf{x}_t, t, \mathbf{c})$ is trained by estimating the noise added to $\mathbf{x}_t$ given the condition $\mathbf{c}$ and diffusion step t. The objective function is to minimize the noise estimation loss as:

$$\min_\theta \mathcal{L}(\mathbf{x}_0) = \min_\theta \mathbb{E}_{\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I}), t \sim \mathcal{U}(1,T)} \|\epsilon - \epsilon_\theta(\mathbf{x}_t, t, \mathbf{c})\|_2^2 ,$$

(8)

where $\mathbf{x}_0 \sim q(\mathbf{x}_0)$ is sampled from the real data distribution, $\mathbf{x}_t$ is a noisy version of $\mathbf{x}_0$.

During the inference phase, given a condition $\mathbf{c}$ and noisy data $\hat{\mathbf{x}}_t$, the denoising transitions $\psi_t(\cdot)$ to get less noisy data $\hat{\mathbf{x}}_{t-1}$ can be formulated as:

$$\hat{\mathbf{x}}_{t-1} = \psi_t(\hat{\mathbf{x}}_t, \mathbf{c}) = \sqrt{\alpha_{t-1}}\hat{\mathbf{x}}_0 + \sqrt{1-\alpha_{t-1}}\epsilon_\theta(\hat{\mathbf{x}}_t, \mathbf{c}, t),$$

$$\hat{\mathbf{x}}_0 = \frac{1}{\sqrt{\alpha_t}}(\hat{\mathbf{x}}_t - \sqrt{1-\alpha_t}\epsilon_\theta(\hat{\mathbf{x}}_t, \mathbf{c}, t)).$$

(9)

This process can also be inverted to $\psi_t^{-1}(\cdot)$, which inversely estimates $\hat{\mathbf{x}}_{t+1}$ given $\hat{\mathbf{x}}_t$ and $\mathbf{c}$:

$$\hat{\mathbf{x}}_{t+1} = \psi_t^{-1}(\hat{\mathbf{x}}_t, \mathbf{c}) = \sqrt{\alpha_{t+1}}\hat{\mathbf{x}}_0 + \sqrt{1-\alpha_{t+1}}\epsilon_\theta(\hat{\mathbf{x}}_t, \mathbf{c}, t).$$

(10)

Discussion: Initial noise issue. Most diffusion models (Yuan & Qiao, 2024; Gu et al., 2025) use Gaussian-distributed random noise $\hat{\mathbf{x}}_T \sim \mathcal{N}(0, \mathbf{I})$ as the initial state during inference. However, this randomly sampled noise is not optimal, as

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[1]$\mathbf{x}$ and $\mathbf{x}_0$ are interchangeable in this paper.

it may introduce properties that conflict with the intrinsic features of clear data $\mathbf{x}_0$, thereby complicating the denoising process, as shown in Fig. 5. To address this, we propose a condition-aware forward process to attribute the intrinsic features of history, leading to more accurate and controllable forecasting, which will be further discussed in Sec. 2.2. We further prove that our method optimizes the initial noise space of the diffusion model in Sec. 3.3.

D. Datasets

Our experimental framework is built upon two primary categories of datasets: **synthetic** and **real-world**. The real-world category is further subdivided into datasets that are originally unimodal (time series only) and those that are multimodal (containing real-world captions). Each of these types requires a distinct data processing pipeline.

For the **unimodal real-world datasets** (`ETTm1`, `Traffic`, `Exchange`), we adopt the augmentation paradigm introduced by VerbalTS (Gu et al., 2025). This involves a two-stage process: first, we extract structured attributes from the raw time series data, then these attributes are used to generate corresponding textual descriptions.

For the **synthetic dataset** (`Synth`), the attributes are not extracted but are algorithmically predefined at the start of the generation process. In contrast, since the **multimodal real-world dataset** (`Weather`) already contains naturally occurring time series-text pairs, our task is to extract structured attributes directly from the provided real-world captions. Finally, for the synthetic and multimodal real-world datasets, the textual descriptions are generated from their respective attributes by populating predefined prompt templates.

The specific implementation details for each of these processes are provided in the corresponding dataset sections that follow.

