# 🔥 SPARK: Skeleton-Guided Reasoning Synthesis from Large-Scale Scientific Literature

**Anonymous ACL submission**


## Abstract

Scientific reasoning remains challenging for open-source models, largely due to the lack of high-quality scientific reasoning data. Existing datasets are often dominated by factual recall or formulaic problem solving, with limited emphasis on mechanism understanding, evidence-grounded reasoning, and hypothesis evaluation. To address this, we introduce **SPARK** (Scientific Paper Abstracted Reasoning sKeleton), a paper-oriented synthesis framework built on SCI-BASE, a large-scale corpus of research papers spanning 10 scientific disciplines. Instead of directly converting papers into question-answer pairs, SPARK treats the *claim-evidence-derivation* structure of a paper as the fundamental unit of reasoning synthesis. Specifically, SPARK (1) distills each paper into a compact reasoning skeleton capturing its central claims and supporting evidence, enabling self-contained question generation, and (2) synthesizes reasoning tasks from four scientific perspectives: *mechanistic reasoning, hypothesis falsification, quantitative derivation, and boundary calibration*. A final consistency verification stage further removes unsupported or contradictory outputs. Using this framework, we construct Spark-234K, a scientific reasoning dataset with substantially higher difficulty and diversity than existing resources. Experiments show that Spark-234K consistently outperforms existing scientific reasoning datasets while achieving stronger performance with significantly fewer training samples.


## 1 Introduction

Recent Large Language Models (LLMs) have achieved strong performance on reasoning tasks such as mathematics and coding (Li et al., 2025; Cai et al., 2025; Pei et al., 2025), but scientific reasoning remains significantly more challenging (Li et al., 2026). A central limitation is the lack of high-quality scientific reasoning data. Existing scientific corpora are often constructed from textbooks, exam problems, or web resources (Lu et al., 2025; Fan et al., 2025), and therefore mainly emphasize factual recall, standard derivations, or routine calculations while underrepresenting the evidence-based and mechanism-driven reasoning processes that characterize real scientific discovery.

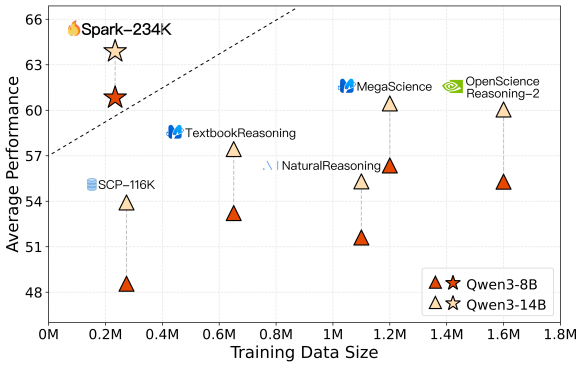


Figure 1: Comparison of the Qwen3-8B base and Qwen3-14B base models trained on baseline datasets versus Spark-234K (benchmark scores in Table 2).

Research papers provide a natural source of scientific reasoning supervision because they contain expert-validated claims, supporting evidence, derivations, assumptions, and experimental analysis at scale (Taylor et al., 2022). Recent works have also explored leveraging scientific literature for reasoning-oriented data construction and scientific question-answering (Noorbakhsh et al., 2026; Dong et al., 2024; Liu et al., 2024). However, synthesizing high-quality reasoning data from papers remains difficult. Scientific papers are long, densely structured documents whose reasoning processes are often distributed across multiple sections, figures, tables, and experimental discussions. As a result, naively generating reasoning data from papers frequently produces samples that are not self-contained (Choi et al., 2021; Dasigi et al., 2021a; Jain and Garimella, 2026), omit critical assumptions or evidence, or fail to preserve the underlying

claim-evidence reasoning structure (examples are shown in Figure 14).

We introduce **SPARK** (Scientific Paper Abstracted Reasoning sKeleton), a paper-oriented synthesis framework for scientific reasoning data construction. Instead of directly generating reasoning data from sections, chunks, or entire documents, SPARK treats a paper's claim-evidence-derivation chain as the fundamental unit of synthesis.

Given a scientific paper, SPARK first extracts its central claims together with the supporting evidence, assumptions, quantitative relations, and boundary conditions, and organizes them into a compact reasoning skeleton. This reasoning skeleton rewrites the core scientific argument into a self-contained form, reducing long-context interference (Liu et al., 2024) while preserving the underlying reasoning process and mitigating the lack of self-containment commonly observed in document-grounded generation (Choi et al., 2021; Dasigi et al., 2021a; Jain and Garimella, 2026).

Based on the reasoning skeleton, SPARK synthesizes scientific reasoning data from four perspectives: (1) *mechanistic reasoning*, which explains why an observed phenomenon occurs (Machamer et al., 2000); (2) *hypothesis falsification*, which distinguishes competing explanations (Pearl, 2009); (3) *quantitative derivation*, which emphasizes modeling and derivation instead of formula substitution (Sun et al., 2024); and (4) *boundary calibration*, which examines the assumptions and validity limits under which conclusions hold. A final consistency verification stage further removes unsupported or contradictory outputs.

Through the above framework and using 370K frontier scientific papers from the open SCIBASE (OpenDataLab, 2026) corpus, we construct Spark-234K, a high-quality scientific reasoning dataset containing 234K synthesized instances. Despite its compact scale, this dataset exhibits exceptional data efficiency and overall performance (Figure 1). Notably, it outperforms massive baseline datasets like MegaScience and OpenScienceReasoning-2 (NVIDIA, 2025), despite these collections being nearly six and eight times its size, respectively. Across distinct base model families and parameter scales, our data surpasses the runner-up datasets on multiple benchmarks by substantial average margins of $+3.10$, $+4.47$, and $+3.43$ points. We will make the extracted reasoning skeletons and the full dataset publicly available once the review process concludes.

## 2 Paper Collection and Preparation

**Source corpus.** SPARK is built on SCIBASE (OpenDataLab, 2026), an open scientific literature base comprising $\sim$3.36M open-access papers across ten disciplines. Each paper includes metadata and is parsed via MinerU (Niu et al., 2025) into an ordered sequence of paragraphs, tables, captions, and equations, preserving LaTeX where available. This structured format is crucial for reconstructing paper-level arguments while retaining the quantitative rigor required for deep reasoning.

**Quality filtering and balanced sampling.** To prepare inputs for the pipeline, we apply strict filtering. We restrict the timeframe to January 2024–March 2026 and discard non-English, incompletely parsed, or review articles lacking a clear trajectory of claims and evidence. Crucially, we prioritize papers rich in concrete observables, such as equations, statistical results, tables, and experimental comparisons. Finally, to mitigate the raw corpus's heavy skew toward medicine and life sciences (Table 5), we apply discipline-balanced sampling across the ten major scientific disciplines it spans. The resulting seed pool comprises roughly 370K argument-structured frontier papers.

## 3 Dataset Construction

Figure 2 illustrates the SPARK pipeline, which converts a screened paper into standalone training instances. The key design choice is to treat a paper as an argument rather than a flat document: SPARK first identifies the core conclusion, reconstructs the evidence trajectory that supports it, and stores this trajectory as a compact *reasoning skeleton*. Questions are then generated from the skeleton under several scientific reasoning perspectives and filtered against the same skeleton for self-containment and source consistency.

### 3.1 Skeleton Extraction

Skeleton extraction makes a long paper usable for supervision without flattening it into sections or fragmenting it into independent chunks. Directly prompting over the full paper risks *context diffusion*: the central scientific argument is diluted by peripheral details, making generation prone to shallow or unfocused questions. Instead of preserving the paper's original layout, skeleton extraction recovers the claim-centered argument: what conclusion the paper advances, what evidence supports it,

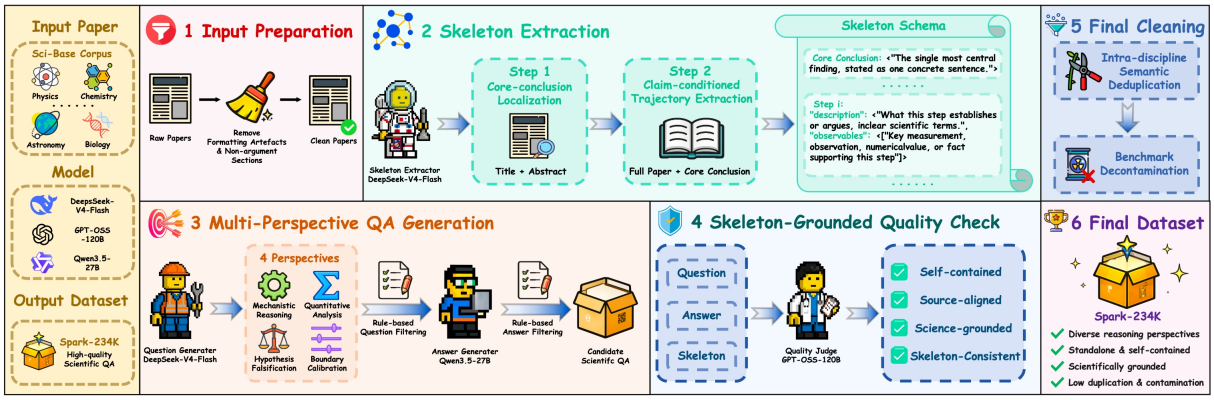


Figure 2: The SPARK data synthesis pipeline. A frontier paper is first condensed into a *reasoning skeleton*. We then generate deep scientific QA pairs via four targeted perspectives, followed by a lightweight consistency check to ensure data quality and self-containment.

and under which assumptions or boundary conditions the conclusion holds.

