Thinking-KT: A Training-Free Large Reasoning Model-based Knowledge Tracing Framework for Unified Prediction and Prescription

Abstract

Knowledge Tracing (KT) aims to estimate a learner's evolving mastery based on interaction histories. Recent studies have explored Large Language Models (LLMs) for KT via autoregressive nature, but such approaches typically require fine-tuning and exhibit unstable or near-random performance. Moreover, prior KT systems primarily focus on prediction and rely on multi-stage pipelines for feedback and recommendation, resulting in increased system complexity and resources. To address this gap, we propose *Thinking-KT*, a training-free KT framework that incorporates Test-Time Scaling (TTS), enabling even small LLMs (1–2B parameters) to achieve competitive KT performance. Moreover, in this framework, a small LLM can jointly perform KT prediction, personalized feedback generation, and learning recommendation in a unified output without degrading prediction accuracy. Beyond performance, we present the systematic analysis of reasoning traces in KT. Our results demonstrate that TTS is a critical yet under-explored factor in LLM-based KT, and that small LLMs can serve as unified ITS engines. Our code is available at Our code is available at https://anonymous.4open.science/r/lokt_thinking_anonymous-2A16

1 Introduction

Knowledge Tracing (KT) aims to estimate a learner's knowledge state over time based on their past interactions with learning tasks (Corbett and Anderson, 1995). Deep learning-based models (Piech et al., 2015; Ghosh et al., 2020; Liu et al., 2023) have achieved strong predictive performance, yet fundamental limitations persist. Educational interaction data is typically too limited in scale for effective self-supervised pretraining, which leads to cold-start problems (Lee et al., 2024; Jung et al., 2024). Moreover, existing KT models are primarily

Figure 1: Comparing No-Think and *Thinking-KT* across KT performance and pedagogical quality of feedback and recommendations. TTS consistently improves both prediction accuracy and pedagogical quality without training.

designed for prediction, requiring separate components to generate pedagogical feedback (FB) or learning recommendations (Rec) in modern intelligent tutoring systems (ITS), which incurs additional inference latency and system overhead (VanLehn, 2011; Ma et al., 2014).

Recent LLM-based approaches have attempted to address these gaps (Fu et al., 2024; Scarlatos et al., 2025; Li et al., 2025), but without fine-tuning, they achieve only BKT-level performance (Cho et al., 2024), and even fine-tuned models fail to generalize. While LOKT (Kim et al., 2024) demonstrated promising training-free KT through prompt engineering, its effectiveness was validated only on frontier Large Language Models (LLMs), and the role of Test-Time Scaling (TTS) was not examined.

The emergence of Large Reasoning Models (LRMs) such as OpenAI's o1 (OpenAI et al., 2024) and DeepSeek-R1 (DeepSeek-AI, 2025) has revealed that TTS is critical for complex tasks. Chain-

Figure 2: Overall framework of *Thinking-KT*. Given a learner's problem-solving history, the LLM receives a structured prompt and performs TTS before prediction. A single inference produces (1) KT prediction, (2) personalized diagnostic FB, and (3) next-step learning Rec. The *right* panel illustrates the evaluation pipeline for both predictive performance and pedagogical quality, highlighting the positive effect of TTS on accuracy and instructional effectiveness.

of-Thought (CoT) prompting (Wei et al., 2022) and TTS (Snell et al., 2024; Xu et al., 2025) reveal that explicit modeling of reasoning processes drives performance gains, rather than model size alone (Yang et al., 2025). However, no prior work has investigated how TTS influences KT performance, nor whether small LLMs can leverage TTS to become effective KT predictors.

To address these gaps, we propose *Thinking-KT*, a training-free KT framework that performs TTS via structured reasoning and jointly generates KT predictions and pedagogical prescriptions, including FB and learning Rec, within a single inference. This framework enables small LLMs (1–2B parameters) to achieve competitive KT performance without additional training. Our experiments further show that TTS is the primary component of performance gains, while other inductive biases contribute only marginally. Moreover, by unifying prediction and prescription in a single inference, *Thinking-KT* reduces reliance on complex multimodel ITS pipelines and provides interpretability through explicit reasoning traces.

Our contributions are summarized as follows:

- We propose *Thinking-KT*, a training-free KT framework that applies TTS via TTS and unifies prediction and pedagogical prescription.

- We show that TTS is the primary driver of performance gains in LLM-based KT.

- We reveal that a small LLM can jointly generate KT predictions, personalized FB, and learning Rec without degrading predictive accuracy.

- We present the systematic analysis of reasoning traces in KT, examining how the traces relate to both prediction accuracy and pedagogical quality.