D.1. Forecasting Task Formulation

Based on these processed datasets, we formulate two distinct forecasting settings, **Factual** and **Counterfactual**, to evaluate model performance under different types of conditions. The implementation of these settings varies depending on the nature of the dataset. We define two types of forecasting settings as follows:

Factual Forecasting. This task is consistent across all dataset types and is represented by the tuple $(\mathbf{x}_h, \mathbf{c}_h, \mathbf{x}_f, \mathbf{c}_f)$. The objective is to predict the actual future time series $\mathbf{x}_f$ given the historical context $(\mathbf{x}_h, \mathbf{c}_h)$ and the corresponding true, observed future condition $\mathbf{c}_f$.

Counterfactual Forecasting. This task evaluates the model's ability to forecast under a future condition that deviates from the observed or expected trajectory. Its implementation differs between real-world and synthetic data:

- For Synthetic Datasets, the task retains the tuple structure $(\mathbf{x}_h, \mathbf{c}_h, \mathbf{x}_f, \mathbf{c}_f)$. Because we control the data generation process, we can still synthesize a corresponding ground-truth future time series $\mathbf{x}_f$ that matches this counterfactual condition.

- For Real-World Datasets, the task is represented by the tuple $(\mathbf{x}_h, \mathbf{c}_h, \varnothing, \tilde{\mathbf{c}}_f)$. Here, $\tilde{\mathbf{c}}_f$ is a hypothetical future condition that the combination of $\mathbf{x}_h$ and $\tilde{\mathbf{c}}_f$ did not actually occur in the real world. Consequently, a ground-truth future time series for this scenario does not exist and is represented by the empty set ($\varnothing$), as the outcome is inherently unobserved.

D.2. Synthetic Dataset

In this work, we utilize a dataset we term `Synth`. The generation process is attribute-driven, where predefined attributes govern the synthesis of both time series and their textual descriptions.

D.2.1. ATTRIBUTE FRAMEWORK FOR SYNTHETIC GENERATION

The generation of each synthetic time series is governed by six attributes. These attributes are randomly sampled for each instance to control the series' fundamental structure, localized events, and stochastic properties, ensuring a diverse data distribution. These attributes are defined as follows:

- **Trend Type:** We define four distinct trend types to model different long-term behaviors: *linear*, *quadratic*, *exponential*,

and *logistic*. The base trend is generated from mathematical formulas, with some types (e.g., logistic) being normalized to the range $[-1, 1]$ for training stability.

- **Trend Direction:** Each generated trend is assigned one of two directions: *upward* or *downward*. This is implemented as a simple sign multiplier ($+1$ or -1) on the base trend component.

- **Seasonality Cycles:** To introduce periodic patterns, each series is assigned a specific number of cycles, with the count selected from $\{0, 1, 2, 4\}$. This component is modeled as a sinusoidal wave, $\mathbf{x}_{\text{season}} = a \sin(2\pi t + \phi)$, where the amplitude $a \sim \mathcal{U}(0.4, 0.6)$ and phase $\phi \sim \mathcal{U}(0, 2\pi)$ are randomly sampled to ensure diversity.

- **Local Shapelets:** We introduce one of five predefined local shapelets: *nothing, peak, sag, double peaks,* or *platform*. Each time series is divided into three equal segments (beginning, middle, end). Within each segment, a shapelet is added with a specific probability.

- **Noise:** We inject additive Gaussian noise into each sample. The noise is sampled independently for each time step from a zero-mean Gaussian distribution, $\mathbf{x}_{\text{noise}} \sim \mathcal{N}(0, \sigma^2)$, where the standard deviation σ is itself randomly sampled from a small range to ensure variability in the noise level across the dataset.

- **Bias:** A constant bias is added to each time series to vary its global vertical offset. The bias value is sampled from one of three predefined ranges (negative, zero, or positive), ensuring variability in the series' mean value across the dataset.

The six attributes are divided into intrinsic features and extrinsic conditions, where **Trend Type**, **Noise**, and **Bias** belong to intrinsic features; **Trend Direction**, **Seasonality Cycles**, and **Local Shapelets** belong to extrinsic conditions. The intrinsic features will remain unchanged between the historical and future sequences, and only the extrinsic conditions will be described in the texts.

D.2.2. SYNTH DATASET

The `Synth` dataset is algorithmically generated by randomly sampling attributes for each instance, ensuring high variability. The entire process yields 14,000 unique samples, which are then partitioned into training (11,200 samples), validation (1,400), and test (1,400) sets using an 8:1:1 ratio.