**Input normalization.** We first convert the parsed structure into a linearized text representation. This preserves the scientific content vital for reasoning, including equations, table text, captions, and numerical results, while stripping away formatting artifacts (such as headers, footers, and affiliations) and non-argument sections (such as references and acknowledgments).

**Two-step extraction.** Skeleton extraction recovers the core argument rather than the original section order. First, *core conclusion localization* identifies the central claim from the title and abstract, which typically state the research question, main finding, and scope while avoiding distracting body content. Second, *trajectory extraction* reads the normalized full paper conditioned on this conclusion, reconstructing the supporting argument as ordered steps. Each step contains a description of its logical role and a set of observables, such as measurements, comparisons, numerical values, formulas, or stated boundary conditions.

The resulting skeleton comprises the core conclusion and an ordered list of steps. As Figure 3 illustrates, it is not a section-level summary (Edge et al., 2025) but a compact evidence trajectory organized entirely around the paper's central claim.

### 3.2 Multi-Perspective Question Generation

The next stage generates questions that probe scientific reasoning rather than surface facts. The skeleton exposes the paper's claim, evidence, inferential links, and boundary conditions, which must be connected to understand the argument (Javaji et al., 2025). We therefore generate questions from four complementary perspectives.

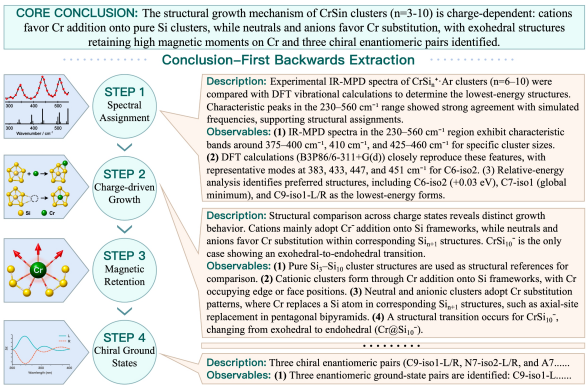


Figure 3: Example skeleton extracted by SPARK from a real paper, condensing the source into a core conclusion and ordered evidence steps with concrete observables.

**Mechanistic reasoning** turns a reported condition–effect relation into a causal explanation problem, asking why a structure, intervention, or regime produces the phenomenon (Machamer et al., 2000). **Hypothesis falsification** uses contrasts, ablations, or ruled-out alternatives to ask which explanatory model is supported by the evidence (Pearl, 2009). **Quantitative derivation** converts numerical observables, formulas, or scaling relations into modeling-first problems whose difficulty lies in selecting and linking principles, rather than substituting values (Sun et al., 2024). **Boundary calibration** asks where a conclusion ceases to be justified, focusing on the assumptions, regimes, confounders, or approximations that delimit the claim.

Together, these perspectives ask why a result holds, which explanation survives the evidence,

how quantities are related, and when the claim breaks down. This shifts generation away from fact retrieval and plug-and-chug computation toward mechanism-level reasoning. To maintain precision, SPARK follows a conservative yielding strategy: for each paper, it uses only the perspectives recommended during skeleton extraction, generates at most one question per perspective, and skips any perspective unsupported by the evidence.

**Filtering.** Generated questions undergo a lightweight, rule-based filtering stage to detect malformed formats and source-leakage phrases (detailed in Appendix F). The central constraint is self-containment: a question depending on unstated figures, tables, or source context is discarded. Finally, questions are audited for information sufficiency and intellectual depth, with thresholds adjusted to prevent the over-correction of valid reasoning trajectories.

### 3.3 Answer Generation

An answer model responds to each accepted question without access to the skeleton or source text. This setup mirrors the downstream fine-tuning environment and empirically verifies that the question is self-contained. We then apply heuristic filters to discard answers that are malformed, excessively short or long, or dominated by repeated $n$-grams.

### 3.4 Skeleton-Grounded Quality Check

While rule-based checks catch formatting issues, they cannot assess scientific grounding. We therefore deploy an LLM judge to evaluate each $\langle$question, answer, skeleton$\rangle$ triple against four criteria. For the **question**, it verifies: (i) self-containment (supplying necessary context independent of the paper), and (ii) consistency with the skeleton. For the **answer**, it checks if the reasoning is (iii) coherent and (iv) logically supported by the evidence trajectory. QA pairs failing any criterion are discarded.

The self-containment check acts primarily as a safeguard, as skeleton extraction prevents most dependencies at the source (evidenced by the low discard rate in Table 6). Crucially, by grounding the answer evaluation directly in the extracted skeleton, we bypass the massive majority voting and iterative rewriting typically required in traditional math and reasoning domains (Tong et al., 2024), keeping the pipeline highly lightweight.

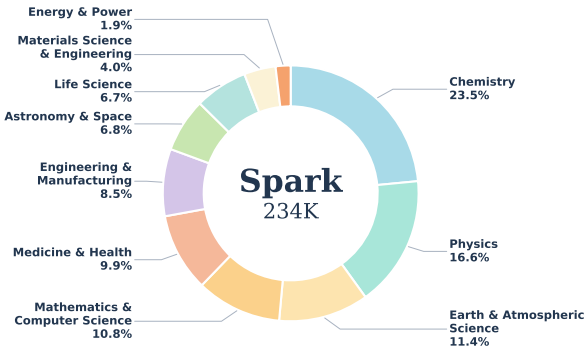


Figure 4: Discipline distribution of Spark-234K.

### 3.5 Final Data Cleaning

Finally, we apply deduplication and decontamination procedures. We perform semantic deduplication within each discipline using Qwen3-Embedding-8B embeddings (Zhang et al., 2025). To prevent benchmark leakage, we enforce 13-gram exact matching against all downstream evaluation sets, discarding any overlapping records.

## 4 Dataset Statistics and Analysis

By applying the proposed synthesis pipeline to the 370K filtered seed papers, we construct Spark-234K, a high-quality instruction tuning dataset dedicated to deep scientific reasoning.

### 4.1 Dataset Statistics

Figure 4 illustrates the disciplinary distribution of Spark-234K. The composition objectively reflects the natural landscape of argument-rich literature across ten scientific domains. Fundamental sciences, such as Chemistry (23.5%) and Physics (16.6%), form the largest segments. This distribution is primarily driven by the inherent variance in reasoning density across different fields, which naturally dictates the volume of extractable questions. In comparison, more comprehensive and applied disciplines, ranging from Earth Sciences (11.4%) to Materials Science (4.0%), account for relatively smaller proportions, yet collectively ensure broad thematic coverage.

Beyond disciplinary diversity, all four reasoning perspectives are well represented within the corpus. Mechanistic reasoning (35.6%) and quantitative derivation (30.2%) constitute the majority, aligning with the empirical nature of scientific papers, whereas boundary calibration (20.4%) and hypothesis falsification (13.9%) provide critical diversity in higher-order analytical evaluation.

Table 1: Comparison of dataset length (average token length) and diversity.

| Dataset | Size | Length | | Diversity | |
|---|---|---|---|---|---|
| | | Q. Len. | Resp. Len. | Vendi ↑ | Cent. Dist. ↑ |
| SCP-116K | 274K | 122.09 | 555.68 | 173.42 | 0.4923 |
| TextbookReasoning | 651K | 63.80 | 409.66 | 283.75 | 0.5598 |
| NaturalReasoning | 1.1M | 76.28 | 766.33 | 349.42 | 0.6163 |
| MegaScience | 1.2M | 170.77 | 692.93 | 373.78 | 0.6150 |
| OpenScienceReasoning-2 | 1.6M | 217.40 | **5691.70** | 290.17 | 0.5610 |
| Spark-234K | 234K | **316.54** | 2711.68 | **384.57** | **0.6183** |

The high yield rate in Table 6 underscores the high quality of our direct generation. In particular, the minimal rejection for self-containment failures confirms that the pipeline inherently produces independent and context-complete questions.

### 4.2 Dataset Analysis

To evaluate Spark-234K, we benchmark it against five established scientific reasoning datasets: SCP-116K, TextbookReasoning, OpenScienceReasoning-2, NaturalReasoning, and MegaScience.

**Length.** Spark-234K features the longest questions among all datasets, averaging 316.54 tokens (Table 1). This extended length is not mere verbosity; it is a rigorous necessity, as genuine scientific problems intrinsically require substantial context, established variables, and boundary conditions to be well-posed. Furthermore, the responses average 2711.68 tokens, ranking second overall. This strikes an optimal balance: it delivers exceptionally dense reasoning supervision while avoiding both the unconstrained, rambling chains typical of overly long-CoT datasets (e.g., OpenScienceReasoning-2) and the shallow supervision of terse no-CoT alternatives.

**Diversity.** We quantify data diversity using the Vendi Score (Friedman and Dieng, 2022) and Centroid Distance (Suwanda et al., 2020). Remarkably, despite its highly curated, compact size (234K) compared to baselines scaling up to 1.6M samples (Table 1), Spark-234K decisively achieves the highest scores on both metrics (384.57 and 0.6183, respectively). This compelling result demonstrates that genuine dataset diversity stems from a systematically designed, multi-perspective generation mechanism rather than the sheer, brute-force volume of the source corpus.

**Answer correctness.** Given the cross-disciplinary breadth of the dataset, comprehensive manual annotation is prohibitive. To systematically assess answer reliability, we conduct a large-scale automated verification on a random sample of 20K questions. We prompt Gemini-3.1 Pro[1] to solve each question independently, then evaluate the semantic equivalence between its solution and the original reference response. The resulting 93.28% consistency rate robustly confirms the factual accuracy of the generated answers.