2 Method

This section introduces *Thinking-KT*, a training-free framework that incorporates TTS and enables a small LLM to perform (1) KT prediction, (2) personalized FB generation, and (3) learning Rec in a unified output.

2.1 Problem Definition

Let a learner's interaction history up to time t be

$$\mathcal{H}_t = \{(q_1, c_1, o_1, y_1), \ldots, (q_t, c_t, o_t, y_t)\},$$

where q_i denotes the question, c_i the associated knowledge component (KC), o_i the selected option, and $y_i \in \{0, 1\}$ the correctness label.

Given the next item (q_{t+1}, c_{t+1}), the goal of KT is to estimate

$$P(y_{t+1} = 1 \mid \mathcal{H}_t, q_{t+1}, c_{t+1}).$$

Thinking-KT addresses this task using a structured natural-language prompt and a TTS mechanism, without any training or parameter updates.

2.2 Thinking-KT

2.2.1 Structured Prompt Setting

Thinking-KT encodes a learner's interaction history and the upcoming question into a structured natural-language prompt (See Appendix A.1). To analyze the effect of prompt structure independently from reasoning, we consider three prompts: No-Option, Option and Weight.

In the No-Option, the prompt includes only the question and the learner's past interaction history. The options are not provided. This setting represents a minimal-information baseline of LLM-based KT. In the Option, all answer options of the multiple-choice question (MCQ) are included in natural language. In the Weight, each answer option is augmented with a textual importance descriptor summarizing its diagnostic relevance. This representation follows prior work (Kim et al., 2024) on textual option weighting for token-efficient LLM-based KT.

All three prompt settings are evaluated under both No-Think and *Thinking-KT* settings. This design allows us to disentangle the effect of prompt structure from the effect of TTS.

2.2.2 TTS

Thinking-KT leverage TTS τ to generate at inference time. Given the structured prompt $\mathbf{x}$, the model performs TTS before producing its outputs. To study the effect of TTS, we impose a Thinking Budget B that constrains the token length of the reasoning trace τ as:

$$|\tau| \leq B.$$

The B controls the depth of TTS and enables systematic analysis of how reasoning trace influences prediction accuracy and quality of FB and Rec.

2.2.3 Unified Multi-Task Output

A central component of *Thinking-KT* is that a single LLM inference produces prediction and instructional outputs jointly. Specifically, the model generates:

$$(\hat{y}_{t+1}, \hat{F}_{t+1}, \hat{R}_{t+1}, \tau),$$

where $\hat{y}_{t+1}$ is the predicted probability of a correct response, $\hat{F}_{t+1}$ is FB describing the learner's recent performance, $\hat{R}_{t+1}$ is a Rec for the next concept or practice item, and τ is the reasoning trace produced during TTS.

2.2.4 Final Formulation

We formally define the complete *Thinking-KT* framework which is a unified, training-free TTS process. Given the structured prompt $\mathbf{x}$ and a Thinking Budget B, a single LLM f_{LLM} produces all outputs in one forward pass:

$$(\hat{y}_{t+1}, \hat{F}_{t+1}, \hat{R}_{t+1}, \tau) = f_{\text{LLM}}(\mathbf{x}; B)$$

where the reasoning trace $|\tau| \leq B$.

2.3 Evaluation

Thinking-KT produces KT prediction, FB and Rec. Each component is evaluated using appropriate metrics and protocols that remain consistent across all LLMs.

2.3.1 Evaluation for KT prediction

For KT prediction, we compute AUC, Accuracy, and F1 using a 10-sample evaluation protocol. Because each LLM forward pass yields only a binary correctness label (`correct` or `incorrect`), a single query does not provide probabilistic information required for AUC. Thus, each test instance is queried ten times, and the empirical correctness probability is used to compute AUC. Accuracy and F1 are computed via majority voting over the ten samples. Traditional KT models (DKT (Piech et al., 2015), DKVMN (Zhang et al., 2017), AKT (Ghosh et al., 2020)) are deterministic and therefore do not require sampling.

2.3.2 Evaluation for FB and Rec

To evaluate the pedagogical quality of generated FB and Rec, we adopt an LLM-as-Judge (Zheng et al., 2023) using Solar-Pro2 (Upstage, 2025) as the evaluator. Solar-Pro2 is selected as the judge model due to its favorable balance between performance and inference cost. For each test instance, a single generation is sampled from the model outputs and independently assessed by the judge model.

The evaluator assesses whether the generated FB and Rec appropriately reflect the learner's interaction history, predicted mastery state, and pedagogical suitability, using a structured five-dimensional rubric: relevance (Rel), specificity (Spec), correctness (Corr), structiveness (Struct), and diagnostic quality (Diag), which rated on a 1–5 Likert scale

Table 1: KT prediction performance on ASSIST09, DBE-KT22, and EdNet. Within the *Thinking-KT* framework, small LLMs outperform larger LLMs and achieve performance competitive with task-specific trained models, despite requiring no additional training.