Attribute Generation. Each time series sample is governed by the attributes proposed above that define its structure. For each sample, we generate a related pair of historical and future segments. A key constraint is that **Trend Type**, **Noise**, and **Bias** are shared between the history and the future, as they represent the invariant intrinsic features of the time series. In contrast, the remaining attributes, **Trend Direction**, **Seasonality Cycles**, and **Local Shapelets**, are extrinsic conditions that may vary between the history and the future and are intended to be described through textual captions.

Caption Generation. A corresponding textual caption is generated for both the historical and future segments using randomized prompt templates. This process ensures diversity while maintaining semantic consistency with the attributes. A representative example of a generated caption pair is as follows:

- **History Caption:** "The trend goes up. There is a sag at end. There is 1 season."

- **Future Caption:** "There is a sag at end. The season cycle number is 0. The trend has a down direction."

This example illustrates a scenario where the trend direction reverses and the number of seasonal cycles changes, providing a challenging test case for conditional forecasting.

D.3. Real-world Datasets

Real-world datasets consist of observational data from real-world processes. Depending on whether the original dataset contains pre-existing text, we categorize them as unimodal or multimodal and apply a distinct data preparation pipeline to each.

Table 5. Summary of global and local features extracted for data augmentation.

	Feature Name	Description
Global Features	Skewness	The asymmetry of the distribution.
	Kurtosis	The sharpness of the distribution.
	Linear Trend	The overall trend direction and rate of change.
	FFT Frequency	The dominant periodicity in frequency domain.
Local Features	Local Linear Trend	The trend direction within each segment.
	Number of Peaks	The number of local maxima within each segment.

D.3.1. UNIMODAL DATASETS

Unimodal datasets in our study initially contain only time series data. To prepare them for multimodal inputs, we follow the augmentation paradigm introduced by VerbalTS (Gu et al., 2025). First, we perform **attribute extraction** by applying the `tsfresh` library (Christ et al., 2018) to the raw time series to derive a set of structured statistical features. These extracted features, which are categorized into global and local characteristics, are summarized in Tab. 5. Second, we perform **caption generation** by using these attributes to populate predefined prompt templates, thereby creating a synthetic textual description for each time series sample. The specific datasets processed with this methodology are as follows.

ETTm1. The `ETTm1` dataset (Zhou et al., 2021) contains 7 variables of electricity transformer data sampled every 15 minutes. We partitioned the data and employed a sliding window (history 48, stride 48, horizon 48) to generate 8,120 training, 1,008 validation, and 1,008 test samples.

Traffic. The `Traffic` dataset (Leo, 2024) contains 3 variables of traffic data from Istanbul. We downsampled the original 1-minute data to an hourly frequency. The data was split and processed with a sliding window (history 48, stride 4, horizon 48) to create 8,106 training, 951 validation, and 951 test samples.

Exchange. The `Exchange` dataset (Lai et al., 2018) consists of 8 daily exchange rates. We used a sliding window (history 48, stride 12, horizon 48) to generate 3,984 training, 448 validation, and 448 test samples.

D.3.2. MULTIMODAL DATASET

Multimodal datasets are those that natively contain both time series data and textual descriptions. Instead of generating text from features, we perform **attribute extraction** from the existing texts. This allows us to generate a new, standardized textual description.

Weather. The `Weather` dataset (Xu et al., 2024) from the Max Planck Institute contains 3 atmospheric variables sampled every 10 minutes. We used data from 2014-2022, splitting it into training, validation, and test sets. A sliding window (history 36, stride 36, horizon 36) was used for sample generation. The training, validation and test samples are 30,573, 4,377 and 4,341. The accompanying textual descriptions were processed using the methodology mentioned before. Specifically, we employed GPT-4 (Achiam et al., 2023) to parse each caption and identify values for a predefined set of seven attributes:

- **Season**: spring, summer, fall, winter.

- **Time of Day**: early morning, morning, afternoon, evening.

- **Weather Condition**: sunny, cloudy, rain, foggy, snowy.

- **Temperature Trend**: increase, decrease, steady.

- **Wind Direction**: S, N, W, E, SW, SE, NW, NE.

- **Atmospheric Condition**: low, average, high.

- **Humidity Level**: low, average, high.