**Difficulty.** Figure 5a empirically highlights the limitations of existing datasets in eliciting deep reasoning. Using DeepSeek-V4-Flash, we grade 20K sampled questions per dataset on a five-level taxonomy (Appendix G). While baseline datasets suffer from high proportions of L1 (Fact recall) and L2 (Routine computation) data, with their combined share exceeding 50% in TextbookReasoning, Spark-234K effectively eradicates these low-tier categories, yielding only 0.02% L1 and 1.2% L2 questions. Instead, over 93% of our dataset demands high-order reasoning, dominated by L4 (Multi-step, 58.5%) and L5 (Research-level, 34.6%) problems. Notably, this exceptional density is achieved intrinsically by the generation paradigm without any explicit difficulty-based filtering, demonstrating that the pipeline naturally resolves shallow supervision at the source.

**Self-containment.** Naively converting scientific papers into QA pairs often yields unusable questions that rely on unstated, external context. As Figure 5b illustrates, multiple baseline datasets suffer from severe dependency issues, with their proportion of non-self-contained data exceeding 15%. In supervised fine-tuning, introducing such a high ratio of contextually broken data is enough to severely degrade training performance, as it inadvertently teaches models to hallucinate missing variables rather than perform rigorous deduction. To isolate the architectural contribution of our reasoning skeleton in solving this structural flaw, we report Spark-234K both before and after the final quality check. Remarkably, even prior to the filtering stage, Spark-234K achieves a 98.55% self-containment rate, drastically outperforming the best baseline (92.39%). This proves that the skeleton extraction paradigm intrinsically solves the context-dependency problem at the source. The final quality check serves merely as a strict safeguard, lifting the final rate to a near-perfect 99.73%.

[1] https://ai.google.dev/gemini-api/docs/models/gemini-3.1-pro-preview

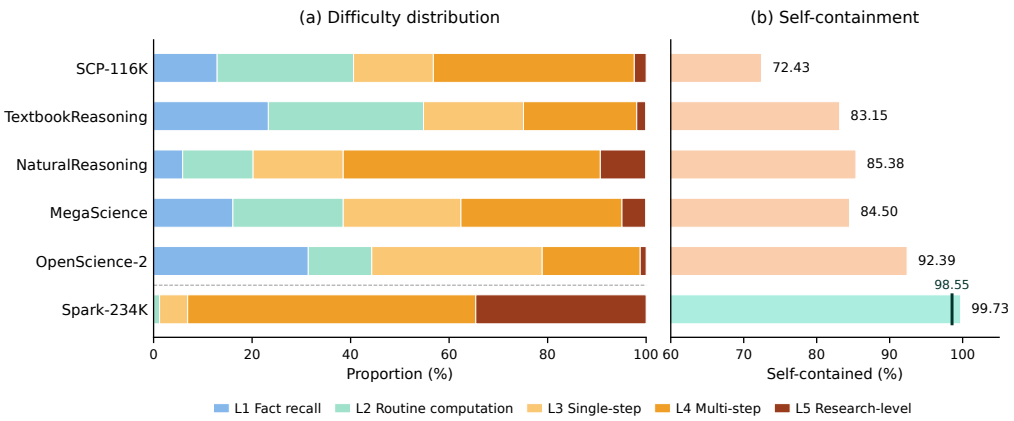


Figure 5: Difficulty distribution over five levels across datasets. Spark-234K shifts mass toward higher difficulty, while baselines concentrate on low-difficulty recall or routine computation.

## 5 Experiments

### 5.1 Experimental Setup

**Training.** Fine-tuning is conducted on Llama3.1-8B-Base (Grattafiori et al., 2024), Qwen3-8B-Base, and Qwen3-14B-Base (Yang et al., 2025). All comparisons share the same training hyperparameters; details are provided in Appendix C.

**Evaluation.** For fair comparison, all models are evaluated in the zero-shot setting across two groups of benchmarks: **(1) general science reasoning benchmarks** (GPQA-Main [GPQA-M] (Rein et al., 2024), GPQA-Diamond [GPQA-D] (Rein et al., 2024), SuperGPQA [S-GPQA] (Du et al., 2026), SciBench (Wang et al., 2024a), MMLU (Hendrycks et al., 2020), and MMLU-Pro (Wang et al., 2024b)) and **(2) domain-specific benchmarks** (ChemBench (Mirza et al., 2024), CS-Bench (Song et al., 2025), PubMedQA (Jin et al., 2019), MedQA-US (Yao et al., 2024), GSM8K (Cobbe et al., 2021), and MATH-500 (Hendrycks et al., 2021)). We report avg@3 or avg@5 for all benchmarks, with details provided in Appendix D.

### 5.2 Main Results

Table 2 reports the evaluation on six scientific reasoning benchmarks. The results empirically validate our central claim: preserving a paper's reasoning skeleton provides far denser supervision than the brute-force scaling of synthetic examples.

**Superiority of Quality over Quantity.** The macro averages immediately highlight the efficiency of our approach. Across all three backbones, Spark-234K consistently achieves the highest overall performance using only 234K examples—less than one-fifth the volume of million-scale baselines like MegaScience (1.2M). For instance, fine-tuning Qwen3-8B on Spark-234K yields an average score of 60.83, decisively outperforming the strongest baseline (56.36). This confirms that high-quality, structurally intact data is significantly more effective than merely scaling shallow QA pairs.

**Breakthroughs in High-Difficulty Reasoning.** The performance gains perfectly mirror the intrinsic high-difficulty nature of our training data. The most substantial improvements manifest in tasks demanding complex, multi-step analytical deduction rather than rote memorization. On the Expert Science MCQ cluster (GPQA series) and the quantitative SciBench, Spark-234K demonstrates overwhelming dominance. For Qwen3-14B, our dataset drives GPQA-M and GPQA-D scores to 53.71 and 55.05, respectively, eclipsing models trained on much larger corpora. Similarly, robust improvements on MMLU-Pro confirm that grounding QA generation in authentic paper skeletons successfully translates high training difficulty into superior downstream reasoning capabilities.

### 5.3 Domain-Specialized Results

Table 3 evaluates performance across distinct scientific disciplines. As our corpus inherently spans ten fields, Spark-234K consistently achieves the highest macro averages across all backbones, demonstrating robust, universal benefits across chemistry, computer science, medicine, and mathematics.

Notably, Spark-234K maintains a significant advantage on highly domain-specific benchmarks like MedQA-US (e.g., 79.36 vs. 72.58 for MegaScience on Qwen3-14B). This confirms that our training

Table 2: Main results on six scientific reasoning benchmarks. Avg. is the macro average over all six. Within each model group, the best result per column is in **bold** and the second best is underlined.

| | | Expert Science MCQ | | | Quant. | Broad Science | | |
|---|---|---|---|---|---|---|---|---|
| **Model / Training Data** | **Size** | **GPQA-M** | **GPQA-D** | **S-GPQA** | **SciBench** | **MMLU** | **MMLU-Pro** | **Avg.** |
| *Llama3.1-8B-Base* | | | | | | | | |
| Base | — | 24.55 | 24.75 | 14.41 | 17.41 | 54.06 | 24.39 | 26.60 |
| + SCP-116K | 274K | 26.83 | 30.71 | 15.09 | 20.37 | 50.71 | 25.81 | 28.25 |
| + TextbookReasoning | 651K | 30.11 | 33.95 | 24.76 | 31.83 | 66.25 | 47.73 | 39.11 |
| + NaturalReasoning | 1.1M | 31.85 | 32.91 | 23.80 | 31.29 | 60.23 | 44.31 | 37.40 |
| + MegaScience | 1.2M | 33.71 | **38.89** | 25.56 | 36.87 | 68.79 | 49.79 | 42.27 |
| + OpenScienceReasoning-2 | 1.6M | 29.91 | 26.77 | 24.09 | 27.59 | **70.10** | 50.61 | 38.18 |
| + Spark-234K (ours) | 234K | **38.38** | 37.37 | **28.47** | **43.80** | 69.36 | **54.83** | **45.37** |
| *Qwen3-8B-Base* | | | | | | | | |
| Base | — | 32.59 | 29.29 | 29.05 | 30.30 | 66.22 | 45.24 | 38.78 |
| + SCP-116K | 274K | 36.93 | 34.62 | 33.80 | 54.13 | 71.24 | 60.63 | 48.56 |
| + TextbookReasoning | 651K | 40.75 | 42.90 | 37.01 | 61.31 | 73.07 | 64.26 | 53.22 |
| + NaturalReasoning | 1.1M | 40.03 | 41.29 | 34.44 | 59.83 | 72.15 | 61.91 | 51.61 |
| + MegaScience | 1.2M | 43.75 | 44.95 | 38.66 | 64.83 | 79.65 | 66.31 | 56.36 |
| + OpenScienceReasoning-2 | 1.6M | 40.78 | 39.36 | 38.55 | 62.37 | 81.15 | 69.55 | 55.29 |
| + Spark-234K (ours) | 234K | **50.22** | **52.53** | **41.84** | **66.35** | **81.50** | **72.54** | **60.83** |
| *Qwen3-14B-Base* | | | | | | | | |
| Base | — | 37.95 | 38.38 | 33.50 | 50.16 | 76.01 | 59.35 | 49.23 |
| + SCP-116K | 274K | 42.80 | 43.75 | 35.29 | 59.29 | 77.37 | 64.99 | 53.92 |
| + TextbookReasoning | 651K | 44.27 | 46.81 | 42.15 | 63.61 | 79.25 | 68.53 | 57.44 |
| + NaturalReasoning | 1.1M | 44.09 | 44.83 | 34.16 | 63.27 | 77.59 | 67.94 | 55.31 |
| + MegaScience | 1.2M | 47.32 | 48.99 | 44.47 | 67.81 | 82.44 | 71.65 | 60.45 |
| + OpenScienceReasoning-2 | 1.6M | 46.64 | 47.83 | 44.21 | 65.41 | **83.99** | 72.20 | 60.05 |
| + Spark-234K (ours) | 234K | **53.71** | **55.05** | **47.62** | **69.55** | 83.65 | **73.68** | **63.88** |

paradigm effectively generalizes to highly specialized, expert-level domains without compromising reasoning fidelity.