Model	Design	ASSIST09			DBE-KT22			EdNet-500		
		AUC	ACC	F1	AUC	ACC	F1	AUC	ACC	F1
Traditional KT Models (Training)										
DKT	–	0.7244	-	-	0.7820	-	-	0.7890*	-	-
DKVMN	–	0.7199	-	-	0.7830	-	-	0.7800*	-	-
AKT	–	0.7881	-	-	0.7980	-	-	0.8100*	-	-
LLM-based KT (No-Think / Training-Free)										
Qwen3-1.7B	No-Option	0.6011	0.7603	0.8540	0.5216	0.7253	0.8377	0.4930	0.5511	0.6716
	Option	0.5846	0.7493	0.8459	0.5262	0.7555	0.8581	0.5096	0.5783	0.7075
	Weight	0.5221	0.7621	0.8637	0.5039	0.7610	0.8643	0.5042	0.6012	0.7497
GPT-5-mini	No-Option	0.6437	0.4522	0.4710	0.5875	0.3471	0.2925	0.5117	0.4068	0.0142
	Option	0.6372	0.4404	0.4561	0.5818	0.3269	0.2414	0.6063	0.6132	0.6892
	Weight	0.6412	0.4494	0.4573	0.5750	0.2994	0.1747	0.5889	0.6016	0.6710
Gemini-2.5-flash	No-Option	0.6992	0.7252	0.8126	0.7105	0.7527	0.8333	0.5875	0.5671	0.5781
	Option	0.6991	0.7434	0.8272	0.6999	0.7445	0.8268	0.5884	0.5731	0.6048
	Weight	0.6824	0.7322	0.8191	0.7105	0.7527	0.8333	0.6058	0.5511	0.5465
***Thinking-KT* (Thinking / Training-Free) (Ours)**										
Qwen3-1.7B	No-Option	0.7276	0.7420	0.8271	0.6958	0.7390	0.8276	0.6046	0.5792	0.6209
	Option	0.7153	0.7630	0.8456	0.6597	0.6978	0.8057	0.6043	0.5932	0.6622
	Weight	0.7026	0.7511	0.8425	0.5953	0.7335	0.8336	0.5612	0.5531	0.6135
GPT-5-mini	No-Option	0.6614	0.7742	0.8576	0.6387	0.7719	0.8576	0.5992	0.5935	0.6666
	Option	0.6694	0.7841	0.8646	0.6367	0.7637	0.8522	0.6053	0.6124	0.6871
	Weight	0.6625	0.7666	0.8520	0.6327	0.7692	0.8536	0.6327	0.7692	0.8536
Gemini-2.5-flash	No-Option	0.6899	0.7252	0.8119	0.7122	0.7362	0.8208	0.6969	0.7388	0.8219
	Option	0.7013	0.7406	0.8250	0.7185	0.7664	0.8446	0.5879	0.5671	0.6000
	Weight	0.6824	0.7322	0.8191	0.6969	0.7388	0.8219	0.6004	0.5551	0.5524

(See Appendix A.2, A.3). For joint FB and Rec outputs (FB+Rec), both rubric sets are applied. Scores are averaged across evaluation samples to produce the final generative quality metrics. The complete evaluation prompts and rubric definitions are provided in the Appendix.

3 Results

This section reports experimental results of *Thinking-KT*, focusing on the role of TTS in LLM-based KT and unified outputs.

3.1 Experiment Settings

All experiments are designed to isolate the effect of TTS from confounding factors such as prompt design and model scale. Our evaluation addresses two questions: (1) how TTS affects KT prediction performance and unified outputs, and (2) whether unified generation of prediction, feedback, and recommendation introduces a trade-off with KT accuracy.

We evaluate three categories of models: traditional KT architectures (DKT, DKVMN and AKT), small LLMs (Qwen3-1.7B), and frontier LLMs (GPT-5-mini and Gemini-2.5-Flash). All LLMs are evaluated under both reasoning-disabled and reasoning-enabled settings.

Experiments are conducted on three benchmark KT datasets: ASSISTments09 (assist09), DBE-KT-22, and EdNet-500. ASSISTments09 is a middle-school mathematics tutoring dataset from the ASSISTments platform, comprising 4,217 students and 346,860 interactions over 26,688 problems with 123 knowledge components (Feng et al., 2009). DBE-KT-22 is a university-level database systems dataset containing 1,361 students and 167,222 interactions across 212 questions annotated with 98 skills (Abdelrahman et al., 2022). EdNet originates from a large-scale TOEIC preparation platform and includes 784,309 learners and 131M interactions in its full form (Choi et al., 2020); following a low-data evaluation setting, we construct EdNet-500 by subsampling interaction histories from 500 learners. For all datasets, interaction sequences are randomly split into training and test sets with an 80/20 ratio.

