Covariant Contrastive Learning for Uncertainty-Aware Anomaly Detection

Shelley Tong[1,2] **Gaia Grosso**[1,2] **Philip Harris**[1,2]
[1]Massachusetts Institute of Technology
[2]NSF AI Institute for Artificial Intelligence and Fundamental Interactions (IAIFI)
Cambridge, MA
{tshelley, gaiag795, pcharris}@mit.edu

Abstract

Machine learning (ML) based anomaly detection offers a promising, model-agnostic alternative to traditional analyses of LHC data, with supervised contrastive learning providing powerful low-dimensional neural embeddings of high-dimensional physics observables. However, the propagation of systematic uncertainties through learned representations remains poorly understood, severely limiting the application of these methods to real analyses. We address this gap with a likelihood-based regularization that fine-tunes the structure of contrastive latent spaces to covary predictably with systematic distortions, returning a model of such distortions that can be directly exploited in a downstream profile-likelihood test for anomaly detection. Using an emulated CMS Level-1 trigger data, we demonstrate that our method successfully captures the effect of jet momentum scale uncertainty via a linear latent model while retaining sensitivity across signal benchmarks, improving interpretability, robustness, and scalability of the anomaly detection task.

1 Introduction

The search for new physics at the Large Hadron Collider (LHC) increasingly involves *anomaly detection* (AD) strategies: signal-agnostic approaches that identify statistically significant deviations from a well-characterized Standard Model (SM) background without committing to a specific signal hypothesis ([1–5]). Supervised contrastive learning with physics process labels has shown remarkable success in producing organized neural embeddings for AD, achieving order-of-magnitude improvements in detection power over direct feature-space methods [6].

Despite this promise, deploying such methods in real LHC analyses faces a fundamental challenge: *systematic uncertainties*. Every physics measurement must account for imperfect detector calibration and theory modeling via nuisance parameters [7], yet the propagation of systematic distortions through ML algorithms is generally uncontrolled, making a calibrated downstream statistical test an open problem.

Systematic uncertainties fall into two broad categories. *Discrete* uncertainties, that are difficult to characterize, such as the choice of parton shower generator, can be handled with *invariance*: treating same-process events from different generator configurations as positive pairs in the contrastive loss makes the embedding insensitive to the generator choice [8]. *Continuous* uncertainties, parameterized by real-valued nuisance parameters ν such as jet energy scale or luminosity, instead require the latent space to *covary* with ν in a controlled way so that ν can be profiled.

This paper proposes a method to impose this covariance structure via a fine-tuning objective that organizes the latent space so that the effect of a systematic distortion on the log-density-ratio is linear

Conference on Physics and AI at Stanford University (PAI 2026).

in ν. The resulting space admits a simple, tractable parametric model of the systematic, enabling a likelihood-ratio AD test [9] at scale. Sections 2–5 cover related work, the method, experiments on CMS Level-1 trigger simulation, and conclusions.

2 Related work

Supervised contrastive embeddings for AD. [6, 10] established that supervised contrastive losses with physics process labels produce latent spaces well-suited for signal-agnostic AD at the LHC, with domain-knowledge-informed label encoding being the key ingredient for statistical discovery performance. That work did not address systematic uncertainties, which is the gap filled here.

Equivariant contrastive learning. [11] showed that augmenting invariance-based SSL with an auxiliary head that predicts the applied transformation—encouraging non-trivial *equivariance*— improves representation quality. We adapt this idea to the physics setting, replacing geometric transformations with systematic distortions parameterized by nuisance parameters.

AD in presence of systematic uncertainties. The "New Physics Learning Machine" [12, 13], extended in [9] to incorporate continuous systematics, provides the statistical backbone of this work. Related approaches to handle systematics uncertainties include parameterized classifiers [14] and uncertainty-aware training [15]; others approach the problem imposing invariance via adversarial decorrelation [16, 17]. Our contribution is to enable [9] to operate in the latent space of a contrastive encoder, by ensuring the background model there has a tractable linear dependence on ν.