An "unknown" category was also included for cases where information was not present in the text.

E. DTTC Model

As introduced in Sec. 2.3, the DTTC (Disentangled Time Series and Text Consistency) model is designed to evaluate forecasts by measuring their consistency between both historical patterns and future textual conditions. The DTTC model leverages contrastive learning to disentangle time series representations into intrinsic features and extrinsic condition-dependent attributes. This section will introduce the architecture and training of the DTTC model in detail.

Conceptually similar to the CLIP model (Radford et al., 2021), the DTTC framework is composed of a dual-encoder architecture: a time series encoder E_{ts} and a text encoder E_{text}, where the complete parameters can be expressed as ϕ. During training, the model processes tuples of data, each containing a historical sequence $\mathbf{x}_h$, its textual conditions $\mathbf{c}_h$, a corresponding future forecast $\mathbf{x}_f$, and the future textual conditions $\mathbf{c}_f$.

The time series encoder, which utilizes the PatchTST architecture (Nie et al., 2022), is trained to disentangle an input time series $\mathbf{x}$ into two distinct representations: an intrinsic feature vector $\mathbf{I}$ and an extrinsic feature vector $\mathbf{E}$. It processes both the historical and future sequences:

- For historical sequence $\mathbf{x}_h$, the output is $(\mathbf{I}_h, \mathbf{E}_h) = E_{ts}(\mathbf{x}_h)$.
- For future forecast $\mathbf{x}_f$, the output is $(\mathbf{I}_f, \mathbf{E}_f) = E_{ts}(\mathbf{x}_f)$.

Correspondingly, the text encoder is designed to map the textual conditions, $\mathbf{c}$, into the same extrinsic feature space, producing an embedding $\tilde{\mathbf{E}}$. In order to handle long text inputs, we adopt the tokenizer from the pre-trained Long-CLIP (Zhang et al., 2024) model. The parameters of the encoder itself, however, are trained from scratch. This encoder also processes both historical and future conditions:

- For historical conditions $\mathbf{c}_h$, the output is $\tilde{\mathbf{E}}_h = E_{text}(\mathbf{c}_h)$.
- For future conditions $\mathbf{c}_f$, the output is $\tilde{\mathbf{E}}_f = E_{text}(\mathbf{c}_f)$.

The training process is guided by two distinct contrastive learning objectives: an intrinsic consistency loss and an extrinsic consistency loss.

The intrinsic consistency loss, $\mathcal{L}_I$, enforces that the intrinsic features of the historical sequence $\mathbf{I}_h$ and the future forecast $\mathbf{I}_f$ remain aligned. This encourages the model to preserve the fundamental, time-invariant dynamics of the series across the historical and future segments. The loss is defined as:

$$\mathcal{L}_I(\phi) = -\frac{1}{B} \sum_{i=1}^{B} \log \frac{\exp(< \mathbf{I}_h[i], \mathbf{I}_f[i] >)}{\sum_{j=1}^{B} \exp(< \mathbf{I}_h[i], \mathbf{I}_f[j] >)}, \tag{11}$$

The second objective, the extrinsic consistency loss, $\mathcal{L}_E$, ensures that the extrinsic features extracted from the time series align with the features from their corresponding textual conditions. This loss comprising two terms that respectively align historical features ($\mathbf{E}_h$ and $\tilde{\mathbf{E}}_h$) and future features ($\mathbf{E}_f$ and $\tilde{\mathbf{E}}_f$):

$$\mathcal{L}_E(\phi) = -\frac{1}{2B} \sum_{i=1}^{B} \left(\log \frac{\exp(< \mathbf{E}_h[i], \tilde{\mathbf{E}}_h[i] >)}{\sum_{j=1}^{B} \exp(< \mathbf{E}_h[i], \tilde{\mathbf{E}}_h[j] >)} + \log \frac{\exp(< \mathbf{E}_f[i], \tilde{\mathbf{E}}_f[i] >)}{\sum_{j=1}^{B} \exp(< \mathbf{E}_f[i], \tilde{\mathbf{E}}_f[j] >)} \right), \tag{12}$$

where $< \cdot, \cdot >$ denotes the inner product and B is the batch size. By jointly optimizing these two objectives, the model learns a representation space suitable for evaluating forecast consistency. The pseudocode for the DTTC model is presented in Algorithm 1 and the detailed model architecture is in Fig. 6.