In addition to prediction-only evaluation, we consider a unified output setting in which a single LLM jointly generates KT prediction, FB and Rec. Unified and prediction-only settings share identical inputs, Thinking Budgets, sampling protocols, and evaluation procedures; they differ only in output

Table 2: Unified output evaluation. Prediction accuracy is largely preserved when adding feedback and recommendation, and TTS further improves both prediction and pedagogical quality.

Model	Category	AUC	Feedback Rubrics					Recommendation Rubrics				
			Rel	Spec	Corr	Struct	Diag	Rel	Spec	Corr	Struct	Diag
Qwen3-1.7B-No-Think	Pred Only	0.5221	–	–	–	–	–	–	–	–	–	–
	FB	0.7019	3.7683	2.8180	3.7951	3.1597	3.0726	–	–	–	–	–
	Rec	0.6340	–	–	–	–	–	3.2633	3.8883	3.4615	3.0543	2.2882
	FB + Rec	0.6857	3.8038	2.9874	3.7766	3.0974	3.2500	3.3480	3.9073	3.3652	3.1287	2.2876
Qwen3-1.7B-Think	Pred Only	0.7026	–	–	–	–	–	–	–	–	–	–
	FB	0.6810	3.8888	3.0037	3.9372	3.4354	3.5048	–	–	–	–	–
	Rec	0.7183	–	–	–	–	–	3.6424	4.0945	3.7241	3.4535	2.8960
	FB + Rec	0.7065	3.9342	3.2503	3.8893	3.3280	3.5445	3.4967	4.0140	3.5567	3.3422	2.5456

specification.

To analyze interactions between reasoning and prompt design, we compare three prompt formulations: No-Option, Option, and Weight. Unless otherwise stated, results use a history length of 25 interactions and a weight portion of 1, referencing (Kim et al., 2024).

3.2 KT Performance

Table 1 reports KT prediction performance across datasets and model categories. Without TTS, LLM-based KT shows unstable behavior across prompt formulations. Performance varies substantially depending on option representations, and in several cases degrades when additional option information is introduced, indicating that prompt-level inductive bias alone is insufficient.

When TTS is enabled, KT performance improves consistently across datasets and prompt designs. As shown in Table 1, performance becomes substantially more robust to prompt variations: while No-Option, Option, and Weight prompts yield divergent results without TTS, their performance differences narrow under reasoning-enabled settings. This indicates that TTS dominates prompt-level effects.

The impact of TTS is particularly pronounced for small open-source models. For Qwen3-1.7B, reasoning yields large AUC gains across datasets, transforming unstable predictions into competitive KT performance and narrowing the gap with larger frontier LLMs. Overall, Table 1 shows that TTS plays a more critical role than prompt complexity or model scale in stabilizing KT predictions and improving ranking quality.

3.3 Unified Output Performance

We examine whether unified generation introduces a trade-off with prediction accuracy. Table 2 summarizes results across four output configurations.

Unified generation does not degrade KT prediction performance: AUC remains comparable between Pred Only and unified settings. This indicates that generating pedagogical outputs does not inherently interfere with knowledge state estimation.

TTS plays a key role in stabilizing unified generation. For Qwen3-1.7B, KT performance varies across output configurations when reasoning is disabled, suggesting interference between prediction and pedagogical generation. With TTS enabled, AUC remains stable across Pred Only, FB, Rec, and FB+Rec settings, indicating that reasoning enables joint generation without performance trade-offs.

In addition to preserving KT accuracy, TTS improves pedagogical quality. As shown in Table 2, *Thinking-KT* achieve higher scores across Rel, Spec, Corr, Struct and Diag. Overall, these results demonstrate that TTS enables unified outputs without sacrificing KT performance, allowing a single LLM to function as a unified ITS engine.

4 Ablation

4.1 Comparison with Thinking Budget

Table 3 shows the impact of the Thinking Budget on KT performance. Introducing TTS yields a substantial AUC improvement over the No-Think setting ($0.5221 \rightarrow 0.7026$ at 2048 tokens), while further increasing the Thinking Budget to 4096 tokens does not provide additional gains and slightly degrades performance. This indicates that KT benefits primarily from the presence of TTS rather than excessive Thinking Budget, suggesting an optimal and task-specific range are needed.

