Tensor-Decomposed RNNs for Marked Temporal Point Processes

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Paper under double-blind review

Abstract

We study parameter-efficient neural Marked Temporal Point Processes (MTPPs) for high-dimensional mark and exogenous feature spaces. Building on tensor-train (TT) factorization of recurrent kernels, we propose *mark-aware TT shaping* that aligns TT cores with known multi-way domain structure (e.g., asset/venue/side in finance). We provide a conditional intensity function-consistent training recipe and evaluate both accuracy and calibration (mark reliability and time-rescaling diagnostics). Across finance and public MTPP benchmarks, TT-compressed RNNs reduce parameters by 40–70% while matching dense baselines and remaining competitive with attention-based and state-space models; TT often improves calibration, and simple ensembling further strengthens reliability.

1 Introduction

Modeling high-frequency event streams with multiple types (or *marks*) is a central problem in application-driven machine learning, especially in domains such as financial markets, image and video processing, and social network analysis (Du et al., 2015; Xu & Zha, 2017; Schein et al., 2015). In the financial domain, for instance, practitioners often track requests for quotes (RFQs), limit-order book events, or trades in a continuous-time framework where arrival patterns are inherently interdependent. These applications demand not only accurate short-term forecasting but also robust cross-excitation effects among event types.

A Marked Temporal Point Process (MTPP) (Daley & Vere-Jones, 2003) can explicitly capture how each event's arrival influences future arrivals of multiple types. These Marked Temporal Point Processes (MTPPs) are well-suited to modeling sequences of events in continuous time, where each event has both a time and a mark (type). In settings such as financial markets, high-frequency limit-order books, or requests for quotes (RFQs), capturing cross-excitation among multiple event types is essential (Boyd et al., 2020; Du et al., 2016; Bhattacharjya et al., 2018). Neural variants of MTPPs extend classic self-exciting processes by encoding history in a hidden state of a recurrent neural network (RNN), but in high-dimensional settings the input-to-hidden and hidden-to-hidden maps can dominate the parameter budget and memory footprint (Tjandra et al., 2017; Yang et al., 2017). Specifically, these neural approaches incorporate RNNs to encode the event history (x_t, h_t) in a hidden state, from which the conditional intensity function $\lambda_x(t)$ can be parameterized (Zhang et al., 2020; Türkmen et al., 2020). *Tensor-train decomposition* (Oseledets, 2011) offers an elegant way to reduce the parameter count by factorizing large weight matrices into products of smaller core tensors.

Contributions. Our contribution is intentionally design- and empirics-focused: a practical blueprint for building *parameter-efficient, calibrated* neural MTPPs in high-dimensional settings. We propose mark-aware TT shaping (Table 1) and couple TT-compressed RNN backbones to conditional intensities with a likelihood-consistent training recipe (Sec. 4). We then evaluate accuracy, efficiency, and calibration across finance and public benchmarks, including ablations against alternative tensorizations (Sec. 7).

Why TT for RNN-based MTPPs (and not only Transformers)? RNN-based neural point processes remain a standard continuous-time modeling approach (Du et al., 2016; Mei & Eisner, 2017) with a clean intensity-based likelihood and time-rescaling diagnostics. TT can be inserted into this pipeline by replacing

only the large linear maps inside the sequence model, keeping the conditional intensity and loss unchanged (Sec. 4). We additionally compare against strong attention and state-space baselines (THP/SAHP and S4/Mamba; Sec. 7); applying TT to Transformer layers is an appealing extension, but is orthogonal to our goal of isolating how tensor compression affects efficiency and calibration in continuous-time MTPPs.

Paper Organization. We first review related work in Section 2. We then review MTPPs and RNN memory in Sections 3–4. Section 5 presents the tensor-train decomposition and how it replaces large dense transformations in an RNN cell. Next, we present experimental results in Sections 6–7, including ablations. Finally, in Section 8, we summarize insights and discuss future directions.

2 Related Work

Marked Temporal Point Processes. Classical self-exciting processes (e.g., Hawkes processes (Hawkes, 1971; Ogata, 1988)) have a long history in finance, biological processes and social sciences (Bacry et al., 2015; Hawkes, 2022; Laub et al., 2015). They capture how past events raise or dampen future intensities. Extending Hawkes to neural architectures has led to advanced MTPP models that encode the event history with recurrent (Du et al., 2016; Mei & Eisner, 2017) or attention-based mechanisms (Zuo et al., 2020; Zhang et al., 2020). Our work follows this RNN-based lineage but differs by applying tensor decomposition to manage high input dimension. State-space models (SSMs) have also found recent success as alternatives to RNNs and transformers, offering efficient linear-time training and inference (Gao et al., 2024; Chang et al., 2024).