### 5.4 Data Efficiency and Scaling

All experiments in this and the following ablation use Qwen3-8B-Base, evaluated on MMLU, MMLU-Pro, SciBench, and GPQA-Diamond under the same training and evaluation protocol as our main experiments. Here we train on progressively larger random subsets of Spark-234K to measure how performance scales with the amount of synthesized data (Figure 6).

While the total dataset volume is relatively compact, the scaling curve exhibits a consistent and incremental improvement across benchmarks as the data size expands. This steady upward trajectory indicates that the model has not yet saturated on the provided scientific reasoning patterns. It suggests a highly promising direction for future work, where simply applying our automated extraction pipeline to a broader corpus of academic literature could naturally yield further scaling gains.

### 5.5 Pipeline Ablation

We ablate the two central designs of SPARK, with all settings trained on a fixed 40K set (Table 4).

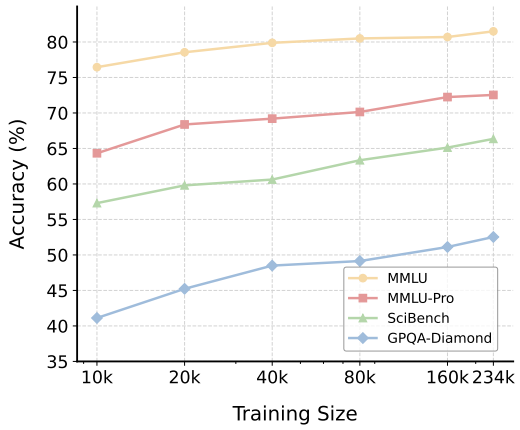


Figure 6: Performance scaling with the number of synthesised training records from Spark-234K.

**Unit of synthesis.** We replace skeleton extraction with three alternatives that feed the generator different representations of the same paper: the whole paper, chunked passages, or an LLM-generated summary. The rest of the pipeline remains unchanged. All baseline representations degrade sharply. Whole-paper input performs worst ($-9.15$), as processing a long document diffuses the central claims and yields shallow questions. Chunking and summarization also lose ground ($-5.63$, $-6.71$) by severing cross-section claim–evidence chains or discarding the reasoning skele-

Table 3: Domain-specialized transfer results across chemistry, computer science, medicine, and mathematics.

| Model / Training Data | Size | ChemBench | CS-Bench | PubMedQA | MedQA-US | GSM8K | MATH-500 | Avg. |
|---|---|---|---|---|---|---|---|---|
| *Llama3.1-8B-Base* | | | | | | | | |
| Base | — | 23.03 | 49.90 | 51.20 | 48.78 | 56.40 | 19.20 | 41.42 |
| + MegaScience | 1.2M | 42.97 | 59.89 | **76.60** | 62.03 | 71.65 | 45.20 | 59.72 |
| + Spark-234K (ours) | 234K | **44.51** | **64.29** | 74.20 | **66.35** | **85.10** | **64.00** | **66.41** |
| *Qwen3-8B-Base* | | | | | | | | |
| Base | — | 49.60 | 69.16 | 61.20 | 55.54 | 88.63 | 70.80 | 65.82 |
| + MegaScience | 1.2M | 53.01 | 76.07 | **77.40** | 66.93 | 93.03 | 79.60 | 74.34 |
| + Spark-234K (ours) | 234K | **55.85** | **77.61** | 75.60 | **75.33** | **94.09** | **81.20** | **76.61** |
| *Qwen3-14B-Base* | | | | | | | | |
| Base | — | 53.73 | 75.98 | 77.00 | 63.71 | 93.86 | 71.60 | 72.65 |
| + MegaScience | 1.2M | **58.82** | 79.92 | **78.80** | 72.58 | 94.77 | 82.00 | 77.82 |
| + Spark-234K (ours) | 234K | 57.63 | **81.50** | 78.20 | **79.36** | **94.82** | **85.37** | **79.48** |

Table 4: Ablation of key SPARK design choices.

| Setting | Avg. | Δ |
|---|---|---|
| SPARK (full) | 63.46 | — |
| *Unit of synthesis* | | |
| w/o Skeleton (→ whole paper) | 54.31 | −9.15 |
| w/o Skeleton (→ chunks) | 57.83 | −5.63 |
| w/o Skeleton (→ summary) | 56.75 | −6.71 |
| *Question generation* | | |
| w/o Mechanistic | 61.59 | −1.87 |
| w/o Falsification | 60.30 | −3.16 |
| w/o Quantitative | 58.82 | −4.64 |
| w/o Boundary | 61.19 | −2.27 |

ton entirely. In contrast, extracting a reasoning skeleton preserves the paper's claim–evidence–derivation trajectory, yielding the highest-quality synthetic data.

**Question generation.** We fix the skeleton and ablate the perspectives leave-one-out, resampling from the remaining three to restore the 40K count so that variants differ only in which perspectives are present. Because the data volume is held fixed, the gaps are smaller, yet every perspective still yields a clear drop, confirming that each contributes signal the others cannot replace. Quantitative derivation matters most ($-4.64$), as it supplies the bulk of computation-intensive questions that strengthen the model's computational ability.

# 6 Related Work

## 6.1 Scientific Reasoning Data

Scientific post-training data has expanded from curricular sources to large synthetic mixtures. TextbookReasoning (Fan et al., 2025) extracts QA from university textbooks, while domain-specific efforts such as ChemData700K (Zhang et al., 2024) tune models on field-focused instruction data. Broader collections, including SCP-116K (Lu et al., 2025), OpenScienceReasoning-2 (NVIDIA, 2025), NaturalReasoning (Yuan et al., 2026), and MegaScience (Fan et al., 2025), improve scale and coverage. However, scale alone does not guarantee depth. Textbooks favor settled knowledge, while synthetic mixtures often default to factual recall and formulaic problem-solving. This motivates sourcing supervision from texts rich in scientific reasoning, rather than mere facts.

## 6.2 Data Synthesis from Scientific Literature

Frontier papers naturally fulfill this requirement, yet scalable task conversion remains nontrivial. While human annotations (Dasigi et al., 2021b) resist scaling, LLM pipelines now synthesize tasks from full papers (Wan et al., 2024; Liu et al., 2026), chunked text (Sarthi et al., 2024), or retrieved passages (Wang et al., 2025). However, treating a paper as a monolithic document diffuses its core claims, while arbitrary chunking severs vital cross-section evidence chains. SPARK instead distills a paper's claims, evidence, and derivations into a compact *reasoning skeleton* as source, yielding self-contained, mechanism-oriented questions.

# 7 Conclusion

We introduced SPARK to address the limitations of existing scientific reasoning data by treating a paper's *claim–evidence–derivation* structure as the fundamental unit of synthesis. SPARK distills papers into reasoning skeletons, generates questions across four scientific perspectives, and enforces strict consistency. The resulting Spark-234K offers greater difficulty and diversity, and experiments demonstrate it substantially improves the scientific reasoning capabilities of base models.

## Limitations

This work has two main limitations. First, constrained by computational resources, our experiments are limited to supervised fine-tuning; we leave the use of Spark-234K for reinforcement learning, including more verifiable reward design, to future work. Second, scientific reasoning spans too many disciplines to recruit qualified human experts across all of them, so our answer verification relies on consistency checks with a strong LLM judge rather than human spot-checking; incorporating expert human evaluation is an important direction for improving reliability.

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## A The Source Corpus: SCI-BASE

SCI-BASE serves as the foundational corpus of open-access scientific literature for our dataset, comprising over 3.36 million parsed and formula-preserving papers with coverage up to March 2026. To ensure strict data quality for downstream synthesis, we applied rigorous filtering criteria to the raw aggregated documents, explicitly removing incomplete papers, such as those missing abstracts or essential metadata.

As detailed in Table 5, the finalized high-quality corpus spans ten major scientific disciplines. While the distribution inherently skews towards Medicine & Health Sciences and Life Sciences (collectively accounting for 61.3%) due to natural open-access publishing volumes, this massive, structured repository provides a highly reliable and diverse pool for our discipline-aware sampling pipeline.

Table 5: Disciplinary distribution of SCI-BASE.

| Discipline | # Papers | % |
|---|---|---|
| Medicine and Health Sciences | 1,213,132 | 38.8% |
| Life Sciences | 704,290 | 22.5% |
| Engineering and Mfg. Science | 370,679 | 11.9% |
| Earth and Atmospheric Sciences | 188,709 | 6.0% |
| Physics | 168,402 | 5.4% |
| Chemistry | 168,491 | 5.4% |
| Math and Computational Science | 124,683 | 4.0% |
| Materials Science and Eng. | 111,204 | 3.6% |
| Astronomy and Space Sciences | 60,657 | 1.9% |
| Energy and Power Science | 16,849 | 0.5% |
| **Total** | 3.36M | 100% |

## B Construction Funnel

Table 6 tracks the precise volume dynamics and explicit rejection rates across each stage of our data synthesis pipeline.