3 Method

Our statistical analysis workflow combines three main steps: (1) building a compressed neural embedding with supervised contrastive learning; (2) modeling the effect of continuous systematic uncertainties in the embedded space via a likelihood-based regularization; and (3) performing a profile-likelihood statistical test for anomaly detection. We describe these steps in turn.

(1) Supervised contrastive learning for neural embedding. We train a transformer-based neural encoder $f_\theta : \mathbb{R}^d \to \mathbb{R}^k$ ($k \ll d$) using the supervised contrastive loss [18]:

$$\mathcal{L}_{\text{supCL}} = -\sum_i \frac{1}{|P(i)|} \sum_{p \in P(i)} \log \frac{e^{\mathbf{z}_i \cdot \mathbf{z}_p / \tau}}{\sum_{a \neq i} e^{\mathbf{z}_i \cdot \mathbf{z}_a / \tau}}, \tag{1}$$

where $\mathbf{z}_i = f_\theta(\mathbf{x}_i)/\|f_\theta(\mathbf{x}_i)\|$ is the ℓ_2-normalized embedding, $P(i)$ indexes events produced according to the same background physics process in the batch, and τ is a temperature hyperparameter. This organizes the latent space by background physics process (data and labels come from simulation), clustering SM events together and naturally isolating potential BSM anomalies.

(2) Systematic uncertainties as a covariance problem. A continuous systematic uncertainty is parameterized by a nuisance parameter ν that induces a deterministic distortion $\mathbf{x}(\nu_0) \mapsto \mathbf{x}(\nu)$ of the observables. After encoding, this produces a transformation of the latent distribution: $\mathbf{z}(\nu_0) \mapsto \mathbf{z}(\nu)$. Without structural constraints on f_θ, this transformation can be arbitrarily nonlinear in ν, making it intractable to construct a parametric model of the log-density-ratio $r(\mathbf{z}|\nu) = {n(\mathbf{z}|R_\nu)}/{n(\mathbf{z}|R_{\nu_0})}$ as required for the statistical test described at step (4).

We therefore propose to impose a *linear covariance* condition on the latent space: the encoder should be organized so that the log-density-ratio is linear in ν,

$$\log r(\mathbf{z}|\nu) = \log \frac{n(\mathbf{z}|R_\nu)}{n(\mathbf{z}|R_{\nu_0})} = g_\phi(\mathbf{z}) \cdot \nu, \tag{2}$$

where $g_\phi(\mathbf{z})$ is a function of the learned embedding only. Under this condition, ν is straightforwardly estimable via maximum likelihood directly in the latent space, making nuisance profiling tractable.

(3) Likelihood-based fine-tuning. We enforce the linear covariance condition (2) by fine-tuning the encoder jointly with a model g_ϕ of the log-density-ratio. We generate labeled pairs $(\mathbf{x}(\nu_0), \mathbf{x}(\nu))$ for a discrete grid of ν values spanning the expected uncertainty range $[-\sigma, +\sigma]$, and train g_ϕ as a parameterized classifier between the nominal and shifted distributions following [9]. Specifically, we

minimize the quadratics loss

$$\mathcal{L}_{\text{cov}} = -\frac{1}{N_\nu} \sum_\nu \left[\sum_{\mathbf{x} \sim R_\nu} \sigma(g_\phi(f_\theta(\mathbf{x})) \cdot \nu)^2 + \sum_{\mathbf{x} \sim R_{\nu_0}} [1 - \sigma(g_\phi(f_\theta(\mathbf{x})) \cdot \nu)]^2 \right], \qquad (3)$$