F. Model Architecture

The architecture of the noise estimator of TADIFF, illustrated in Fig. 7, is inspired by the DiT model (Peebles & Xie, 2023), and is adapted for the specific demands of time series forecasting with multi-modal conditioning.

First, the inputs are converted into embeddings. The historical time series $\mathbf{x}_{h,0} \in \mathbb{R}^{L_h}$ and the noisy future time series $\mathbf{x}_{f,t} \in \mathbb{R}^{L_f}$ are separately passed through a patchify module to obtain token sequences $\mathbf{P}_h \in \mathbb{R}^{N_h \times D}$ and $\mathbf{P}_f \in \mathbb{R}^{N_f \times D}$,

Figure 6. The model architecture of the DTTC Model.

Algorithm 1 Pseudocode for the DTTC Model Training

Input: A batch of training tuples $(\mathbf{x}_h^{(i)}, \mathbf{c}_h^{(i)}, \mathbf{x}_f^{(i)}, \mathbf{c}_f^{(i)})_{i=1}^B$, where $\mathbf{x}$ are time series and $\mathbf{c}$ are texts.
Output: Total loss $\mathcal{L}_{\text{total}}$.

1: **# Disentangle features using encoders**
2: $(\mathbf{I}_h, \mathbf{E}_h) \leftarrow E_{\text{ts}}(\mathbf{x}_h)$ ▷ Disentangled historical features.
3: $(\mathbf{I}_f, \mathbf{E}_f) \leftarrow E_{\text{ts}}(\mathbf{x}_f)$ ▷ Disentangled future features.
4: $\tilde{\mathbf{E}}_h \leftarrow E_{\text{text}}(\mathbf{C}_h)$ ▷ Historical text features.
5: $\tilde{\mathbf{E}}_f \leftarrow E_{\text{text}}(\mathbf{C}_f)$ ▷ Future text features.

6: **# Compute pairwise similarity matrices**
7: $\mathbf{S}_I \leftarrow \text{Sim}(\mathbf{I}_h, \mathbf{I}_f)$ ▷ $\mathbf{S}_I \in \mathbb{R}^{B \times B}$, intrinsic similarity matrix.
8: $\mathbf{S}_{Eh} \leftarrow \text{Sim}(\mathbf{E}_h, \tilde{\mathbf{E}}_h)$ ▷ $\mathbf{S}_{Eh} \in \mathbb{R}^{B \times B}$, historical extrinsic similarity.
9: $\mathbf{S}_{Ef} \leftarrow \text{Sim}(\mathbf{E}_f, \tilde{\mathbf{E}}_f)$ ▷ $\mathbf{S}_{Ef} \in \mathbb{R}^{B \times B}$, future extrinsic similarity.

10: **# Compute intrinsic and extrinsic losses**
11: Let $\mathbf{I}_{\text{diag}} \in \mathbb{R}^{B \times B}$ be the identity matrix, serving as the ground-truth labels.
12: $\mathcal{L}_I \leftarrow \text{CrossEntropy}(\mathbf{S}_I, \mathbf{I}_{\text{diag}})$ ▷ Intrinsic consistency loss.
13: $\mathcal{L}_{Eh} \leftarrow \text{CrossEntropy}(\mathbf{S}_{Eh}, \mathbf{I}_{\text{diag}})$
14: $\mathcal{L}_{Ef} \leftarrow \text{CrossEntropy}(\mathbf{S}_{Ef}, \mathbf{I}_{\text{diag}})$
15: $\mathcal{L}_E \leftarrow (\mathcal{L}_{Eh} + \mathcal{L}_{Ef})/2$ ▷ extrinsic consistency loss.

16: **# Compute total training loss**
17: $\mathcal{L}_{\text{total}} \leftarrow \mathcal{L}_I + \mathcal{L}_E$ ▷ Total objective.
18: **Return:** $\mathcal{L}_{\text{total}}$

---

which are then concatenated along the token dimension to form $\mathbf{P} \in \mathbb{R}^{N \times D}$ with $N = N_h + N_f$. Meanwhile, the diffusion step t is transformed into a time embedding $\mathbf{e}_{\text{time}} \in \mathbb{R}^D$, and the textual condition $\mathbf{c}_f$ is processed by a text encoder to yield the text embedding $\mathbf{e}_{\text{text}} \in \mathbb{R}^D$. The text encoder is composed of a pre-trained Long-CLIP tokenizer (Zhang et al., 2024) and two transformer layers trained from scratch. We combine these two embeddings by element-wise addition to obtain the final

Figure 7. The model architecture of the noise estimator in TADIFF.