4.2 Importance of History Length and Few-shot Prompt Structure

Figure 4 shows that enlarging the history window alone provides limited benefits without TTS,

| (a) Label transition patterns | (b) Transition difference | (c) Trace complexity |

Figure 3: Structural analysis of reasoning traces. Correct predictions are characterized by analytically centered transition structures, greater diversity, and denser transition patterns, whereas incorrect predictions exhibit more fragmented and self-referential dynamics.

Table 3: Effect of Thinking Budget on KT prediction performance for Qwen3-1.7B.

Thinking Budget	AUC	ACC	F1
No-Think	0.5221	0.7621	0.8637
Think-2048	**0.7026**	0.7511	0.8425
Think-4096	0.6863	0.7411	0.8360

Table 4: Effect of model size on KT prediction performance under *Thinking-KT* (Thinking Budget = 2048).

Model Size	AUC	ACC	F1
Qwen3-0.6B	0.6168	0.7291	0.8308
Qwen3-1.7B	**0.7276**	0.7420	0.8271
Qwen3-4B	0.7182	**0.7775**	**0.8579**

Figure 4: Effect of history length on AUC. Thinking-KT (2048 tokens) consistently improves performance across all lengths, with saturation around 20–25 interactions.

whereas *Thinking-KT* yields substantial AUC gains (+0.10–0.17) across prompt settings, with performance saturating at moderate history lengths. This suggests that TTS, rather than prompt complexity, is the primary factor driving KT improvements.

4.3 Effect of Model Size

We analyze the effect of model scale using three Qwen3 variants (0.6B, 1.7B, and 4B) under identical settings on ASSIST09, with the same structured prompt (Weight) and a fixed reasoning budget of 2048 tokens. As shown in Table 4, TTS yields meaningful KT performance even for the smallest model (AUC = 0.6168), while scaling to 1.7B achieves the best AUC (0.7276); further scaling to

4B does not improve AUC and slightly degrades it. In contrast, Accuracy and F1 increase monotonically with model size, suggesting that larger models make more confident binary decisions, whereas the ranking quality of knowledge state estimation saturates at moderate scales, indicating that TTS rather than model size is the primary driver of KT performance.

5 Analysis

This section examines the reasoning traces of *Thinking-KT*. We first define an analytical framework based on Schoenfeld's Episode Theory, then examine structural patterns distinguishing correct from incorrect predictions, their pedagogical interpretation, and the qualitative impact on feedback and recommendations.

5.1 Experimental Setup

To isolate the impact of TTS, we compare two settings applied to Qwen3-1.7B model. The No-Think baseline requires the model to predict the final KT outcome directly from the input prompt, without generating explicit reasoning traces. In contrast, the *Thinking-KT* framework allocates a reasoning budget of 2048 tokens, allowing the model to externalize its cognitive process as a reasoning trace before outputting the final answer. Our framework adapts Schoenfeld's Episode Theory (Schoenfeld,

Table 5: Taxonomy of reasoning traces based on Schoen-feld's Episode Theory.

Label	Description
Read	Identifying problem and student history.
Plan	Formulating pedagogical strategies and subsequent steps.
Implement	Executing calculations or logical operations.
Analyze	Evaluating theoretical relationships and mastery states.
Monitor	Regulating and calibrating the reasoning flow in real-time.
Explore	Testing hypotheses through trial-and-error reasoning.
Verify	Confirming the consistency and correctness of results.

1985) to categorize 11,082 reasoning traces. As shown in Table 5, each trace is mapped to seven cognitive labels. The labels are designed to assess the depth and structural integrity of the TTS process. Following 3, we use Solar-Pro2 (Upstage, 2025) for labeling.

Pattern	Think	No-Think	Δ
Evidence specificity	78%	24%	+54pp
Performance differentiation	64%	18%	+46pp
Prediction-feedback alignment	86%	62%	+24pp

Table 6: Feedback pattern frequencies across conditions (n=50 per condition).

5.2 Structural Systematicity of Reasoning Traces

Analysis of reasoning traces reveals three major differences of structural systematicity between correct and incorrect predictions.

First, we observe that correct predictions tend to show rapid transition from problem comprehension to analysis. As shown in Figure 3a, 66.1% of Read episodes transition to Analyze in correct predictions, compared to 51.7% in incorrect predictions. This pattern is consistent with the hypothesis that effective KT may benefit from immediate engagement with the underlying problem structure through Read→Analyze, though causal relationships cannot be established from this observational analysis.