A closer examination of the filtering statistics within the Skeleton-grounded check phase yields two significant insights into the pipeline's behavior. First, only a marginal fraction of data (7.92%) is discarded due to non-self-contained questions. This exceptionally low rate demonstrates that our upstream skeleton extraction successfully preempts contextual dependency issues by anchoring the generations appropriately. Instead, the overwhelming majority of rejections (65.87%) stem from answers being inconsistent with the original paper skeleton. This distribution underscores the uncompromising rigor of our quality auditor, which strictly penalizes hallucinatory behaviors and logical drift rather than superficial formatting flaws.

Table 6: Construction funnel of Spark-234K. Size is the retained count after each stage; Filtered is shown only for stages with explicit filtering.

| Phase | Size | Filtered |
|---|---|---|
| Initial sampling | 370K | – |
| Skeleton extraction | 325K | – |
| Question generation | 293K | – |
| Answer generation | 283K | – |
| Skeleton-grounded check | 241K | 14.97% |
| Question not self-contained | – | 7.92% |
| Question not paper-derived | – | 13.61% |
| Answer inconsistent with skeleton | – | 65.87% |
| Answer internally incoherent | – | 12.60% |
| Dedup. + Decontamination | 234K | 3.04% |

Second, in the final Deduplication and Decontamination stage, the remaining 3.04% of data was filtered entirely due to textual duplication. Strikingly, zero instances were discarded due to overlap or contamination with downstream benchmarks. This absolute absence of evaluation contamination empirically demonstrates that synthesizing data from recent, peer-reviewed academic literature serves as an inherent defense against benchmark leakage, ensuring the scientific integrity of downstream evaluations.

**Source Provenance and Data Diversity.** To characterize the composition of the finalized dataset, Figure 7 illustrates the distribution of source publishing venues and platforms within Spark-234K. The underlying corpus aggregates literature from a highly heterogeneous mix of prominent academic publishers and preprint repositories. As shown in the treemap, the dataset draws significantly from major venues including MDPI (24.1%), Elsevier (13.4%), Wiley (6.5%), arXiv (5.4%), and Frontiers (5.4%). This is supplemented by specialized platforms and premium societies, such as IOP (5.1%), ACS (3.2%), BMC (3.2%), Springer (2.7%), Nature Portfolio (2.4%), bioRxiv/medRxiv (1.7%), RSC (1.6%), Oxford Academic (1.5%), and IEEE (1.2%), alongside a long-tail category of various other venues comprising 22.6%.

This broad institutional provenance establishes a critical foundation for data diversity. Different publishers and academic societies inherently enforce distinct typesetting styles, structural layouts, vocabulary preferences, and writing conventions. By exposing downstream models to this rich, multi-source mixture of writing paradigms and layout-induced linguistic variations, Spark-234K effectively mitigates stylistic overfitting. This ensures that the fine-tuned models capture invariant, domain-agnostic scientific reasoning patterns

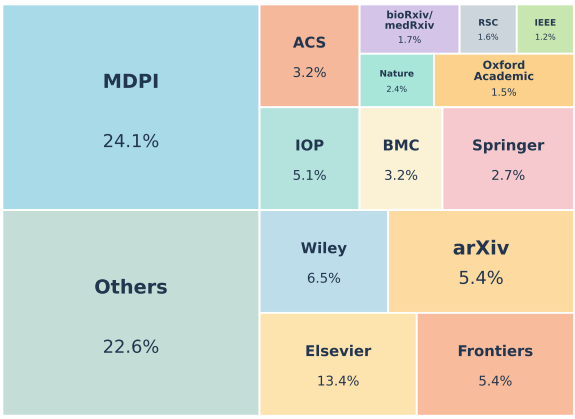


Figure 7: Publisher Distribution.

rather than artifacts specific to the templates of a single publisher.

## C Training Details

We conduct fine-tuning using LlamaFactory (Zheng et al., 2024). To ensure rigorous evaluation integrity, all baseline datasets undergo a strict 13-gram exact match decontamination process against all downstream test benchmarks prior to training. Unless otherwise specified, experiments utilize 16 GPUs with a per-device batch size of 4 and 2 gradient accumulation steps. For 32-GPU runs, we adjust gradient accumulation to 1 to maintain a consistent global batch size. Table 7 summarizes the remaining shared hyperparameters.

Table 7: Training Configuration.

| Configuration | Value |
|---|---|
| Cutoff length | 32,768 |
| Epochs | 3.0 |
| Learning rate | 5.0e-6 |
| Warmup ratio | 0.05 |
| Per-device batch size | 4 |
| Gradient accumulation (16 GPUs) | 2 |
| Gradient accumulation (32 GPUs) | 1 |
| Flash attention | FlashAttention-2 |
| Liger Kernel | Enabled |
| Thinking mode | Enabled |
| Average tokens across devices | True |
| Drop last dataloader batch | False |

## D Evaluation Details

We organize evaluation benchmarks into two groups. The first group contains general science reasoning benchmarks used in the main comparison, covering expert science QA, quantitative scientific problem solving, and broad multidisciplinary science understanding. The second group contains domain-specific benchmarks for chemistry, computer science, medicine, and mathematics, which evaluate whether scientific fine-tuning transfers to specialized fields. Table 8 summarizes all evaluation sets.

For evaluation implementation, we use the same codebase as MegaScience[2], which standardizes prompting, decoding, and answer extraction across benchmarks. All models are evaluated in the zero-shot setting on 8 GPUs with temperature set to 0, and reported results are avg@3 or avg@5 depending on the benchmark.

## E Pipeline Details

### E.1 Model and Decoding Configuration

Table 9 summarizes the API configuration used for skeleton extraction and multi-perspective question generation. Both stages call DeepSeek-V4-Flash with thinking enabled and high reasoning effort.

Answer generation and skeleton-grounded quality checking are performed with locally deployed models. Qwen3.5-27B is used to generate answers, while GPT-OSS-120B is used as the quality checker. Table 10 reports the decoding configuration for both stages.

### E.2 Prompt Templates

We provide the prompt templates used in the pipeline. Skeleton extraction uses two prompts: Figure 8 localizes the core conclusion from the title and abstract, and Figure 9 reconstructs the claim-conditioned trajectory from the full paper content.

Question generation is implemented as a modular prompt. Figure 11 gives the shared prompt framework, which defines the global objective, self-containment constraints, skip conditions, and output schema. The perspective-specific content is injected through the placeholder `{perspective_guidance}`: at runtime, it is replaced by one of the four definitions in Figure 10. This design keeps the output format and global quality constraints fixed while allowing each generated question to target a different reasoning role, such as mechanism explanation, hypothesis falsification, quantitative derivation, or boundary calibration. Finally, Figure 12 shows the answer-generation prompt, and Figure 13 shows

[2] https://github.com/GAIR-NLP/lm-open-science-evaluation

the skeleton-grounded quality-check prompt used to filter QA pairs.

## F Source Leakage Patterns

We apply a deterministic source-leakage filter to remove questions that implicitly require access to the original document. The filter consists of 21 case-insensitive regular-expression patterns and is applied to generated questions before they enter the final dataset. Table 11 summarizes the pattern groups. Rather than attempting to judge all forms of self-containment, this filter targets explicit linguistic cues that a question is referring back to the source paper, provided context, or document structure. Any record matching one or more patterns is discarded.

## G Difficulty Taxonomy

We evaluate question difficulty with a five-level reasoning taxonomy. For each dataset, we sample 20K questions and ask DeepSeek-V4-Flash to assign one of the following levels according to the minimum reasoning required to obtain the answer:

- **L1 — Fact Retrieval.** The answer can be directly retrieved as a fact, definition, or given value from knowledge or the source. No reasoning, derivation, or inference is required.
- **L2 — Routine Calculation.** The answer is obtained by applying a known formula or standard procedure and substituting the provided values. No modeling, method selection, or multi-step reasoning is required.
- **L3 — Single-Step Reasoning.** The question requires one non-trivial inference, conceptual link, or causal/mechanistic explanation beyond direct retrieval or mechanical substitution.
- **L4 — Multi-Step Reasoning.** The question requires a chain of reasoning steps, mechanistic analysis, or discrimination among multiple competing explanations or hypotheses.
- **L5 — Research-Level Reasoning.** The question requires constructing a model from principles, synthesizing multiple pieces of evidence, carrying out a derivation, or analyzing boundary conditions, approximations, or counterfactuals.

The resulting labels are used only for aggregate analysis rather than as a training signal. This protocol is intended to compare the reasoning profile of datasets under a consistent rubric, not to provide definitive expert judgments for individual examples.

## H Diversity Metric Calculations

To rigorously evaluate the semantic span of Spark-234K and baseline data, we use two complementary metrics: Vendi Score (Friedman and Dieng, 2022) and Centroid Distance (Suwanda et al., 2020). Let $X = \{x_1, x_2, \ldots, x_N\}$ be the set of embeddings for the instructions or questions in a dataset, where $N$ is the sample size. All embeddings are computed with `Qwen3-Embedding-8B` (Zhang et al., 2025), and the embedding dimensionality is fixed to 4096 for all samples. Unless otherwise specified, distance is measured by cosine distance, $d(x_i, x_j) = 1 - \frac{x_i \cdot x_j}{\|x_i\|\|x_j\|}$.