where σ denotes the sigmoid function and the sum runs over the grid of nuisance values. By the likelihood-ratio argument of [9], the minimizer of this loss satisfies $g_\phi(\mathbf{z}) \cdot \nu \rightarrow \log r(\mathbf{z}|\nu)$, so training g_ϕ directly implements the approximation in (2). The encoder and classifier are then jointly optimized with the combined objective $\mathcal{L} = \mathcal{L}_{\text{supCL}} + \alpha \mathcal{L}_{\text{cov}}$, where $\alpha > 0$ controls the relative weight of the two terms. Backpropagating through g_ϕ into f_θ incentivizes the encoder to concentrate the systematic effect into latent directions that are linearly aligned with ν, yielding a tractable and interpretable distortion model. After the joint optimization has converged the embedding is frozen and the linear model is further fine-tuned to reach higher levels of accuracy, requried for step (4).

(4) Statistical anomaly detection in the regulated latent space. The fine-tuned encoder and distortion model g_ϕ integrate directly into the profile-likelihood AD framework of [9]. Following that strategy, we compute the standard profile-likelihood ratio test

$$t(\mathcal{D}) = 2 \log \frac{\max_{\nu, \zeta} \left[\mathcal{L}(H_{\nu,\zeta} \,|\, \mathcal{D}) \cdot \mathcal{L}_{\text{aux}}(\nu) \right]}{\max_{\nu'} \left[\mathcal{L}(R_{\nu'} \,|\, \mathcal{D}) \cdot \mathcal{L}_{\text{aux}}(\nu') \right]}, \qquad (4)$$

where $\mathcal{L}_{\text{aux}}(\nu)$ is an auxiliary Gaussian likelihood term constraining the nuisance parameter. The reference SM hypothesis, R_ν, is modeled according to Eq. 2: $n(x|R_\nu) = n(x|R_{\nu_0}) \cdot e^{g_\phi(\mathbf{z}) \cdot \nu}$. The alternative hypothesis $H_{\nu,w}$ is modeled with an additional neural network h_ζ $n(x|H_{\nu,\zeta}) = n(x|R_{\nu_0}) \cdot e^{g_\phi(\mathbf{z}) \cdot \nu + h_\zeta(\mathbf{z})}$.

4 Application

Dataset. We validate the method on simulated CMS Level-1 trigger data [19] available on Zenodo [20–24]. Each event is represented by up to 19 reconstructed objects: 4 electrons/photons, 4 muons, 10 jets, and one missing transverse energy (MET) slot. Each object is described by (p_T, η, ϕ), yielding 57 input features per event, with zero padding applied when fewer objects are present. The background sample consists of W (59.2%), QCD multijet (33.8%), Z (6.7%), and $t\bar{t}$ (0.3%) events, while the signal benchmarks are $\text{LQ} \rightarrow b\tau$, $A \rightarrow 4\ell$, $h^0 \rightarrow \tau\tau$, and $h^\pm \rightarrow \tau^\pm \nu$. To model systematic effects, we introduce a nuisance parameter ν that rescales the jet transverse momentum as $p_T(\nu) = e^\nu p_T(0)$, with nominal value $\nu_0 = 0$, and we set the standard uncertainty $\sigma = 2.5\%$, a typical percent-level size of jet energy scale uncertainties in LHC analyses [25].

Embedding Model. Following Ref. [6], we use a Transformer-based model to map 57-dimensional input into a 4-dimensional embedding, which gave the strongest AD performance among the tested dimensions. We leave the systematic study of nuisance uncertainty in higher dimensional embeddings to future work. Nominal SM background events are used for the contrastive task with physics labels. The model is trained in a 5-fold co-training setup with a linear model (2.1×10^6 events per fold per ν dataset, 60 epochs, batch size 1024, learning rate 2×10^{-6}). Although co-training takes longer than standard contrastive training, it is only trained once and frozen in NPLM tests. The covariance loss plateaus in training, while linear nuisance model benefits from longer fine-tuning.