Table 6. The configuration of TADIFF on different datasets. L_h and L_f represent the history length and forecasting horizon, respectively. $\lambda_F : \lambda_A$ is the loss weight ratio of forecasting and attribution during training. $\lambda_I : \lambda_E$ is the loss weight ratio of intrinsic consistency and extrinsic consistency during finetuning.

Type	Configuration	Synth	ETTm1	Traffic	Exchange	Weather
Data	(L_h, L_f)	$(128, 128)$	$(48, 48)$	$(48, 48)$	$(48, 48)$	$(36, 36)$
Training	Epoch	700	700	700	700	700
	Batch size	1024	1024	1024	1024	1024
	$\lambda_F : \lambda_A$	$2 : 1$	$2 : 1$	$2 : 1$	$2 : 1$	$2 : 1$
Finetuning	Epoch	-	200	200	200	100
	Batch size	-	256	256	256	256
	$\lambda_I : \lambda_E$	-	$5 : 1$	$20 : 1$	$10 : 3$	$1 : 1$

condition embedding $\mathbf{e}_c = \mathbf{e}_{\text{time}} + \mathbf{e}_{\text{text}} \in \mathbb{R}^D$.

The core of the estimator is a stack of N identical conditional Transformer blocks, architecturally similar to DiT (Peebles & Xie, 2023) but adapted to time-series tokens. Each block follows a pre-normalization design, consisting of a multi-head self-attention sub-layer and a feed-forward sub-layer. The condition embedding $\mathbf{e}_c$ is fed into a lightweight conditioning MLP to produce a conditioning signal, which is then injected into the block to modulate the token features. This yields the refined representation for the next layer: $\mathbf{H}^j = \text{Block}_j(\mathbf{H}^{j-1}, \mathbf{e}_c)$, with $\mathbf{H}^0 = \mathbf{P}$.

Finally, after all blocks, the output tokens are passed through a prediction head and then an unpatchify module to map patch features back to the original time-series space, producing the estimated noise for the future series $\hat{\boldsymbol{\epsilon}}_t \in \mathbb{R}^{L_f}$.

Figure 8. The sensitivity study of masking different ratios of relevant or irrelevant tokens in the generated text on ETTm1 and Exchange datasets. M_{irr} represents masking irrelevant tokens, M_{rel} represents masking relevant tokens.

G. Implementation Setting and More Experiment Results

G.1. Implementation Setting

We adopt dataset-specific configurations for each dataset, as shown in Tab. 6. Since Synth already contains diverse conditions with ground truth future time series, only the training is applied. All experiments are run on a single Nvidia A40 GPU with three random seeds.

G.2. Model Efficiency Analysis

In this section, we present the efficiency comparison of TADIFF with other baselines. Specifically, we compared model size and average inference time per sample on the Weather dataset using a single NVIDIA A40 GPU (batch size = 1). As shown in the Tab. 7, although our model incurs a higher inference cost than non-diffusion models, it is competitive with both foundation and diffusion baselines. Given its significant forecasting improvements, the increase in model size and the reduction in inference speed are considered acceptable trade-offs.

Table 7. Model size and inference time comparison on Weather dataset.

Method	TADIFF	VerbalTS	Sundial	TimeMMD
Model size (MB)	14	16	128	35
Inference time (ms)	340	463	272	17

G.3. Sensitivity Study on Constructed Text Templates

In this section, we provide a sensitivity study to prove that TADIFF is not overfitting to the text templates in the generated text mentioned in Appendix D.3.1 but successfully captures the meaningful contents.

We manually classified the tokens appearing in the generated text into two categories: relevant and irrelevant. Relevant tokens contain meaningful semantics related to the time series, while irrelevant tokens mainly serve to maintain valid sentence structure. For example, in the sentence "The trend direction is up.", the tokens "trend", "direction", and "up" are relevant, whereas "The", "is", and "." are irrelevant. We independently masked relevant and irrelevant tokens at varying ratios and analyzed the resulting performance degradation. We conducted the experiment on the factual data of the ETTm1 and Exchange datasets, where both datasets use generated text.