**Vendi Score.** The Vendi Score measures intrinsic diversity by interpreting a dataset's semantic spread as the effective number of independent modes. It is calculated from the eigenvalues of a kernel matrix $K$, where $K_{ij} = k(x_i, x_j)$ denotes the similarity between samples. We use the cosine-similarity kernel. The Vendi Score is defined as the exponential of the Shannon entropy of the normalized eigenvalues:

$$\mathrm{Vendi}(X) = \exp\left(-\sum_{i=1}^{N} \lambda_i \ln \lambda_i\right), \quad (1)$$

where $\lambda_1, \ldots, \lambda_N$ are the normalized eigenvalues of $K/N$. A higher Vendi Score indicates that the dataset contains a larger number of effective independent semantic clusters. In practice, we compute Vendi Score using the reference implementation released by the original authors.[3]

**Centroid Distance.** Centroid Distance measures geometric dispersion in the embedding space. We first compute the global centroid $\mu$ of the dataset:

$$\mu = \frac{1}{N} \sum_{i=1}^{N} x_i. \quad (2)$$

Centroid Distance is then defined as the complement of the average cosine similarity between each sample $x_i$ and the centroid $\mu$:

$$\mathrm{Dist}_{\mathrm{cent}}(X) = 1 - \frac{1}{N} \sum_{i=1}^{N} \frac{x_i \cdot \mu}{\|x_i\|\|\mu\|}. \quad (3)$$

[3] https://github.com/vertaix/Vendi-Score

***Prompt for Core-Conclusion Localization***

```
### Role
You are a senior scientific reviewer identifying the central claim of a research paper.

### Task
Read the title and abstract and articulate the paper's core conclusion. Capture the main finding
     precisely; where a single sentence cannot do it justice, use the supporting fields to record
     the qualifications, scope, or significance that make the claim complete.

### Guidance
- The headline conclusion must be a concrete scientific assertion, not a topic description. Prefer "
     X increases Y under condition Z" over "this work studies the relationship between X and Y".
- Many findings are only meaningful with their conditions, mechanism, or scope attached. Do not
     amputate these to fit one sentence; place them in the supporting fields instead.
- Record only what the abstract actually commits to. Do not invent results, and do not promote
     previewed methods into findings.
- If there is no clear scientific argument (e.g. an editorial, news piece, abstract collection, or
     purely descriptive catalog without a central thesis), output an empty JSON object {{}}.

### Output Schema
Return ONLY a JSON object with this exact structure:
{{
  "core_conclusion": "The single most central finding, stated as one concrete sentence.",
  "key_qualifications": ["A condition, scope limit, or boundary under which the conclusion holds"],
  "significance": "Why this finding matters or what it resolves, in one sentence (empty string if
     the abstract does not state it)."
}}

### Critical Rules
- core_conclusion must be one substantive, self-contained sentence naming the specific subject and
     the asserted effect or mechanism. Keep it focused; offload conditions and scope to
     key_qualifications rather than overloading this sentence.
- key_qualifications captures the decisive conditions, parameters, or limits that the conclusion
     depends on. Use an empty list only when the finding is genuinely unconditional.
- significance is a single sentence and may be an empty string if not stated.
- If the conclusion is vague, hedged beyond recovery, or absent, output {{}}.
- Output ONLY the raw JSON object. Do NOT wrap it in markdown formatting or ```json code fences. No
     explanatory prose.
- Do not refer to "the paper", "the authors", "the study", sections, figures, or tables.

### Title
{paper_title}

### Abstract
{paper_abstract}
```

Figure 8: Prompt for Core-Conclusion Localization.

A higher Centroid Distance indicates that samples are more widely dispersed around the dataset center, covering a broader semantic region rather than clustering tightly around a narrow set of topics.

## I Self-Containment Bad Cases

Figure 14 shows representative self-containment failures observed in baseline data. These examples illustrate why a fluent question can still be unusable for standalone reasoning: it may refer to missing definitions, omitted equations, or unstated variables.

## J Qualitative Examples

To provide qualitative insight into the output of our automated data construction pipeline, we present examples of a generated paper skeleton and corresponding generated questions and answers in Figure 15. The figure illustrates the clear structure extracted for a sample paper, highlighting key entities, processes, and findings. Linked to specific points in this skeleton are sequential examples of different question types—entity-based, procedural, causal, and more—each accompanied by a grounded answer derived directly from the skeleton content. Subtle visual links demonstrate the grounding and diversity of the generated data, ensuring a robust and factually anchored fine-tuning dataset for scientific reasoning.

## K Use of AI Assistants

We used a large language model only for light writing assistance, limited to grammar checking and minor clarity edits on a small number of sentences. All technical content, experiments, and analyses in this paper were written by the authors.

Table 8: Benchmark details for our evaluation.

| Benchmark | Size | Report | Category | Description |
|---|---|---|---|---|
| *General science reasoning benchmarks* | | | | |
| GPQA-Main (Rein et al., 2024) | 448 | avg@5 | Expert science QA | Graduate-level, Google-proof multiple-choice questions across biology, chemistry, and physics. |
| GPQA-Diamond (Rein et al., 2024) | 198 | avg@5 | Expert science QA | The higher-confidence GPQA subset selected for expert agreement and difficulty. |
| SuperGPQA (Du et al., 2026) | 26,529 | avg@3 | Broad graduate science | Large-scale graduate-level benchmark spanning many disciplines and subfields. |
| SciBench (Wang et al., 2024a) | 640 | avg@5 | Quantitative science | Aggregated evaluation over the tested chemistry, mathematics, and physics subsets. |
| MMLU (Hendrycks et al., 2020) | 14,042 | avg@3 | Broad knowledge | Multitask benchmark covering broad academic and professional subjects, including science. |
| MMLU-Pro (Wang et al., 2024b) | 12,032 | avg@3 | Broad knowledge | More challenging multitask benchmark with harder options and stronger reasoning demands. |
| *Domain-specific benchmarks* | | | | |
| ChemBench (Mirza et al., 2024) | 2,788 | avg@5 | Chemistry | Aggregated evaluation over the tested multiple-choice and string-match subsets. |
| CS-Bench (Song et al., 2025) | 1,778 | avg@5 | Computer science | Aggregated evaluation over the tested assertion and multiple-choice subsets. |
| PubMedQA (Jin et al., 2019) | 500 | avg@5 | Medicine | Biomedical question answering over PubMed-derived contexts. |
| MedQA-US (Yao et al., 2024) | 1,273 | avg@5 | Medicine | Medical licensing-style multiple-choice questions from the US subset. |
| GSM8K (Cobbe et al., 2021) | 1,319 | avg@5 | Mathematics | Grade-school math word problems requiring multi-step arithmetic reasoning. |
| MATH-500 (Hendrycks et al., 2021) | 500 | avg@5 | Mathematics | A 500-problem subset of competition-style mathematical reasoning problems. |

***Prompt for Claim-Conditioned Trajectory Extraction***

```
### Role
You are a senior scientific reviewer reconstructing the logical structure that supports a paper's
     stated conclusion.

### Task
The core conclusion has already been established. Treat it as the fixed endpoint of the argument.
     Your work has two parts:
1. Read the full content and reconstruct the step-by-step argumentation chain that leads to this
     conclusion, identifying key logical steps (not sections) and focusing on how the conclusion is
     reached through experiments, observations, derivations, or reasoning.
2. Judge which training perspectives the reconstructed trajectory genuinely supports, using the
     definitions below.

### Core Conclusion (fixed target)
{core_conclusion}

### Training Perspectives
Match perspectives to the nature of the trajectory itself:
- mechanistic_reasoning -> the work centers on a new mechanism or causal account of why/how
     something happens.
- hypothesis_falsification -> the work hinges on testing competing explanations and ruling some out.
- quantitative_derivation -> the work is computation-heavy, rich in values, units, and formulas.
- boundary_calibration -> the work is careful about what its evidence does and does not justify.

### Critical Rules
- steps must capture the logical flow from evidence to the given conclusion. Do NOT produce a
     section-by-section summary.
- Each step must describe one logical unit of the argument (an experiment that tests a hypothesis, a
      comparison that rules out an alternative, a derivation that connects observations to a
     mechanism, etc.).
- The "description" MUST explicitly mention the specific experimental conditions, chemical names,
     mathematical operators, or equipment setups used. Avoid generic phrasing like "an analysis was
     conducted".
- The "observables" MUST contain concrete anchors: exact numerical values with units, specific
     formulas/variables, statistical bounds, key entities, or distinct phenomenological signs. Never
      write placeholder text like "did an experiment and got a result".
- recommended_perspectives: list 1-4 perspectives from the four above (exact strings), ordered best-
     fitting first, picking those that match the character of this trajectory. Do not default to a
     fixed mix.
- If the full content does not actually support a coherent chain toward the given conclusion, output
      an empty JSON object {{}}.
- Output ONLY the raw JSON object. Do NOT wrap it in markdown formatting or ```json code fences. No
     explanatory prose.
- Do not refer to "the paper", "the authors", "the study", sections, figures, or tables.

### Paper Content
{paper_content}

### Output Schema
Return ONLY a JSON object with this exact structure:
{{
  "steps": [
    {{
      "step_number": 1,
      "description": "What this step establishes or argues, in clear scientific terms.",
      "observables": ["Key measurement, observation, numerical value, or fact supporting this step"]
    }}
  ],
  "recommended_perspectives": [
    "mechanistic_reasoning",
    "hypothesis_falsification"
  ]
}}
```

Figure 9: Prompt for Claim-Conditioned Trajectory Extraction.