Linear Model. We co-train a downstream linear model on the learned embeddings. The model is implemented as a fully connected network with architecture $(4, 512, 256, 128, 64, 32, 1)$, ReLU activations in the hidden layers, and a linear output. It is trained jointly with the supervised contrastive embedding model using a learning rate of 2×10^{-6}, L_2 regularization of 10^{-6}, and co-training regularization $\alpha = 0.1$, then further fine-tuned on 1.6×10^6 events per nuisance parameter. Both nominal and nuisance-shifted samples at $\pm 1\sigma$ and $\pm 2\sigma$ are used for this task.

NPLM Model. h_ζ is implemented as a fully connected neural network with architecture $(4, 4, 4, 1)$ (45 trainable parameters), sigmoid activation in the hidden layers and linear output. As in [13], a weight clipping regularizer is tuned using 50 pseudo-experiments drawn from the nominal reference sample R_0 to produce an empirical test statistic distribution matching a χ^2_{45}. We train using 52,000 reference events and 10,000 background events (D) per replica. The optimal weight clipping is 1.96.

NPLM Validation Tests. We validate the calibrated model on nuisance-shifted SM samples $D \sim R_\nu$ using the same event counts. The feature-wise comparison between the nuisance-shifted samples and

the fitted nuisance model is shown in Figure 1. We validate the nuisance dependence of the embedding distributions by comparing the $\nu = \pm 1\sigma$ and nominal R_0 background-only distributions using a KS test. We use 200 replicas per ν value. As shown in Table 1, all p-values are greater than 0.5, indicating good agreement. This shows that the linear nuisance model captures the nuisance-induced deformation of the embedding space, rather than misidentifying it as new-physics-like structure.

Signal Injection. We assess the sensitivity of the method by injecting a 1% signal component (100 events) into the SM background sample and testing for departures from the null expectation. We compute the resulting z-score with respect to the empirical test-statistic distribution under R_0, estimated from 200 replica. A large deviation from the null indicates excess structure not accounted for by systematic effects alone, consistent with a detectable new-physics-like signal. The resulting z-scores for each injected signal benchmark are summarized in Table 1. The sensitivity of the test is independent of the ν setting.

Compute Resources. Embedding models were trained on 48 GB GPU, with a typical training time of 4 hours 45 minutes. Linear-model fine-tuning was performed on 48 GB GPU, with a typical training time of 3 hours. The NPLM model was trained on CPUs, with a typical training time of 50 minutes.

Code Availability. The code and detailed documentation to reproduce the experiments can be found at `https://github.com/tshelley200/cl4ad_uncertainty`.

5 Conclusion

We introduced a method to impose linear covariance of continuous systematic uncertainties in contrastive latent spaces, enabling rigorous profile-likelihood anomaly detection at the LHC. By fine-tuning the encoder with an auxiliary objective that enforces the log-density-ratio to be linear in the nuisance parameter, the method integrates directly with the AD framework of [9], yielding a scalable and statistically well-founded workflow for anomaly detection in the presence of continuous systematics. Future work will extend the method to multiple simultaneous nuisance parameters, bringing contrastive AD pipelines closer to deployment in full-scale analyses.

Figure 1: **Validation of the linear nuisance model in the latent space.** Top: feature distributions for the reference sample at $\nu = 0$ (gray fill), nuisance-shifted test samples (solid lines), and fitted model predictions at $\nu = \pm 1\sigma$ (dash-dotted lines). Middle: corresponding $\log(N_\nu/N_0)$ ratios. Bottom: ratios of fitted model to test sample, $N_\nu^{\text{fit}}/N_\nu^{\text{test}}$.