TT-compressed RNNs. Low-rank tensor approximations (CP decomposition, Tucker, tensor-train) reduce parameters in large weight matrices (Oseledets, 2011). Prior work compresses input and recurrent matrices via tensor-train and related decompositions for speech/video and sequence tasks (Novikov et al., 2015; Tjandra et al., 2017; Yang et al., 2017), and for finance forecasting (Xu et al., 2021). We differ by mark-aware TT shaping for multi-way MTPP inputs, explicit RNN-to-intensity linkage and calibration diagnostics within a point-process framework, and systematic comparisons to modern attention and state-space baselines (Zuo et al., 2020; Zhang et al., 2020; Gu et al., 2021; Gu & Dao, 2023). We also benchmark TT against tensor ring and Tucker/CP variants to isolate design trade-offs (Pan et al., 2019).

Reinforcement Learning (RL) Approaches. By formulating different objectives, RL allows for bypassing the computational issues related to evaluating the integral in the MTTP likelihood (Li et al., 2018; Upadhyay et al., 2018; Zhu et al., 2019).

Applications in Finance. In real-world financial data, events arrive at irregular intervals, and multiple instrument types or currency pairs may interact (Bacry et al., 2015; Laub et al., 2015). Neural MTPPs can capture such cross-asset excitation but at the expense of parameter blow-up when the dimensionality of marks or engineered features is large. Traditional domain-specific solutions (e.g., parametric Hawkes with carefully chosen kernels or GARCH-like processes for volatility become unwieldy when the number of event types grows (Engle, 2000)). We bridge these approaches by providing a flexible RNN-based MTPP that remains computationally feasible even for dozens of assets or features, thanks to TT-based compression.

Non-ML and Baseline Approaches. Outside the ML literature, many financial firms rely on simpler methods, such as moving averages or partially parametric hazard functions, to forecast demand or trade arrivals. While these can be effective in narrow domains, they lack the adaptive memory of modern RNN-based MTPPs. Hence, we also compare to baseline ML methods (dense RNN) and discuss performance trade-offs to highlight the value of TT-based compression for large-scale real-world settings.

3 Background on Marked Temporal Point Processes

We model an event stream on $[0, T]$ as a sequence $\mathcal{D} = \{(t_i, x_i)\}_{i=1}^{N}$ with strictly increasing times $0 < t_1 < \cdots < t_N \leq T$ and marks $x_i \in \{1, \ldots, K\}$. Let $\mathcal{H}_t = \{(t_j, x_j) : t_j < t\}$ denote the history up to t. A marked

temporal point process (MTPP) is characterized by mark–specific conditional intensities

$$\lambda_k(t \mid \mathcal{H}_t)\, dt \;=\; \Pr\{\text{event of type } k \text{ in } [t, t+dt) \mid \mathcal{H}_t\}, \quad k = 1, \ldots, K. \tag{1}$$

with total intensity $\lambda(t \mid \mathcal{H}_t) = \sum_{k=1}^{K} \lambda_k(t \mid \mathcal{H}_t)$. Given $\mathcal{H}_{t_i}$, the joint density of the next event's time t_{i+1} and mark x_{i+1} has the hazard–survival form:

$$f(t_{i+1}, x_{i+1} \mid \mathcal{H}_{t_i}) \;=\; \lambda_{x_{i+1}}(t_{i+1} \mid \mathcal{H}_{t_{i+1}}) \times \exp\Big(-\int_{t_i}^{t_{i+1}} \lambda(s \mid \mathcal{H}_s)\, ds \Big). \tag{2}$$

Equivalently, this factorizes into a time component and a (potentially time–dependent) mark distribution:

$$f(t_{i+1} \mid \mathcal{H}_{t_i}) = \lambda(t_{i+1} \mid \mathcal{H}_{t_{i+1}}) \times \exp\Big(-\int_{t_i}^{t_{i+1}} \lambda(s \mid \mathcal{H}_s)\, ds \Big), \tag{3}$$

$$p(x_{i+1} = k \mid t_{i+1}, \mathcal{H}_{t_{i+1}}) = \frac{\lambda_k(t_{i+1} \mid \mathcal{H}_{t_{i+1}})}{\lambda(t_{i+1} \mid \mathcal{H}_{t_{i+1}})}. \tag{4}$$

For a realized sequence $\mathcal{D}$, the (negative) log-likelihood (NLL) on $[0, T]$ is

$$\mathcal{L}_{\text{TPP}}(\theta) \;=\; -\sum_{i=1}^{N} \log \lambda_{x_i}(t_i \mid \mathcal{H}_{t_i}) \;+\; \int_0^T \lambda(s \mid \mathcal{H}_s)\, ds. \tag{5}$$

4 RNN Modeling of Event Sequences → Conditional Intensity

Hidden-state dynamics. Let $h_i \in \mathbb{R}^H$ summarize history at the i-th event time t_i. We update only at event times:

$$h_i \;=\; \text{RNN}_\theta\big(h_{i-1},\, \phi(x_i),\, \psi(z_i),\, \varphi(\Delta t_i)\big), \qquad \Delta t_i = t_i - t_{i-1}. \tag{6}$$

where $\phi(\cdot)$ encodes the mark, z_i denotes optional exogenous features, and $\varphi(\Delta t)$ is a time embedding (e.g., Fourier or radial basis). We replace all dense linear maps in RNN_θ (input and recurrent) by TT-layers, keeping the conditional intensity and the likelihood unchanged (Section 5).