Second, incorrect predictions exhibit undirected self-referential patterns, as highlighted by the red regions in Figure 3b. Explore→Explore transitions are 6.2pp higher in incorrect traces, Verify→Verify loops are 7.1pp higher, and notably, Implement→Implement shows a 10.2pp

Episode Label	Diagnostic Analogue	Evidence
Read	Evidence gathering	Initiates 89% of traces
Read→Analyze	Cue interpretation	66% (correct) vs 51% (incorrect)
Analyze	Judgment formation	40.83% vs 34.80% centrality

Table 7: Mapping between Schoenfeld's episode labels and teacher diagnostic competence components.

gap. These patterns indicate that incorrect predictions become trapped in repetitive cognitive cycles without analytical guidance, cycling through exploration or verification without reaching productive conclusions.

Third, beyond transition dynamics, correct predictions demonstrate systematically higher trace complexity (Figure 3c). This suggests an optimal range of reasoning depth for knowledge tracing tasks.

These findings suggest that *Thinking-KT*'s performance gains and robustness are associated with structured analytical reasoning patterns.

5.3 Pedagogical Interpretation of Thinking

We interpret reasoning traces through the lens of *teacher diagnostic competence* which is the cognitive processes of teachers who employ to assess student knowledge states and inform instructional decisions (Helmke and Schrader, 1987; Südkamp et al., 2012).

The reasoning patterns observed in *Thinking-KT* exhibit structural analogies to expert diagnostic reasoning. Table 7 maps Schoenfeld's episode labels to diagnostic competence components.

This mapping aligns with Herppich et al. (2018)'s three-component model: (1) perceiving relevant student cues, (2) interpreting cues against domain knowledge, and (3) integrating information into judgments. The importance of Analyze in correct predictions corresponds to the cue interpretation phase, which Südkamp et al. (2012) identified as the primary differentiator between accurate and inaccurate teacher judgments (k=75 studies). Conversely, incorrect predictions show elevated Explore and fragmented Verify patterns, analogous to novice diagnostic behavior characterized by insufficient analytical depth.

These findings indicate that TTS organizes the model's assessment process into a diagnostic reasoning traces that resembles how expert teachers reason. However, this similarity should be understood as structural rather than functional.

5.4 Qualitative Analysis of Feedback and Recommendation

We conducted exploratory qualitative analysis based on ground theory (Glaser, 1965) to characterize how TTS affects the pedagogical properties of generated outputs. A single researcher performed open coding on 200 samples (50 per condition: Think-FB, No-Think-FB, Think-Rec, No-Think-Rec), generating 16 codes that were grouped into 5 emergent patterns through constant comparison.

Three patterns distinguished Think from No-Think feedback (Table 6): *Evidence Specificity* (citing question IDs vs. general KC references), *Performance Differentiation* (distinguishing success/struggle areas vs. uniform characterization), and *Prediction-Feedback Alignment* (internal consistency). These patterns relate to Hattie and Timperley (2007)'s feedback model, where effective feedback addresses "How am I going?" with concrete instances and enables targeted "Where to next?" guidance.

Two patterns emerged for recommendations: *Gap-Targeting* (recommending struggled items; Think 72% vs. No-Think 34%) and *Rationale Provision* (explaining why; Think 68% vs. No-Think 22%). The Gap-Targeting pattern reflects Narciss (2008)'s distinction between corrective and confirmatory strategies, with Think exhibiting predominantly corrective orientation.

6 Related Work

KT aims to predict students' knowledge states and future performance. Bayesian Knowledge Tracing (BKT) (Corbett and Anderson, 1995) pioneered this field, and DKT (Piech et al., 2015) revolutionized it by applying deep learning. Subsequent research has advanced through attention (Ghosh et al., 2020; Liu et al., 2023; Yin et al., 2023), graph learning (Cheng et al., 2024), and uncertainty-aware modeling (Cheng et al., 2025; Xia and Li, 2025). However, KT research faces persistent challenges: the trade-off between performance and interpretability (Bai et al., 2024; Sun et al., 2024), and the cold-start problem (Jung et al., 2024), as educational data lacks the scale amenable to self-supervised learning (Lee et al., 2024).

Recent LLM-based approaches have attempted to address these limitations (Fu et al., 2024; Scarlatos et al., 2025; Li et al., 2025). However LLMs achieve only BKT-level performance (Cho et al., 2024), and even fine-tuned models often fail to generalize beyond specific scenarios (Jung et al., 2024; Lee et al., 2024; Kim et al., 2024). While LOKT (Kim et al., 2024) showed promise through efficient textual encoding, critical gaps remain: reasoning capabilities and smaller models remain largely untested.

In parallel, LRMs have demonstrated that explicit multi-step reasoning, rather than model size alone, can drive substantial performance gains across diverse domains (Wei et al., 2022; Snell et al., 2024; Xu et al., 2025). However, despite these advances, the role of TTS remains largely unexplored in educational settings (Lee et al., 2025), particularly in KT, motivating our proposal of *Thinking-KT*.