***Perspective Guidance for Question Generation***

```
[mechanistic_reasoning]
Target: Probe the reasoning link between a condition, intervention, or structure and an observed
     phenomenon. Frame this link as a universal scientific problem, abstracting away paper-specific
     identifiers so that solving it requires general mechanistic reasoning rather than reading
     comprehension.
Style: Answerable in 2-5 paragraphs of mechanistic reasoning without extensive math. Focus entirely
     on the system/phenomenon itself.
Construction:
- State the setup using generic descriptors (e.g. "a two-component system under periodic forcing").
- The expected answer should be a chain of mechanistic steps, each justified by a general principle,
      not a single recalled fact.
Perspective Guardrails:
- Anti-Stipulation: Do NOT stipulate a counterintuitive finding and ask "why". The solver must
     engage via general principles to deduce the outcome.
- Anti-Comprehension: Must not be a mere reading-comprehension question. If it requires having read
     the specific paper to start reasoning, reject it.
- Single-Mechanism Focus: Center one dominant causal mechanism. Do not bundle several loosely
     related effects into one prompt.

[hypothesis_falsification]
Target: Test whether the evidence rules out plausible but competing explanatory models, forcing the
     solver to identify which single model the evidence is consistent with.
Style: MCQ format. The `question` string MUST end with four options labeled (A), (B), (C), (D)
     separated by newlines. Do NOT indicate the correct answer in the question.
Construction:
- Present a concrete body of evidence in the stem, then offer four candidate explanations.
- Each distractor must be defeated by a DIFFERENT, identifiable piece of the evidence, so
     elimination requires genuine discrimination rather than plausibility ranking.
Perspective Guardrails:
- Structural Rivalry: Options must be structurally different explanatory models or historical
     misconceptions, NOT paraphrases or lexical variants of the same answer.
- Lexical Decoupling: Avoid technical terms in the stem that act as "giveaways" via direct
     vocabulary matching with the correct option. The correct option must not be identifiable by
     surface word overlap alone.
- Balanced Distractors: Keep options comparable in length, specificity, and technical register so
     none stands out by form rather than content.

[quantitative_derivation]
Target: Convert numerical observables into a modeling-first problem. The solver must formulate the
     relevant physical, chemical, or statistical relations and derive an analytical expression,
     bound, scaling relation, or key calculated quantity.
Style: A rigorous graduate-level theoretical problem. State knowns objectively and demand derivation
     .
Construction:
- Provide only the observables genuinely needed; let the solver decide which principles couple them.
- Ask for a symbolic result first (expression, bound, or scaling), with any numerical evaluation as
     a final, minor step.
Perspective Guardrails:
- Modeling-First: The intended difficulty MUST lie in constructing the model and connecting
     principles, NOT in tedious arithmetic or plug-and-chug substitution.
- Anti-Fragmentation: Focus on ONE core modeling challenge. Avoid sub-questions that are purely
     arithmetic continuations.
- No Over-Specification: Do NOT pre-state the governing equation, the regime, or the solution method
     . Handing the solver the premise removes the modeling step that defines this perspective.

[boundary_calibration]
Target: Target the qualifiers, assumptions, parameter regimes, or confounders under which the claim
     would no longer be justified.
Style: Concise critique targeting a specific assumption/approximation breakdown (e.g., "At what
     parameter regime does this approximation break down?").
Construction:
- Anchor on one specific claim, then ask where its supporting evidence stops holding.
- Frame the answer around a concrete switch: a parameter crossing a threshold, an assumption being
     violated, or a confounder becoming non-negligible.
Perspective Guardrails:
- Sharp Critique: Point to a SPECIFIC, scientifically reachable approximation, regime, or confounder
     . Do not ask vague "what could go wrong" questions.
- No Sci-Fi: The boundary must be physically or operationally reachable, not an absurd hypothetical
     (e.g., halving gravity).
- Justified-vs-Unjustified: The item should hinge on distinguishing what the evidence does support
     from what it does not, not on listing every conceivable caveat.
```

Figure 10: Perspective Guidance for Question Generation.

***Shared Prompt for Multi-Perspective Question Generation***

```
### Role & Objective
You are an expert data architect crafting high-quality Supervised Fine-Tuning data to train next-
     generation reasoning models.
Distill a PhD-level scientific problem from the 'Paper Trajectory' based on the requested
     perspective. The item must function as a rigorous logic stress test requiring complex, multi-
     step deduction.

### Input Context
- Requested Perspective: {requested_perspective}

### Perspective Focus
{perspective_guidance}

### Global Guardrails & Structural Bans (CRITICAL)
To prevent dataset mode collapse, enforce these rules strictly:
1. Universal Abstraction (No Source Referencing): The problem MUST be entirely self-contained. NEVER
      use labels like "In this study," "the authors," "the trajectory," or result-reporting verbs ("
     found," "measured").
2. No Hyperlocal Naming: Replace sample-specific IDs, specific instrument names, or isolated
     regional names with generic scientific descriptors.
3. No Meta/Lazy Evaluations: NEVER end with meta-questions (e.g., "Is this justified?", "What
     remains unknown?").
4. Target Difficulty: Difficulty must stem from intricate mechanistic chains, subtle tradeoffs, or
     advanced modeling->not niche trivia.

### Global Skip Conditions
Output EXACTLY `[]` (an empty array) with no other text if ANY of the following apply:
- The trajectory lacks the fundamental depth, alternatives, or theoretical bounds required for the
     `{requested_perspective}`.
- The core conclusion is just a descriptive observation/high-level summary with no "black box" left
     to interrogate.
- The question cannot be made self-contained without relying on paper-specific data.
- The question degrades into a trivial textbook variant of a standard field problem.

### Output Schema
  {{
    "question": "The fully formulated scientific problem (append (A)-(D) options here if MCQ).",
    "evidence": ["Concise scientific fact 1 from trajectory", "Fact 2"],
    "solvability_justification": "Rigorous proof the question is well-posed. For open math: explain
     theoretical steps. For MCQs: state correct option AND detailed elimination logic for
     distractors."
  }}
]

### Paper Trajectory
{trajectory_text}
```

Figure 11: Shared Prompt for Multi-Perspective Question Generation.

***Prompt for Answer Generation***

```
{question}
Solve the above problem step by step.
```

Figure 12: Prompt for Answer Generation.

***Prompt for Skeleton-Grounded Quality Checking***

```
### Role & Objective
You are a scientific QA auditor. Rule-based checks already catch format failures; your job is the
     part rules cannot decide: whether this QA pair is scientifically grounded in the paper
     trajectory. Judge it for reasoning-model SFT training and return a single KEEP/DISCARD decision
     .

### What You Receive
- A Paper Trajectory: the extracted core conclusion (the scientific direction) plus the step-by-step
      evidence chain (the evidence anchors).
- A Generated Question and a Generated Answer to audit against that trajectory.

### Audit Dimensions

#### Dimension 1: Question
1. Self-Containment
The question must provide the conditions, variables, and context needed to be answered WITHOUT the
     original paper. All custom variables, experimental settings, and boundary conditions must be
     stated. Common universal scientific constants need not be restated. Flag any question that
     silently depends on unstated paper-specific content.

2. Source Match
The question must correspond to what the trajectory actually establishes. Flag a source mismatch
     when the question concerns an entity, quantity, or claim the trajectory does not support, or
     fabricates premises absent from it.

#### Dimension 2: Answer
1. Reasoning Coherence
The reasoning chain must be coherent and complete: no logical jumps, no meaningless repetition or
     loops, no interrupted or truncated output. The final answer must be definite and well-organized
     .
*Rigorous self-correction, re-evaluation of earlier steps, and explicitly resolving uncertainty
     within the text are valuable and fully permitted.*

2. Trajectory Grounding
The answer must be consistent with the scientific direction of the trajectory's core conclusion AND
     not be contradicted by its evidence chain (steps and observables). Equivalent academic
     statements, synonymous expressions, and reasonable paraphrased reasoning are acceptable; only
     essential conflicts with the established direction or evidence are disqualifying.

### Hard Elimination Rules
1. Dependency Defect: Missing essential custom variables; unanswerable without extra paper context.
     -> DISCARD
2. Source Mismatch: Question targets claims/entities the trajectory does not support, or invents
     absent premises. -> DISCARD
3. Generation Defect: Incoherent reasoning -> meaningless loops, arbitrary guessing without
     deduction, truncated output, or serious hallucination. -> DISCARD
4. Grounding Conflict: Answer's core direction is inconsistent with the trajectory's conclusion, or
     is contradicted by its evidence chain. -> DISCARD

Supplementary Rule: Standard multi-step inference, causal analysis, and logical self-correction all
     count as qualified responses.

### Output Specification
Output a single, strictly valid JSON object. Do NOT add any extra symbols, markdown formatting
     outside the JSON, or conversational text. Use the exact schema below:

{{
  "reasoning_steps": "First, write your thorough step-by-step reasoning and analysis here.",
  "checks": {{
    "is_question_self_contained": true,
    "is_question_source_matched": true,
    "is_answer_coherent": true,
    "is_answer_trajectory_grounded": true
  }},
  "fatal_flaw_details": "Concrete flaw reason based on the Hard Elimination Rules, or 'none'.",
  "final_decision": "KEEP"
}}
// Note: "final_decision" must be strictly either "KEEP" or "DISCARD".

### Paper Trajectory
{trajectory_text}

### Generated Question
{question}

### Generated Answer
{answer}
```

Figure 13: Prompt for Skeleton-Grounded Quality Checking.

***Self-Containment Bad Cases from Baseline Data***

**MegaScience.**
**Case 1: Missing definitions.**

> Show that if a binary sequence $\langle X_n \rangle$ is R5-random (as per Definition R5), and if $\langle s_n \rangle$ is any computable sequence as in Definition R4, then $\overline{\Pr}(X_{s_n} = 1) \geq \frac{1}{2}$ and $\Pr(X_{s_n} = 1) \leq \frac{1}{2}$.