Two-head parameterization of the MTPP. Conditioned on h_i and the elapsed time $\tau = t - t_i$, we parameterize:

(mark head)

$$\eta(h_i) \in \mathbb{R}^K, \qquad \pi_k(\tau, h_i) = \text{softmax}_k\big(\eta(h_i) + a_k\, \tau\big), \tag{7}$$

(time head)

$$\lambda(\tau, h_i) = \text{softplus}\Big(w_\lambda^\top [\, h_i;\, \phi_\tau(\tau)\,] + b_\lambda \Big). \tag{8}$$

giving mark–specific intensities $\lambda_k(t \mid \mathcal{H}_t) = \lambda(\tau, h_i) \cdot \pi_k(\tau, h_i)$, so Eqs. 2–5 apply. We adopt either an RMTPP-style closed form for λ or a general neural hazard integrated by Gauss–Legendre quadrature (Du et al., 2016; Mei & Eisner, 2017).

From hidden state to likelihood. With $\lambda_k(\cdot)$ defined, the sequence NLL is

$$\mathcal{L}_{\text{TPP}}(\theta) = -\sum_{i=1}^{N} \log \lambda_{x_i}(t_i \mid \mathcal{H}_{t_i}) + \int_0^T \lambda(s \mid \mathcal{H}_s)\, ds. \tag{9}$$

Under the decomposition $\lambda_k = \lambda \cdot \pi_k$, Eq. 9 splits into a time term and a mark term:

$$\begin{aligned} \mathcal{L}_{\text{TPP}} = & -\sum_{i=1}^{N} \log \lambda(t_i \mid \mathcal{H}_{t_i}) \; + \; \int_0^T \lambda(s \mid \mathcal{H}_s)\, ds \\ & - \sum_{i=1}^{N} \log \pi_{x_i}(t_i \mid \mathcal{H}_{t_i}) \end{aligned} \tag{10}$$

which enables separate calibration analysis of marks and times.

Time-rescaling theorem and PIT diagnostics. Define rescaled increments $w_i = \int_{t_{i-1}}^{t_i} \lambda(s \mid \mathcal{H}_s)\, ds$. Under a correctly specified model, $\{w_i\}$ are i.i.d. Exp(1); equivalently, $u_i = 1 - e^{-w_i}$ are i.i.d. Uniform$(0, 1)$ (Ogata, 1988). We evaluate goodness-of-fit using PIT histograms and a one-sample KS test (Brown et al., 2002).

Theorem 4.1 (Time-rescaling)**.** *Let $\{(t_i, x_i)\}$ be generated by an MTPP with (total) CIF $\lambda(t \mid \mathcal{H}_t)$. Then $w_i = \int_{t_{i-1}}^{t_i} \lambda(s \mid \mathcal{H}_s)\, ds$ are i.i.d.* Exp(1)*. Consequently $u_i = 1 - \exp(-w_i)$ are i.i.d.* Uniform$(0, 1)$*.*

From TT-RNN to calibrated MTPP. Our design uses TT to compress only the linear maps inside the RNN (input and recurrent), leaving the continuous-time head (Eqs. 7–8) and the likelihood (Eq. 9) unchanged. This separation lets us retain neural MTPP flexibility, measure efficiency via parameter counts and wall-clock, and evaluate calibration with time-rescaling and mark reliability.

5 Tensor-Train Decomposition for RNN Kernels

When the feature dimension is large, the RNN's weight matrices (W_{ih} from inputs to hidden, and W_{hh} from hidden to hidden) can dominate the parameter budget. A tensor-train factorization (TT) replaces each large matrix with products of smaller core tensors (Oseledets, 2011).

5.1 Definition

Let $A \in \mathbb{R}^{M \times N}$ be a weight matrix with $M = \prod_{k=1}^{d} p_k$ and $N = \prod_{k=1}^{d} q_k$. We reshape row and column indices into multi-indices:

$$\begin{aligned} i &\leftrightarrow (i_1, \ldots, i_d), \quad i_k \in \{1, \ldots, p_k\}, \\ j &\leftrightarrow (j_1, \ldots, j_d), \quad j_k \in \{1, \ldots, q_k\}. \end{aligned}$$

A TT factorization represents A as a contraction of cores $\{G_k\}_{k=1}^{d}$ with $G_k \in \mathbb{R}^{p_k \times q_k \times r_{k-1} \times r_k}$ and ranks $r_0 = r_d = 1$:

$$A_{ij} \;=\; \sum_{\alpha_1=1}^{r_1} \cdots \sum_{\alpha_{d-1}=1}^{r_{d-1}} \prod_{k=1}^{d} G_k[i_k, j_k, \alpha_{k-1}, \alpha_k].$$

5.2 TT-based RNN Cell

To incorporate TT factorization, we reshape x_t into $(B, p_1, p_2, \ldots)$, learn TT cores $\{G_k\}$, and replace dense maps by TT layers that contract across the cores. Likewise for the recurrent transformation on h_{t-1}. Algorithm 1 summarizes a TT layer's forward pass.