As shown in Fig. 8, masking irrelevant tokens leads to significantly smaller performance drops compared with masking relevant tokens. Notably, for MAE and MSE, masking 70% of the irrelevant tokens still yields performance comparable to masking only 10% of the relevant tokens. These results demonstrate that TADiff indeed learns from the meaningful semantic information in the generated text rather than overfitting to the constructed templates.

G.4. Conditional Decoupling Capability of Text-Attribution

In this section, we prove that the text-attribution of TADIFF can decouple the intrinsic features of the sequence from the extrinsic conditions. Specifically, we hope to verify the dependency between intrinsic features $\mathbf{x}_{h,T}$ and extrinsic conditions $\mathbf{c}_h$. We train a contrastive learning model (similar to CLIP (Radford et al., 2021)) to verify whether the relationship between $\mathbf{x}_{h,T}$ and $\mathbf{c}_h$ can be effectively captured (i.e., $\mathbf{x}_{h,T}$ is dependent of $\mathbf{c}_h$) or not ($\mathbf{x}_{h,T}$ is truly independent of $\mathbf{c}_h$).

We first use our model (TADIFF) to estimate the initial noise $\mathbf{x}_{h,T}$ based on $\mathbf{x}_{h,0}$ and $\mathbf{c}_h$. Then, we train CLIP models to learn a shared latent space between $\mathbf{x}_{h,T}$ and $\mathbf{c}_h$ through contrastive learning. We evaluate the CLIP model by measuring its accuracy in retrieving the most similar condition $\mathbf{c}_h$ from three candidates given $\mathbf{x}_{h,T}$. For comparison, we also train additional CLIP models between $\mathbf{x}_{h,0}$ and $\mathbf{c}_h$ using the same model architecture.

The results in the following Tab. 8 prove the independence between $\mathbf{x}_{h,T}$ and $\mathbf{c}_h$. It can be observed that retrieving $\mathbf{c}_h$ given $\mathbf{x}_{h,T}$ yields significantly lower accuracy compared to retrieving $\mathbf{c}_h$ given $\mathbf{x}_{h,0}$, with the performance of the former approaching random guessing. It illustrates that the derived initial noise from the text-attribution stage has truly become independent of $\mathbf{c}_h$, decoupling the intrinsic features of the sequence from the extrinsic conditions.

Table 8. Accuracy of retrieving the most similar $\mathbf{c}_h$ from 3 candidates, the ideal accuracy of random guessing is approximately 33%.

Setting	Synth	ETTm1	Exchange	Traffic	Weather
$\mathbf{x}_{h,0} \to \mathbf{c}_h$	97.42	93.34	98.17	96.75	77.71
$\mathbf{x}_{h,T} \to \mathbf{c}_h$	32.27	37.84	42.93	39.70	37.18

G.5. Robustness of the hyper-parameters

In this section, we investigate the effect of the loss weight ratio during training and counterfactual finetuning, and the results are shown in Fig. 9. The influence of $\lambda_F : \lambda_A$ remains stable in most cases, and significant performance differences are observed only when the ratios take extreme values. In counterfactual fine-tuning, a trade-off arises between DTTC-I and DTTC-E, which is intuitive and expected, since these two metrics are directly linked to their corresponding optimization objectives during fine-tuning. We adopt a balanced loss weight ratio to achieve simultaneous improvements in both metrics compared with forecasting without finetuning.

Figure 9. Sensitivity study on loss weight ratio. In the left figure, we study the impact of $\lambda_F : \lambda_A$ in joint training, where the dotted lines indicate the performance of TADIFF without attribution. In the right figure, we study the impact of $\lambda_I : \lambda_E$ in counterfactual finetuning, where the dotted lines indicate the performance of TADIFF without finetuning.

G.6. Case Study

In this section, we provide several visualization results of TADIFF on Synth dataset, including both the factual and counterfactual forecasting. The results are presented in Fig. 10, which demonstrates that TADIFF considers both the constraint of the historical intrinsic feature and control of the future condition. Furthermore, TADIFF demonstrates strong generalization capabilities to diverse future conditions, providing accurate forecasts in both factual and counterfactual settings.

Figure 10. The case study of time series forecasting on Synth dataset.