Nuisance setting	KS p-value	z-score for injected signal benchmark			
		$LQ \to b\tau$	$A \to 4\ell$	$h^0 \to \tau\tau$	$h^\pm \to \tau^\pm \nu$
$\nu = 0$	—	$1.31^{+0.29}_{-0.23}$	≥ 2.58	$0.68^{+0.21}_{-0.18}$	≥ 2.58
$\nu = +0.025$	$0.79^{+0.1}_{-0.01}$	$1.26^{+0.28}_{-0.22}$	≥ 2.58	$0.68^{+0.21}_{-0.18}$	≥ 2.58
$\nu = -0.025$	$0.79^{+0.1}_{-0.01}$	$1.26^{+0.28}_{-0.22}$	≥ 2.58	$0.57^{+0.20}_{-0.18}$	≥ 2.58

Table 1: **Validation and signal-injection results.** The second column gives the KS-test p-value for the SM-only validation test, comparing the empirical test-statistic distribution at $\nu = \pm 1\sigma$ to the $\nu = 0$ background-only reference. The remaining columns give the median observed z-scores for each injected signal benchmark. Errors represent the Clopper-Pearson 68% confidence intervals.

References

[1] Vladimir Chekhovsky et al. Model-agnostic search for dijet resonances with anomalous jet substructure in proton–proton collisions at $\sqrt{s} = 13$ TeV. *Rept. Prog. Phys.*, 88(6):067802, 2025. doi: 10.1088/1361-6633/add762.

[2] Aram Hayrapetyan et al. Machine-learning techniques for model-independent searches in dijet final states. 12 2025. doi: 10.5281/zenodo.16656501.

[3] Georges Aad et al. Dijet resonance search with weak supervision using $\sqrt{s} = 13$ TeV pp collisions in the ATLAS detector. *Phys. Rev. Lett.*, 125(13):131801, 2020. doi: 10.1103/PhysRevLett.125.131801.

[4] Georges Aad et al. Weakly supervised anomaly detection for resonant new physics in the dijet final state using proton-proton collisions at s=13 TeV with the ATLAS detector. *Phys. Rev. D*, 112(7):072009, 2025. doi: 10.1103/2yq5-vj59.

[5] Georges Aad et al. Anomaly detection search for new resonances decaying into a Higgs boson and a generic new particle X in hadronic final states using $\sqrt{s} = 13$ TeV pp collisions with the ATLAS detector. *Phys. Rev. D*, 108:052009, 2023. doi: 10.1103/PhysRevD.108.052009.

[6] Kyle Metzger, Lana Xu, Mia Sodini, Thea K. Arrestad, Katya Govorkova, Gaia Grosso, and Philip Harris. Anomaly-preserving contrastive neural embeddings for end-to-end model-independent searches at the LHC. *Phys. Rev. D*, 112(7):072011, 2025. doi: 10.1103/5n77-ynsp.

[7] Glen Cowan, Kyle Cranmer, Eilam Gross, and Ofer Vitells. Asymptotic formulae for likelihood-based tests of new physics. *Eur. Phys. J. C*, 71:1554, 2011. doi: 10.1140/epjc/s10052-011-1554-0. [Erratum: Eur.Phys.J.C 73, 2501 (2013)].

[8] Philip Harris, Michael Kagan, Jeffrey Krupa, Benedikt Maier, and Nathaniel Woodward. Re-Simulation-based Self-Supervised Learning for Pre-Training Foundation Models. 3 2024.

[9] Raffaele Tito D'Agnolo, Gaia Grosso, Maurizio Pierini, Andrea Wulzer, and Marco Zanetti. Learning new physics from an imperfect machine. *Eur. Phys. J. C*, 82(3):275, 2022. doi: 10.1140/epjc/s10052-022-10226-y.

[10] Samuel Bright-Thonney, Christina Reissel, Gaia Grosso, Nathaniel Woodward, Katya Govorkova, Andrzej Novak, Sang Eon Park, Eric Moreno, and Philip Harris. Autoscidact: Automated scientific discovery through contrastive embedding and hypothesis testing. *arXiv preprint arXiv:2510.21935*, 2025.