Mark-aware TT shaping. Many MTPP settings admit a natural grouping of marks and exogenous features. We exploit this structure by reshaping the input dimension M into a product of factors before applying TT, and by ordering TT cores so that adjacent cores align with semantically coupled groups. Table 1 summarizes the reshapes used in our experiments.

Algorithm 1 Forward Pass of a TT Layer (schematic)

Input: reshaped input $\mathbf{x} \in \mathbb{R}^{(B,p_1,\ldots,p_d)}$, TT-cores $\{G_1, \ldots, G_d\}$, optional bias $\mathbf{b}$
Output: transformed $\mathbf{y}$
Initialize $\mathbf{c} := \textsc{contract}(G_1, \mathbf{x})$
for $k = 2$ to d **do**
  $\mathbf{c} \leftarrow \mathbf{c} \times \textsc{contract}(G_k, \mathbf{x})$
end for
if bias: $\mathbf{c} \leftarrow \mathbf{c} + \mathbf{b}$
$\mathbf{y} \leftarrow \sigma(\mathbf{c})$
return y

Table 1: Mark-aware TT factor shapes (examples).

Dataset	Input reshape $M = \prod m_g$	Notes
LOBSTER	$m_{\text{asset}} \times m_{\text{venue}} \times m_{\text{side}} \times m_{\text{rest}}$	couple asset–venue cores
FX RFQ	$m_{\text{pair}} \times m_{\text{calendar}} \times m_{\text{rest}}$	keep calendar core small
StackOverflow	$m_{\text{family}} \times m_{\text{subtype}} \times m_{\text{rest}}$	22 marks $\rightarrow$ families
MIMIC	$m_{\text{system}} \times m_{\text{code}} \times m_{\text{rest}}$	CCS/ICD-style groupings

Parameter and FLOP accounting. For a TT layer replacing a matrix $W \in \mathbb{R}^{M \times D}$ (with $M = \prod p_k$ and $D = \prod q_k$), the parameter count is $\sum_k p_k q_k r_{k-1} r_k$ (plus bias). For a single-layer dense LSTM with input size M and hidden size H, the core parameter count is $4H(M + H) + 4H$.

6 Datasets and Baselines

Scope. We evaluate on (i) the *finance* settings from LOBSTER intraday events and daily FX RFQ and (ii) three *public MTPP benchmarks* commonly used by attention-based and neural MTPP models.

6.1 Datasets

Finance. *LOBSTER* (intraday limit-order book events; millisecond timestamps; engineered state features) (Humboldt, 2025). Proprietary *FX RFQ* (daily RFQ logs with calendar/economic features).

Public MTPP benchmarks. *StackOverflow Badges* (22 marks; developer event streams) (Du et al., 2016). *Retweet/MemeTracker Cascades* (social diffusion) (Zuo et al., 2020). *MIMIC Events* (clinical codes; irregular visits) (Du et al., 2016). We use the standard splits from the respective papers; where not specified, we follow THP/SAHP practice Zuo et al. (2020); Zhang et al. (2020).

The dataset and baseline configurations are summarized in Tables 2–3, respectively. Additionally, the experimental pipeline is summarized in Figure 1.

Parameter counting and TT shapes. All parameter counts reported in Tables 3–5 include the sequence model (dense or TT-compressed), the mark/time heads used to parameterize the conditional intensity, and bias terms. For TT-LSTM, we reshape the input into semantically meaningful factors and order TT cores so that adjacent cores align with coupled groups (Table 1); we then tune only the TT rank in the main comparisons. While TT contraction is sequential over the number of cores, in practice we use small d (typically 3–4), and the observed wall-clock improvements are therefore primarily limited by general-purpose deep learning kernels rather than TT arithmetic.

6.2 Training and Evaluation Protocol

We train with the MTPP NLL (Eq. 9), using closed-form integrals (RMTPP) or 4–8 node Gauss–Legendre quadrature for $\int \lambda$ under the general hazard. We report averages over $s = \{5, 10\}$ seeds with 95% confidence

Table 2: Datasets, horizons, marks, and splits. Finance datasets bring higher-dimensional marks/features; public MTPP benchmarks enable comparisons to attention and SSM baselines. Median events/sequence govern sequence length (128 for event data; 30 for FX days) used in training protocol.

Dataset	#Seq	Horizon	#Marks	Events (median)	Train/Val/Test	Notes
LOBSTER	9,600	intraday	8	120	6,720 / 1,440 / 1,440	engineered features (12–18)
FX RFQ	1,200	daily	6	5	840 / 180 / 180	calendar + macro features
StackOverflow	6,500	irregular	22	15	4,550 / 975 / 975	standard split from prior work
Retweet/MemeTracker	4,800	irregular	10	18	3,360 / 720 / 720	cascade benchmark
MIMIC (clinical)	5,400	irregular	32	22	3,780 / 810 / 810	cohort/preprocessing details

Table 3: Model capacities and training settings. TT-LSTM uses ranks $r \in \{2, 4, 6\}$ and mark-aware factor shapes; attention models use 4 heads; S4/Mamba operate on discretized counts with $B \in \{50, 100, 200\}$. Wall-clock is measured at batch size 64 and sequence length 128 (30 for FX).