7 Conclusion

We proposed *Thinking-KT*, a training-free framework for LLM-based KT that leverages reasoning to enable prediction and unified pedagogical generation. Experimental results show that reasoning is the dominant factor for stabilizing KT performance, surpassing the effects of prompt design and model scale, and allows small LLMs to achieve competitive performance without task-specific training. We further demonstrate that TTS enables a single LLM to jointly generate KT predictions, FB, and Rec without degrading prediction accuracy, eliminating the need for multi-stage ITS pipelines. These findings highlight TTS as a practical foundation for building lightweight, unified, and scalable educational AI systems.

8 Limitation

Despite its effectiveness, *Thinking-KT* has several limitations that suggest directions for future research. First, although the framework is training-free, test-time Thinking introduces additional inference cost and latency, which may restrict its deployment in strict real-time intelligent tutoring systems. Future work will explore adaptive or early-exit reasoning mechanisms that dynamically allocate Thinking Budget based on uncertainty or task difficulty, reducing unnecessary computation. Second, while the observed reasoning traces exhibit structural similarities to expert teacher diagnostic processes, they should not be interpreted as faithful representations of human cognition. Future studies will incorporate human-in-the-loop evaluations, such as expert teacher annotations or think-aloud protocols, to more rigorously assess the pedagog-

ical validity and interpretability of model reasoning. Third, the pedagogical quality of feedback and recommendations is evaluated using an LLM-as-Judge with structured rubrics, which may still introduce implicit model bias. Future work will complement automated evaluation with human expert assessment and investigate cross-model or ensemble judging strategies to improve robustness. Fourth, our experiments are limited to multiple-choice knowledge tracing benchmarks. Generalization to open-ended problem solving, dialog-based tutoring, and multi-turn instructional interactions remains an open challenge. Extending *Thinking-KT* to these settings will be a key direction for future research. Finally, we observe that the optimal Thinking Budget is task- and dataset-dependent, indicating that a fixed reasoning depth may be suboptimal. Future work will investigate adaptive reasoning control policies that adjust Thinking Budget in response to learner state, task complexity, or confidence signals, enabling more efficient and personalized KT.

9 GenAI Usage Disclosure

GPT-5, 5.1 and 5.2 were used for minor language editing. Gemini-2.5-Flash, GPT-5-Mini, and Solar-Pro2 were used solely to run model predictions and evaluations. All scientific ideas, analyses, and experimental designs were conducted by the human authors.

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A Appendix

A.1 prompt: structured prompt for inference

Analyze the student's problem-solving history and predict their performance on the next question.
Student's problem-solving history: 1. Question ID sequence: {question_ids} 2. KC ID sequence: {kc_ids} (Note: This is a list of KC IDs associated with the next question. For example, if next_kc_id is {3, 72}, it means the next question involves KC IDs 3 and 72.) 3. Selected option sequence: {option_sequence} 4. Selected option weights: {option_weights} 5. Correctness sequence: {answer_sequence} Next question details: 1. Next question ID: {next_question_id} 2. Next question's KC ID: {next_kc_id}
Based on the above information, predict whether the student will answer the next question (ID: {next_question_id}, KC ID: {next_kc_id}) correctly ('correct') or incorrectly ('wrong').
Consider the following when making your prediction: 1. The student's overall correctness pattern. 2. The complexity and difficulty levels of the questions and KC IDs. 3. How the selected options reflect their weight on the student's understanding and confidence. 4. Recent trends in the student's performance. 5. The student's progression and knowledge improvement over time. 6. The student's current knowledge state for each KC and how it matches the KC IDs in the next question. 7. Ignore any NaN values in the option weights.
Output only the single word ['correct' or 'wrong']. No other words or punctuation should be included.

A.2 prompt: feedback evaluation

You are an expert educational assessment evaluator. Your task is to evaluate the quality of personalized feedback generated by a knowledge tracing system.
Context:

- Student History: <STUDENT_HISTORY>

- Prediction: <PREDICTION>

- Ground Truth: <GROUND_TRUTH>

- Generated Feedback: <GENERATED_FEEDBACK>

Evaluation Task: Evaluate the generated feedback using the rubric below. For each criterion, assign a score from 1 to 5 and provide a brief explanation.
Rubric:
1. Relevance (1–5): Does the feedback directly address the student's learning history and current knowledge state? 1 = Completely irrelevant or generic 2 = Somewhat related but mostly generic 3 = Moderately relevant with limited personalization 4 = Highly relevant with clear personalization 5 = Perfectly tailored to the student's specific situation
2. Specificity (1–5): Does the feedback provide concrete, actionable guidance? 1 = Extremely vague, no actionable guidance 2 = Mostly generic statements 3 = Some specific elements mixed with generic advice 4 = Mostly specific with clear guidance 5 = Highly specific with detailed, actionable steps
3. Accuracy (1–5): Is the feedback consistent with the student's performance history and prediction outcome? 1 = Contradicts evidence 2 = Partially inconsistent 3 = Generally consistent with minor inaccuracies 4 = Accurate and consistent 5 = Perfectly aligned with all evidence
4. Constructiveness (1–5): Does the feedback support learning improvement or reinforcement? 1 = No constructive value 2 = Minimal constructive guidance 3 = Some helpful elements 4 = Clear and constructive guidance 5 = Highly motivating and instructional feedback
5. Diagnostic Quality (1–5): Does the feedback identify specific knowledge gaps or strengths based on KC patterns? 1 = No diagnostic insight 2 = Vague or incorrect diagnosis 3 = Basic diagnostic insight 4 = Clear identification of gaps or strengths 5 = Deep diagnostic insight with clear pedagogical implications
Output Format: Return a JSON object with a score and explanation for each criterion.

A.3 prompt: recommendation evaluation

> You are an expert educational assessment evaluator. Your task is to evaluate the quality of question recommendations generated by a knowledge tracing system.
> Context:
>
> - Student History: <STUDENT_HISTORY>
>
> - Prediction: <PREDICTION>
>
> - Ground Truth: <GROUND_TRUTH>
>
> - Generated Feedback: <GENERATED_FEEDBACK>
>
> Evaluation Task: Evaluate the generated recommendation using the rubric below. For each criterion, assign a score from 1 to 5 and provide a brief explanation.
> Rubric:
> 1. Relevance (1–5): Does the recommendation address the student's learning history and current knowledge state? 1 = Completely irrelevant 2 = Weakly related, mostly generic 3 = Moderately relevant 4 = Highly relevant and personalized 5 = Perfectly tailored to the student's knowledge gaps
> 2. Specificity (1–5): Does the recommendation specify a concrete question and clear reasoning? 1 = No specific question or vague reasoning 2 = Question present but generic reasoning 3 = Question with some specific reasoning 4 = Specific question with clear reasoning 5 = Highly specific question with detailed pedagogical rationale
> 3. Accuracy (1–5): Is the recommended question grounded in the student's interaction history and evidence? 1 = Question not in history or reasoning incorrect 2 = Question in history but reasoning partially incorrect 3 = Generally accurate with minor issues 4 = Accurate and consistent 5 = Perfectly aligned with all evidence
> 4. Constructiveness (1–5): Does the recommendation support learning improvement or reinforcement? 1 = No constructive value 2 = Minimal learning value 3 = Some constructive elements 4 = Clear pedagogical benefit 5 = Strongly supports learning progress
> 5. Diagnostic Quality (1–5): Does the recommendation reflect specific knowledge gaps or

> strengths based on KC patterns? 1 = No diagnostic basis 2 = Vague or incorrect diagnosis 3 = Basic diagnostic insight 4 = Clear identification of relevant gaps or strengths 5 = Deep diagnostic analysis linked to learning goals
> Output Format: Return a JSON object with a score and explanation for each criterion.

A.4 prompt: labeling reasoning traces

We use Solar-Pro2 (Upstage, 2025) to classify reasoning traces based on Schoenfeld's Episode Theory (Schoenfeld, 1985).The following prompt is used for labeling:

> You are an expert in analyzing mathematical problem-solving processes based on Schoenfeld's Episode Theory.
> Given a segment of reasoning trace from a knowledge tracing model, classify it into one of the following categories:
> 1. Read: Identifying problem and student history. (e.g., "The problem asks to find the value of x when $2x + 5 = 10$.")
> 2. Plan: Formulating pedagogical strategies and subsequent steps. (e.g., "Next, I will differentiate both sides of the equation with respect to x.")
> 3. Implement: Executing calculations or logical operations. (e.g., "Substituting $x = 3$ into the equation: $2(3) + 5 = 6 + 5 = 11$.")
> 4. Analyze: Evaluating theoretical relationships and mastery states. (e.g., "According to the Pythagorean theorem, in a right triangle, the square of the hypotenuse equals the sum of squares of the other two sides.")
> 5. Monitor: Regulating and calibrating the reasoning flow in real-time. (e.g., "Wait, something seems off here.")
> 6. Explore: Testing hypotheses through trial-and-error reasoning. (e.g., "Perhaps substituting different values for x might reveal a pattern.")
> 7. Verify: Confirming the consistency and correctness of results. (e.g., "Let me check my calculation again... Yes, it matches the previous result.")
> Reasoning Trace Segment:
> Output: Return only the label name (Read, Plan, Implement, Analyze, Monitor, Explore, or Verify).