[11] Rumen Dangovski, Li Jing, Charlotte Loh, Seungwook Han, Akash Srivastava, Brian Cheung, Pulkit Agrawal, and Marin Soljačić. Equivariant contrastive learning. *arXiv preprint arXiv:2111.00899*, 2021.

[12] Raffaele Tito D'Agnolo and Andrea Wulzer. Learning new physics from a machine. *Physical Review D*, 99(1):015014, 2019.

[13] Raffaele Tito D'Agnolo, Gaia Grosso, Maurizio Pierini, Andrea Wulzer, and Marco Zanetti. Learning multivariate new physics. *Eur. Phys. J. C*, 81(1):89, 2021. doi: 10.1140/epjc/s10052-021-08853-y.

[14] Pierre Baldi, Kyle Cranmer, Taylor Faucett, Peter Sadowski, and Daniel Whiteson. Parameterized neural networks for high-energy physics. *The European Physical Journal C*, 76(5):235, 2016.

[15] Pablo De Castro and Tommaso Dorigo. Inferno: inference-aware neural optimisation. *Computer Physics Communications*, 244:170–179, 2019.

[16] Gilles Louppe, Michael Kagan, and Kyle Cranmer. Learning to pivot with adversarial networks. *Advances in neural information processing systems*, 30, 2017.

[17] Gregor Kasieczka and David Shih. Disco fever: Robust networks through distance correlation. *arXiv preprint arXiv:2001.05310*, 2020.

[18] Prannay Khosla, Piotr Teterwak, Chen Wang, Aaron Sarna, Yonglong Tian, Phillip Isola, Aaron Maschinot, Ce Liu, and Dilip Krishnan. Supervised contrastive learning. *Advances in neural information processing systems*, 33:18661–18673, 2020.

[19] Ekaterina Govorkova, Ema Puljak, Thea Aarrestad, Maurizio Pierini, Kinga Anna Woźniak, and Jennifer Ngadiuba. Lhc physics dataset for unsupervised new physics detection at 40 mhz. *Scientific Data*, 9(1):118, 2022.

[20] Thea Aarrestad, Ekaterina Govorkova, Jennifer Ngadiuba, Ema Puljak, Maurizio Pierini, and Kinga Anna Wozniak. Unsupervised new physics detection at 40 mhz: Training dataset, June 2021. URL `https://doi.org/10.5281/zenodo.5046389`.

[21] Thea Aarrestad, Ekaterina Govorkova, Jennifer Ngadiuba, Ema Puljak, Maurizio Pierini, and Kinga Anna Wozniak. Unsupervised new physics detection at 40 mhz: A -> 4 leptons signal benchmark dataset, June 2021. URL `https://doi.org/10.5281/zenodo.5046446`.

[22] Thea Aarrestad, Ekaterina Govorkova, Jennifer Ngadiuba, Ema Puljak, Maurizio Pierini, and Kinga Anna Wozniak. Unsupervised new physics detection at 40 mhz: Lq -> b tau signal benchmark dataset, July 2021. URL `https://doi.org/10.5281/zenodo.5055454`.

[23] Thea Aarrestad, Ekaterina Govorkova, Jennifer Ngadiuba, Ema Puljak, Maurizio Pierini, and Kinga Anna Wozniak. Unsupervised new physics detection at 40 mhz: h0 -> tau tau signal benchmark dataset, July 2021. URL `https://doi.org/10.5281/zenodo.5061633`.

[24] Thea Aarrestad, Ekaterina Govorkova, Jennifer Ngadiuba, Ema Puljak, Maurizio Pierini, and Kinga Anna Wozniak. Unsupervised new physics detection at 40 mhz: h+ -> tau nu signal benchmark dataset, July 2021. URL `https://doi.org/10.5281/zenodo.5061688`.

[25] ATLAS Collaboration. A precise measurement of the jet energy scale derived from single-particle measurements and in situ techniques in proton-proton collisions at 13 TeV with the ATLAS detector. 2024.