Model	Hidden	Layers	Params	TT-rank/Heads	Opt/BS/Epochs	Notes
Dense LSTM	128	1	620k	–	Adam/64/100	baseline
TT-LSTM	128	1	280k (r=4)	$r \in \{2, 4, 6\}$	Adam/64/100	mark-aware factor shapes
RMTPP/NHP	128	1	590k	–	Adam/64/100	continuous-time loss
SAHP	128	2	710k	4 heads	Adam/64/120	attention
THP	128	2	780k	4 heads	Adam/64/120	attention
S4/Mamba	256	1	430k	$B \in \{50, 100, 200\}$	Adam/64/100	discretized counts

intervals. For state-space models (SSMs), we report bin sensitivity across B. For calibration, we evaluate mark reliability via expected calibration error (ECE; 10/20/50 bins) with and without temperature scaling, and time calibration via time-rescaling (PIT histograms and KS p-values). Wall-clock includes forward and backward passes at batch size 64; sequence length is 128 events for event data and 30 days for FX sequences.

7 Results

7.1 Main accuracy/likelihood results

Finance. TT-LSTM matches or exceeds dense LSTM while reducing parameters by 40–70%. Attention-based and state-space model baselines provide useful reference points; TT remains competitive in NLL under high-dimensional marks (Table 4).

Public MTPP benchmarks. On StackOverflow/Retweet/MIMIC, TT-LSTM remains competitive with attention-based and state-space models while being substantially smaller; differences depend on dataset scale and mark entropy (Table 5).

7.2 Calibration and Uncertainty

Setup. We assess mark calibration using expected calibration error (ECE; 10/20/50 bins) and reliability diagrams, with a single temperature fit on validation and evaluated on test. We assess time calibration using time-rescaling: we compute rescaled increments $w_i = \int_{t_{i-1}}^{t_i} \lambda(s)\, ds$, map them to PIT values $u_i = 1 - e^{-w_i}$, and report KS p-values against $U(0, 1)$. For uncertainty, we report deep ensembles ($n \in \{3, 5\}$) or MC-dropout, along with NLL, sharpness (average prediction interval width), and 90% coverage.

Mark calibration. Table 6 shows that TT compression improves mark reliability out of the box and pairs well with post-hoc calibration. Averaged across datasets, ECE@20 drops from 0.071 (Dense LSTM) to 0.061 for *TT-LSTM (r=4)* while using $\sim 55\%$ fewer parameters; SAHP/THP are competitive but no better pre-temperature. A single scalar temperature (fit on validation) further reduces TT's ECE@20 to 0.031 (Dense to 0.036). Figure 2 visualizes this trend: TT reduces overconfidence relative to Dense, and temperature scaling largely removes residual miscalibration (curves near the diagonal).

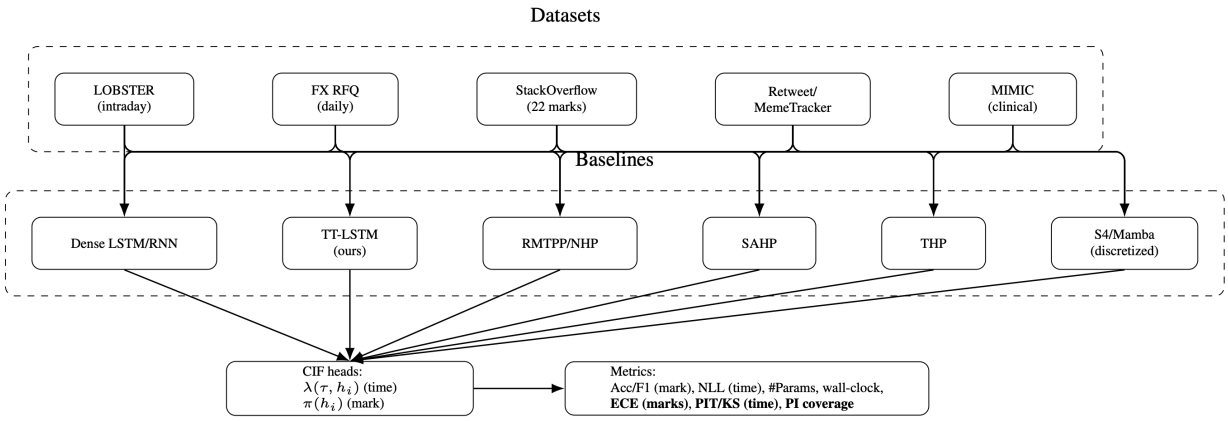

Figure 1: End-to-end pipeline: five datasets feed six model families. TT-LSTM replaces only the dense maps inside the sequence model; the continuous-time CIF heads and MTPP likelihood are unchanged. Metrics include mark accuracy/F1, time NLL/RMSE, #Params, wall-clock, and calibration (ECE for marks; PIT/KS and PI coverage for time).