**Reason:** The question refers to Definition R5 and Definition R4, but the definitions are not provided. A solver cannot independently interpret the assumptions.

**Case 2: Missing referenced equation.**

> Prove why the last equality holds true for a function in the Dirichlet space.

**Reason:** The phrase "the last equality" refers to an omitted equation, so the target statement to be proved is unavailable.

**Case 3: Missing required variable.**

> A roller coaster is moving at an initial velocity of 10 m/s and comes to a stop after a distance of 50 m. Calculate the average force supplied by the brakes to stop the roller coaster. Assume a constant acceleration and neglect any frictional forces. Use the following equations: $V_1 = 10$ m/s, $\Delta D = 50$ m, $V_2 = 0$ m/s, $F_{\text{net}} = F_{\text{brakes}} = ma$.

**Reason:** The mass of the roller coaster is not specified, so the average braking force cannot be determined.

**SCP-116K.**
**Case 4: Missing circuit diagram.**

> Two AC signals, $V_1$ and $V_2$, are to be combined such that $V_{\text{out}} = \frac{3}{2}V_2 - \frac{5}{2}V_1$. The subtracting amplifier circuit shown is used. What must be the values of $R_1$, $R_2$, $R_3$, and $R_4$? Circuit diagram: $V_1$ connected via $R_1$; $V_2$ connected via $R_2$; operational amplifier with feedback resistance $R_3$; ground connection via $R_4$. (Professional Publications, Inc.)

**Reason:** The question refers to an external circuit diagram. Without the actual diagram, the resistor topology and value relationships are under-specified.

**Case 5: Missing section dependency.**

> Using the results of Section 7.5, find the transformation $x = Tw$ that puts the system $\frac{dx}{dt} = \begin{pmatrix} 1 & -1 & 2 \\ 0 & -2 & 1 \\ -1 & 3 & 0 \end{pmatrix} x + \begin{pmatrix} 1 & 3 \\ 0 & 1 \\ 0 & 2 \end{pmatrix} u$ into the form $\frac{dw}{dt} = \begin{pmatrix} 0 & -3 & 6 \\ -1 & -1 & 0 \\ 0 & 1 & 0 \end{pmatrix} w + \begin{pmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 1 \end{pmatrix} u$.

**Reason:** The question depends on results from Section 7.5, but those results are not provided. A solver cannot recover the required transformation rule from the question alone.

**Case 6: Missing referenced formulas.**

> Calculate the Hilbert transforms of $\cos(\omega_0 t)$ and $\sin(\omega_0 t)$. Hint: Use Euler's identity in the defining integral (7.10.12) for the Hilbert transform of a time signal, and you may also find that recalling (7.9.3) is helpful.

**Reason:** The prompt relies on formula numbers (7.10.12) and (7.9.3), but the formulas themselves are omitted.

**NaturalReasoning.**
**Case 7: Undefined property.**

> What should be the cardinality of $A_n$ to ensure that the subset of infinite binary sequences having a certain property is countable/uncountable, considering the set $R_n$ of binary sequences of length $n$ and the subset $A_n$ of sequences having that property?

**Reason:** The question never defines "a certain property", so the solver cannot determine which sequences belong to $A_n$ or what condition is being analyzed.

**Case 8: Missing humidity information.**

> Given the temperature of 18 degrees Celsius and the atmospheric pressure of 782 mm Hg, calculate the air density using the ideal gas law equation, considering the effects of humidity. Show your work and explain your reasoning.

**Reason:** The question asks the solver to account for humidity but provides no relative humidity, water-vapor partial pressure, or equivalent humidity-related quantity.

Figure 14: Representative self-containment failures from baseline data. Each example appears plausible but lacks information required for standalone solution.

***Dataset Synthesis: From Structured Extraction to Deep Reasoning QA***

**Phase 1: Extracted Paper Framework**

*Core Conclusion:* A tail wave formed behind density cusps in nonlinear laser wakefields driven by a Gaussian laser pulse provides simultaneous focusing and acceleration for externally injected positrons, enabling nearly 100% trapping efficiency with terawatt-class laser systems.

- **Step 1: Defocusing mechanism & Tail wave proposal.**
  - *Description:* Establish that nonlinear wakefields naturally defocus positively charged particles. Propose that a tail wave forms behind density cusps when laser intensity marginally exceeds the nonlinear threshold, converging plasma electrons into an on-axis filament.
  - *Observables:* $a_0 = 1.6$, $w_0 = 12\lambda_0$, peak intensity $3.5 \times 10^{18}$ W/cm$^2$. Regime thresholds based on $n(0)/n_{e0}$: I ($\geq 0.2$), II (0.1–0.2), III ($\leq 0.1$).
- **Step 2: Unloaded dynamics.**
  - *Description:* Using 3D PIC simulations (OSIRIS), demonstrate tail wave dynamics without positron loading. The focusing region for positrons expands from a limited cusp to about half a bubble as laser intensity increases.
  - *Observables:* Grid $200 \times 200 \times 2400$. Transverse field maps show focusing region expanding.
- **Step 3: Beam loading & Field reversal.**
  - *Description:* Load a uniform positron beam into the second bubble. The beam's space-charge attracts tail wave electrons, converting a defocusing transverse field into a focusing field. However, tail wave III causes transverse loss.
  - *Observables:* Positron $n_{+0} = 0.5n_{e0}$, initial energy 20 MeV. Trapping efficiency $\sim 60\%$ due to tail wave III.
- **Step 4: Channel optimization.**
  - *Description:* Increase the plasma channel radius to weaken relativistic self-focusing and suppress tail wave III, maintaining the required on-axis electron density throughout propagation.
  - *Observables:* Channel radius $r_0 = 14\lambda_0 > w_0$. Density $n(0)/n_{e0} \geq 0.1$ (avoiding regime III). Trapping efficiency $> 95\%$ after $1000\lambda_0$.
- **Step 5: Beam evolution.**
  - *Description:* Characterize the accelerated positron beam, showing reduced transverse size, limited emittance growth, and stable longitudinal acceleration.
  - *Observables:* Transverse size reduced to $\sim 1/3$. Acceleration gradient $\sim 100$ GV/m. Final energy peak at 177 MeV (average gain 110 MeV) with 3% FWHM energy spread.
- **Step 6: Parameter robustness.**
  - *Description:* Vary drive laser parameters and beam offsets to map the viability of the scheme.
  - *Observables:* $a_0 \in [1.2, 1.8]$, $w_0 \in [8\lambda_0, 12\lambda_0]$ for high trapping. Longitudinal offset tolerance within $2\lambda_0$; transverse tolerance $\sim 0.5\lambda_0$.

---

**Phase 2: Synthesized SPARK-QA**

In a laser-driven plasma wakefield used for positron acceleration, the transverse field that a witness positron beam will experience is predicted from a simulation of the *bare* wake—one run without the beam present (an "unloaded" field map). A positron beam of density $n_+ = 0.5\, n_{e0}$ ($n_{e0}$ = ambient plasma density) is then injected into an accelerating bucket of this wake, and its focusing or defocusing is read off from the sign of the unloaded transverse field at the beam's location. Which of the following is the most fundamental limitation of using the unloaded field map to predict the focusing experienced by the *loaded* beam?

(A) As the drive laser propagates, relativistic self-focusing reshapes the pulse and therefore the wake's longitudinal profile, so a field map taken at one propagation distance no longer applies further downstream.

(B) The guiding plasma channel imposes a transverse density gradient that the bare-wake simulation does not reproduce, so the off-axis transverse field is mis-estimated across the beam's radial extent.

(C) The positron beam's own space charge draws plasma electrons toward the axis, adding on-axis negative charge that the unloaded map omits; this can convert a region that is defocusing for positrons in the bare wake into a focusing one.

(D) The transverse field varies strongly with longitudinal phase within a single bucket, so a map read at one slice of the bucket mis-predicts the field at the precise phase the beam occupies.

Figure 15: Dataset synthesis pipeline. Phase 1 details the extraction of a logically closed paper framework, structurally decoupling qualitative descriptions from quantitative observables. Phase 2 leverages this structured context to generate a self-contained, expert-level scientific reasoning question.

Table 9: API configuration for skeleton extraction and question generation.

| Configuration | Value |
|---|---|
| Model | DeepSeek-V4-Flash |
| Thinking | Enabled |
| Reasoning effort | High |

Table 10: Local model configuration for answer generation and skeleton-grounded quality checking.

| Configuration | Answer generation | Quality check |
|---|---|---|
| Model | Qwen3.5-27B | GPT-OSS-120B |
| Max new tokens | 32,768 | 16,384 |
| Max input tokens | 2048 | 32,768 |
| Temperature | 1.0 | 0.2 |
| Top-$p$ | 0.95 | 0.95 |
| Top-$k$ | 20 | 20 |
| Min-$p$ | 0.0 | 0.0 |
| Presence penalty | 1.5 | 1.5 |
| Repetition penalty | 1.0 | 1.0 |

Table 11: Summary of source-leakage pattern groups.

| Pattern group | Representative cues |
|---|---|
| Source-document references | "the paper", "the study", "the authors", "the article", "the passage", "this research" |
| Provided-context references | "provided text", "provided material", "provided information", "provided context", "according to the provided" |
| Internal evidence references | "supporting evidence", "supporting facts", "scientific context", "internal context", "internal scientific facts" |
| Text-reporting constructions | "the text states", "the text shows", "the text reports", "the text demonstrates", and related verb variants |
| Document-element references | "section $N$", "figure $N$", "table $N$", "reference $N$", "appendix $N$" |