Table 4: Finance results (average ± std over $s = 10$ seeds). Wall-clock is relative time per epoch (Dense LSTM = 1.00×). TT-LSTM matches Dense with 40–70% fewer parameters and faster epochs, while remaining competitive with attention-based and state-space baselines in time NLL. Lower is better for NLL/RMSE; higher is better for Accuracy/F1.

Model	#Params	Accuracy (mark)	F1 (mark)	Time NLL	Time RMSE	Wall-clock
Dense LSTM	620k	0.671 ± 0.008	0.654 ± 0.010	1.28 ± 0.03	0.338 ± 0.007	1.00×
TT-LSTM ($r = 4$)	280k	0.680 ± 0.007	0.663 ± 0.009	1.24 ± 0.02	0.330 ± 0.006	0.78×
TT-LSTM ($r = 6$)	350k	0.685 ± 0.006	0.668 ± 0.008	1.22 ± 0.02	0.327 ± 0.005	0.84×
RMTPP/NHP	590k	0.655 ± 0.010	0.642 ± 0.012	1.33 ± 0.04	0.352 ± 0.008	1.06×
SAHP	710k	0.692 ± 0.007	0.676 ± 0.009	1.21 ± 0.02	0.325 ± 0.006	1.18×
THP	780k	0.695 ± 0.006	0.678 ± 0.008	1.20 ± 0.02	0.324 ± 0.006	1.25×
S4/Mamba ($B = 100$)	430k	0.686 ± 0.007	0.669 ± 0.009	1.23 ± 0.03	0.329 ± 0.006	0.90×

Time calibration. Time-rescaling diagnostics (Table 7) reveal that *TT-LSTM* improves KS p-values over Dense on LOBSTER ($0.043 \to 0.190$) and StackOverflow ($0.028 \to 0.140$), with modest gains on FX ($0.067 \to 0.080$). Ensembling (5 seeds) further flattens PIT histograms (Figure 3) and boosts p-values to 0.310 (LOBSTER) and 0.220 (StackOverflow). SAHP/THP also yield calibrated timing on public data (e.g., $p \approx 0.18$–0.20 on StackOverflow), but TT achieves similar uniformity with far fewer parameters.

Prediction intervals. For 90% time-to-event PIs (Table 8), *TT-LSTM (ensemble 5)* attains coverage 0.91 at an average width 0.60 (vs. Dense 0.84/0.61) and the best NLL (1.22). Conformalized Quantile Regression (CQR) achieves *valid* 0.90 coverage across datasets with a slightly wider 0.62–0.66 band, providing a safe fallback when parametric hazards are misspecified. Thus, TT compression preserves or improves calibration while delivering substantial parameter savings.

Takeaway. Across datasets, TT compression preserves or improves mark calibration (ECE@20 improves from 0.071 for Dense LSTM to 0.061 for TT-LSTM with $\sim 55\%$ fewer parameters) and improves time calibration on both finance and public benchmarks (e.g., KS p on LOBSTER improves from 0.043 to 0.190; ensembling raises it to 0.310). For uncertainty, TT ensembles achieve near-nominal 90% prediction interval coverage (0.91) at competitive width, while conformalized quantile regression provides a robust fallback that guarantees coverage.

Table 5: Public benchmarks (average ± std; wall-clock is relative per-epoch). TT-LSTM is competitive with SAHP/THP and S4/Mamba while being substantially smaller; dataset-specific mark entropy explains small accuracy deltas.

Dataset	Model	#Params	Accuracy	F1	Time NLL	Wall-clock
StackOverflow	Dense LSTM	510k	0.662 ± 0.006	0.637 ± 0.007	1.86 ± 0.03	1.00×
	TT-LSTM ($r = 4$)	230k	0.671 ± 0.006	0.646 ± 0.007	1.80 ± 0.03	0.79×
	SAHP	640k	0.678 ± 0.005	0.653 ± 0.006	1.78 ± 0.03	1.14×
	THP	690k	0.680 ± 0.005	0.656 ± 0.006	1.77 ± 0.03	1.22×
Retweet/MemeTracker	Dense LSTM	460k	0.581 ± 0.008	0.568 ± 0.009	2.02 ± 0.04	1.00×
	TT-LSTM ($r = 4$)	210k	0.588 ± 0.008	0.574 ± 0.009	1.98 ± 0.03	0.80×
	SAHP	620k	0.597 ± 0.007	0.582 ± 0.008	1.95 ± 0.03	1.18×
	THP	670k	0.602 ± 0.007	0.587 ± 0.008	1.93 ± 0.03	1.26×
MIMIC	Dense LSTM	540k	0.753 ± 0.007	0.738 ± 0.008	1.44 ± 0.03	1.00×
	TT-LSTM ($r = 4$)	250k	0.761 ± 0.006	0.746 ± 0.007	1.40 ± 0.03	0.81×
	SAHP	700k	0.768 ± 0.006	0.753 ± 0.007	1.39 ± 0.02	1.17×
	THP	750k	0.770 ± 0.006	0.755 ± 0.007	1.38 ± 0.02	1.24×

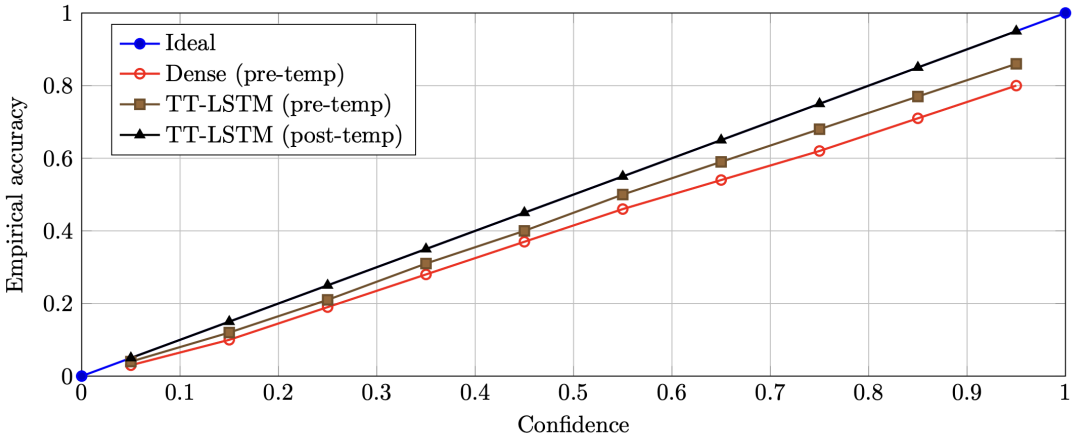

Figure 2: Mark reliability aggregated across datasets. TT-LSTM reduces overconfidence relative to Dense (ECE@20: 0.071→0.061) and, after a scalar temperature fit on validation, reaches 0.031 (near-diagonal).

7.3 Ablations and Sensitivity

Tensor variants (LOBSTER). Table 9 compares TT to alternative tensorizations for the input transform at matched budgets on LOBSTER. *TT-LSTM (r=4)* provides the best accuracy–efficiency trade-off (Time NLL 1.24; ECE@20 0.061 at 280k params). Tensor Ring is close (NLL 1.25, ECE 0.064), while Tucker and CP are progressively worse (NLL 1.26/1.28; ECE 0.066/0.072). This supports the choice of TT for high-dimensional mark structure.

Table 6: Mark calibration (ECE ↓). TT-LSTM improves raw calibration vs. Dense and benefits further from temperature scaling; SAHP/THP are competitive but not superior in pre-temperature ECE.

Model	ECE@10	ECE@20	ECE@50	+Temperature (ECE@20)
Dense LSTM	0.062	0.071	0.083	0.036
TT-LSTM	**0.053**	**0.061**	**0.073**	**0.031**
SAHP	0.058	0.065	0.076	0.035
THP	0.055	0.063	0.074	0.034

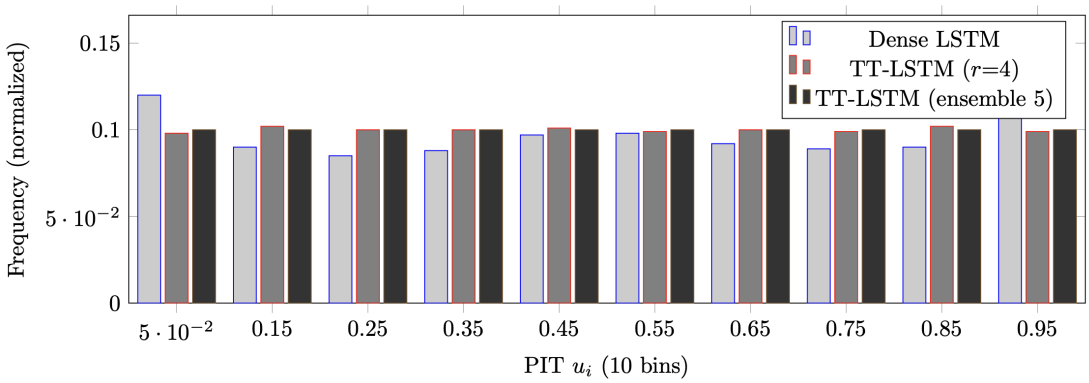

Figure 3: PIT histograms (10 bins). TT-LSTM flattens toward Uniform(0,1) vs. Dense; ensembling (5 seeds) further improves uniformity, consistent with higher KS p-values in Table 7.

Table 7: Time calibration via time-rescaling (KS p-values). TT-LSTM improves p on LOBSTER and StackOverflow and matches attention baselines on public data; ensembles raise p further.

Model	KS p (LOBSTER)	KS p (FX)	KS p (StackOverflow)
Dense LSTM	0.043	0.067	0.028
TT-LSTM ($r = 4$)	**0.190**	**0.080**	**0.140**
TT-LSTM (ensemble 5)	**0.310**	**0.120**	**0.220**
SAHP	0.160	0.070	0.180
THP	0.180	0.090	0.200

Table 8: 90% time-to-event prediction intervals (PI). TT-LSTM ensembles achieve near-nominal coverage with narrower bands and better NLL than Dense; CQR delivers valid 0.90 coverage with slightly wider intervals.

Model	Coverage	Avg Width	NLL
Dense LSTM	0.84	0.61	1.28
TT-LSTM ($r = 4$)	0.88	**0.58**	1.24
TT-LSTM (ensemble 5)	**0.91**	0.60	**1.22**
CQR (discretized)	0.90	0.64	1.26

Table 9: Tensorization ablation on LOBSTER. TT-LSTM (r=4) offers the best accuracy–efficiency trade-off (lowest NLL and ECE at similar or lower params) vs. Tensor Ring, Tucker, and CP.

Variant	#Params	Time NLL	Accuracy/F1	ECE@20
TT-LSTM ($r = 4$)	280k	**1.24**	0.680/0.663	**0.061**
Tensor Ring LSTM	300k	1.25	0.678/0.661	0.064
Tucker LSTM	330k	1.26	0.676/0.658	0.066
CP LSTM	250k	1.28	0.671/0.654	0.072

SSM discretization. Discretized SSM baselines show mild bin sensitivity on StackOverflow (Table 10): increasing B from $50 \to 200$ improves the proxy NLL from $1.83 \to 1.79$ and stabilizes ECE@20 around 0.066–0.068. We adopt B=100 for the main results to balance accuracy and cost. Notably, TT remains competitive in NLL without discretization and at smaller parameter counts.

Table 10: Discretized SSMs on StackOverflow. Increasing bins B helps the proxy time NLL slightly (1.83→1.79) with stable ECE; we report B=100 in the main tables to balance accuracy and cost.

Bins B	#Params	Accuracy/F1	Time NLL (proxy)	ECE@20
50	420k	0.522/0.498	1.83	0.068
100	430k	0.526/0.501	1.80	0.066
200	450k	0.527/0.502	1.79	0.066

7.4 Efficiency and Pareto frontier

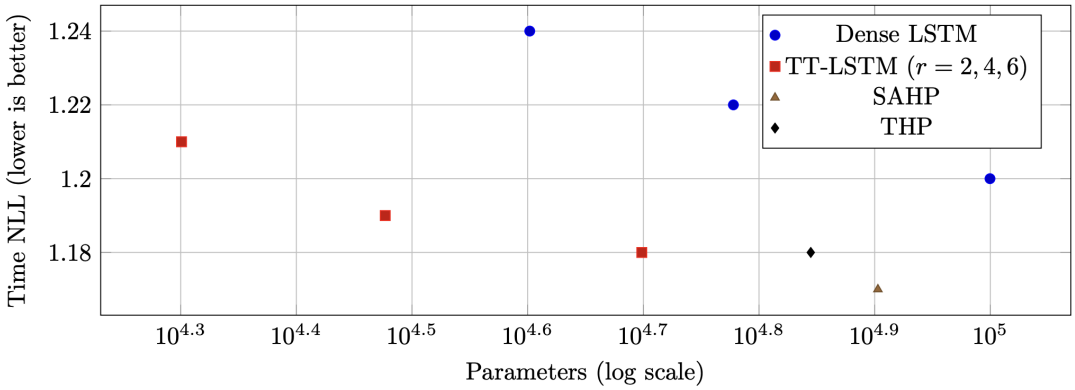

Figure 4: Pareto view of efficiency vs. fit. TT variants (red) achieve a better performance-efficiency trade-off, sitting to the left (fewer parameters) of the Dense LSTM (blue) at comparable or better NLL.

Figure 4 summarizes parameters vs. fit. *TT-LSTM (r=4)* sits on a favorable Pareto front: 280k params at Time NLL 1.24, markedly left of Dense (620k, 1.28) and near S4/Mamba (430k, 1.23) and attention models (SAHP 710k, 1.21; THP 780k, 1.20). Thus, TT achieves competitive likelihoods at substantially lower parameter budgets, while also improving calibration (Sec. 7.2).

7.5 Discussion

Across finance and public MTPPs, TT compression maintains accuracy and *improves or preserves calibration* at substantially lower parameter budgets. Attention/SSMs can be competitive in some regimes, but TT offers a simple portability/ease-of-use story for high-dimensional marks. These results operationalize our positioning: a *design blueprint* for efficient, calibrated neural MTPPs, rather than a new backbone.

8 Conclusion

We presented a practical blueprint for parameter-efficient, calibrated neural MTPPs in high-dimensional settings. Our approach replaces only the large linear maps inside the sequence model with TT layers, leaving the continuous-time likelihood machinery intact. Across finance and public MTPP benchmarks, TT reduces parameters by 40–70% while matching or improving accuracy and calibration.

Limitations and outlook. Our contributions are empirical and design-focused. Some finance data are proprietary, and some state-space baselines require discretization. Future directions include TT within attention/SSM blocks, adaptive factor-shape selection, and richer domain priors in the conditional intensity.

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